

Comparison of conventional deep learning models and Generative Adversarial Network for stock price prediction

QF634 - Applied Quantitative Research Methods

Group member

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Objective

- Generative Adversarial Network (GAN) is a new machine learning framework introduced in 2014. After it was introduced, there
 have been only few papers that applied it to stock price prediction
- The main objective of this project is to compare the efficacy of the GAN framework with conventional deep learning models such as Long-Short Term Memory (LSTM) and Gated Recurrent Unit (GRU) for the purpose of stock price prediction

Outline

1.) Theoretical Background

Deep learning models

- Long short-term memory model (LSTM)
- Gated Recurrent Unit (GRU)
- Convolutional neural networks (CNN)

Generative Adversarial Network (GAN)

2.) Datasets and Features

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- DatasetsAAPL
- EBAY
- SBUX

Features

- Basic features
- Fundamental Indicators
- Technical Indicators

3.) Methodology

Data preprocessing

- Normalization
- Reshaping data
- Train test split

LSTM architecture

GRU architecture

.... GAN architecture

4.) Experimental Result

Performance measurement

Experimental Result

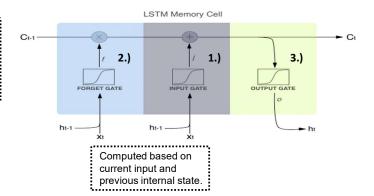
- AAPL
- EBAY
- SBUX



1.) Theoretical Background

Long short-term memory networks (LSTM)

- LSTM is a more advanced version of Recurrent Neural Network (RNN) that solves the vanishing gradients, exploding gradients, and long-term dependency problems in RNN. RNNs are not able to preserve the context for long range sequences.
- The basic components of LSTM include an input gate, an output gate, and a forget gate. The purpose of these gates is to control the flow of information within the LSTM model.
- 2.) Forget gate decides on how much of the longterm state should be erased.



1.) Input gate decides on how the internal state will be updated.

3.) Output gate gate controls which part of the long-term state should be read and output at this timestep.

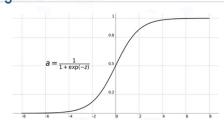
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1.) Theoretical Background

Long short-term memory networks (LSTM)

Sigmoid Function



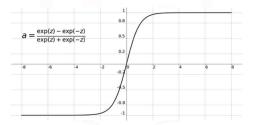
- activation functions, which produces an output of
- An output of 0 means that the gate is blocking everything, while an output of 1 means that the gate allows everything to pass through it.

:

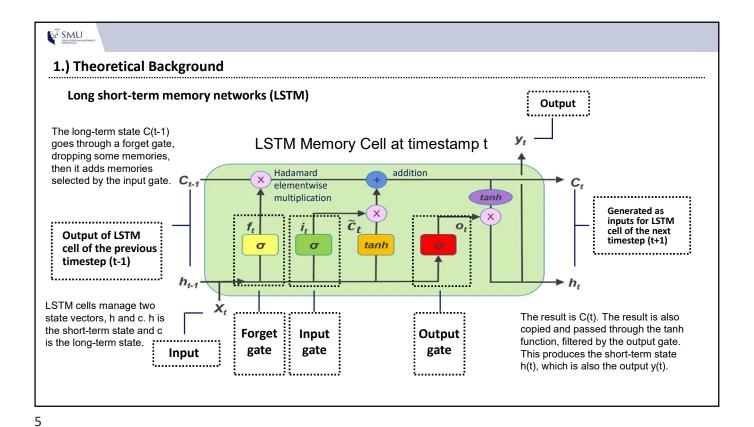
0, 1 or a value between.

Gates in the LSTM model make use of sigmoid

Hyperbolic Tangent Function



- Tanh activation function is also used in the LSTM Model, but it is mostly used for hidden layers.
- Tanh is similar to sigmoid but its range is from -1 to 1 and it results in zero centered data which helps data normalization and leads to faster data convergence.



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1.) Theoretical Background

Long short-term memory networks (LSTM)

LSTM Summary

- LSTM cell can learn to recognize an important input (input gate)
- Store it in the long-term state (state vector c)
- · Learn to preserve it for as long as it is needed (forget gate)
- · Learn to extract it whenever it is needed
- Thus, LSTM models have been successful at capturing long-term patterns in time series



1.) Theoretical Background

Gated Recurrent Unit (GRU)

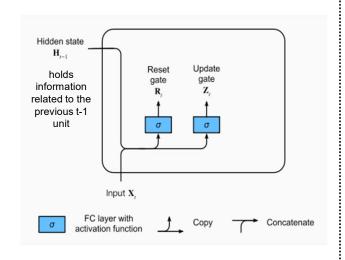
• GRU, similar to LSTM, is able to selectively remember and forget information over time. Thus, GRU is also suitable for the modelling of sequential data.

Parameters	LSTMs	GRUs	
Structure	More complex	Simpler than LSTM	
Training	Can be more difficult	Easier than LSTM	
Performance	Good for complex tasks	Can be intermediate between simple and complex tasks	
Hidden state	Multiple (memory cell)	Single In GRU, both state vectors (c and h) are merged into a single vector h	
Gates	Input, output, forget	Update, reset	
Ability to retain long-term dependencies	Strong	Intermediate between RNNs and LSTMs	

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1.) Theoretical Background

Gated Recurrent Unit (GRU)



Reset gate for time step t:

$$r_t = \sigma(w_{xr}x_t + w_{hr}h_{t-1} + b_r)$$

The **reset gate** decides how much of the previous hidden state to forget

Update gate for time step t:

parameters

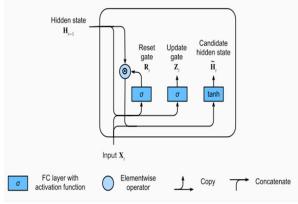
$$z_t = \sigma(w_{xz}x_t + w_{hz}h_{t-1} + b_z)$$

- The **update gate** decides how much of the candidate activation vector should be incorporated into the new hidden state
- The reset gates capture **short-term** dependencies in sequences, while the update gates capture **long-term** dependencies in sequences



1.) Theoretical Background

Gated Recurrent Unit (GRU)



Candidate hidden state for timestep t

bias

 $\widetilde{H_t} = \tanh(x_t w_{xh} + (R_t \odot H_{t-1}) w_{hh} + b_h)$ Hadamard (elementwise)

product operator

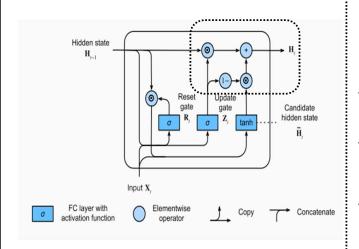
- The candidate hidden state combines information from the input and the previous hidden state
- GRU computes a candidate hidden state at each time step, which is then used to update the hidden state for the following time step

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1.) Theoretical Background

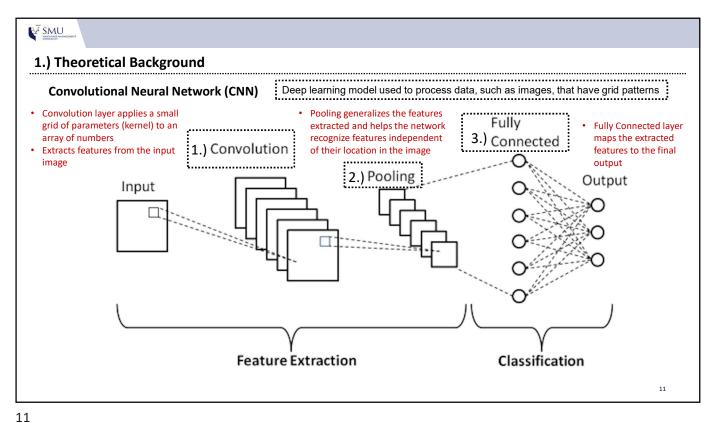
Gated Recurrent Unit (GRU)



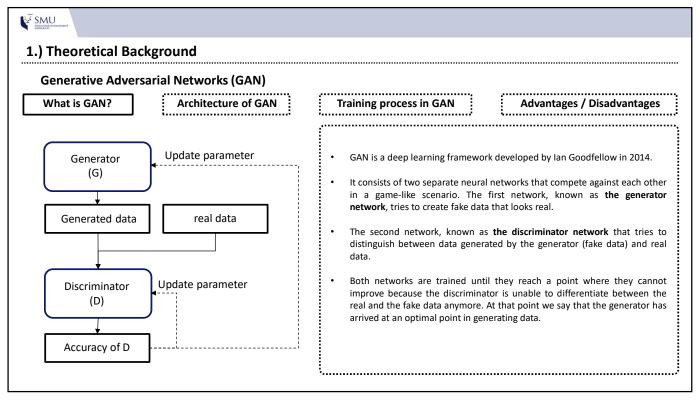
Hidden step for timestamp t

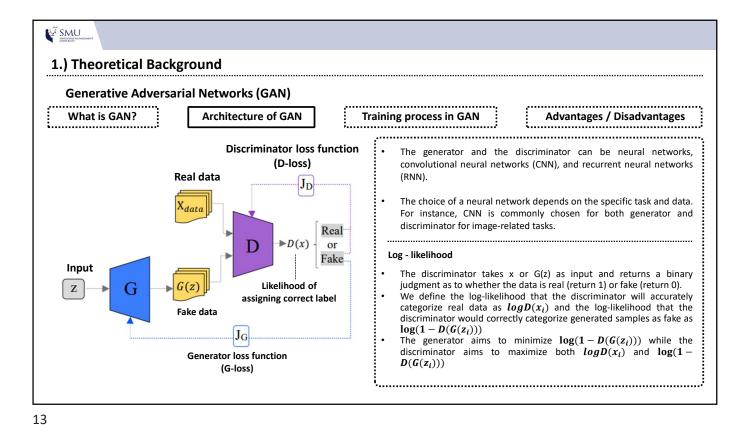
 $H_t = Z_t \odot H_{t-1} + (1-Z_t) \odot \widetilde{H}_t$ Hadamard (elementwise) product operator

- In the hidden step, the update gate Z_t determines how much of the new hidden state H_t matches the previous hidden state H_{t-1} , and the new candidate state \widetilde{H}_t .
- When the value of the output gate Z_t is 1, we retain the hidden step of the previous timestamp H_{t-1} , and we ignore the input x_t . This would be equivalent to excluding information related to timestep t.
- On the other hand, when the value of the output gate Z_t is 0, the hidden state of timestamp t would approach the candidate hidden state \widetilde{H}_t .

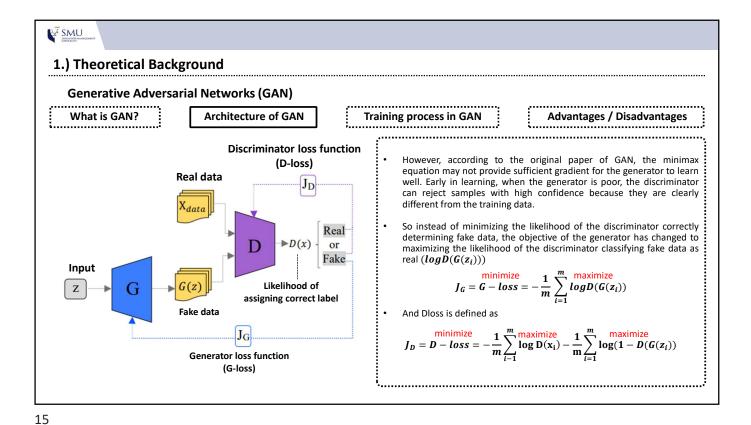


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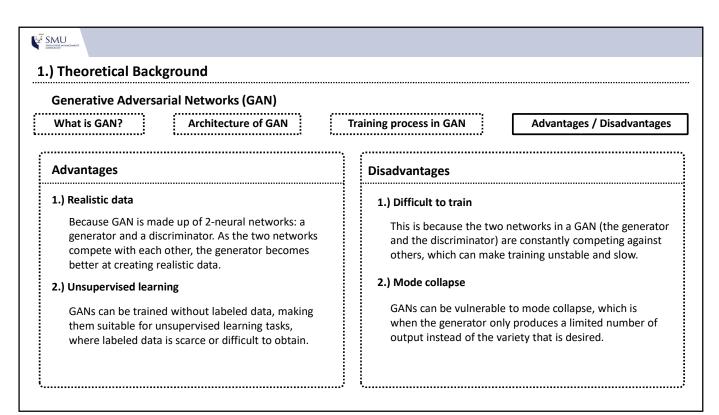


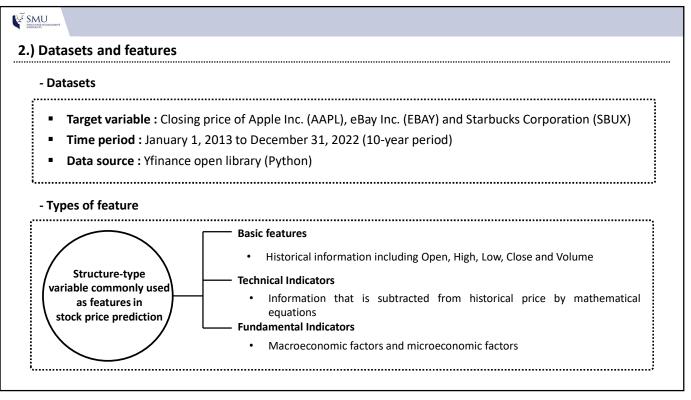


SMU SMU 1.) Theoretical Background **Generative Adversarial Networks (GAN) Architecture of GAN** What is GAN? Training process in GAN Advantages / Disadvantages **Discriminator loss function** From the definition of log(D(x)) and $log(D(G(z_i)))$, GAN can be (D-loss) modeled as a two-player minimax game with simultaneous training Real data of both generator and discriminator network. Minimax GAN Loss is $m J_D$ regarded as an optimization strategy in two-player games whereby each player reduces their losses or increases the costs of the other player. Minimax refers to minimizing the loss in the generator and Real maximizing the loss in the discriminator. D The discriminator seeks to maximize the probability of assigning proper labels to the data. On the contrary, the generator seeks to generate a series of samples that can fool discriminator. Likelihood of assigning correct label The equation explaining minimax game is given as: Fake data $\min_{C} \max_{D} (G, D) = E_{x \sim p_{data}(x)} [log(D(x))] + E_{z \sim p_{z}(z)} [log(1 - D(G_{zi}))]$ J_G **Generator loss function** (G-loss)



SMU SINGAPORE MANA 1.) Theoretical Background **Generative Adversarial Networks (GAN)** What is GAN? **Architecture of GAN** Training process in GAN Advantages / Disadvantages Real data Discriminative distribution D distribution P_{data} Generative distribution P_G (d) (b) (c) 2.) The discriminator then is updated by Dloss Real data distribution (figure c). Steps of training through backpropagation and becomes better in 4.) After several steps of training, the distinguishing according to the last generated 1.) The generator generates the fake data. The generator and discriminator will reach a point discriminator tries to distinguish between fake (fake) data (figure b) where the distribution of fake data equals to and real data. The first Gloss and Dloss are 3.) The generator is then updated by Gloss the distribution of real data and the calculated (figure a) through backpropagation and produces the fake discriminator is unable to differentiate data that has distribution closer to the between the two distributions (D(X) = 1/2)







2.) Datasets and features

Features used in the analysis:

• Basic features: Previous studies suggested that closing price is the most significant feature for forecasting closing price

Data source: Yfinance open library (Python)

- **Technical Indicators**: 5 technical indicators were calculated from closing price and used as features to capture information regarding price movement.
 - 1.) Simple Moving Average (SMA21) : = $\frac{P_t + P_{t-1} + P_{t-2} + \dots + P_{t-20}}{21}$
 - **2.)** Relative Strength Index (RSI) := 100 (100/1 + RS) where : $RS = \frac{Average\ gain\ (14\ days)}{Average\ loss\ (14\ days)}$
 - **3.)** Moving Average Convergence Divergence (MACD) : $= EMA (12 \ days) EMA (26 \ days)$
 - **4.)** Upper Bollinger Band : = SMA21 + (2 x standard deviation)
 - **5.)** Lower Bollinger Band : = SMA21 (2 x standard deviation)

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Features used in the analysis:

- Fundamental Indicators :
 - Microeconomic factors: 4 financial metrics from quarterly financial statement that demonstrate the profitmaking capability and the financial health of the company were included as

features.

Data Source: Wharton Research Data Service (WRDS)

1.) Earning per share (TTM)

Closing price

2.) Net profit margin (TTM)

Closing price

3.) Book value per share

Closing price

4.) Debt-to-Equity ratio

Closing price

• All metrics were divided by closing price to make them move on a daily basis.

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 The report date was utilized instead of end-of-quarter date to reflect the date when the public becomes aware of the updated fundamental data, ensuring that the analysis incorporates the most current and publicly available information



2.) Datasets and features

Features used in the analysis:

Fundamental Indicators :

Macroeconomic factors: We included 5 macroeconomic factors that are commonly used as economic

indicators.

Data source: Yfinance open library (Python)

1.) Crude oil price : When the global economy is robust and growing, demand for oil tends to increase as industries

expand and consumer activities rise.

2.) Gold price : Investors tend to flock to gold as a store of value and a hedge against inflation or economic

downturns. Therefore, an increase in the demand for gold and a rise in its price may indicate

concerns about the stability of financial markets and the overall economy.

3.) S&P500 index : An upward movement in stock index values are generally associated with economic expansion

4.) NASDAQ100 index and investor confidence, while a downward movement may signal concerns about economic

growth or stability.

5.) Federal funds rate: The federal funds rate is a key interest rate that influences borrowing costs throughout the

economy, serving as an indicator of the fed's monetary policy stance and it also provides

insights about the overall economic condition.

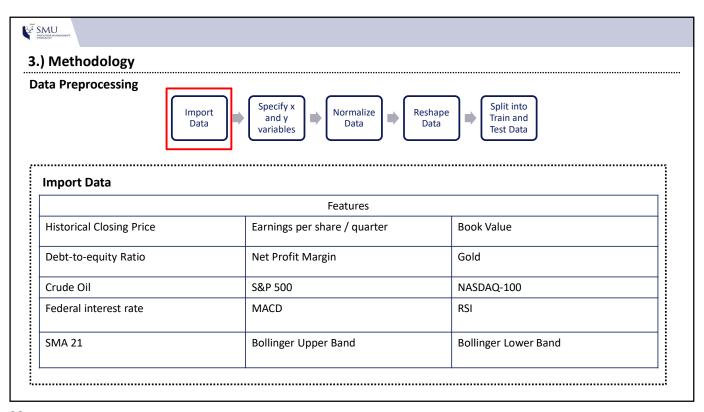
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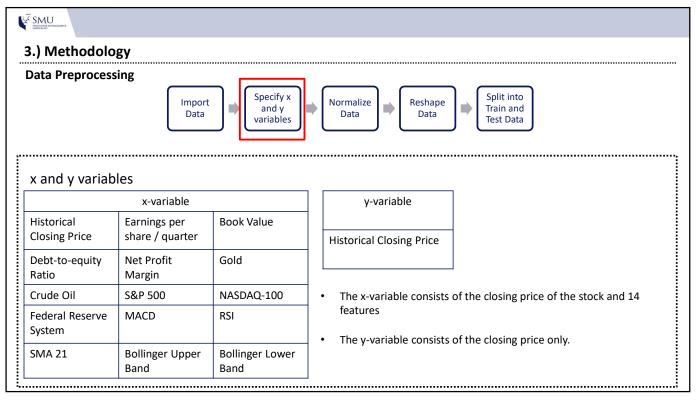


2.) Datasets and features

Features used in the analysis:

No.	Feature type Feature		Data source	
1.)	Basic feature	Closing price	yfinance library	
2.)		SMA (21 day)		
3.)		RSI (14-day window length)	1	
4.)	Technical indicators MACD (12 short, 26 long)		Calculated from closing price	
5.)		Upper Bollinger band		
6.)		Lower Bollinger band		
7.)		Earnings per share / closing price		
8.)		Book value per share / closing price		
9.)		Debt-to-equity ratio / closing price		
10.)		Net profit margin / closing price	7	
11.)	Fundamental indicators	Federal interest rate		
12.)		Gold price		
13.)	Crude oil price		yfinance library	
14.)		S&P500 index		
15.)		Nasdag100 index	7	







3.) Methodology

Data Preprocessing



Normalization

- Normalization was applied to both the 16 input features and the targeted variable
- This was to ensure that all input features are on a consistent scale
- · Also, it would promote faster convergence and mitigating issues related to vanishing or exploding gradients
- And enhance the model's generalization to unseen data.
- We had used the MinMax Scaler as it is known to effectively manage outlier data. Thus, ensuring a robust scaling transformation.

$$X_{scaled} = rac{X - X_{min}}{X_{max} - X_{min}}$$
 and $Y_{scaled} = rac{Y - Y_{min}}{Y_{max} - Y_{min}}$

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3.) Methodology

Data Preprocessing

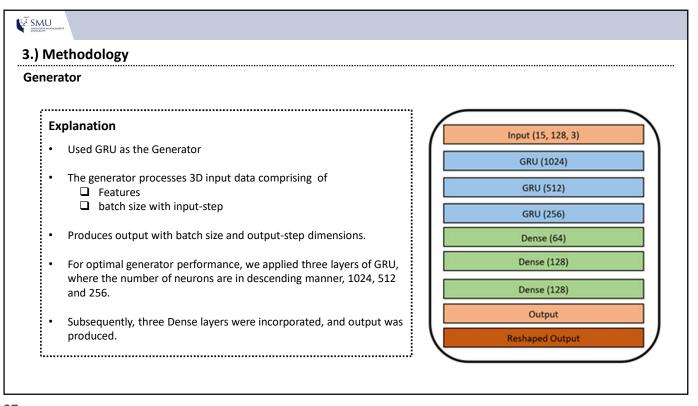


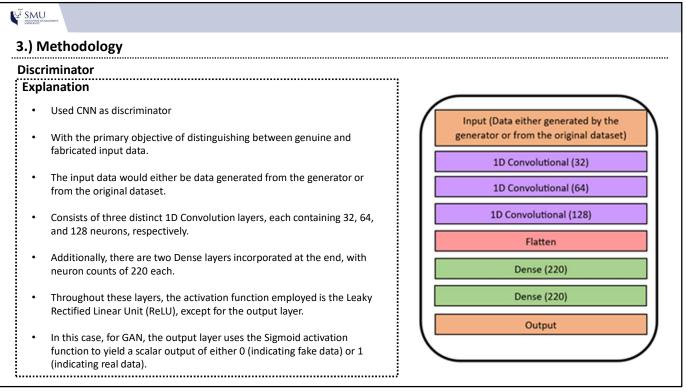
Data Reshaping

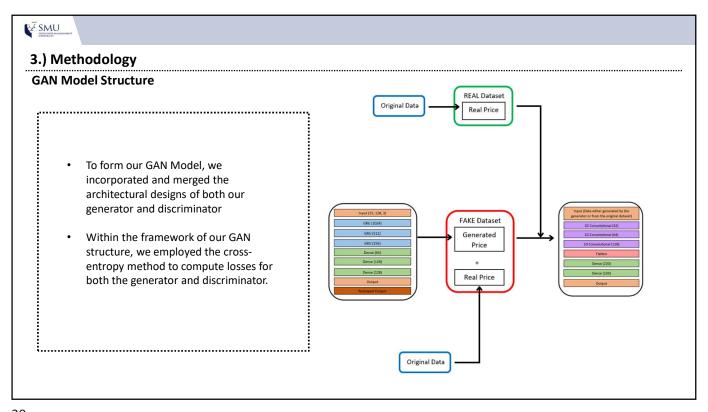
- A predictive model was developed using a sequence of three-day historical data (T-1, T-2, T-3) to forecast the stock price on the subsequent day (T).
- During the reshaping, the 3-day features' data was formatted as input, and the stock price of the following day served as the output for model training and testing.
- The reshaping of data resulted in a total of 2503 observations for both X (features) and y (targeted variable).

Train & Test Split

- 70%: Train and 30%: Test
- Training Set consisted of historical price data spanning from the start of 2013 to the end of 2019, a total of 1,752 observations
- Testing Set consisted of data from the beginning of 2020 to the end of 2022, a total of 751 observations.







which can be either 0 or 1.

actual value

then calculates the score that penalizes the probabilities based on the

.

distance from the expected value, which means how close or far from the

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3.) Methodology **GAN Model Structure Cross Entropy** Types of Cross Entropy 2 types of cross-entropy which are: Cross-entropy is a mathematical idea ☐ Binary cross-entropy, and that finds extensive applications in a □ Categorical cross-entropy range of domains, such as information theory, machine learning, and In our model, we have used binary cross-entropy (log loss) as we statistics. were dealing with 2 possible outcomes. (e.g. 0 or 1). is a particularly common choice as a **Binary Cross Entropy** loss function in machine learning models Binary cross entropy measures the dissimilarity between the predicted especially when dealing with probability distribution and the true binary labels of a dataset. classification tasks. compares each of the predicted probabilities to actual class output

serves as a metric to gauge the

dissimilarity between the predicted probability distribution and the actual

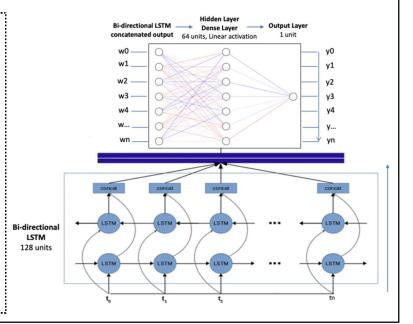
probability distribution of outcomes.



3.) Methodology

LSTM Model Structure

- Bidirectional LSTM with 128 units captures patterns in both forward and backward directions. Each LSTM layer has its own parameter
- The output of the Bi-LSTM layer comprises of the hidden states from both the forward and backward LSTM layers at each time step combined through concatenation.
- First dense layer (64 units) acts as an intermediary representation and final dense layer (1 unit) maps this representation to the output space.
- Training Details:
 - ✓ Adam optimizer with a learning rate of 0.001 is used.
 - Mean Squared Error (MSE) is the chosen loss function.
 - Training executed for 50 epochs with a batch size of 64.



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3.) Methodology

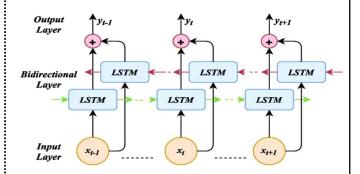
Bi-directional Long short-term memory networks (Bi-LSTM)

 Bi-LSTM consists of two LSTM layers and uses bidirectional processing to process sequential data simultaneously in two directions, both forward and backward.

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- Both the forward and backward LSTM, based on the current input and the previous hidden state and memory cell, will update its memory cell and compute its hidden state.
- Eventually, the hidden states of each LSTM layer are combined at each time step, when both forward and backward processes are complete.
- The benefit of Bi-LSTM is that it captures not only the context that comes before a specific time step but also the context that follows. It allows to capture richer dependencies in the input sequence

Backward processing: the input sequence is fed into the backward LSTM layer from the last to the first step.



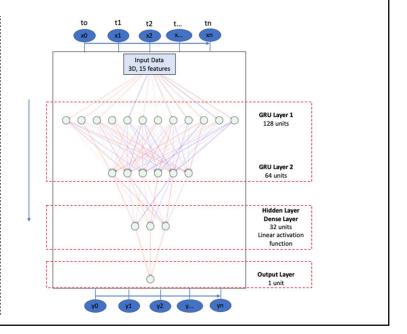
Forward processing: Input sequence is fed into the forward LSTM layer from the first to the last step.



3.) Methodology

GRU Model Structure

- Two GRU layers, 1st layer (128 units), 2nd layer (64 units)
- The model, utilizing two GRU layers to captures both local and global patterns in sequential data
- First dense layer (32 units) captures intermediary representations.
- Final dense layer (1 unit) maps this representation to the output space.
- Training Details:
 - ✓ Adam optimizer with a learning rate of 0.0001 is used.
 - Mean Squared Error (MSE) is the chosen loss function.
 - ✓ Training executed for 50 epochs with a batch size of 64.



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4.) Experimental results

Performance measurements:

Root Mean Squared Error (RMSE)

- Measures the square root of average squared differences between predicted and actual values.
- Lower RMSE indicates better model performance.

Mean Absolute Error (MAE)

- Calculates average absolute differences between predicted and actual values.
- · Lower MAE values signify better performance.

Mean Absolute Percentage Error (MAPE)

- Evaluates errors in terms of relative size of predicted values.
- · Lower MAPE values indicate more accurate predictions.

Mean Squared Logarithmic Error (MSLE)

- Useful for target variables with exponential growth patterns.
- Lower MSLE values indicate better accuracy on a logarithmic scale.

R-squared (R2)

- Assesses how much of the dependent variable's variance is predictable.
- Higher R2 indicates a better fit of the model to the data.

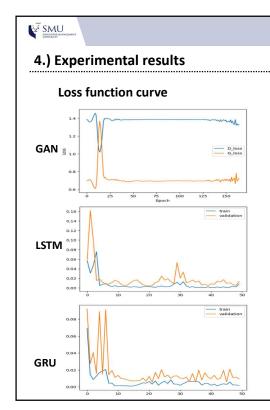
$$RMSE = \sqrt{\frac{\sum_{i=1}^{n} \left(\widehat{Y}_{i} - Y_{i}\right)^{2}}{n}}$$

$$MAE = \frac{\sum_{i=1}^{n} \left| \widehat{Y}_{i} - Y_{i} \right|}{n}$$

$$MAPE = \frac{1}{n} \sum_{i=1}^{n} \left| \frac{\widehat{Y}_i - Y_i}{Y_i} \right| \times 100$$

$$MSLE = \frac{\sum_{i=1}^{n} \left(\log \left(\widehat{Y}_{i} + 1 \right) - \log(Y_{i} + 1) \right)^{2}}{n}$$

$$R^{2} = 1 - \frac{\sum_{i=1}^{n} (Y_{i} - \widehat{Y}_{i})^{2}}{\sum_{i=1}^{n} (Y_{i} - \overline{Y})^{2}}$$



Observation of Loss Functions:

- LSTM and GRU: Observable patterns with decreasing and stabilized losses.
- · GANs: Distinct, counterintuitive behaviour.

Dynamics in GANs:

- Unlike LSTM and GRU, D-loss plateaus at a relatively high point.
- Competitive interplay between generator (G-loss) and discriminator (D-loss).

Adversarial Dynamics in GANs:

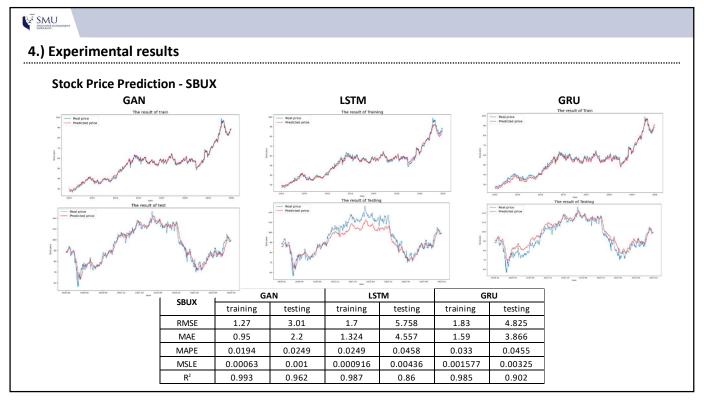
- Improvements in one component leads to higher losses in the other.
- Both discriminator and generator losses converge to stable values.

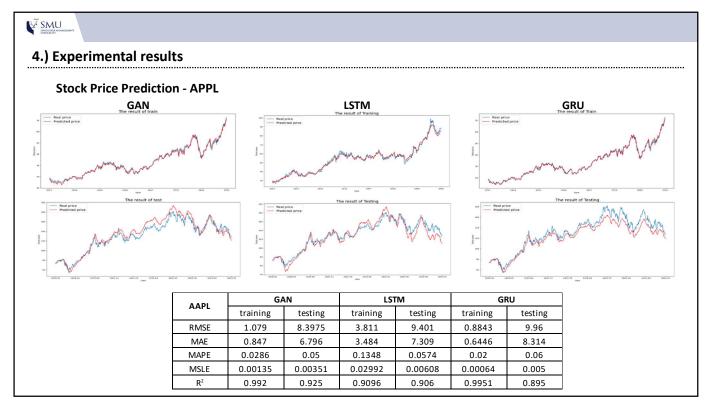
Equilibrium and Training Success:

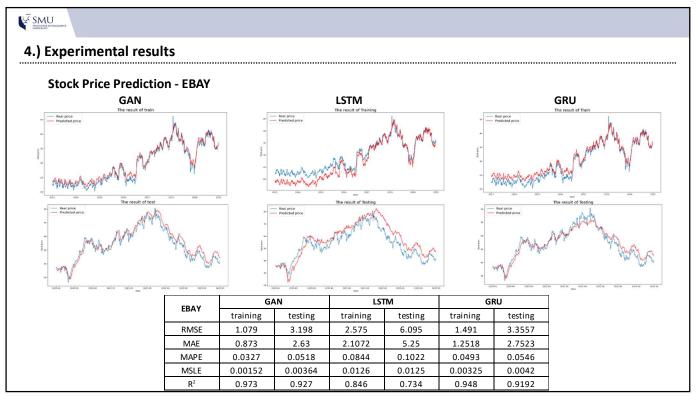
- Generator learns to produce realistic samples.
- Discriminator unable to effectively distinguish between real and generated data.

Factors for Successful Training:

- Hyperparameter Adjustment.
- Choosing the right Network Architecture.
- Continuous Monitoring of Loss Functions.









4.) Experimental results

- GAN consistently achieves higher testing accuracy compared to other models. Notable superiority in capturing time series representations.
- GRU demonstrates superior training performance in specific scenarios compared to GAN and LSTM.
- GRU has comparable training results with GAN, but GAN excels in testing accuracy.
- LSTM and GRU lagss behind and GAN in overall accuracy.
- GAN's testing accuracy is consistently higher across various datasets.
- GAN architecture excels in capturing time series representations.
- GAN architecture indicates superior accuracy compared to traditional LSTM and GRU models.

SBUX	GAN		LSTM		GRU	
	training	testing	training	testing	training	testing
RMSE	1.27	3.01	1.7	5.758	1.83	4.825
MAE	0.95	2.2	1.324	4.557	1.59	3.866
MAPE	0.0194	0.0249	0.0249	0.0458	0.033	0.0455
MSLE	0.00063	0.001	0.000916	0.00436	0.001577	0.00325
R ²	0.993	0.962	0.987	0.86	0.985	0.902
AAPL	GAN		LSTM		GRU	
	training	testing	training	testing	training	testing

3.811

9.401

0.8843

9.96

MAE	0.847	6.796	3.484	7.309	0.6446	8.314
MAPE	0.0286	0.05	0.1348	0.0574	0.02	0.06
MSLE	0.00135	0.00351	0.02992	0.00608	0.00064	0.005
R ²	0.992	0.925	0.9096	0.906	0.9951	0.895
EBAY	GAN		LSTM		GRU	
EDAT	training	testing	training	testing	training	testing
RMSE	1.079	3.198	2.575	6.095	1.491	3.3557
MAE	0.873	2.63	2.1072	5.25	1.2518	2.7523
MAPE	0.0327	0.0518	0.0844	0.1022	0.0493	0.0546
MSLE	0.00152	0.00364	0.0126	0.0125	0.00325	0.0042

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5.) Conclusion & Future Studies

GAN Outperforms in Accuracy:

 GAN network excels in capturing time series representations. It demonstrates a remarkable ability to capture representations within time series data.

RMSE

1.079

8.3975

Demonstrates superior accuracy compared to traditional LSTM and GRU models.

Complex Architecture:

- GAN framework has a complex architecture.
- Extensive trial and error needed during hyperparameter tuning.

Future Studies:

- Future studies can explore more effective approaches in determining the model combination and hyperparameters used.
- Aim to streamline the hyperparameter tuning process to optimize GAN framework performance.
- Include feature selection process by using algorithms such as DecisionTreeClassifier and ExtraTreeClassifier

Significant Potential:

- Despite challenges, GANs offer significant potential for advancing predictive modeling in financial contexts.
- Ongoing research and refinement can unlock even greater capabilities.