

LINEAR SEARCH $O(n)$

IN ORDER TO FETCH AN ITEM, WE CHECK EVERY ELEMENT IN THE ARRAY

2, 4, 1, 0, 7, 8, 6

BINARY SEARCH $O(\log n)$

IN BINARY SEARCH WE NEED ORGANIZE OUR DATA TO ACHIEVE $(\log n)$

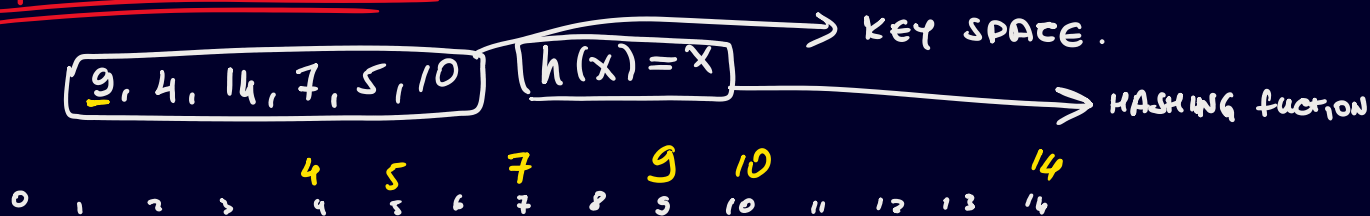
HASHTABLE (ADT)

HAS AN AVERAGE SEARCH TIME $O(1)$. HOWEVER DEPENDING ON THE IMPLEMENTATION IT MIGHT REQUIRE MORE MEMORY.

SUPPORTED OPERATIONS.

- INSERT (item)
- DELETE (item)
- SEARCH (key)

WHEN WE INSERT ELEMENTS IN A ARRAY WE CALCULATE THEIR INDEX INTO THAT ARRAY.

HASHING TECHNIQUES

IN ORDER TO AVOID ALLOCATING LARGE MEMORY SPACE, WE COULD MODIFY THE HASHING FUNCTION.

$$h(x) = x \% \text{size.}$$

$$h(5) = 5 \% 10$$

$$h(14) = 14 \% 10$$



WE NEED TO RESOLVE COLLISIONS GRACEFULLY.

COLLISION RESOLUTION TECHNIQUES.

- OPEN ADDRESSING (OPEN HASHING) \Rightarrow CHAINING

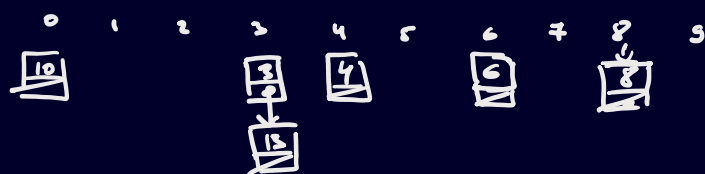
- OPEN ADDRESSING (OPEN HASHING) \Rightarrow CHAINING
- LINEAR PROBING
- QUADRATIC PROBING
- DOUBLE HASHING
- PERFECT HASHING
- UNIVERSAL HASHING

CHAINING

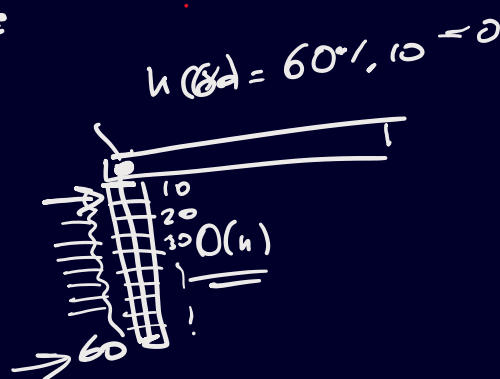
SIMPLEST HASHING TECHNIQUE, WHERE WE ALLOCATE A LINKED LIST AT THE DESIRED ARRAY POSITION

KEY SPACE

8, 3, 13, 6, 4, 10 $h(x) = x \% \text{size}$



20, 30, 40, 60, 10.



LINEAR PROBING

9, 4, 14, 7, 5, 10 $h(x) = x \% \text{size}$



10 4 14 5 7 9
0 1 2 3 4 5 6 7 8 9

$$f(i) = i$$

$$h'(x) = [h(x) + f(i)] \% \text{size} \quad \text{where } f(i) = 0, 1, 2, \dots$$

$$h'(4) = [h(4) + f(0)] \% 10 = 4$$

$$h'(14) = [h(14) + f(0)] \% 10 = 4$$

$$h'(14) = [h(14) + f(1)] \% 10 = 5$$

QUADRATIC PROBING

SIMILAR TO LINEAR PROBING BUT HAS A DIFFERENT HASHING FUNCTION TO AVOID CLUSTERING.

HASHING FUNCTION TO AVOID CLUSTERING.

$$h'(x) = [h(x) + f(i)] \% \text{size}$$

$$f(i) = i^2$$

DOUBLE HASHING

SIMILAR TO QUADRATIC AND LINEAR PROBING,
EXCEPT IT RELIES ON TWO HASHING FUNCTIONS INSTEAD OF ONE.

$h_1(x) = x \% \text{size}$ THE SECOND ONE WILL BE

$h_2(x) = m - (x \% m)$ WHERE m IS THE CLOSEST
PRIME NUMBER TO THE SIZE OF THE ARRAY. (ART OF COMPUTER PROGRAMMING)

final hashing function

$$h_1(x) + j h_2(x)$$

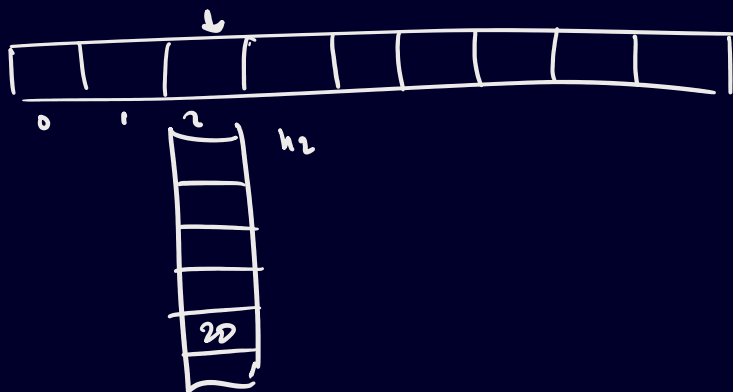
$$j \Rightarrow 1, 2, 3, 4, 5$$

PERFECT HASHING

IT HAS SIMILAR CONCEPT TO CHAINING, EXCEPT, INSTEAD OF USING
LINKED LISTS IT USES HASHTABLE

$h_1(x) \Rightarrow$ TO FIND POSITION IN THE ARRAY

$h_2(x) \Rightarrow$ FIND POSITION IN THE SUB ARRAY.



UNIVERSAL HASHING

IT RELIES ON HAVING A COLLECTION OF HASHING FUNCTIONS
THROUGHOUT THE

IT RELIES ON HAVING A COLLECTION OF HASHING FUNCTIONS THAT WE PICK AT RANDOM AND WE STICK THROUGHOUT THE RUNNING OF THE PROGRAM.

1 → CHOOSE A VERY LARGE PRIME NUMBER P

2 → $b \in \{0, 1, 2, \dots, P-1\}$

3 → $a \in \{1, 2, 3, \dots, P-1\}$

4 → $m = \text{SIZE OF THE ARRAY}$

$$h_{a,b}(X) = [(aX + b) \% P] \% m.$$

DICTIONARY $\langle f, k \rangle$