VELAMMAL BODHI CAMPUS

CLASS: X GRAND TEST 1 DATE: 30.11.2023

MARKS: 80 MATHS DURATION: 3.00HRS

GENERAL INSTRUCTIONS:

- 1. This question paper has 5 Sections A-E.
- 2. Section A has 20 MCQs carrying 01 mark each.
- 3. Section B has 5 questions carrying 02 marks each.
- 4. Section C has 6 questions carrying 03 marks each.
- 5. Section D has 4 questions carrying 05 marks each.
- 6. Section E has 3 case based integrated units of assessment (04 marks each) with sub-parts of the values of 1, 1 and 2 marks each respectively.
- 7. All questions are compulsory. However, an internal choice in 2 Qs of 5 marks, 2 Os of 3 marks and 2 Os of 2 marks has been provided. An internal choice has been provided in the 2 marks questions of Section E.
- 8. Draw neat figures wherever required. Take $\pi = 22/7$ wherever required if not stated.

SECTION A

Section A consists of 20 questions of 1 mark each.

1. The LCM	of the	smallest t	wo digit	number	and	the	smallest	compo	site
number is	S								

- a. 12
- b. 20
- c. 4
- d. 44

2. If the product of the zeros of the quadratic polynomial $3x^2 + 5kx + k$ is $\frac{-2}{3}$, then the value of k is

- a. -3
- b. -2
- c. 2
- d. 3

3. The value of k for which the system of linear equations x + 2y = 3, 5x + ky + 7 = 0 is inconsistent is

- a. $\frac{-14}{3}$
- b. $\frac{2}{5}$
- c. 5
- d. 10

4. If one root of the equation $ax^2 + bx + c = 0$ is three times the other, then

- a. $b^2 = 16ac$ b. $b^2 = 3ac$ c. $3b^2 = 16ac$ d. $16b^2 = 3ac$

5. If the second term of an A.P is 13 and 5th term is 25 then 7th term is

- a. 30
- b. 33

- c. 37
- d. 38

4	\triangle ABC ~ \triangle PQR a	and AB ² : PQ ²	= 4:9, then AM : P	N =
	a. 16:81	b. 4:9	c. 3:2	d. 2:3
•	In figure, if PQR whose centre is PR and $\triangle AQB$ is	O, AB is a ch	nt to a circle at Q ord parallel to	A B
	a. 20° c. 35°	b. 40° d. 45°		70° Q
			es are 4cm and 5c ngent to the other	m then the length of each circle is
	a. 3cm	b. 6cm	c. 9cm	d. 1cm
	The ratio in whi s divided by x-		gment joining the j	points A(3, -4) and B(-2,7)
	a. 3:2	b. 2:3	c. 4:7	d. 7:4
10.	The point which joining the point is the point which is a second or the point which is a seco		_	ctor of the line segment
	a. (0, 0)	b. (0, 2)	c. (2, 0)	d. (-2, 0)
11.	If $\sin\theta + \cos\theta$	$=\sqrt{2}\cos\theta$, θ	\neq 90°, then tan θ =	·
	a. $\sqrt{2}$ - 1	b. $\sqrt{2} + 1$	c. $\sqrt{2}$	d $\sqrt{2}$
12.	If x tan60°cos6	50° = sin60°co	0.00° then x =	
	a. cos30°	b. tan30°	c. sin30°	d. cot30°
13.	fixed and the a	angle of elevat round is 30° tl	ion of the top of th hen the angle of el	the tower on which it is the tower as seen from a tevation of the top of the
	a. 45°	b. 30°	c. 60°	d. 90°
14.	If the area of a	circle is 64π	cm^2 , then its circu	ımference is
	a. $7\pi\mathrm{cm}$	b. 16πcm	c. 14πcm	d. $21\pi\mathrm{cm}$
15.			30cm having leng e centre O of the c	th 19cm then the angle ircle is
	a. 36.27°	b. 36°	c. 30.99°	d. 34°
16.	The mean of fi	rst n odd natu	aral numbers is $\frac{n^2}{81}$	then n =
	a. 9	b. 81	c. 27	d. 18

6. If AM and PN are altitudes, of ΔABC and ΔPQR respectively. If

17. From the letters of the word "MOBILE", if the letter is selected then the probability that it is a vowel is

a. $\frac{1}{2}$

c. $\frac{3}{7}$

d. $\frac{1}{2}$

18. A number x is chosen at random from the numbers -3, -2, -1, 0, 1, 2, 3. The probability that |x| < 2 is

b. $\frac{2}{7}$ c. $\frac{3}{7}$

d. $\frac{1}{7}$

Direction: In the question number 19 and 20, Assertion (A) is followed by a Reason (R). Choose the correct option.

- a. Both assertion (A) and reason (R) are true and reason (R) is the correct explanation of assertion (A).
- b. Both assertion (A) and reason (R) are true and reason (R) is not the correct explanation of assertion (A).
- c. Assertion (A) is true but reason (R) is false.
- d. Assertion (A) is false but reason (R) is true.
- 19. Assertion (A): If x + 1, 3x and 4x + 2 are in A.P then x = 3.

Reason (R): If the seventh term of an A.P is $\frac{1}{6}$ and its ninth term is $\frac{1}{7}$ then its 63rd term is 1.

20. **Assertion (A):** Three cubes each of volume 8 cubic centimeters are joined end to end to form a cuboid. The surface area of the resulting cuboid is 28cm².

Reason (R): If n cubes each of volume a³ cubic units are joined end to end to form a cuboid then the surface area of the resulting cuboid is 2(2n + 1) a² square units.

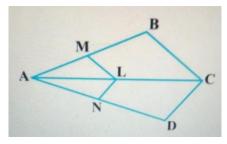
SECTION B

Section B consists of 5 questions of 2 marks each.

21. If the HCF of 35 and 45 is 5, LCM of 35

and 45 is 63xa, then find the value of a.

22. In figure, if LM || CB and LN || CD, prove that $\frac{AM}{AB} = \frac{AN}{AD}$.



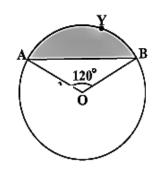
- 23. Prove that the tangents drawn at the ends of a diameter of a circle are parallel.
- 24. If $\sin (A-B) = \frac{1}{2}$, $\cos (A+B) = \frac{1}{2}$, $0^{\circ} < A+B \le 90^{\circ}$, A > B, find A and B.

In a $\triangle ABC$, right angled at B, $\triangle A = \triangle C$, find the value of

- i. sinAcosC+cosAsinC ii. sinAsinB+cosAcosB
- 25. In a circle of radius 21cm, an arc subtends an angle of 60° at the centre. Find i) the length of an arc. ii) Area of the sector formed by the arc.

OR

Find the area of the segment AYB, if radius of the circle is 21cm and $\triangle AOB = 120^{\circ}$. (Use $\pi = \frac{22}{7}$)



SECTION C

Section C consists of 6 questions of 3 marks each.

- 26. Prove that $\sqrt{5}$ is an irrational number.
- 27. Find the zeros of the polynomial $f(x) = 4\sqrt{3} x^2 + 5x 2\sqrt{3}$ and verify the relationship between the zeros and its coefficients.
- 28. Determine the value of a and b for which the following system of linear equations has infinitely many solutions:

$$2x-(a-4)y = 2b + 1$$
; $4x-(a-1)y = 5b-1$

OR

In a \triangle ABC, $\bot C = 3 \bot B = 2 (\bot A + \bot B)$. Find the three angles.

29. Two tangents TP and TQ are drawn to a circle with centre O from an external point T. Prove that $\angle PTQ = 2 \angle OPQ$.

OR

Prove that a parallelogram circumscribing a circle is a rhombus.

- 30. Prove that $\frac{tan\theta + sec\theta 1}{tan\theta sec\theta + 1} = \frac{1 + sin\theta}{\cos \theta}$.
- 31. Find the median of the following frequency distribution:

Weekly	60-69	70-79	80-89	90-99	100-109	110-119
Wages (in Rs)						
No. of days	5	15	20	30	20	8

SECTION D

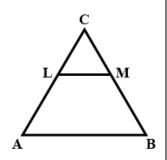
Section D consists of 4 questions of 5 marks each

32. The speed of a boat in still water is 15km/hr. It can go 30km upstream and return downstream to the original point in 4 hours 30 minutes. Find the speed of the stream.

OR

If the roots of the equation $(c^2 - ab) x^2 - 2 (a^2 - bc) x + b^2 - ac = 0$ are equal, Prove that either a = 0 (or) $a^3 + b^3 + c^3 = 3abc$.

33. State and Prove Basic Proportionality Theorem. In figure, LM \parallel AB. If AL= x - 3, AC = 2x, BM = x - 2 and BC = 2x + 3, find the value of x.



34. A solid toy is in the form of a hemisphere surmounted by a right circular cone. The height of the cone is 2cm and the diameters of the base is 4cm. Determine the volume of the toy. If a right circular cylinder circumscribes the toy, find the difference of the volume of the cylinder and the toy. (Take $\pi = 3.14$)

OR

Due to heavy floods in a state, thousands were rendered homeless. 50 schools collectively offered to the state Government to provide place and canvas for 1500 tents to be fixed by the Government and decided to share the whole expenditure equally. The lower part of each tent is cylindrical of base radius 2.8m and height 3.5m, with conical upper part of the same base radius but of height 2.1m. If the canvas used to make the tents costs Rs. 120 per sq.m, find the amount shared by each school to set up the tents.

35. The mean of the following frequency table is 50. But the frequencies f_1 and f_2 in class 20-40 and 60-80 are missing. Find the missing information.

C.I	0-20	20-40	40-60	60-80	80-100	TOTAL
FREQUENCY	17	\mathbf{f}_1	32	f_2	19	120

SECTION E

Case study based questions are compulsory.

36. In November 2020, some new animals were added to a zoo. As a result the number of visitors to the zoo, increased daily by 10. A total of 6150 people visited zoo during that month.

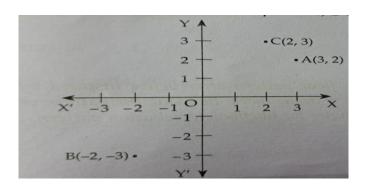
Based on the above information, answer the following questions:

- i. How many visitors visited the zoo on 1st November?
- ii. On which day of the month did 250 visitors visit the zoo?
- iii. How many persons visited the zoo in the last 5 days of the month of November?

How much collection (in rupees) from sale of tickets was done in the zoo on 15th November., if each entry ticket costs Rs. 50?

37. The following diagram shows the position of three electric poles A, B and C in a society park.

In spite of three poles in the park, the kids playing in the park complained about darkness in the park, So the society president decided to place 2 more poles in the park.



Based on the above information, answer the following questions:

- i. Find the type of triangle formed by joining the points A, B and C.
- ii. The fourth pole D is to be placed such that it divides the line segment joining A and B in the ratio 2:3. Then find the coordinates of position of pole D.
- iii. The fifth pole is placed at a point E such that ABEC forms a ||gm. Find the coordinates of the point E.

OR

Find the coordinates of the point of intersection of diagonals of ||gm ABEC.

38. Gadisar Lake is located in the Jaisalmer district of Rajasthan. It was built by the King of Jaisalmer and rebuilt by Gadsi Singh in 14th century. The lake has many Chhatris One of them is shown below:



Observe the picture. From a point A, h meters above from water level, the angle of elevation of top of Chhatri (point B) is 45° and angle of depression of its reflection in water (point C) is 60°. If the height of Chhatri above water level is (approximately) 10m, then

- i. Draw a well- labeled figure based on the above information:
- ii. Find the length (h) of the point A above water level. (Use $\sqrt{3}$ = 1.73)