```
In [54]: #importing necessary libraries
import numpy as np
import pandas as pd
import seaborn as sns
import statsmodels.api as sm
from statsmodels.stats.outliers_influence import variance_inflation_facto
from statsmodels.compat import lzip
import statsmodels.stats.api as sms
import matplotlib.pyplot as plt
from scipy.stats import shapiro
from statsmodels.formula.api import ols
from sklearn.linear_model import LinearRegression, Ridge, Lasso
from sklearn.model_selection import train_test_split
from sklearn.metrics import mean_absolute_error, mean_squared_error, r2_s
from sklearn.preprocessing import StandardScaler
```

In [55]: #Load the data set and create a data frame for the same.
df = pd.read_csv('Jamboree_Admission.csv')
df.head()

N	111	+	П	5	5	н	=
U	u	L	L	J	J	1	1

	Serial No.	GRE Score	TOEFL Score	University Rating	SOP	LOR	CGPA	Research	Chance of Admit
0	1	337	118	4	4.5	4.5	9.65	1	0.92
1	2	324	107	4	4.0	4.5	8.87	1	0.76
2	3	316	104	3	3.0	3.5	8.00	1	0.72
3	4	322	110	3	3.5	2.5	8.67	1	0.80
4	5	314	103	2	2.0	3.0	8.21	0	0.65

In [56]: #Checking the shape of the data set

df.shape

Out[56]: (500, 9)

In [57]: #statistical summary of the data set . Serial No. is out of scope for thi
 df_stat_summary = df.drop('Serial No.', axis=1).describe()
 df_stat_summary

Out[57]:

	GRE Score	TOEFL Score	University Rating	SOP	LOR	CGPA
count	500.000000	500.000000	500.000000	500.000000	500.00000	500.000000
mean	316.472000	107.192000	3.114000	3.374000	3.48400	8.576440
std	11.295148	6.081868	1.143512	0.991004	0.92545	0.604813
min	290.000000	92.000000	1.000000	1.000000	1.00000	6.800000
25%	308.000000	103.000000	2.000000	2.500000	3.00000	8.127500
50%	317.000000	107.000000	3.000000	3.500000	3.50000	8.560000
75%	325.000000	112.000000	4.000000	4.000000	4.00000	9.040000
max	340.000000	120.000000	5.000000	5.000000	5.00000	9.920000

In [58]: #datatypes for the dataset df.info()

> <class 'pandas.core.frame.DataFrame'> RangeIndex: 500 entries, 0 to 499 Data columns (total 9 columns):

		· · · · · · · · · · · · · · · · · · ·	- · ·	
	#	Column	Non-Null Count	Dtype
-				
	0	Serial No.	500 non-null	int64
	1	GRE Score	500 non-null	int64
	2	TOEFL Score	500 non-null	int64
	3	University Rating	500 non-null	int64
	4	SOP	500 non-null	float64
	5	LOR	500 non-null	float64
	6	CGPA	500 non-null	float64
	7	Research	500 non-null	int64
	8	Chance of Admit	500 non-null	float64

dtypes: float64(4), int64(5) memory usage: 35.3 KB

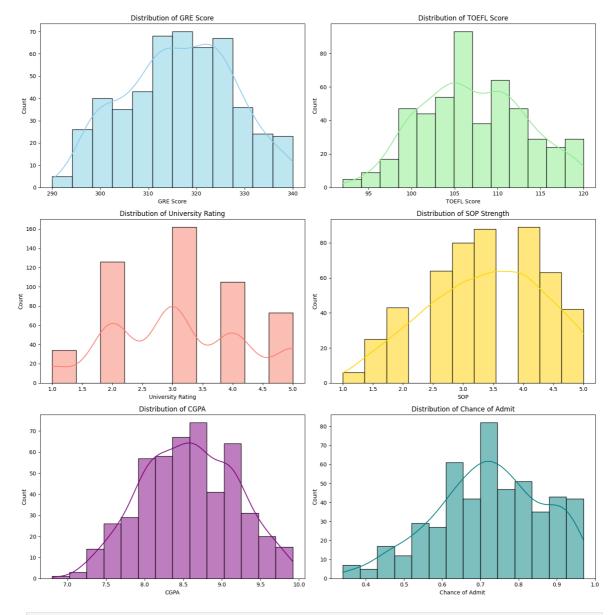
In [59]: #Missing values in the dataset

df.isnull().sum()

Out [59]:

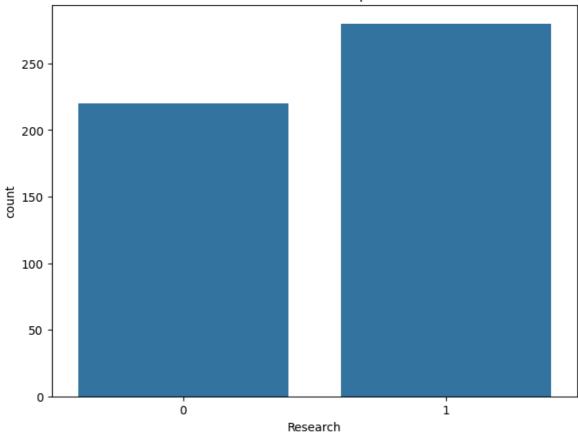
0

```
Serial No. 0
               GRE Score 0
             TOEFL Score 0
         University Rating 0
                    SOP 0
                    LOR 0
                   CGPA 0
                Research 0
          Chance of Admit 0
        dtype: int64
In [60]: #Duplicate entry count in the data set
         duplicate_count = df.duplicated().sum()
         duplicate_count
Out[60]: 0
In [61]: #Univariate Analysis
         # Set up subplots
         fig, axes = plt.subplots(3, 2, figsize=(15, 15))
         # Plot distributions
         sns.histplot(df['GRE Score'], kde=True, ax=axes[0, 0], color='skyblue')
         axes[0, 0].set_title('Distribution of GRE Score')
         sns.histplot(df['TOEFL Score'], kde=True, ax=axes[0, 1], color='lightgree
         axes[0, 1].set_title('Distribution of TOEFL Score')
         sns.histplot(df['University Rating'], kde=True, ax=axes[1, 0], color='sal
         axes[1, 0].set_title('Distribution of University Rating')
         sns.histplot(df['SOP'], kde=True, ax=axes[1, 1], color='gold')
         axes[1, 1].set_title('Distribution of SOP Strength')
         sns.histplot(df['CGPA'], kde=True, ax=axes[2, 0], color='purple')
         axes[2, 0].set_title('Distribution of CGPA')
         sns.histplot(df['Chance of Admit '], kde=True, ax=axes[2, 1], color='teal
         axes[2, 1].set_title('Distribution of Chance of Admit')
         plt.tight_layout()
         plt.show()
```



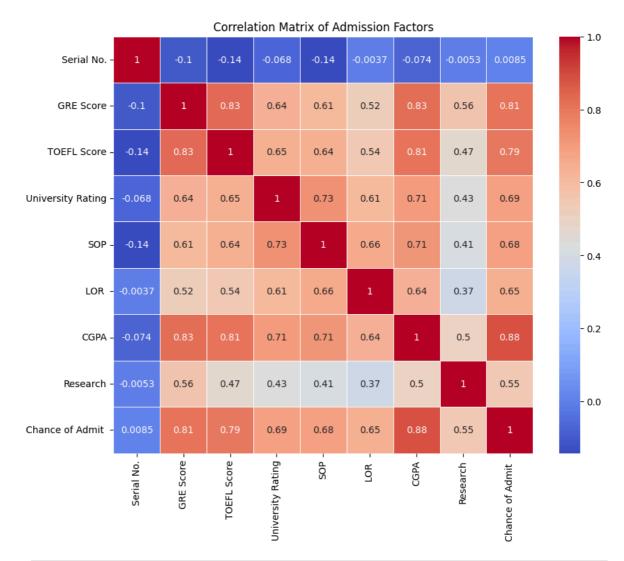
In [62]: # count plot for continous variable
 plt.figure(figsize=(8, 6))
 sns.countplot(x=df['Research'])
 plt.title('Count of Research Experience')
 plt.show()

Count of Research Experience

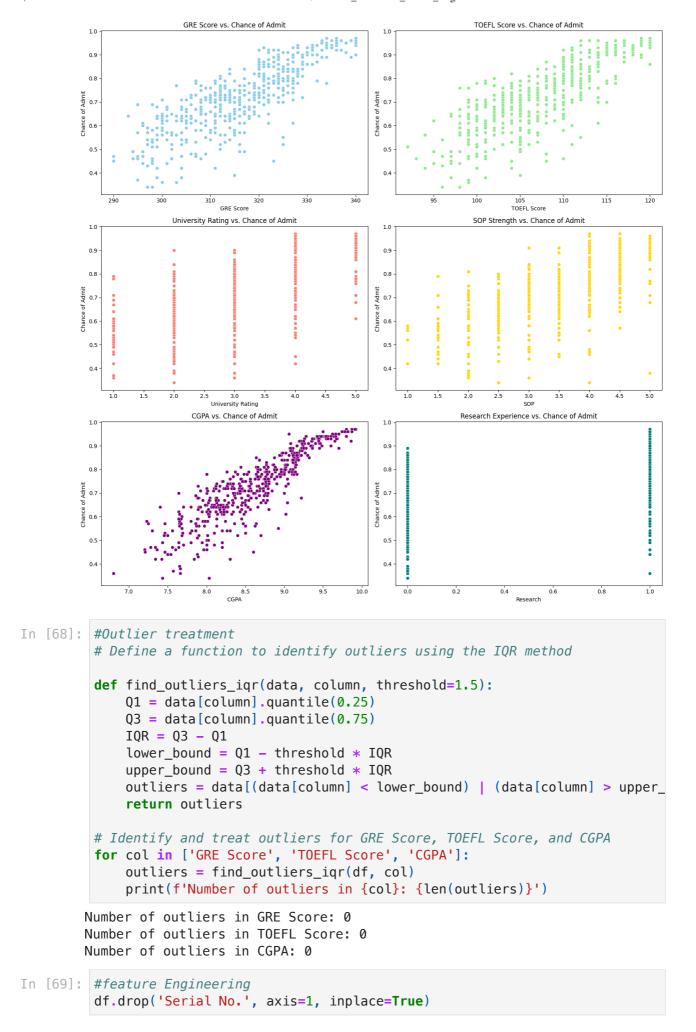


```
In [63]: # Compute the correlation matrix
    correlation_matrix = df.corr()

# Plot the correlation matrix
    plt.figure(figsize=(10, 8))
    sns.heatmap(correlation_matrix, annot=True, cmap='coolwarm', linewidths=0
    plt.title('Correlation Matrix of Admission Factors')
    plt.show()
```



```
In [64]: # Set up scatter plots for bivariate analysis
         fig, axes = plt.subplots(3, 2, figsize=(15, 15))
         # Plot scatter plots
         sns.scatterplot(x=df['GRE Score'], y=df['Chance of Admit '], ax=axes[0, 0
         axes[0, 0].set_title('GRE Score vs. Chance of Admit')
         sns.scatterplot(x=df['TOEFL Score'], y=df['Chance of Admit '], ax=axes[0,
         axes[0, 1].set_title('TOEFL Score vs. Chance of Admit')
         sns.scatterplot(x=df['University Rating'], y=df['Chance of Admit '], ax=a
         axes[1, 0].set_title('University Rating vs. Chance of Admit')
         sns.scatterplot(x=df['SOP'], y=df['Chance of Admit '], ax=axes[1, 1], col
         axes[1, 1].set_title('SOP Strength vs. Chance of Admit')
         sns.scatterplot(x=df['CGPA'], y=df['Chance of Admit '], ax=axes[2, 0], co
         axes[2, 0].set_title('CGPA vs. Chance of Admit')
         sns.scatterplot(x=df['Research'], y=df['Chance of Admit '], ax=axes[2, 1]
         axes[2, 1].set_title('Research Experience vs. Chance of Admit')
         plt.tight_layout()
         plt.show()
```



```
In [71]: # Prepare the data for modeling
         X = df.drop('Chance of Admit ', axis=1)
         y = df['Chance of Admit']
         # Scale the features using StandardScaler
         scaler = StandardScaler()
         X scaled = scaler.fit transform(X)
         # Split the data into training and testing sets
         X_train, X_test, y_train, y_test = train_test_split(X_scaled, y, test_siz
         # Print the shapes of the training and testing sets
         print(f'X_train shape: {X_train.shape}')
         print(f'X_test shape: {X_test.shape}')
         print(f'y_train shape: {y_train.shape}')
         print(f'y_test shape: {y_test.shape}')
        X_train shape: (400, 7)
        X_test shape: (100, 7)
        y_train shape: (400,)
        y_test shape: (100,)
In [73]: #Linear Regression model
         # Build the Linear Regression model
         model = LinearRegression()
         model.fit(X_train, y_train)
         # Print model coefficients with column names
         coefficients = pd.DataFrame({'Feature': X.columns, 'Coefficient': model.c
         print('\nModel Coefficients:')
         print(coefficients)
         # Predict on the test set
         y pred = model.predict(X test)
         print(y_pred)
```

```
Model Coefficients:
            Feature Coefficient
          GRE Score
                       0.027470
1
        TOEFL Score
                        0.018202
2
  University Rating
                       0.002935
3
                S0P
                        0.001796
4
               L0R
                        0.015937
5
               CGPA
                        0.067990
6
           Research
                        0.011927
[0.91457473 0.79518127 0.57265986 0.70736968 0.81588282 0.86206561
 0.47459746 0.64850923 0.82378728 0.80741498 0.72193204 0.72589118
 0.65632227 0.93677168 0.8241518 0.50979177 0.83931942 0.59727295
 0.53339576 0.57155958 0.66548168 0.55305833 0.72232308 0.79506004
 0.78027648 0.60248654 0.94840363 0.84741471 0.62777011 0.74343096
 0.55533035 0.73004034 0.54474225 0.86116288 0.65713016 0.7371816
 0.55423839 0.95718977 0.64364267 0.71057279 0.97036982 0.57495143
 0.67075391 0.85830422 0.94112903 0.57793762 0.9583926 0.83902765
 0.79591651 0.92570648 0.88805969 0.56366238 0.70359711 0.52658929
 0.9536427 0.59746814 0.95600396 0.73916386 0.66256982 0.5012903
 0.62950759 0.68031188 0.59896721 0.59203806 0.44085868 0.58866369
 0.69152566 0.56271019 0.5542953 0.65084583 0.84627224 0.86373777
 0.53729574 0.63142139 0.76958036 0.84812916 0.61693172 0.8471071
 0.73411583 0.6668525 0.60444455 0.73875671 0.78899999 0.66320147
 0.7428225   0.90802002   0.91576583   0.65056489   0.77694407   0.43563138
 0.68664259 0.78598826 0.73469446 0.64865736]
```

```
In [102... #Model Statistics
    # Add a constant to the features
    X_train_sm = sm.add_constant(X_train)

# Build the OLS model
    model_sm = sm.OLS(y_train, X_train_sm)
    model_fitted = model_sm.fit()

# Print the model summary
    print('\nModel Summary:')
    print(model fitted.summary())
```

Model Summary:

OLS Regression Results

=======================================	=======	========	====	======	=========	=======	======	
==== Dep. Variable:	Ch	ance of Adm	it	R-saua	ared:			
0.821				·				
Model: 0.818			0LS	Adj. F	R-squared:			
Method:		Least Squa	res	F-stat	2			
57 . 0				Doorlo	(F -+-+:-+:-)		2 44 -	
Date: -142	Tu	e, 18 Feb 2	025	Prob (F-statistic):			3.41e	
Time:		17:41	:50	Log-L:	56			
1.91								
No. Observatio 108.	ns:		400	AIC:			-1	
Df Residuals:			392	BIC:			-1	
076.								
Df Model:		ط معر معر م	7					
Covariance Typ				=======		=======		
====								
a1	coef	std err		t	P> t	[0.025	0.	
975]								
const	0.7228	0.003	240	ð . 717	0.000	0.717		
0.729 x1	0 0275	0.007		1 106	0 000	0.015		
0.040	0.0273	0.007	2	4.190	0.000	0.013		
x2	0.0182	0.006	3	3.174	0.002	0.007		
0.029	0.0000	0.005	,	0 611	0 544	0 007		
x3 0.012	0.0029	0.005	(0.611	0.541	-0.007		
x4	0.0018	0.005	(ð . 357	0.721	-0.008		
0.012								
x5 0.024	0.0159	0.004	3	3.761	0.000	0.008		
x6	0.0680	0.007	10	0.444	0.000	0.055		
0.081								
x7	0.0119	0.004	3	3.231	0.001	0.005		
0.019 ========	=======	:=======	====	=======	=========	=======	======	
====								
Omnibus:		86.	232	Durbin	n-Watson:			
2.050 Prob(Omnibus):		0	000	larque	e-Bera (JB):		19	
0.099		0.	000	Jarque	e-bera (5b).		19	
Skew:		-1.	107	Prob(3	JB):		5.25	
e-42		F	1	Canal	Na			
Kurtosis: 5.72		5.	551	Cond.	INO .			
=======================================			====					
====								

Notes:

 $\[1\]$ Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
In [77]: # Ridge Regression
         ridge = Ridge(alpha=1.0)
         ridge.fit(X_train, y_train)
         y_pred_ridge = ridge.predict(X_test)
         # Lasso Regression
         lasso = Lasso(alpha=0.1)
         lasso.fit(X_train, y_train)
         y_pred_lasso = lasso.predict(X_test)
In [103... # Calculate VIF scores
         vif = pd.DataFrame()
         vif['Feature'] = X.columns
         vif['VIF'] = [variance_inflation_factor(X.values, i) for i in range(X.sha
         print('\nVIF Scores:')
         print(vif)
        VIF Scores:
                     Feature
                                       VTF
        0
                   GRE Score 1308.061089
                 T0EFL Score 1215,951898
        2 University Rating
                                20.933361
        3
                         S0P
                                 35,265006
        4
                        L0R
                                30.911476
        5
                        CGPA 950.817985
                                 2.869493
                    Research
In [110... # Drop variables with VIF > 5 iteratively
         X \text{ vif} = X.\text{copy()}
         dropped = True
         while dropped:
             vif = pd.DataFrame()
             vif['Feature'] = X_vif.columns
             vif['VIF'] = [variance_inflation_factor(X_vif.values, i) for i in ran
             max_vif = vif['VIF'].max()
             if max_vif > 5:
                 drop_feature = vif.loc[vif['VIF'].idxmax(), 'Feature']
                 X_vif = X_vif.drop(drop_feature, axis=1)
                 print(f'Dropped {drop_feature} due to high VIF')
             else:
                 dropped = False
         print('\nFeatures after VIF reduction:')
         print(X_vif.columns)
         # Scale the features using StandardScaler
         scaler = StandardScaler()
         X_vif_scaled = scaler.fit_transform(X_vif)
         # Split the data into training and testing sets
         X_train_vif, X_test_vif, y_train_vif, y_test_vif = train_test_split(X_vif
         # Build the Linear Regression model
         model_vif = LinearRegression()
         model_vif.fit(X_train_vif, y_train_vif)
         # Predict on the test set
         y_pred_vif = model_vif.predict(X_test_vif)
```

```
Dropped GRE Score due to high VIF
Dropped CGPA due to high VIF
Dropped SOP due to high VIF
Dropped LOR due to high VIF
Dropped University Rating due to high VIF
```

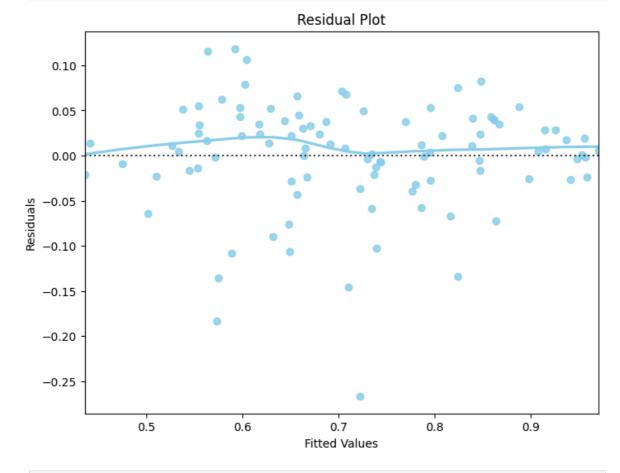
Features after VIF reduction: Index(['TOEFL Score', 'Research'], dtype='object')

```
In [112... #Mean of Residuals
# Calculate residuals
residuals = y_test - y_pred

# Check if the mean of residuals is nearly zero
mean_residuals = np.mean(residuals)
print(f'Mean of residuals: {mean_residuals}')
```

Mean of residuals: -0.0054536237176613465

```
In [113... #Linearity of variables
# Plot residuals vs. fitted values
plt.figure(figsize=(8, 6))
sns.residplot(x=y_pred, y=residuals, lowess=True, color='skyblue')
plt.title('Residual Plot')
plt.xlabel('Fitted Values')
plt.ylabel('Residuals')
plt.show()
```



```
In [115... # Perform the Goldfeld-Quandt test for homoscedasticity
   name = ['F statistic', 'p-value']
   test = sms.het_goldfeldquandt(residuals, X_test)
   print('Goldfeld-Quandt Test:')
   print(lzip(name, test))
```

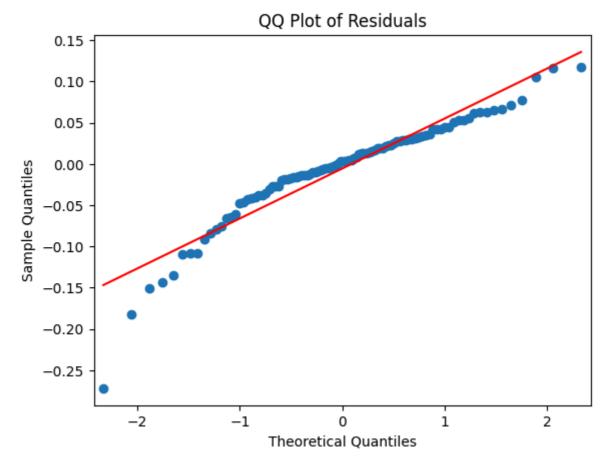
```
Goldfeld-Quandt Test:
[('F statistic', 0.49493874916994285), ('p-value', 0.9883892329316785)]
```

```
In [116... #normality of residuals
# Shapiro-Wilk Test
shapiro_test = shapiro(residuals)
print(f'\nShapiro-Wilk Test: {shapiro_test}')

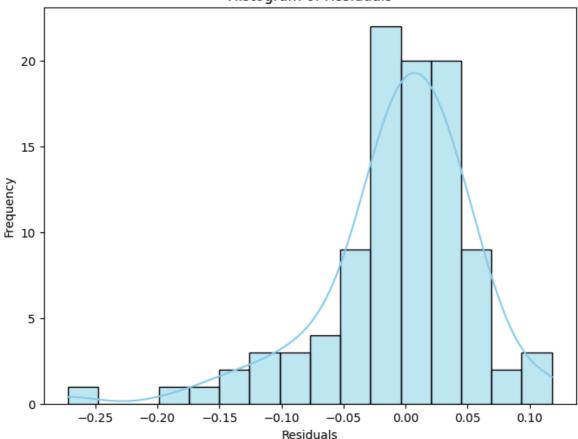
# QQ Plot
sm.qqplot(residuals, line='s')
plt.title('QQ Plot of Residuals')
plt.show()

# Histogram of Residuals
plt.figure(figsize=(8, 6))
sns.histplot(residuals, kde=True, color='skyblue')
plt.title('Histogram of Residuals')
plt.xlabel('Residuals')
plt.ylabel('Frequency')
plt.show()
```

Shapiro-Wilk Test: ShapiroResult(statistic=0.9178703251544267, pvalue=1.08 69980466510536e-05)



Histogram of Residuals



```
In [118... # Calculate evaluation metrics
    mae = mean_absolute_error(y_test, y_pred)
    rmse = np.sqrt(mean_squared_error(y_test, y_pred))
    r2 = r2_score(y_test, y_pred)
    adj_r2 = 1 - (1 - r2) * (len(y_test) - 1) / (len(y_test) - X_test.shape[1]

    print(f'MAE: {mae}')
    print(f'RMSE: {rmse}')
    print(f'R2 Score: {r2}')
    print(f'Adjusted R2 Score: {adj_r2}')
```

MAE: 0.042722654277053664 RMSE: 0.060865880415783113 R2 Score: 0.8188432567829629

Adjusted R2 Score: 0.8050595915381884

```
# Calculate evaluation metrics for Ridge Regression
mae_ridge = mean_absolute_error(y_test, y_pred_ridge)
rmse_ridge = np.sqrt(mean_squared_error(y_test, y_pred_ridge))
r2_ridge = r2_score(y_test, y_pred_ridge)
adj_r2_ridge = 1 - (1 - r2_ridge) * (len(y_test) - 1) / (len(y_test) - X_

print(f'Ridge Regression - MAE: {mae_ridge}')
print(f'Ridge Regression - RMSE: {rmse_ridge}')
print(f'Ridge Regression - R2 Score: {r2_ridge}')
print(f'Ridge Regression - Adjusted R2 Score: {adj_r2_ridge}')
```

Ridge Regression - MAE: 0.04274636477332955 Ridge Regression - RMSE: 0.06087335867674351 Ridge Regression - R2 Score: 0.8187987385531802

Ridge Regression - Adjusted R2 Score: 0.8050116860517917

```
In [121... # Calculate evaluation metrics for Lasso Regression
                       mae_lasso = mean_absolute_error(y_test, y_pred_lasso)
                       rmse_lasso = np.sqrt(mean_squared_error(y_test, y_pred_lasso))
                       r2_lasso = r2_score(y_test, y_pred_lasso)
                       adj_r2_lasso = 1 - (1 - r2_lasso) * (len(y_test) - 1) / (len(y_test) - X_len(y_test) - X_len
                       print(f'Lasso Regression - MAE: {mae lasso}')
                       print(f'Lasso Regression - RMSE: {rmse_lasso}')
                       print(f'Lasso Regression - R2 Score: {r2_lasso}')
                       print(f'Lasso Regression - Adjusted R2 Score: {adj_r2_lasso}')
                    Lasso Regression - MAE: 0.09858647394745274
                    Lasso Regression - RMSE: 0.12296387645200821
                    Lasso Regression - R2 Score: 0.2606300776476902
                    Lasso Regression - Adjusted R2 Score: 0.20437367051218847
In [124... # Calculate evaluation metrics for VIF reduced model
                       mae_vif = mean_absolute_error(y_test_vif, y_pred_vif)
                       rmse_vif = np.sqrt(mean_squared_error(y_test_vif, y_pred_vif))
                       r2_vif = r2_score(y_test_vif, y_pred_vif)
                       adj_r2\_vif = 1 - (1 - r2\_vif) * (len(y_test_vif) - 1) / (len(y_test_vif))
                       print(f'VIF Reduced Model - MAE: {mae_vif}')
                       print(f'VIF Reduced Model - RMSE: {rmse_vif}')
                       print(f'VIF Reduced Model - R2 Score: {r2_vif}')
                       print(f'VIF Reduced Model - Adjusted R2 Score: {adj_r2_vif}')
                    VIF Reduced Model - MAE: 0.0623718521016161
                    VIF Reduced Model - RMSE: 0.08043761005252416
                    VIF Reduced Model - R2 Score: 0.6836083564321792
                    VIF Reduced Model - Adjusted R2 Score: 0.6770848173895437
  In [ ]:
  In []:
```