



Advanced Algorithms 2020/2021

Project 1

String Matching

This project considers the string matching problem. The delivery deadline for the project code is April 21st, at 17:00. You should not use existing code for the algorithms described in the project, either from software libraries or other electronic sources.

It is important to read the full description of the project before starting to design and implement the solution.

You need to deliver a working implementation of the project in the mooshak system.

1 Text Searching

1.1 Overview

In this project we will implement and compare several online algorithms for matching small patterns against a large texts. This problem is recurrent in computer science and specially in bioinformatic applications, therefore we will use a reference database of DNA sequences.

The input will consist of several DNA sequences. A reference sequence T and several search patterns P. Since the sequences are DNA the underlying alphabet will be A, C, T, G.

The first algorithm will simply be the naive algorithm, which tests P at every possible location. We will then implement the Knuth-Morris-Pratt and Boyer Moore.

1.2 Knuth-Morris-Pratt

Since the naive algorithm may require O(nm) time, where n is the size of T and m is the size of P, it is important to find more efficient algorithms. You should

find examples where this bad performance occurs, these examples will be useful for the experimental validation.

For this purpose we will implement the Knuth-Morris-Pratt algorithm. This algorithm starts by computing the π table which for every i store the size of the longest suffix of P[..i] that is also a proper prefix. Note that this processing step must be computed in O(m), but the technique is similar to the general algorithm. In general the KMP algorithm keeps track of the size of the longest prefix of P that matches a suffix of T[..i]. At each step the value of i is incremented, in which case the size of the prefix of P can increase by 1, or be decreased using the π table. This is determined by comparing T[i], with a given letters, or letters of P. Both reference books [1, 2] contain detailed explanations of this algorithm.

For this algorithm we want to output the locations of all the occurrences of P in T. Moreover we, also, want to count how many times a letter of P is compared with a letter of T, note that you should not count comparisons when pre-processing P. We want to count both the comparisons that extend the prefix of P and those that lead to accesses to the table π . What is the relation between this value and n? Validate this relation experimentally.

1.3 Boyer-Moore

The Boyer-Moore is another "efficient" algorithm for exact string matching. This algorithm is in fact a combination of heuristics, a proper combination of which yields an O(m+n) time algorithm. These heuristics can be adapted for the kind of text in question. The proof of this bound is intricate and beyond the scope of this course.

The algorithm matches P against T and after a match of a fail P is shifted to the right, P starts in the beginning of T and finishes at the end. However contrary to the naive algorithm or KMP the letters in P are compared from right to left, i.e., the first letter to compare is the last letter of P. A match is found when all the letters of P, up to P[0], match the corresponding letters of T.

The algorithm obtains its good performance by using "large" shifts. There are two heuristics for shifting, the bad character rule and the good suffix rule.

The bad character rule, uses a table L, which for every letter c of Σ stores the position of the rightmost occurrence of c in P. Whenever a letter c of T fails to match a letter of P we use the table L to shift P so that the rightmost c of P is now aligned with the c in T. Notice that this might mean that the pattern was shifted backwards, i.e., to the left, in that we case we instead shift P one position to the right. This rule can be improved to the extended bad character rule that stores all the positions of every letter in P, this rule fixes the previous problem in a more efficient way, using essentially the same time and space requirements. For the purposes of this project we will implement only the "simple" rule.

Another rule the algorithm also uses is the (strong) good suffix rule, it is similar in spirit both to KMP and to the previous rule. For every suffix P[i..], of size ℓ , we store the location k of the right most occurrence of the same string in P, i.e., $P[i..] = P[k..k + \ell - 1]$ and $P[i..] \neq P[k'..k' + \ell - 1]$ for any k' > k. If this was the only restriction then it would be a weak good suffix rule. To be a strong good suffix rule we further require that k is the beginning of P, i.e., k = 0, or that $P[k - 1] \neq P[i - 1]$. This means that in the strong rule k is

the rightmost occurrence of the suffix P[i..] that cannot be extended to the left. Hence the restriction on k' must also be updated.

Whenever P need to be shifted the Boyer-Moore algorithms computes both these shifts and chooses the largest one. For further details on this algorithm see Gusfield's book [2]. Notice that pre-processing of the bad character rule is quite straight forward, but the strong good suffix is more intricate, in fact it requires the Z algorithm.

With these two rules it is possible to guarantee that the Boyer-Moore algorithm runs in O(m+n) time. Provided that P does not occur in T. Present an example where this algorithm requires O(mn) time. To fix this bad performance it is possible use the Galil rule, which avoids having to math the pattern all the way to the end. We will not implement this rule.

Like the KMP algorithm the output should contain the locations of all the occurrences of P in T. Moreover we, also, want to count how many times a letter of P is compared with a letter of T, note that you should not count comparisons when pre-processing P. What is the relation between this value and n, when P does not occur in T? Validate this relation experimentally. Why is the BM algorithm claimed to be sub-linear?

1.4 Specification

To automatically validate the index we use the following conventions. The binary is executed with the following command:

```
./project < in > out
```

The file in contains the input commands that we will describe next. The output is stored in a file named out. The input and output must respect the specification bellow precisely. The output file will be validated against an expected result, stored in a file named check, with the following command:

```
diff out check
```

This command should produce no output, thus indicating that both files are identical.

Each operation is issued in a separate line, it begins by a letter that identifies it and is followed by a sequence of argument or options.

- T followed by single space ' ' followed by the string T. This strings consists of characters A, C, G, T and ends with a, single, newline character '\n'. This commands specified the text that will be used for the sub-sequent search. Note that more than one T command may be issued, in which case the previous text is replaced by the new one. Only one text is considered. Note that the size of the text is not specified, and it might be large. Therefore you should use appropriate dynamic memory techniques to increase the necessary space.
- N followed by single space ' ' followed by the string P. Upon receiving this command the program should do a naive online search for P in T. At least one T must have been issued before this command. The input files and test files verify this restriction, which therefore does not need to be checked. For each occurrence this command should print its position followed by a space ' '. After printing all the occurrence positions the command issues a newline '\n'.

- K , same as the N command, but using the KMP algorithm. Moreover the output should include a second line containing the number of character comparisons, a space ' ' and a newline '\n'. For example for printf the format is "%d \n".
- $\, B \,$, same as the B command, but using the BM algorithm, for the occurrences and the number of comparisons.
- X , terminates the program without producing output

1.5 Sample Behaviour

The following examples show the expected output for the given input. These files are available on the course webpage.

input 1

```
T TCGCAGGGCG
```

N TC

K TC

в тс

X

output 1

0

0

11

0

7

input 2

T AAAAAAAA

N AAA

K AAA

B AAA

X

output 2

```
0 1 2 3 4 5 6 7
0 1 2 3 4 5 6 7
17
0 1 2 3 4 5 6 7
24
```

input 3

T AGGTACCCAT

K CA

X

```
output 3
13
input 4
T AAAAAAAA
K AAA
X
output 4
0 1 2 3 4 5 6 7
17
input 5
T GCCCAAAGAC
B CA
X
output 5
3
9
input 6
T AAAAAAAA
B AAA
X
output 6
0 1 2 3 4 5 6 7
24
```

2 Grading

The final grade will result from the number of points obtained in the mooshak system.

The mooshak system accepts several programming languages, click on Help button for the a list of the languages and the respective compilers. Projects that do not compile in the mooshak system will be graded 0. Only the code that compiles in the mooshak system will be considered, commented code, or including code in the report will not be considered for evaluation.

Submissions to the mooshak system should consist of a single file. The system identifies the language through the file extension, an extension .c means the C language. To determine the other extension check mooshak's Help. The compilation process should produce absolutely no errors or warnings, otherwise

the file will not compile. The resulting binary should behave exactly as explained in the specification section. Be mindful that diff will produce output even if a single character is different, such as a space or a newline.

Notice that you can submit the project to mooshak several times, but there is a 10 minute waiting period between submissions. You are strongly advised to submit several times and as early as possible. Only the last version is considered for grading purposes, all other submissions are ignored. There will be **no** deadline extensions. Submissions by email will **not** be accepted.

References

- [1] Cormen, T. and Leiserson, C. and Rivest, R. and Stein, C. *Introduction to algorithms*. The Massachusetts Institute of Technology, 2nd Edition, 2001.
- [2] Gusfield, D. Algorithms on strings, trees, and sequences: computer science and computational biology. Cambridge Univ Press, 1997.