



# Chapter 8: Relational Database Design

Database System Concepts, 6<sup>th</sup> Ed.

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# Chapter 8: Relational Database Design

- Features of Good Relational Design
- Atomic Domains and First Normal Form
- Decomposition Using Functional Dependencies
- Functional Dependency Theory
- Algorithms for Functional Dependencies
- Database-Design Process
- Modeling Temporal Data



# Combine Schemas?

- Suppose we combine *instructor* and *department* into *inst\_dept*
  - (*No connection to relationship set inst\_dept*)
- Result is possible repetition of information

| <i>ID</i> | <i>name</i> | <i>salary</i> | <i>dept_name</i> | <i>building</i> | <i>budget</i> |
|-----------|-------------|---------------|------------------|-----------------|---------------|
| 22222     | Einstein    | 95000         | Physics          | Watson          | 70000         |
| 12121     | Wu          | 90000         | Finance          | Painter         | 120000        |
| 32343     | El Said     | 60000         | History          | Painter         | 50000         |
| 45565     | Katz        | 75000         | Comp. Sci.       | Taylor          | 100000        |
| 98345     | Kim         | 80000         | Elec. Eng.       | Taylor          | 85000         |
| 76766     | Crick       | 72000         | Biology          | Watson          | 90000         |
| 10101     | Srinivasan  | 65000         | Comp. Sci.       | Taylor          | 100000        |
| 58583     | Califieri   | 62000         | History          | Painter         | 50000         |
| 83821     | Brandt      | 92000         | Comp. Sci.       | Taylor          | 100000        |
| 15151     | Mozart      | 40000         | Music            | Packard         | 80000         |
| 33456     | Gold        | 87000         | Physics          | Watson          | 70000         |
| 76543     | Singh       | 80000         | Finance          | Painter         | 120000        |



# A Combined Schema Without Repetition

- Consider combining relations
  - $\text{sec\_class}(\text{course\_id}, \text{sec\_id}, \text{semester}, \text{year}, \text{building}, \text{room\_number})$  and
  - $\text{section}(\text{course\_id}, \text{sec\_id}, \text{semester}, \text{year})$
- into one relation
- $\text{section}(\text{course\_id}, \text{sec\_id}, \text{semester}, \text{year}, \text{building}, \text{room\_number})$
- No repetition in this case



# What About Smaller Schemas?

- Suppose we had started with *inst\_dept*. How would we know to split up (**decompose**) it into *instructor* and *department*?
- Write a rule “if there were a schema (*dept\_name*, *building*, *budget*), then *dept\_name* would be a candidate key”
- Denote as a **functional dependency**:  
$$\text{dept\_name} \rightarrow \text{building}, \text{budget}$$
- In *inst\_dept*, because *dept\_name* is not a candidate key, the building and budget of a department may have to be repeated.
  - This indicates the need to decompose *inst\_dept*

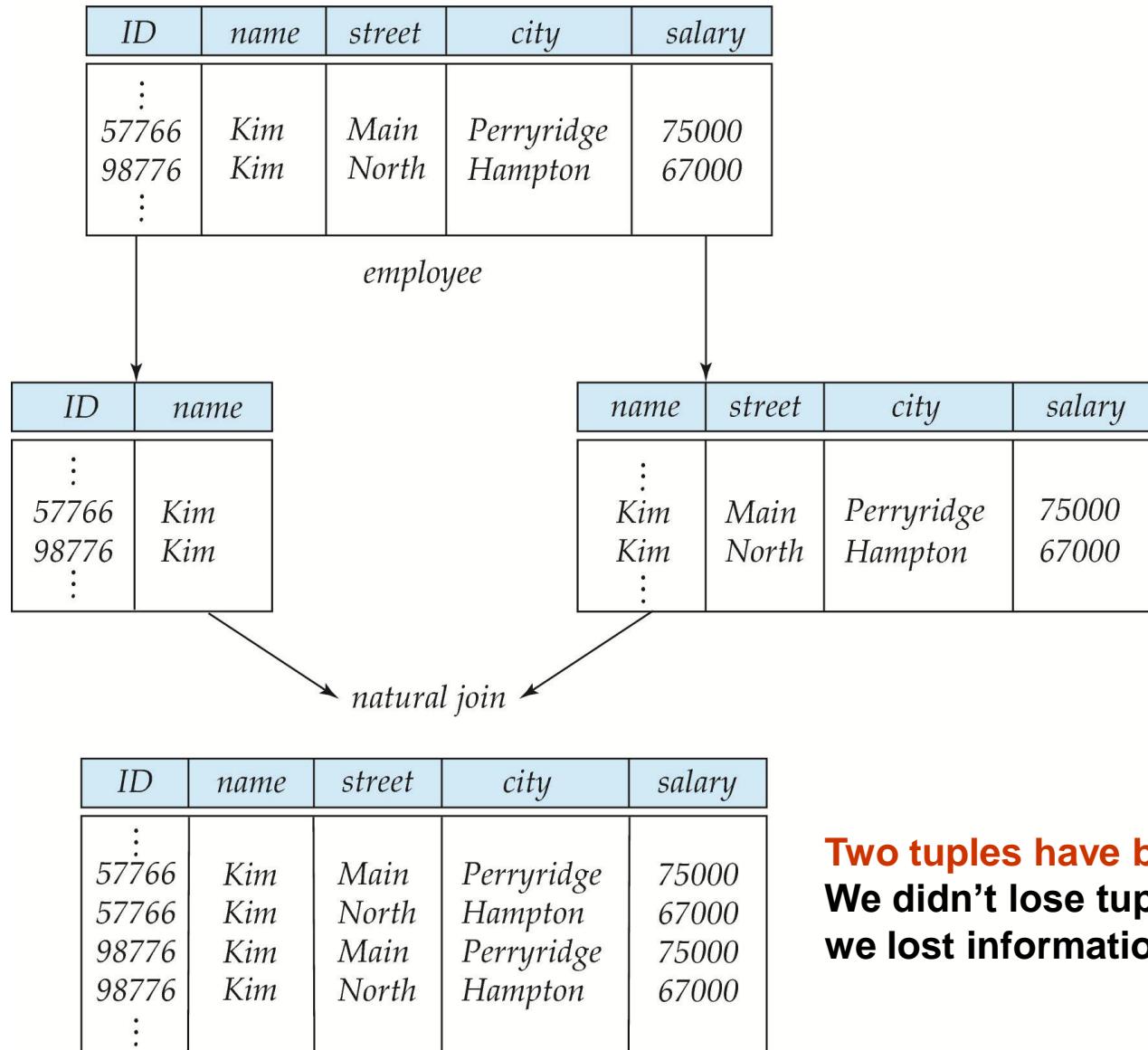


# Lossy Decomposition

- Not all decompositions are good. Suppose we decompose  $\text{employee}(ID, name, street, city, salary)$  into  
 $\text{employee1 } (ID, name)$   
 $\text{employee2 } (name, street, city, salary)$
- The next slide shows how we lose information -- we cannot reconstruct the original  $\text{employee}$  relation -- and so, this is a **lossy decomposition**.



# A Lossy Decomposition





# Example of Lossless-Join Decomposition

- **Lossless join decomposition**
- Decomposition of  $R = (A, B, C)$   
 $R_1 = (A, B)$        $R_2 = (B, C)$

|          |   |   |
|----------|---|---|
| A        | B | C |
| $\alpha$ | 1 | A |
| $\beta$  | 2 | B |

$r$

|          |   |
|----------|---|
| A        | B |
| $\alpha$ | 1 |
| $\beta$  | 2 |

$\Pi_{A,B}(r)$

|   |   |
|---|---|
| B | C |
| 1 | A |
| 2 | B |

$\Pi_{B,C}(r)$

$\Pi_A(r) \bowtie \Pi_B(r)$

|          |   |   |
|----------|---|---|
| A        | B | C |
| $\alpha$ | 1 | A |
| $\beta$  | 2 | B |

*In general decomposition is lossless provided certain functional dependencies hold; more on this later.*



# First Normal Form

- Domain is **atomic** if its elements are considered to be indivisible units
  - Examples of non-atomic domains:
    - ▶ Set of names, composite attributes
    - ▶ Identification numbers like CS101 that can be broken up into parts
- A relational schema R is in **first normal form** if the domains of all attributes of R are atomic
- Non-atomic values complicate storage and encourage redundant (repeated) storage of data
  - Example: Set of accounts stored with each customer, and set of owners stored with each account
  - We assume all relations are in first normal form (and revisit this in Chapter 22: Object Based Databases)



# First Normal Form (Cont'd)

- Atomicity is actually a property of how the elements of the domain are used.
  - Example: Strings would normally be considered indivisible
  - Suppose that students are given roll numbers which are strings of the form CS0012 or EE1127
  - If the first two characters are extracted to find the department, the domain of roll numbers is not atomic.
  - Doing so is a bad idea: leads to encoding of information in application program rather than in the database.



# Goal — Devise a Theory for the Following

- Decide whether a particular relation  $R$  is in “good” form.
- In the case that a relation  $R$  is not in “good” form, decompose it into a set of relations  $\{R_1, R_2, \dots, R_n\}$  such that
  - each relation is in good form
  - the decomposition is a lossless-join decomposition
- Our theory is based on:
  - functional dependencies
  - multivalued dependencies (see book for details)



# Functional Dependencies

- Constraints on the set of legal relations.
- Require that the value for a certain set of attributes determines uniquely the value for another set of attributes.
- A functional dependency is a generalization of the notion of a key.



# Functional Dependencies (Cont.)

- Let  $R$  be a relation schema

$$\alpha \subseteq R \text{ and } \beta \subseteq R$$

- The **functional dependency**

$$\alpha \rightarrow \beta$$

**holds on**  $R$  if and only if for any legal relations  $r(R)$ , whenever any two tuples  $t_1$  and  $t_2$  of  $r$  agree on the attributes  $\alpha$ , they also agree on the attributes  $\beta$ . That is,

$$t_1[\alpha] = t_2[\alpha] \Rightarrow t_1[\beta] = t_2[\beta]$$

- Example: Consider  $r(A,B)$  with the following instance of  $r$ .

|   |   |
|---|---|
| 1 | 4 |
| 1 | 5 |
| 3 | 7 |

- On this instance,  $A \rightarrow B$  does **NOT** hold, but  $B \rightarrow A$  does hold.



# Functional Dependencies (Cont.)

- $K$  is a superkey for relation schema  $R$  if and only if  $K \rightarrow R$
- $K$  is a candidate key for  $R$  if and only if
  - $K \rightarrow R$ , and
  - for no  $\alpha \subset K$ ,  $\alpha \rightarrow R$
- Functional dependencies allow us to express constraints that cannot be expressed using superkeys. Consider the schema:  
*inst\_dept (ID, name, salary, dept\_name, building, budget).*

We expect these functional dependencies to hold:

$dept\_name \rightarrow building$

and             $ID \rightarrow building$

but would not expect the following to hold:

$dept\_name \rightarrow salary$



# Use of Functional Dependencies

- We use functional dependencies to:
  - test relations to see if they are legal under a given set of functional dependencies.
    - ▶ If a relation  $r$  is legal under a set  $F$  of functional dependencies, we say that  $r$  **satisfies**  $F$ .
  - specify constraints on the set of legal relations
    - ▶ We say that  $F$  **holds on**  $R$  if all legal relations on  $R$  satisfy the set of functional dependencies  $F$ .
- Note: A specific instance of a relation schema may satisfy a functional dependency even if the functional dependency does not hold on all legal instances.
  - For example, a specific instance of *instructor* may, by chance, satisfy
$$name \rightarrow ID.$$



# Functional Dependencies (Cont.)

- A functional dependency is **trivial** if it is satisfied by all instances of a relation
  - Example:
    - ▶  $ID, name \rightarrow ID$
    - ▶  $name \rightarrow name$
  - In general,  $\alpha \rightarrow \beta$  is trivial if  $\beta \subseteq \alpha$



# Closure of a Set of Functional Dependencies

- Given a set  $F$  of functional dependencies, there are certain other functional dependencies that are logically implied by  $F$ .
  - For example: If  $A \rightarrow B$  and  $B \rightarrow C$ , then we can infer that  $A \rightarrow C$
  - More on functional dependency inference later...
- The set of **all** functional dependencies logically implied by  $F$  is the **closure** of  $F$ .
- We denote the *closure* of  $F$  by  $F^+$ .
- $F^+$  is a superset of  $F$ .



# Boyce-Codd Normal Form

A relation schema  $R$  is in BCNF with respect to a set  $F$  of functional dependencies if for all functional dependencies in  $F^+$  of the form

$$\alpha \rightarrow \beta$$

where  $\alpha \subseteq R$  and  $\beta \subseteq R$ , at least one of the following holds:

- $\alpha \rightarrow \beta$  is trivial (i.e.,  $\beta \subseteq \alpha$ )
- $\alpha$  is a superkey for  $R$

Example schema *not* in BCNF:

*instr\_dept (ID, name, salary, dept\_name, building, budget )*

because  $dept\_name \rightarrow building, budget$   
holds on *instr\_dept*, but *dept\_name* is not a superkey



# Decomposing a Schema into BCNF

- Suppose we have a schema  $R$  and a non-trivial dependency  $\alpha \rightarrow \beta$  causes a violation of BCNF.

We decompose  $R$  into:

- $(\alpha \cup \beta)$
- $(R - (\beta - \alpha))$

- In our example,

- $\alpha = \text{dept\_name}$
- $\beta = \text{building}, \text{budget}$

and  $\text{inst\_dept}$  is replaced by

- $(\alpha \cup \beta) = (\text{dept\_name}, \text{building}, \text{budget})$
- $(R - (\beta - \alpha)) = (\text{ID}, \text{name}, \text{salary}, \text{dept\_name})$



# BCNF and Dependency Preservation

- Constraints, including functional dependencies, are costly to check in practice unless they pertain to only one relation
- If it is sufficient to test only those dependencies on each individual relation of a decomposition in order to ensure that *all* functional dependencies hold, then that decomposition is *dependency preserving*.
- Because it is not always possible to achieve both BCNF and dependency preservation, we consider a weaker normal form, known as *third normal form*.



# Third Normal Form

- A relation schema  $R$  is in **third normal form (3NF)** if for all:

$$\alpha \rightarrow \beta \text{ in } F^+$$

at least one of the following holds:

- $\alpha \rightarrow \beta$  is trivial (i.e.,  $\beta \in \alpha$ )
- $\alpha$  is a superkey for  $R$
- Each attribute  $A$  in  $\beta - \alpha$  is contained in a candidate key for  $R$ .

(**NOTE**: each attribute may be in a different candidate key)

- If a relation is in BCNF it is in 3NF (since in BCNF one of the first two conditions above must hold).
- Third condition is a minimal relaxation of BCNF to ensure dependency preservation (will see why later).



# Goals of Normalization

- Let  $R$  be a relation schema with a set  $F$  of functional dependencies.
- Decide whether a relation schema  $R$  is in “good” form.
- In the case that a relation schema  $R$  is not in “good” form, decompose it into a set of relation schema  $\{R_1, R_2, \dots, R_n\}$  such that
  - each relation schema is in good form
  - the decomposition is a lossless-join decomposition
  - Preferably, the decomposition should be dependency preserving.



# Functional-Dependency Theory

- We now consider the formal theory that tells us which functional dependencies are implied logically by a given set of functional dependencies.
- We then develop algorithms to generate lossless decompositions into BCNF and 3NF
- We then develop algorithms to test if a decomposition is dependency-preserving



# Closure of a Set of Functional Dependencies

- Given a set  $F$  of functional dependencies, there are certain other functional dependencies that are logically implied by  $F$ .
  - For e.g.: If  $A \rightarrow B$  and  $B \rightarrow C$ , then we can infer that  $A \rightarrow C$
- The set of **all** functional dependencies logically implied by  $F$  is the **closure** of  $F$ .
- We denote the *closure* of  $F$  by  $F^+$ .



# Closure of a Set of Functional Dependencies

- We can find  $F^+$ , the closure of  $F$ , by repeatedly applying **Armstrong's Axioms**:
  - if  $\beta \subseteq \alpha$ , then  $\alpha \rightarrow \beta$  **(reflexivity)**
  - if  $\alpha \rightarrow \beta$ , then  $\gamma \alpha \rightarrow \gamma \beta$  **(augmentation)**
  - if  $\alpha \rightarrow \beta$ , and  $\beta \rightarrow \gamma$ , then  $\alpha \rightarrow \gamma$  **(transitivity)**
- These rules are
  - **sound** (generate only functional dependencies that actually hold), and
  - **complete** (generate all functional dependencies that hold).



# Example

■  $R = (A, B, C, G, H, I)$

$F = \{ A \rightarrow B$

$A \rightarrow C$

$CG \rightarrow H$

$CG \rightarrow I$

$B \rightarrow H\}$

■ some members of  $F^+$

- $A \rightarrow H$

- ▶ by transitivity from  $A \rightarrow B$  and  $B \rightarrow H$

- $AG \rightarrow I$

- ▶ by augmenting  $A \rightarrow C$  with  $G$ , to get  $AG \rightarrow CG$  and then transitivity with  $CG \rightarrow I$

**Quiz Q1:** Given the above FDs, the functional dependency  $AB \rightarrow B$

(1) cannot be inferred (2) can be inferred using transitivity

(3) can be inferred using reflexivity (4) can be inferred using augmentation



# Closure of Functional Dependencies (Cont.)

## ■ Additional rules:

- If  $\alpha \rightarrow \beta$  holds and  $\alpha \rightarrow \gamma$  holds, then  $\alpha \rightarrow \beta\gamma$  holds (**union**)
- If  $\alpha \rightarrow \beta\gamma$  holds, then  $\alpha \rightarrow \beta$  holds and  $\alpha \rightarrow \gamma$  holds (**decomposition**)
- If  $\alpha \rightarrow \beta$  holds and  $\beta \rightarrow \delta$  holds, then  $\alpha\beta \rightarrow \delta$  holds (**pseudotransitivity**)

The above rules can be inferred from Armstrong's axioms.

**Quiz Q2:** Given a schema  $r(A, B, C, D)$  with functional dependencies  $A \rightarrow B$  and  $B \rightarrow C$ , then which of the following is a candidate key for  $r$ ?

- (1) A      (2) AC      (3) AD      (4) ABD)



# Closure of Attribute Sets

- Given a set of attributes  $\alpha$ , define the ***closure*** of  $\alpha$  **under  $F$**  (denoted by  $\alpha^+$ ) as the set of attributes that are functionally determined by  $\alpha$  under  $F$
- Algorithm to compute  $\alpha^+$ , the closure of  $\alpha$  under  $F$

```
result :=  $\alpha$ ;  
while (changes to result) do  
  for each  $\beta \rightarrow \gamma$  in  $F$  do  
    begin  
      if  $\beta \subseteq result$  then result := result  $\cup$   $\gamma$   
    end
```



# Example of Attribute Set Closure

- $R = (A, B, C, G, H, I)$
- $F = \{A \rightarrow B, CG \rightarrow H, B \rightarrow H, A \rightarrow C, CG \rightarrow I\}$
- $(AG)^+$ 
  1.  $result = AG$
  2.  $result = ABCG$  ( $A \rightarrow C$  and  $A \rightarrow B$ )
  3.  $result = ABCGH$  ( $CG \rightarrow H$  and  $CG \subseteq AGBC$ )
  4.  $result = ABCGHI$  ( $CG \rightarrow I$  and  $CG \subseteq AGBCH$ )
- Is  $AG$  a candidate key?
  1. Is  $AG$  a super key?
    1. Does  $AG \rightarrow R$ ? == Is  $(AG)^+ \supseteq R$
    2. Is any subset of  $AG$  a superkey?
      1. Does  $A \rightarrow R$ ? == Is  $(A)^+ \supseteq R$
      2. Does  $G \rightarrow R$ ? == Is  $(G)^+ \supseteq R$



# Quiz Time

**Quiz Q3:** Given the functional dependencies

$A \rightarrow B$ ,  $B \rightarrow CD$  and  $DE \rightarrow F$

the attribute closure  $A^+$  is:

- (1) ABC
- (2) ABCD
- (3) BCD
- (4) ABCDF



# Uses of Attribute Closure

There are several uses of the attribute closure algorithm:

- Testing for superkey:
  - To test if  $\alpha$  is a superkey, we compute  $\alpha^+$ , and check if  $\alpha^+$  contains all attributes of  $R$ .
- Testing functional dependencies
  - To check if a functional dependency  $\alpha \rightarrow \beta$  holds (or, in other words, is in  $F^+$ ), just check if  $\beta \subseteq \alpha^+$ .
  - That is, we compute  $\alpha^+$  by using attribute closure, and then check if it contains  $\beta$ .
  - Is a simple and cheap test, and very useful
- Computing closure of  $F$ 
  - For each  $\gamma \subseteq R$ , we find the closure  $\gamma^+$ , and for each  $S \subseteq \gamma^+$ , we output a functional dependency  $\gamma \rightarrow S$ .



# Lossless-join Decomposition

- For the case of  $R = (R_1, R_2)$ , we require that for all possible relations  $r$  on schema  $R$

$$r = \Pi_{R1}(r) \bowtie \Pi_{R2}(r)$$

- A decomposition of  $R$  into  $R_1$  and  $R_2$  is lossless join if at least one of the following dependencies is in  $F^+$ :
  - $R_1 \cap R_2 \rightarrow R_1$
  - $R_1 \cap R_2 \rightarrow R_2$
- The above functional dependencies are a sufficient condition for lossless join decomposition; the dependencies are a necessary condition only if all constraints are functional dependencies



# Example

- $R = (A, B, C)$   
 $F = \{A \rightarrow B, B \rightarrow C\}$ 
  - Can be decomposed in two different ways
- $R_1 = (A, B), \quad R_2 = (B, C)$ 
  - Lossless-join decomposition:
$$R_1 \cap R_2 = \{B\} \text{ and } B \rightarrow BC$$
    - Dependency preserving
- $R_1 = (A, B), \quad R_2 = (A, C)$ 
  - Lossless-join decomposition:
$$R_1 \cap R_2 = \{A\} \text{ and } A \rightarrow AB$$
    - Not dependency preserving  
(cannot check  $B \rightarrow C$  without computing  $R_1 \bowtie R_2$ )



# Dependency Preservation

- Let  $F_i$  be the set of dependencies  $F^+$  that include only attributes in  $R_i$ .
  - ▶ A decomposition is **dependency preserving**, if
$$(F_1 \cup F_2 \cup \dots \cup F_n)^+ = F^+$$
  - ▶ If it is not, then checking updates for violation of functional dependencies may require computing joins, which is expensive.
- See book for efficient algorithm for checking dependency preservation



# Example

- $R = (A, B, C)$   
 $F = \{A \rightarrow B$   
 $\quad B \rightarrow C\}$   
Key = {A}
- $R$  is not in BCNF
- Decomposition  $R_1 = (A, B)$ ,  $R_2 = (B, C)$ 
  - $R_1$  and  $R_2$  in BCNF
  - Lossless-join decomposition
  - Dependency preserving



# Testing for BCNF

- To check if a non-trivial dependency  $\alpha \rightarrow \beta$  causes a violation of BCNF
  1. compute  $\alpha^+$  (the attribute closure of  $\alpha$ ), and
  2. verify that it includes all attributes of  $R$ , that is, it is a superkey of  $R$ .
- **Simplified test:** To check if a relation schema  $R$  is in BCNF, it suffices to check only the dependencies in the given set  $F$  for violation of BCNF, rather than checking all dependencies in  $F^+$ .
  - If none of the dependencies in  $F$  causes a violation of BCNF, then none of the dependencies in  $F^+$  will cause a violation of BCNF.
- However, **simplified test using only  $F$  is incorrect when testing a relation in a decomposition of  $R$** 
  - Consider  $R = (A, B, C, D, E)$ , with  $F = \{ A \rightarrow B, BC \rightarrow D \}$ 
    - ▶ Decompose  $R$  into  $R_1 = (A, B)$  and  $R_2 = (A, C, D, E)$
    - ▶ Neither of the dependencies in  $F$  contain only attributes from  $(A, C, D, E)$  so we might be misled into thinking  $R_2$  satisfies BCNF.
    - ▶ In fact, dependency  $AC \rightarrow D$  in  $F^+$  shows  $R_2$  is not in BCNF.



# Testing Decomposition for BCNF

- To check if a relation  $R_i$  in a decomposition of  $R$  is in BCNF,
  - Either test  $R_i$  for BCNF with respect to the **restriction** of  $F$  to  $R_i$  (that is, all FDs in  $F^+$  that contain only attributes from  $R_i$ )
  - or use the original set of dependencies  $F$  that hold on  $R$ , but with the following test:
    - for every set of attributes  $\alpha \subseteq R_i$ , check that  $\alpha^+$  (the attribute closure of  $\alpha$ ) either includes no attribute of  $R_i - \alpha$ , or includes all attributes of  $R_i$ .
- ▶ If the condition is violated by some  $\alpha \rightarrow \beta$  in  $F$ , the dependency
$$\alpha \rightarrow (\alpha^+ - \alpha) \cap R_i$$
can be shown to hold on  $R_i$ , and  $R_i$  violates BCNF.
- ▶ We use above dependency to decompose  $R_i$

E.g. given  $\{ A \rightarrow B, BC \rightarrow D \}$  and decomposition  $R1 (A,B)$  and  $R2 (A,C,D, E)$ ,  $AC^+ = ABCD$ , so  $R2$  violates BCNF due to the dependency  $AC \rightarrow D$



# BCNF Decomposition Algorithm

```
result := {R};  
done := false;  
compute  $F^+$ ;  
while (not done) do  
  if (there is a schema  $R_i$  in result that is not in BCNF)  
    then begin  
      let  $\alpha \rightarrow \beta$  be a nontrivial functional dependency that  
      holds on  $R_i$ , such that  $\alpha \rightarrow R_i$  is not in  $F^+$ ,  
      and  $\alpha \cap \beta = \emptyset$ ;  
      result := (result -  $R_i$ )  $\cup$  ( $R_i - \beta$ )  $\cup$  ( $\alpha, \beta$ );  
    end  
  else done := true;
```

Note: each  $R_i$  is in BCNF, and decomposition is lossless-join.



# Example of BCNF Decomposition

- $R = (A, B, C)$   
 $F = \{A \rightarrow B$   
 $\quad B \rightarrow C\}$   
Key = {A}
- $R$  is not in BCNF ( $B \rightarrow C$  but  $B$  is not superkey)
- Decomposition
  - $R_1 = (B, C)$
  - $R_2 = (A, B)$

**Quiz Q4:** Given relation  $r(A, B, C, D)$  and the functional dependency  $A \rightarrow CD$  the BCNF decomposition is:

- (1) ABC, ACD
- (2) AB, ACD
- (3) AB, BCD
- (4) ABC, CD



# Example of BCNF Decomposition

- *class (course\_id, title, dept\_name, credits, sec\_id, semester, year, building, room\_number, capacity, time\_slot\_id)*
- Functional dependencies:
  - $\text{course\_id} \rightarrow \text{title}, \text{dept\_name}, \text{credits}$
  - $\text{building}, \text{room\_number} \rightarrow \text{capacity}$
  - $\text{course\_id}, \text{sec\_id}, \text{semester}, \text{year} \rightarrow \text{building}, \text{room\_number}, \text{time\_slot\_id}$
- A candidate key  $\{\text{course\_id}, \text{sec\_id}, \text{semester}, \text{year}\}$ .
- BCNF Decomposition:
  - $\text{course\_id} \rightarrow \text{title}, \text{dept\_name}, \text{credits}$  holds
    - ▶ but  $\text{course\_id}$  is not a superkey.
  - We replace *class* by:
    - ▶ *course(course\_id, title, dept\_name, credits)*
    - ▶ *class-1 (course\_id, sec\_id, semester, year, building, room\_number, capacity, time\_slot\_id)*



# BCNF Decomposition (Cont.)

- *course* is in BCNF
  - How do we know this?
- *building, room\_number*→*capacity* holds on *class-1*
  - but {*building, room\_number*} is not a superkey for *class-1*.
  - We replace *class-1* by:
    - ▶ *classroom* (*building, room\_number, capacity*)
    - ▶ *section* (*course\_id, sec\_id, semester, year, building, room\_number, time\_slot\_id*)
- *classroom* and *section* are in BCNF.



# BCNF and Dependency Preservation

It is not always possible to get a BCNF decomposition that is dependency preserving

- $R = (J, K, L)$   
 $F = \{JK \rightarrow L$   
 $L \rightarrow K\}$

Two candidate keys =  $JK$  and  $JL$

- $R$  is not in BCNF
- Any decomposition of  $R$  will fail to preserve

$$JK \rightarrow L$$

This implies that testing for  $JK \rightarrow L$  requires a join



# Third Normal Form: Motivation

- There are some situations where
  - BCNF is not dependency preserving, and
  - efficient checking for FD violation on updates is important
- Solution: define a weaker normal form, called Third Normal Form (3NF)
  - Allows some redundancy (with resultant problems; we will see examples later)
  - But functional dependencies can be checked on individual relations without computing a join.
  - There is always a lossless-join, dependency-preserving decomposition into 3NF.



# Third Normal Form

- A relation schema  $R$  is in **third normal form (3NF)** if for all:

$$\alpha \rightarrow \beta \text{ in } F^+$$

at least one of the following holds:

- $\alpha \rightarrow \beta$  is trivial (i.e.,  $\beta \in \alpha$ )
- $\alpha$  is a superkey for  $R$
- Each attribute  $A$  in  $\beta - \alpha$  is contained in a candidate key for  $R$ .  
**(NOTE:** each attribute may be in a different candidate key)

- If a relation is in BCNF it is in 3NF (since in BCNF one of the first two conditions above must hold).
- Third condition is a minimal relaxation of BCNF to ensure dependency preservation (will see why later).



# 3NF Example

## ■ Relation *dept\_advisor*:

- $\text{dept\_advisor}(s\_ID, i\_ID, \text{dept\_name})$   
 $F = \{s\_ID, \text{dept\_name} \rightarrow i\_ID, i\_ID \rightarrow \text{dept\_name}\}$ 
  - ▶ i.e. a student can have at most one advisor in a department
- Two candidate keys:  $s\_ID, \text{dept\_name}$ , and  $i\_ID, s\_ID$
- $R$  is in 3NF
  - ▶  $s\_ID, \text{dept\_name} \rightarrow i\_ID$ 
    - $s\_ID, \text{dept\_name}$  is a superkey
  - ▶  $i\_ID \rightarrow \text{dept\_name}$ 
    - $\text{dept\_name}$  is contained in a candidate key



# Redundancy in 3NF

- There is some redundancy in this schema
- Example of problems due to redundancy in 3NF

- $R = (J, K, L)$

- $F = \{JK \rightarrow L, L \rightarrow K\}$

| $J$         | $L$   | $K$   |
|-------------|-------|-------|
| $j_1$       | $l_1$ | $k_1$ |
| $j_2$       | $l_1$ | $k_1$ |
| $j_3$       | $l_1$ | $k_1$ |
| <i>null</i> | $l_2$ | $k_2$ |

- repetition of information (e.g., the relationship  $l_1, k_1$ )
  - ( $i\_ID, dept\_name$ )
- need to use null values (e.g., to represent the relationship  $l_2, k_2$  where there is no corresponding value for  $J$ ).
  - ( $i\_ID, dept\_name$ ) if there is no separate relation mapping instructors to departments



# Testing for 3NF

- Testing a given schema to see if it satisfies 3NF has been shown to be NP-hard
- Possible to achieve 3NF by repeated decomposition based on finding functional dependencies that show violation of 3NF
  - similar to BCNF decomposition, NP hardness not a big deal since schemas tend to be small
  - BUT does not guarantee dependency preservation
    - ▶ e.g.  $R = (A, B, C)$   
 $F = \{A \rightarrow B, B \rightarrow C\}$ , decomposed using  $A \rightarrow B$
- Coming up: an algorithm to compute a dependency preserving decomposition into third normal form
  - Based on the notion of a “canonical cover”
  - Interestingly, runs in polynomial time, even though testing for 3NF is NP hard



# Canonical Cover

- Sets of functional dependencies may have redundant dependencies that can be inferred from the others
  - For example:  $A \rightarrow C$  is redundant in:  $\{A \rightarrow B, B \rightarrow C, A \rightarrow C\}$
  - Parts of a functional dependency may be redundant
    - ▶ E.g.: on RHS:  $\{A \rightarrow B, B \rightarrow C, A \rightarrow CD\}$  can be simplified to
$$\{A \rightarrow B, B \rightarrow C, A \rightarrow D\}$$
    - ▶ E.g.: on LHS:  $\{A \rightarrow B, B \rightarrow C, AC \rightarrow D\}$  can be simplified to
$$\{A \rightarrow B, B \rightarrow C, A \rightarrow D\}$$
- Intuitively, a canonical cover of F is a “minimal” set of functional dependencies equivalent to F, having no redundant dependencies or redundant parts of dependencies



# Extraneous Attributes

- Consider a set  $F$  of functional dependencies and the functional dependency  $\alpha \rightarrow \beta$  in  $F$ .
  - Attribute  $A$  is **extraneous** in  $\alpha$  if  $A \in \alpha$  and  $F$  logically implies  $(F - \{\alpha \rightarrow \beta\}) \cup \{(\alpha - A) \rightarrow \beta\}$ .
  - Attribute  $A$  is **extraneous** in  $\beta$  if  $A \in \beta$  and the set of functional dependencies  $(F - \{\alpha \rightarrow \beta\}) \cup \{\alpha \rightarrow (\beta - A)\}$  logically implies  $F$ .
- Note: implication in the opposite direction is trivial in each of the cases above, since a “stronger” functional dependency always implies a weaker one
- Example: Given  $F = \{A \rightarrow C, AB \rightarrow C\}$ 
  - $B$  is extraneous in  $AB \rightarrow C$  because  $\{A \rightarrow C, AB \rightarrow C\}$  logically implies  $A \rightarrow C$  (I.e. the result of dropping  $B$  from  $AB \rightarrow C$ ).
- Example: Given  $F = \{A \rightarrow C, AB \rightarrow CD\}$ 
  - $C$  is extraneous in  $AB \rightarrow CD$  since  $AB \rightarrow C$  can be inferred even after deleting  $C$



# Testing if an Attribute is Extraneous

- Consider a set  $F$  of functional dependencies and the functional dependency  $\alpha \rightarrow \beta$  in  $F$ .
- To test if attribute  $A \in \alpha$  is extraneous in  $\alpha$ 
  1. compute  $(\{\alpha\} - A)^+$  using the dependencies in  $F$
  2. check that  $(\{\alpha\} - A)^+$  contains  $\beta$ ; if it does,  $A$  is extraneous in  $\alpha$
- To test if attribute  $A \in \beta$  is extraneous in  $\beta$ 
  1. compute  $\alpha^+$  using only the dependencies in
$$F' = (F - \{\alpha \rightarrow \beta\}) \cup \{\alpha \rightarrow (\beta - A)\},$$
  2. check that  $\alpha^+$  contains  $A$ ; if it does,  $A$  is extraneous in  $\beta$

- Example: Given  $F = \{A \rightarrow C, AB \rightarrow C\}$ :  
 $B$  is extraneous in  $AB \rightarrow C$  because  $AB - B = A$ , and  $A^+$  contains  $C$
- Example: Given  $F = \{A \rightarrow C, AB \rightarrow CD\}$ :  
 $C$  is extraneous in  $AB \rightarrow CD$  since  $(AB)^+$  under  $\{A \rightarrow C, AB \rightarrow D\}$   
 $(AB)^+ = ACD$ , which contains  $C$



# Canonical Cover

- A **canonical cover** for  $F$  is a set of dependencies  $F_c$  such that
  - $F$  logically implies all dependencies in  $F_c$ , and
  - $F_c$  logically implies all dependencies in  $F$ , and
  - No functional dependency in  $F_c$  contains an extraneous attribute, and
  - Each left side of functional dependency in  $F_c$  is unique.



# Computing a Canonical Cover

- To compute a canonical cover for  $F$ :  
**repeat**

    Use the union rule to replace any dependencies in  $F$

$\alpha_1 \rightarrow \beta_1$  and  $\alpha_1 \rightarrow \beta_2$  with  $\alpha_1 \rightarrow \beta_1 \beta_2$

    Find a functional dependency  $\alpha \rightarrow \beta$  with an  
        extraneous attribute either in  $\alpha$  or in  $\beta$

        /\* Note: test for extraneous attributes done using  $F_c$ , not  $F^*$  \*/

    If an extraneous attribute is found, delete it from  $\alpha \rightarrow \beta$

**until**  $F$  does not change

- Note: Union rule may become applicable after some extraneous attributes have been deleted, so it has to be re-applied



# Computing a Canonical Cover

- $R = (A, B, C)$   
 $F = \{A \rightarrow BC$   
 $\quad B \rightarrow C$   
 $\quad A \rightarrow B$   
 $\quad AB \rightarrow C\}$
- Combine  $A \rightarrow BC$  and  $A \rightarrow B$  into  $A \rightarrow BC$ 
  - Set is now  $\{A \rightarrow BC, B \rightarrow C, AB \rightarrow C\}$
- $A$  is extraneous in  $AB \rightarrow C$ 
  - Check if the result of deleting  $A$  from  $AB \rightarrow C$  is implied by the other dependencies
    - ▶ Yes: in fact,  $B \rightarrow C$  is already present!
  - Set is now  $\{A \rightarrow BC, B \rightarrow C\}$
- $C$  is extraneous in  $A \rightarrow BC$ 
  - Check if  $A \rightarrow C$  is logically implied by  $A \rightarrow B$  and the other dependencies
    - ▶ Yes: using transitivity on  $A \rightarrow B$  and  $B \rightarrow C$ .
      - Can use attribute closure of  $A$  in more complex cases
- The canonical cover is:  
 $A \rightarrow B$   
 $B \rightarrow C$



# 3NF Decomposition Algorithm

Let  $F_c$  be a canonical cover for  $F$ ;

$i := 0$ ;

**for each** functional dependency  $\alpha \rightarrow \beta$  in  $F_c$  **do**

**if** none of the schemas  $R_j$ ,  $1 \leq j \leq i$  contains  $\alpha \beta$

**then begin**

$i := i + 1$ ;

$R_i := \alpha \beta$

**end**

**if** none of the schemas  $R_j$ ,  $1 \leq j \leq i$  contains a candidate key for  $R$

**then begin**

$i := i + 1$ ;

$R_i :=$  any candidate key for  $R$ ;

**end**

/\* Optionally, remove redundant relations \*/

**for all**  $R_k$

**if** schema  $R_k$  is contained in another schema  $R_k$

**then**  $R_k = R_i$ ;  $i=i-1$ ; /\* delete  $R_k$  \*/

**return**  $(R_1, R_2, \dots, R_i)$



# 3NF Decomposition Algorithm (Cont.)

■ Above algorithm ensures:

- each relation schema  $R_i$  is in 3NF
- decomposition is dependency preserving and lossless-join



# 3NF Decomposition: An Example

- Relation schema:

$\text{cust\_banker\_branch} = (\underline{\text{customer\_id}}, \underline{\text{employee\_id}}, \text{branch\_name}, \text{type})$

- The functional dependencies for this relation schema are:

1.  $\text{customer\_id}, \text{employee\_id} \rightarrow \text{branch\_name}, \text{type}$
2.  $\text{employee\_id} \rightarrow \text{branch\_name}$
3.  $\text{customer\_id}, \text{branch\_name} \rightarrow \text{employee\_id}$

- We first compute a canonical cover

- $\text{branch\_name}$  is extraneous in the r.h.s. of the 1<sup>st</sup> dependency
- No other attribute is extraneous, so we get  $F_C =$

$\text{customer\_id}, \text{employee\_id} \rightarrow \text{type}$   
 $\text{employee\_id} \rightarrow \text{branch\_name}$   
 $\text{customer\_id}, \text{branch\_name} \rightarrow \text{employee\_id}$



# 3NF Decomposition Example (Cont.)

- The **for** loop generates following 3NF schema:

$(customer\_id, employee\_id, type)$

$(\underline{employee\_id}, branch\_name)$

$(customer\_id, branch\_name, employee\_id)$

- Observe that  $(customer\_id, employee\_id, type)$  contains a candidate key of the original schema, so no further relation schema needs be added

- At end of for loop, detect and delete schemas, such as  $(\underline{employee\_id}, branch\_name)$ , which are subsets of other schemas
  - result will not depend on the order in which FDs are considered
- The resultant simplified 3NF schema is:

$(customer\_id, employee\_id, type)$

$(customer\_id, branch\_name, employee\_id)$



# Comparison of BCNF and 3NF

- It is always possible to decompose a relation into a set of relations that are in 3NF such that:
  - the decomposition is lossless
  - the dependencies are preserved
- It is always possible to decompose a relation into a set of relations that are in BCNF such that:
  - the decomposition is lossless
  - it may not be possible to preserve dependencies.



# Design Goals

- Goal for a relational database design is:
  - BCNF.
  - Lossless join.
  - Dependency preservation.
- If we cannot achieve this, we accept one of
  - Lack of dependency preservation
  - Redundancy due to use of 3NF
- Interestingly, SQL does not provide a direct way of specifying functional dependencies other than superkeys.

Can specify FDs using assertions, but they are expensive to test,  
(and currently not supported by any of the widely used databases!)
- Even if we had a dependency preserving decomposition, using SQL we would not be able to efficiently test a functional dependency whose left hand side is not a key.



# Multivalued Dependencies

- Suppose we record names of children, and phone numbers for instructors:
  - $inst\_child(ID, child\_name)$
  - $inst\_phone(ID, phone\_number)$
- If we were to combine these schemas to get
  - $inst\_info(ID, child\_name, phone\_number)$
  - Example data:
    - (99999, David, 512-555-1234)
    - (99999, David, 512-555-4321)
    - (99999, William, 512-555-1234)
    - (99999, William, 512-555-4321)
- This relation is in BCNF
  - Why?
- Even though phone number is not uniquely determined by ID, the connection between ID and phone number is independent of all other attributes (child\_name in this case)



# Multivalued Dependencies

- See book for details on
  - Modeling above redundancy via **multivalued dependencies**
    - ▶ In above example ID multivalue determines phone number
    - ▶ written as:  $ID \rightarrow\!\!\! \rightarrow phone\_number$
  - Normalization using multivalued dependencies, to get **fourth normal form (4NF)**
- **Idea:** use functional dependencies **and** multivalued dependencies to decompose schema



# Database Design Process

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# Overall Database Design Process

- We have assumed schema  $R$  is given
  - $R$  could have been generated when converting E-R diagram to a set of tables.
  - $R$  could have been a single relation containing *all* attributes that are of interest (called **universal relation**).
  - Normalization breaks  $R$  into smaller relations.
  - $R$  could have been the result of some ad hoc design of relations, which we then test/convert to normal form.



# ER Model and Normalization

- When an E-R diagram is carefully designed, identifying all entities correctly, the tables generated from the E-R diagram should not need further normalization.
- However, in a real (imperfect) design, there can be functional dependencies from non-key attributes of an entity to other attributes of the entity
  - Example: an *employee* entity with attributes *department\_name* and *building*, and a functional dependency  $\text{department\_name} \rightarrow \text{building}$
  - Good design would have made department an entity
- Functional dependencies from non-key attributes of a relationship set possible, but rare --- most relationships are binary



# Other Design Issues

- Some aspects of database design are not caught by normalization
- Examples of bad database design, to be avoided:

Instead of *earnings* (*company\_id*, *year*, *amount*), use

- *earnings\_2004*, *earnings\_2005*, *earnings\_2006*, etc., all on the schema (*company\_id*, *earnings*).
  - ▶ Above are in BCNF, but make querying across years difficult and needs new table each year
- *company\_year* (*company\_id*, *earnings\_2004*, *earnings\_2005*, *earnings\_2006*)
  - ▶ Also in BCNF, but also makes querying across years difficult and requires new attribute each year.
  - ▶ Is an example of a **crosstab**, where values for one attribute become column names
  - ▶ Used in spreadsheets, and in data analysis tools



# Redundancy Across Relations

- E.g. given FDs  $A \rightarrow B$ , and  $B, C \rightarrow A$  3NF algorithm may give a schema such as
  - $R1(A, B, C)$
  - $R2(A, B)$
- The 3NF algorithm allows  $R2$  to be deleted. But if we do not delete  $R2$ , the schema consisting of  $R1$  and  $R2$  is still in 3NF.
- We can then have value  $A1$  associated with  $B1$  in  $R1$ , and with  $B2$  in  $R2$ , which is clearly inconsistent with the FD  $A \rightarrow B$
- There are more complex situations in the 3NF algorithm, where we cannot delete a whole relation, and there is still redundancy across relations
- Can also happen with BCNF
- Formal theory to avoid such redundancy is a bit complex, but at least watch out for simple cases in your design.



# Denormalization for Performance

- May want to use non-normalized schema for performance
- For example, displaying *prereqs* along with *course\_id*, and *title* requires join of *course* with *prereq*
- Alternative 1: Use denormalized relation containing attributes of *course* as well as *prereq* with all above attributes
  - faster lookup
  - extra space and extra execution time for updates
  - extra coding work for programmer and possibility of error in extra code
- Alternative 2: use a materialized view defined as
$$\text{course} \bowtie \text{prereq}$$
  - Benefits and drawbacks same as above, except no extra coding work for programmer and avoids possible errors



# Modeling Temporal Data

- **Temporal data** have an association time interval during which the data are *valid*.
- A **snapshot** is the value of the data at a particular point in time
- Several proposals to extend ER model by adding valid time to
  - attributes, e.g. address of an instructor at different points in time
  - entities, e.g. time duration when a student entity exists
  - relationships, e.g. time during which an instructor was associated with a student as an advisor.
- But no accepted standard
- Adding a temporal component results in functional dependencies like
$$ID \rightarrow street, city$$
not to hold, because the address varies over time
- A **temporal functional dependency**  $X \xrightarrow{\tau} Y$  holds on schema  $R$  if the functional dependency  $X \rightarrow Y$  holds on all snapshots for all legal instances  $r(R)$



# Modeling Temporal Data (Cont.)

- In practice, database designers may add start and end time attributes to relations
  - E.g.  $\text{course}(\text{course\_id}, \text{course\_title})$  is replaced by  $\text{course}(\text{course\_id}, \text{course\_title}, \text{start}, \text{end})$ 
    - ▶ Constraint: no two tuples can have overlapping valid times
      - Databases are beginning to support such constraints
- Foreign key references may be to current version of data, or to data at a point in time
  - E.g. student transcript should refer to course information at the time the course was taken



# End of Chapter

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