

P6Project: Test a Perceptual Phenomenon

Sara Uenoyama

Questions: https://docs.google.com/document/d/1-0kpZLjG_kX9J6LIQ5lItsqMzVWjh36QpnP2RYpVdPU/pub?embedded=True

Dataset: <https://drive.google.com/file/d/0B9Yf01UaIbUgQXpYb2NhZ29yX1U/view>

1. Our Independent variable and dependent variable
In this case, our independent variable is the two conditions of words: congruent or incongruent. Our dependent variable is the time it takes for participants to name the ink colors of words on a list.
2. Appropriate hypotheses and statistical test of this task
We call the time to name the ink colors on congruent words list as x_i and one to name ink colors on incongruent words list of the same person as y_i .
Appropriate null hypothesis is that there is no difference in time to name ink colors of congruent words list and incongruent words list. On the other hand, alternative hypothesis is that it takes shorter time to name ink colors of incongruent words list than congruent words list. We can write down as follows in mathematical way.
 - Null hypotheses: $x_i = y_i$
 - Alternative hypotheses: $x_i < y_i$

Appropriate test is one-sided t-test for following reasons.

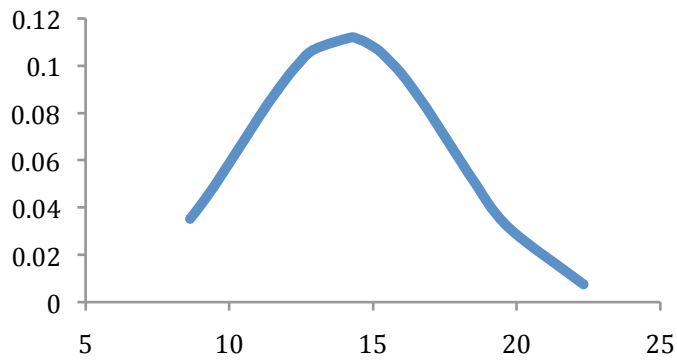
- We expect that congruent words list takes shorter time to name its colors.
- We only have sample data, not knowing μ and σ , which is used for z-test.

Assumptions made for the t-test are

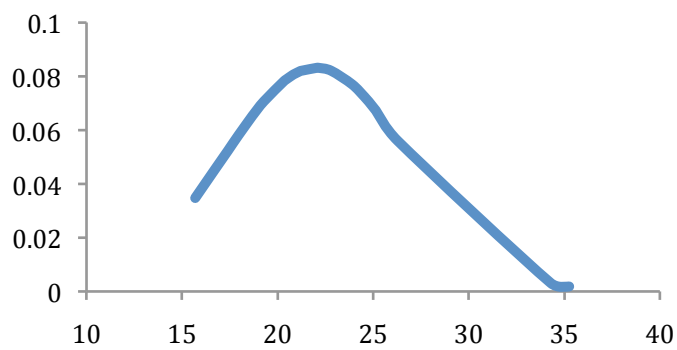
- The scale of measurement applied to this data collection is continuous scale, "time".
- The data is collected from randomly selected people from total population.
- As showed in my answer to question 4, the sample data is normally distributed.
- The sample size, 24, is reasonably large enough to draw bell-shaped distribution curve.

3. Descriptive statistics
Calculating from the dataset, sample mean and sample standard distribution from each group are
 - $\bar{x}_A = 14.05$
 - $s_A = 3.56$
 - $\bar{y}_B = 22.02$
 - $s_B = 4.8$

A stands for sample data of congruent words and B stands for sample data of incongruent words.
4. Visualization of the distribution of the sample data
The sampling distribution of congruent words data is normal distribution as showed below.



The sample data of incongruent words is normally distributed as well.



5. One-tailed t-test

Calculate $d_i = y_i - x_i$ for each sample data.

	Congruent	Incongruent	d_i
1	12.079	19.278	7.199
2	16.791	18.741	1.95
3	9.564	21.214	11.65
4	8.63	15.687	7.057
5	14.669	22.803	8.134
6	12.238	20.878	8.64
7	14.692	24.572	9.88
8	8.987	17.394	8.407
9	9.401	20.762	11.361
10	14.48	26.282	11.802
11	22.328	24.524	2.196
12	15.298	18.644	3.346
13	15.073	17.51	2.437
14	16.929	20.33	3.401
15	18.2	35.255	17.055
16	12.13	22.158	10.028
17	18.495	25.139	6.644
18	10.639	20.429	9.79
19	11.344	17.425	6.081
20	12.369	34.288	21.919
21	12.944	23.894	10.95
22	14.233	17.96	3.727
23	19.71	22.058	2.348
24	16.004	21.157	5.153
mean	14.05	22.02	7.96
sd	3.56	4.8	4.86

Mean difference \bar{d} is

$$\bar{d} = \bar{y}_B - \bar{x}_A = 7.96$$

Standard deviation of the difference is

$$s_d = 4.86$$

Since the sample size is $n = 24$, degree of freedom is

$$Df = 24 - 1 = 23$$

Standard error of mean can be calculated from the number of samples and sample standard deviations.

$$SE(\bar{d}) = s_d / \sqrt{n} = 0.99$$

Using the SEM value, we can calculate t-statistics.

$$T\text{-statistics} = \bar{d} / SE(\bar{d}) = 8.03$$

When α level is 0.05, t-critical value is 1.676.

$$t(46) = 1.676, p = 0.05, \text{one-tailed}$$

Since $t\text{-statistics} > t(46)$, we reject the null hypothesis. $p < 0.05$.

In conclusion, in a Stroop effect experiment, the time it takes to name ink color of congruent word and one of incongruent word are different. As we expected, it takes more time to name ink color of words on incongruent words list.

Reference

<https://www.investopedia.com/ask/answers/073115/what-assumptions-are-made-when-conducting-ttest.asp>