

Parcial 3 - teórico

Punto 23

$$d) \quad h(\alpha) = \phi(x_k + \alpha r_k) \quad \left\{ \begin{array}{l} \text{función a minimizar} \end{array} \right.$$

$$x_{k+1} = x_k + \alpha_k r_k \quad \left\{ \begin{array}{l} \text{dirección} \end{array} \right.$$

Derivamos $h(\alpha)$

$$* \nabla(\phi(x_k)) = Ax_k - b$$

$$h'(\alpha) = \phi'(x_k + \alpha r_k) \cdot (x_k' + (\alpha r_k)')$$

$$h'(\alpha) = \nabla \phi(x_k + \alpha r_k) \cdot (x_k' + (\alpha r_k)')$$

$$h'(\alpha) = [A(x_k + \alpha r_k) - b] (0 + r_k)$$

$$h'(\alpha) = [(Ax_k + A\alpha r_k) - b] r_k$$

Iguálamos $h'(\alpha) = 0$

$$0 = (Ax_k - b + A\alpha r_k) r_k$$

$$0 = (r_k + A\alpha r_k) r_k$$

$$0 = r_k^T r_k + r_k^T A \alpha r_k$$

Como α es escalar, podemos reorganizarlo:

$$0 = r_k^T r_k + \alpha r_k^T A r_k$$

$$r_k^T \cdot r_k = \alpha \underbrace{r_k^T A r_k}$$

como este valor
es escalar, podemos
pasarle a dividir

$$-\frac{r_k^T \cdot r_k}{r_k^T A r_k} = \alpha$$