15CSE374 INTRODUCTION TO DATA STRUCTURES AND ALGORITHMS

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Last Lecture

- · ADT & DS.
- Design Patterns.
- Using Concepts of OOP for ADT.
- Algorithm analysis.

Growth rate

- Rate at which the cost of the algorithm grows as the size of its input grows.
- For different functions.
- Linear
 - Quadratic
 - Exponential
 - Constant

Asymptotic analysis

- Measures the efficiency of algorithm as input size becomes large.
- No information about relative merits.
- Widely preferred to determine if a particular algorithm is worth considering for implementation.
- Critical resources- Running time and space required to run the program.
- Time :: Factors like speed of CPU, hardware peripherals.
- Coding efficiency.

- Common environment for comparison.
- Same compiler, same computer, equally efficient implementation.
- Standard benchmark conditions.
- Number of inputs.

Moving beyond Experimental Analysis

- Independent of the hardware and software environment.
- Perform analysis by studying a high level description of the algorithm.

Basic complexity analysis.

- · Best,
- Worst
- Average case

Ex- Searching a number in a list.

Big-O Notation

- Gives upper bound of the complexity in the worst case.
- Helps to quantify performance as the input size becomes arbitrarily large.
- Key Points.
 - Worst case.
 - Input very large.

Big-O Notation

n- The size of the input.

Constant time : O(1)

Logarithmic Time : O(log(n))

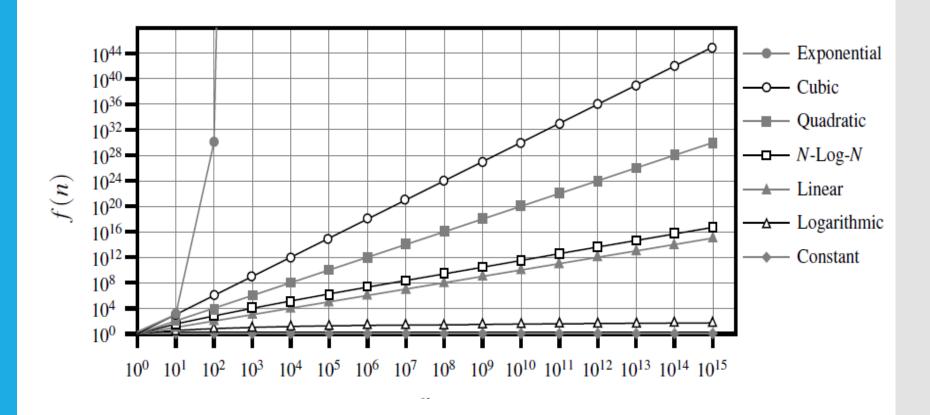
Linear Time : O(n)

Linear Logarithmic Time : O(nlog(n))

Quadratic Time $: O(n^2)$

Cubic Time $: O(n^3)$

Exponential Time $: O(a^n), a>1$



constant	logarithm	linear	n-log-n	quadratic	cubic	exponential
1	$\log n$	n	$n \log n$	n^2	n^3	a^n

Properties

- When Input is very large(infinity)
- O(n+c)=O(n)
- O(cn) = O(n), C > 0
- C is a constant.

$$f(n) = 7\log(n)^3 + 15n^2 + 2n^3 + 8$$

 $\log(f(n)) = \log(n^3)$

Examples

The following run in constant time: 0(1)

The following run in linear time: O(n)

$$i := 0$$
 $i := 0$

While $i < n$ Do

 $i = i + 1$ $i = i + 3$

$$f(n) = n$$

$$O(f(n)) = O(n)$$

$$f(n) = n/3$$

$$O(f(n)) = O(n)$$

Second 3 times faster.

```
For (i := 0; i < n; i = i + 1)

For (j := 0; j < n; j = j + 1)

f(n) = n*n = n^2, O(f(n)) = O(n^2)
```

N times N

For
$$(i := 0 ; i < n; i = i + 1)$$

For $(j := i ; j < n; j = j + 1)$

- Since i goes from 0 to n, hence amount of looping done is directly determined by what i is.
- If i = 0 we do n work
- If i = 1 we do n-1 work
- If i = 2 we do n-2 work
- •
- If i = n-1 we do 1 work
- Finally we get

$$(n) + (n-1) + (n-2) + (n-3) + \dots + 3 + 2 + 1$$

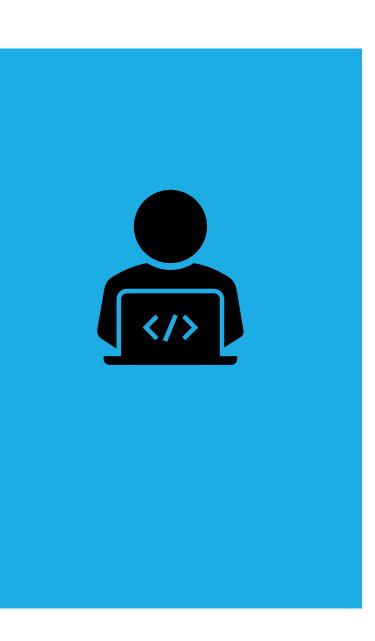
$$O(\frac{n(n+1)}{2}) = O(\frac{n^2+n}{2}) = O(n^2)$$

```
i := 0
While i < n Do
    j = 0
    While j < 3*n Do
        j = j + 1
    j = 0
    While j < 2*n Do
        j = j + 1
    i = i + 1

f(n) = n * (3n + 2n) = 5n<sup>2</sup>
    O(f(n)) = O(n<sup>2</sup>)
```

Points to remember

- Ignore Constants.
- Multiply –loops in different levels
- Addition –loops in same levels



THANK YOU!!!!!