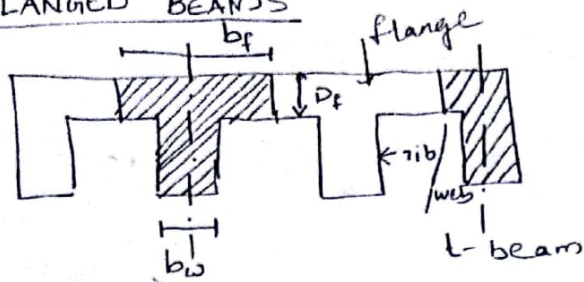


MODULE-2

FLANGED BEAMS



b_f :- width of the flange
 D_f :- Depth of the flange
 b_w :- width of the web

Parameters of a flanged beam

The most common type of reinforced concrete floor & roof system comprises of concrete slabs monolithically casted with floor beams in the span range of 5-10m. In such cases the compressive flange is made up of the width of the rib and a portion of the slab length on either side of the rib reinforced to as the effective width of flange. Fig shows the prominent design parameters of flanged (T-beam) beams using the notation used in IS 456:2000 code [cl 23.1 page 36, IS 456:2000]

- Q) A ~~tee~~ beam slab floor of an office building comprises of a slab 150mm thick spanning b/w ribs spaced at 3m centres. The effective span of the beam is 8m. live load on floors is 4 kN/m^2 . Using M_{20} concrete and F_{415} steel bars, design one of the intermediate T-beams

Solution :-

Given Details

$$D_f = 150 \text{ mm}$$

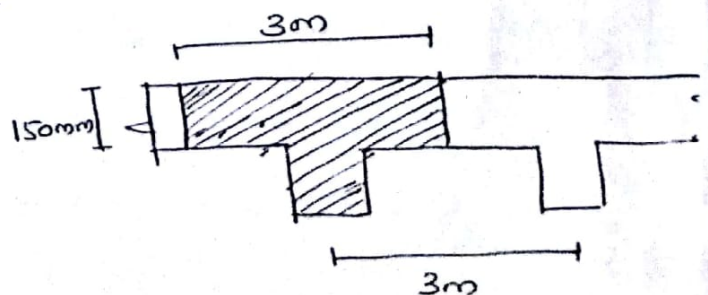
$$\text{Spacing of tee beam} = 3 \text{ m}$$

$$l_{\text{eff of beam}} = 8 \text{ m}$$

$$L.L = 4 \text{ kN/m}^2$$

$$f_{ck} = 20 \text{ N/mm}^2$$

$$f_y = 415 \text{ N/mm}^2$$



Span to depth ratio for S.S beam = 20
[cl. 23.2.1 of IS 456:2000]

-2-

Assume width of the rib = 300mm and flanged width = 3m.

$$\therefore \text{ratio of web to flanged width} = \frac{0.3}{3} = 0.1$$

From cl 23.2.1. Fig 6, page 36 of IS 456:2000]

Reduction value = 0.80

$$\frac{l}{d} = 20 \times 0.8$$
$$= 16$$

$\therefore \frac{l}{d}$ ratio is taken as 16.

Thus effective depth of T-beam, $d = \frac{8000}{16}$
 $= 500\text{mm}$

Assume effective cover of 50mm

$$\therefore \text{overall Depth} = 500 + 50$$
$$= 550\text{mm}$$

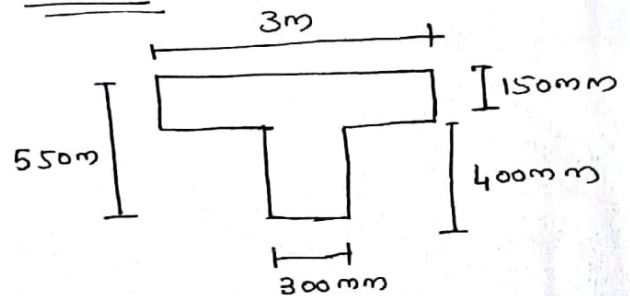
\therefore Tee beams parameters are:-

$$d = 500\text{mm}$$

$$D = 550\text{mm}$$

$$b_w = 300\text{mm}$$

$$D_f = 150\text{mm}$$



STEP: 2 :- LOADS & BENDING MOMENT

$$\text{Self weight of the slab} = 3 \times 0.15 \times 25 = 11.25 \text{ kN/m}$$

$$\text{Self weight of the rib} = 0.3 \times 0.4 \times 25$$
$$= 3 \text{ kN/m}$$

$$\text{live load (given)} = 4 \text{ kN/m}$$

$$\text{Assume finishing load} = 1.8 \text{ kN/m}$$

$$\text{Total } \overset{\text{Design}}{\text{Load}} = 20.05$$

Utilization

$$BM = \frac{wl^2}{8}$$

$$= \frac{20.05 \times 8^2}{8} = 160.4 \text{ kNm}$$

Ultimate moment, $M_u = 240.60 \text{ kNm}$

$$\text{Shear Force, } V_u = \frac{wl \times fs}{2} = \frac{20.05 \times 8 \times 1.5}{2} = 120.3 \text{ kN}$$

STEP: 3 :-

Effective width of flange,

$$i) b_f = \frac{l_0}{6} + b_w + 6D_f \quad \left[\text{cl 23.1.2, page 37 of IS 456:2000} \right]$$

$$= \frac{8}{6} + 0.3 + 6 \times 0.15$$

$$= 2.8 \text{ m}$$

$$= \underline{\underline{2530 \text{ mm}}}$$

$$ii) c/c \text{ distance of ribs}$$

$$= \underline{\underline{3000 \text{ mm}}}$$

Least value is considered as effective width of flange

$$\therefore b_f = \underline{\underline{2530 \text{ mm}}}$$

STEP: 4 :-

Moment capacity of the section.

$$M_{ulimit} = 0.36 \frac{x_{u\max}}{d} \left[1 - 0.42 \frac{x_{u\max}}{d} \right] b d^2 f_{ck}$$

If x_u lies in the flange.

$$= 0.36 f_{ck} b_f D_f [d - 0.42 D_f]$$

$$= 0.36 \times 20 \times 2530 \times 150 [500 - 0.42 \times 150]$$

$$= 1194 \times 10^6 \text{ Nmm}$$

$$= \underline{\underline{1194 \text{ kNm}}}$$

$$\therefore M_u < M_{ulimit}$$

$$246 < 1194$$

~~ie, $x_u < D_f$~~

ie, $x_u < D_f$

Hence, the section is considered as a rectangular section

such width = width of flange. $[b = b_f]$

Step:5 - COMPUTATION of A_{st}

$$\therefore M_u = 0.87 f_y A_{st} d \left[1 - \frac{A_{st} f_y}{b_f d f_{ck}} \right]$$

$$246 \times 10^6 = 0.87 \times 415 \times A_{st} \times 500 \left[1 - \frac{A_{st} \times 415}{2530 \times 500 \times 20} \right]$$

$$A_{st} = 1417 \text{ mm}^2, \text{ No. of bars} = \frac{A_{st}}{\frac{\pi}{4} \times 25^2} = 2.9 \approx 3$$

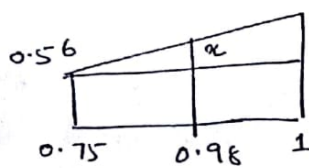
$$\text{Provide 3 bars of 25mm } \left[A_{st} \text{ provided} = 3 \times \frac{\pi}{4} \times 25^2 \right] = 1473 \text{ mm}^2$$

also provide 2 hanger bars of 8mm dia on the compression side.

Step-6 :- Design of shear reinforcement.

$$\tau_v = \frac{V_u}{bd} = \frac{120.24 \times 10^3}{300 \times 500} = 0.802 \text{ N/mm}^2$$

$$\tau_c \Rightarrow P_t = 100 \frac{A_s}{bd} = \frac{100 \times 1473}{300 \times 500} = 0.98$$



$$\text{we have, } \tau_c = 0.56 + x$$

$$\frac{0.98 - 0.75}{1 - 0.75} = \frac{x}{0.62 - 0.56}$$

$$\therefore x = 0.0552$$

$$\tau_c = 0.56 + 0.0552$$

$$= 0.6152 \text{ N/mm}^2$$

$$\tau_{cmax} = 2.8 \text{ N/mm}^2$$

$$\tau_c < \tau_v < \tau_{cmax}$$

Since $T_v > T_c$. Provide design shear reinforcement in the form of vertical stirrups.

$$\text{Balanced shear, } V_{us} = V_u - T_c b w d$$

$$= 120.3 \times 10^3 - 0.615 \times 300 \times 500$$

$$= 28050 \text{ N}$$

$$\text{Assume 2 legged stirrups of } \frac{28.05 \text{ kN}}{8 \text{ mm } \phi}$$

$$S_v = \frac{0.87 f_y A_{s_v} d}{V_{us}}$$

$$= \frac{0.87 \times 415 \times 500 \times 2 \times \frac{\pi}{4} \times 8^2 \times 2}{28050}$$

$$= 646 \text{ mm.}$$

Q: 7 check for spacing of shear reinforcement.

i) $0.75d = 375 \text{ mm.}$

ii) 300 mm

iii) 646 mm.

least value is taken

provide 2 legged stirrup of $8 \text{ mm } \phi$ @ 300 mm c/c

