

Transverse Reinforcement
Pitch

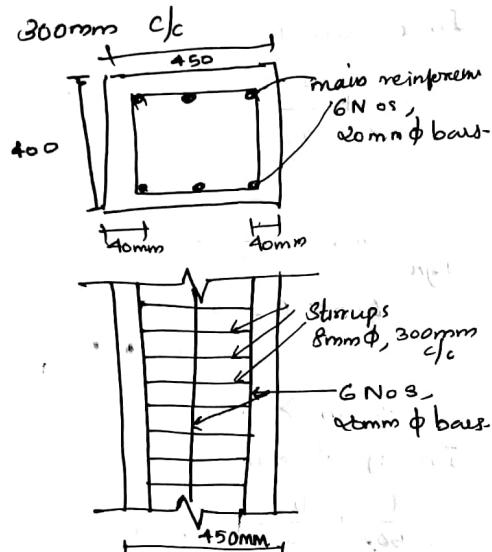
c.l. 26.5.3.2

(i) least lateral dimension = 400

$$(ii) 16 \phi = 16 \times 20 = 320$$

(iii) 300mm

provide 8mm ϕ bars @



MODULE 4

ISOLATED FOOTING

ISOLATED FOOTING FOR AXIALLY LOADED COLUMNS

ISOLATED FOOTING FOR UNIFORM DEPTH FOR RCC COLUMN

Design a isolated footing of uniform thickness for a RCC column having a vertical load of 600kN and having a base of size foot 300mm. The safe bearing capacity of soil is 120 kN/m². Use M₂₀ concrete & Fe 415 steel.

$$W = 600\text{kN} \quad q_u = 120 \text{ kN/m}^2$$

$$b = 500\text{mm}$$

$$d = 500\text{mm}$$

$$f_{ck} = 20 \text{ N/mm}^2 \quad f_y = 415 \text{ N/mm}$$

Design of the section

i. Depth on the basis of bending compression

The max bending moment act at the face of column

Step 1: Dimension of the section

Let w' be the selfweight of the column 10% of Super imposed load.

$$w' = 10\% \cdot W \\ = 600 \times 10 = 60 \text{ kN}$$

$$\text{Total load} = 600 + 60 = 660 \text{ kN}$$

$$\text{Area} = \frac{\text{Load}}{\text{Pressure}} \\ = \frac{660}{120} \\ = 5.5 \text{ m}^2$$

So provide a square column of size $B^2 = 5.5$

$$B = 2.34 \approx$$

$$B = 2.4 \text{ m}$$

Provide a square footing of $2.4 \times 2.4 \text{ m}$

Net upward pressure =

$$\frac{\text{Actual load}}{\text{Area}} = \frac{600}{2.4 \times 2.4}$$

$$= 104.17 \text{ kN/m}^2$$

Moment

$$M = P_0 B \left(\frac{B-b}{2} \right) \times \frac{\text{load}}{\text{load}}$$

$$M = \frac{P_0 B}{8} (B)$$

$$M = \frac{104.17 \times 2.4}{8} \\ = 112.8 \text{ kNm}$$

$$M_u = M \times 1.5 \\ = 169.20 \\ = 169.2 \times$$

calculate 'd'

$$Mu_{int} = 0.36 \frac{\sum u_{max}}{d} [1 -$$

$$169.2 \times 10^6 = 0.36 \times 0.48 \times \frac{1}{2400} \times d^2$$

$$d = 159.85 \text{ mm}$$

$$= 120 \text{ kN/m}$$

umn.

$$f_y = 415 \text{ N/mm}$$

ion of

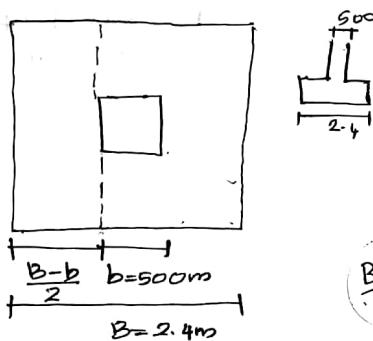
self weight
10% of
load.

$$\frac{D}{D_0} = 60 \text{ kN} \\ \rightarrow D = 660 \text{ kN}$$

Design of the section

1. Depth on the basis of bending compression.

The max bending moment act at the face of the column. \Rightarrow moment load addition

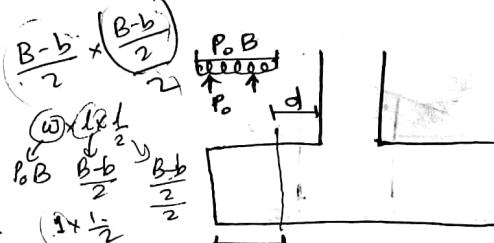


Assume clear cover of 50mm & 20mm Ø bars.

$$D = 160 + 50 + \frac{20}{2} \\ = 220 \text{ mm}$$

2. Depth on the basis of one way shear.

\Rightarrow force load
For one way shear the critical section is located at a distance d from the face of the column.



$$P = \frac{\text{Load Area}}{\text{Area}} \\ 120 = \frac{\dots}{\text{Area}} \\ = \dots$$

Moment

$$M = P_0 B \frac{(B-b)}{2} \times \frac{(B-b)}{2}$$

$$M = \frac{P_0 B}{8} (B-b)^2$$

$$M = \frac{104.17 \times 2.4}{8} (2.4 - 0.5)^2 \\ = 112.8016 \text{ kNm}$$

$$M_u = M \times 1.5 \\ = 169.20 \text{ kNm} \\ = 169.2 \times 10^6 \text{ Nmm}$$

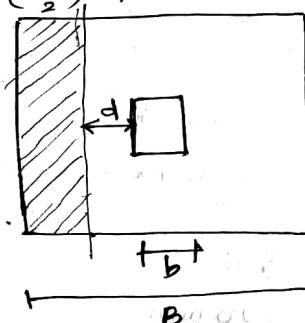
calculate ' d '

$$M_{uhint} = 0.36 \frac{\chi_{umax}}{d} \left[1 - 0.048 \frac{\chi_{umax}}{d} \right]$$

$$bd^2 f_{ck}$$

$$169.2 \times 10^6 = 0.36 \times 0.48 \left[1 - 0.048 \times 0.48 \right] \times 2000 \times d^2 \times 20$$

$$d = 159.85 \text{ mm} \approx 160 \text{ mm}$$



$$\text{Shear force, } V = P_0 B \left[\left(\frac{B-b}{2} \right) - d \right]$$

$$= 104.17 \times 2.4 \times \left[\left(\frac{2.4 - 0.5}{2} \right) - d \times 10^3 \right] \\ = 237.5076 - 0.25008 d$$

$$V_u = (237.5076 - 0.25008 d) \times 1.5 \\ = 356.2614 - 0.375012 d$$

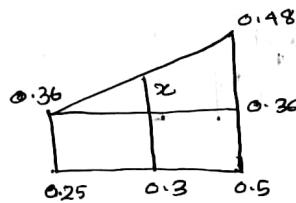
Nominal shear stress is equated to the permissible shear stress.

$$T_v = k T_c$$

$$\frac{V_u}{bd} = k T_c \rightarrow \text{Pgs 73}$$

Assume 0.3% of % tensile reinforcement.

$$\frac{100 A_s}{bd} = P_t = 0.3\%$$



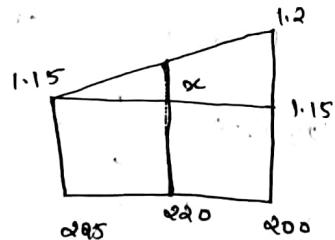
$$\frac{0.48 - 0.36}{x} = \frac{0.5 - 0.25}{0.3 - 0.25}$$

$$x = 0.024$$

$$T_c = 0.36 + x = 0.384$$

value of k

$$D = 220 \text{ mm}$$



$$\frac{1.2 - 1.15}{x} = \frac{225 - 220}{225 - 220}$$

$$x = 0.01$$

$$k = 1.15 + x = 1.16 \text{ mm}$$

$$\frac{(356.2614 - 0.315012 d) 10^3}{2400 \times d} = 1.16 \times 0.1$$

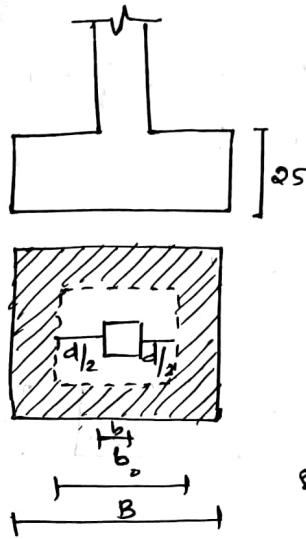
CHECK FOR TWO.

$$1.069d \\ = 1063.48$$

$$356.2614 \times 10^3 = 376.08d \\ = 1438.5d$$

$$d = 947.29$$

$$d = 247.6 \\ \approx 250 \text{ mm}$$



Shear force

Shear stress

from cl. 31.6 & 3.1 of

Permissible shear

where, $k_g = 0.5 +$

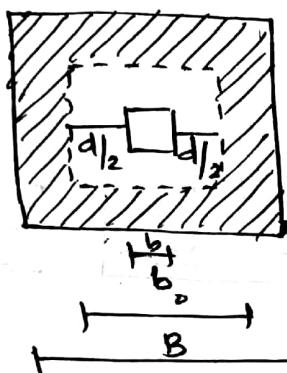
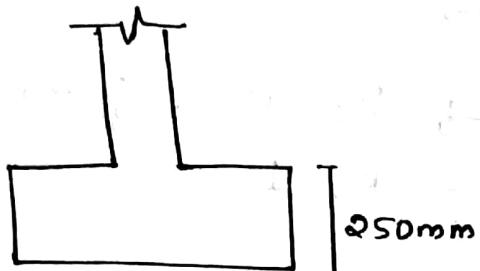
$B_c = \text{ratio}$
show

$$M = \frac{P_0 D C B}{8}$$

$$= 103.8 \times 2.4 \times 3.4 \times \frac{8}{8}$$

$$= 371.007 \text{ KN}$$

CHECK FOR TWO-WAY SHEAR / PUNCHING SHEAR



S/I lies @ $d/2$ distance from the column face all around

$$b_o = b + \frac{d}{2} + \frac{d}{2}$$

$$= 500 + \frac{250}{2} + \frac{250}{2} \\ = 750 \text{ mm}$$

$$\text{Area}_v = B^2 - b_o^2$$

$$\begin{aligned} \text{Shear load} &= \text{Area} \times \text{Pressure} \\ &= 2.4^2 - 0.75^2 \\ &= 5.1975 \text{ m}^2 \end{aligned}$$

Shear force around the S/I

= Pressure \times Area

$$\begin{aligned} V &= 104.17 \times (2.4^2 - 0.75^2) \\ &= 541.424 \text{ kN} \end{aligned}$$

$$V_u = 812.136 \text{ kN}$$

$$\begin{aligned} \text{Shear stress} &= \frac{V_u}{b_o d} = \frac{812.136 \times 10^3}{4 \times 750 \times 250} \\ &= 1.08 \text{ MPa} \end{aligned}$$

from cl. 31.6 & 3.1 of IS 456:2000

Permissible shear stress = $k_s T_c$

where, $k_s = 0.5 + B_{cl}$

B_{cl} = ratio of longer side to shorter side.

$$M = \frac{P_o d^2}{8}$$

~ 2

'd' distance from the plane of the column

$$\frac{500}{500} = 1$$

$$k_s = 0.5 + 1 = 1.5$$

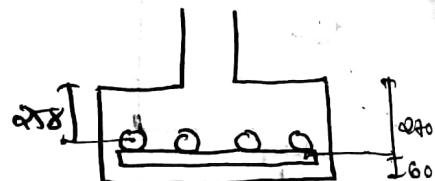
Since the value of k_s is subjected to a max of 1. Take $k_s = 1$

$$T_c = 0.25 \sqrt{f_{ck}}$$

$$= 0.25 \sqrt{20} = 1.118$$

$$k_s T_c = 1.118$$

$$T_v < k_s T_c$$



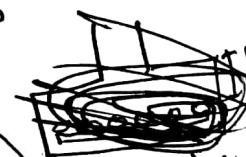
footing is safe

\therefore Provide a footing of size $2.4m \times 2.4m$ with effective depth = 250mm

Assume effective cover of 60mm

$$\text{Overall depth} = 250 + 60 = 310 \text{ mm}$$

Design of steel reinforcement



Since the actual depth provided is greater than the depth required for bending compression reinforcement it is as per Annex G.

$$M_u = 0.87 \text{ fig Astd}$$

$$\left[1 - \frac{A_{st} f_y}{bd f_{ck}} \right]$$

$$169.224 \times 10^6 = 0.87 \times 415 \times A_{st} \times 258$$

$$\left[1 - \frac{A_{st} \times 415}{4400 \times 258 \times 20} \right]$$

$$1816.665 = A_{st} \approx 3.35 \times 10^{-5} A_{st}^2$$

$$A_{st} = 1943.156$$

$$\text{No. of bars} = \frac{A_{st}}{\text{Area of 1 bar}}$$

$$= \frac{1943.156}{\pi / 4 \times 20^2} = 17.19 \approx 18 \text{ No.}$$

$d^2 f_{ck}$

$0.42x$
 0.48

Check for development length

Min development length, $L_d = 47 \times \phi$

billet

$$(47 + 12 + 16) = 47 \times 12$$

$$= 564 \text{ mm}$$

1. 60mm
2. 700

$$\text{Length of the bar} = \frac{B - b}{2} - 60$$

$$= \frac{2400 - 500}{2} - 60$$

- end

$$= 890 > L_d$$

footing is safe

reaction

Transfer of load at the column base

direct

cl. 34.4 Pg: 65

Permissible bearing stress =

$$0.45 f_{ck} \sqrt{\frac{A_1}{A_2}}$$

$$\frac{100(B-b)}{8}$$

as

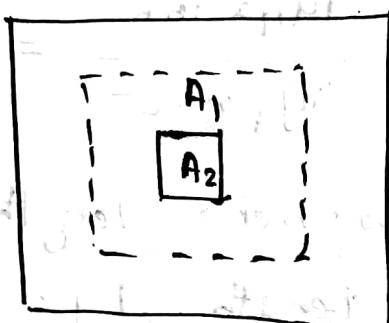
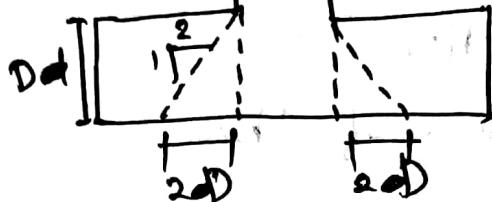
$$= 103.8 \times 3.4 / 3.4 - 0.57^2$$

'd' critical section at
'd' distance from the
Phase of the column.

Load area of the column = A_2

$$= 500 \times 500$$

$$= 250000$$



$$A_1 + = (2D + 500 + 2D)^2$$

$$= (2 \times 330 + 500 + 2 \times 330)^2$$

$$= 3312400 \text{ mm}^2$$

$$\sqrt{\frac{A_1}{A_2}} = 3.64$$

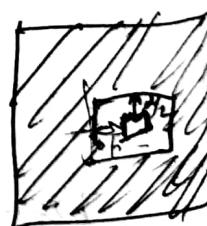
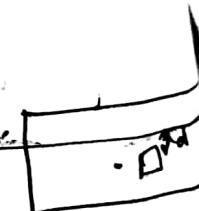
∴ It is greater than 2
adopt max value 2

∴ permissible bearing stress

$$= 0.45 f_{ck} \sqrt{\frac{A_1}{A_2}}$$

$$= 0.45 \times 20 \times 2$$

$$= 18 \text{ N/mm}^2$$



Actual bearing pressure = $\frac{F.O.S \times \text{load}}{\text{Area}}$

$$= \frac{1.5 \times 600 \times 10^3}{500 \times 500} = 3.6 \text{ N/mm}$$

Actual stress < Permissible bearing stress

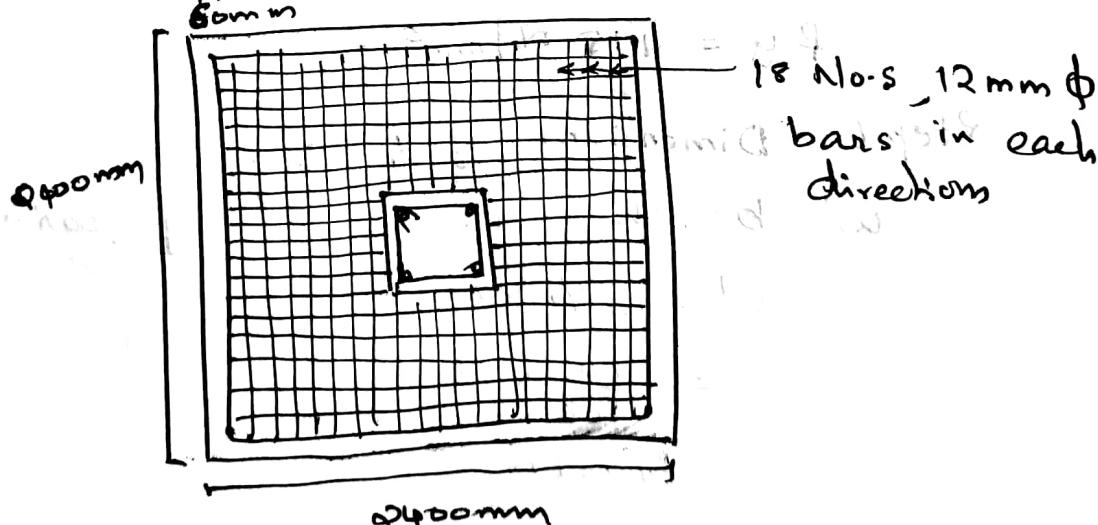
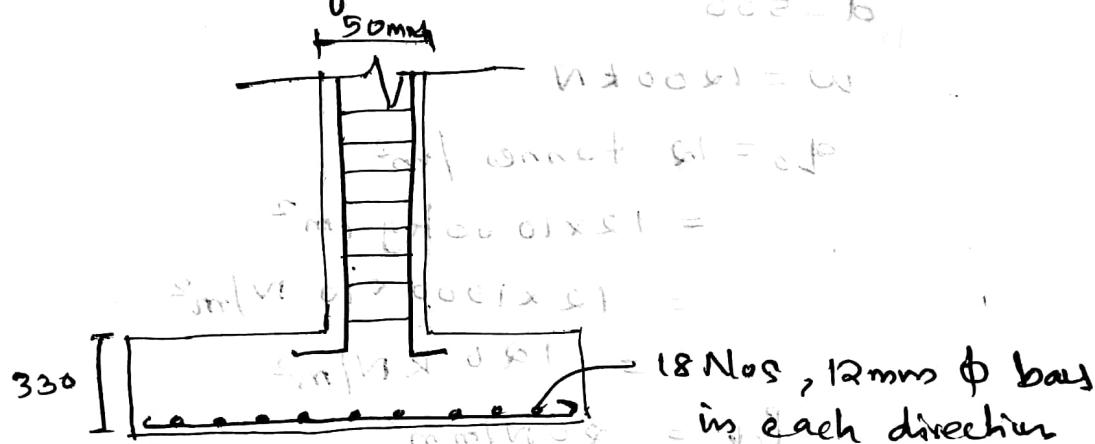
Bearing

Stress + due to friction of contact

f_c^2

∴ It is safe

No separate bars are required
to transfer the load.



Assume critical

M

(B-b)

ISOLATED SQUARE SLOPED FOOTING

Design an isolated square sloped footing for a column 500mm x 500mm transverse to the axis, located at 1200kN. The column is reinforced with 8 bars of 20mm diameter. The safe bearing capacity of soil is 12 tonnes per meter². Use M20 concrete & Fe415 Steel.

Given

$$b = 500$$

$$d = 500$$

$$w = 1200 \text{ kN}$$

$$q_{s0} = 12 \text{ tonnes/m}^2$$

$$= 12 \times 1000 \text{ kg/m}^2$$

$$= 12 \times 1000 \times 10 \text{ N/m}^2$$

$$\text{and } \phi_{\text{soil}} = 30^\circ \Rightarrow 120 \text{ kN/m}^2$$

$$\text{with } f_{ck} = 20 \text{ N/mm}^2$$

$$f_y = 415 \text{ N/mm}^2$$

Step 1: Dimensions of footing.

Let w' be the self weight of footing.

$$w' = 10\% w$$

$$= \frac{10}{100} \times 1200$$

$$= 120 \text{ kN}$$

$$\text{total load} = w + w' \\ = 1200 + 120 = 1320 \text{ kN}$$

$$\text{Area} = \frac{\text{load}}{\text{pressure}} = \frac{1320}{120} = 11 \text{ m}^2$$

$$B^2 = 11$$

$$B = \sqrt{11} = 3.31 \approx 3.4 \text{ m}$$

So provide a footing of $3.4 \text{ m} \times 3.4 \text{ m}$

$$\text{Net upward pressure} = \frac{1200}{3.4 \times 3.4} \\ = 103.8 \text{ kN/m}^2$$

1²

3.4
0

60
70

nd

chic

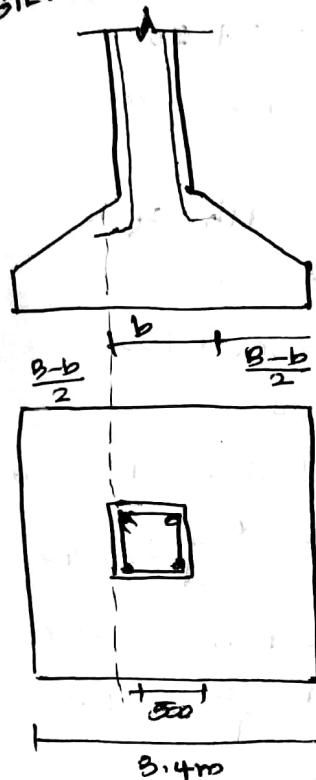
ed

$$b = 3.4 \text{ m}$$

size $3.4 \text{ m} \times 3.4 \text{ m}$

Net pressure 103.8 kN/m^2

STEP 2. DESIGN OF SECTION



1. Depth on the basis of bending compression.

The max bending moment occurs at the phase of the column & the magnitude is given by

$$M = P_o B \left(\frac{B-b}{2} \right) \times \frac{B-b}{4}$$

load.

$$M = \frac{P_o B (B-b)^2}{8}$$

$$= \frac{103.8 \times 3.4 (3.4 - 0.5)^2}{8}$$

$$= 371.007 \text{ kNm}$$

$$M_u = M \times 1.5$$

$$= 556.510 \text{ kNm}$$

Depth Annex 9

$$M_{\text{limit}} = 0.36 f_{ck} \frac{x_{\text{max}}}{d}$$

$$\left[1 - 0.42 \frac{x_{\text{max}}}{d} \right] b d^2 f_{ck}$$

$$556.51 \times 10^6 = 0.36 \times 0.48 \left[1 - 0.42 \frac{x_{\text{max}}}{0.48} \right]$$

$$500 \times 500 \times d^2 \times 20$$

$$d = 635.117 \text{ mm}$$

fix overall depth $D = 600 \text{ mm}$

assuming effective cover 60mm
effective depth $d = 760 - 60 = 700$

effective depth in other direction $= 760 - 12 = 688$

Provide overall depth at end
 $= 200 \text{ mm}$

Effective depth in one direction

$$200 - 60 = 140 \text{ mm}$$

Effective depth in other direct

$$140 - 12 = 128 \text{ mm}$$

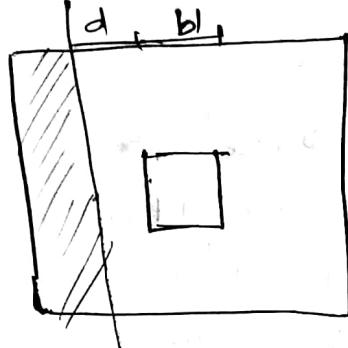
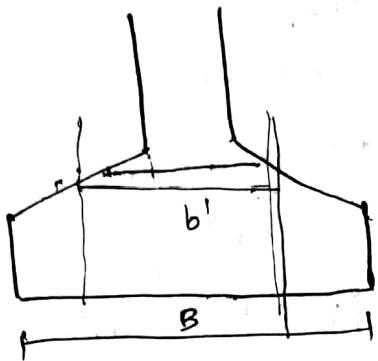
CHECK FOR SHEAR

Check for one way shear
Beams shear

Assume critical section at 'd' distance from the phase of the column

Shear force at section

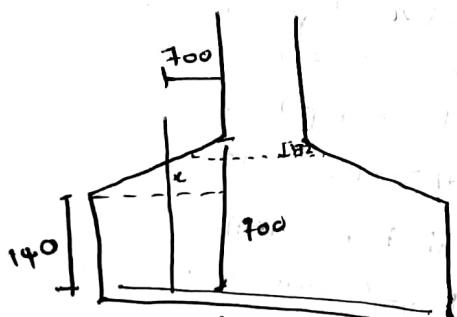
$$V = P_o B \left[\frac{B-b}{2} - d \right]$$



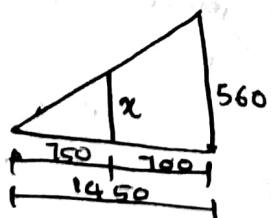
$$V = 103.8 \times 3.4 \left[\frac{3.4 - 0.5}{2} - 0.7 \right]$$

$$= 264.69$$

effective $V_u = 264.69 \times 1.5 = 391.035$
Depth at critical section $d' = 140 + x$



$$\frac{3400 - 500}{2} = d' = 140 + x$$



$$T_v = \frac{V_u}{bd} \cdot n$$

$$\frac{560}{x} = \frac{1450}{750}$$

$$x = 289.6 \text{ mm}$$

$$d' = 289.6 + 140$$

$$d' = 429.66 \\ = 430 \text{ mm}$$

Top width of the section

@ the section =

$$700 + 500 + 700 \\ = 1900$$

For a balanced section

we have $\frac{x_{\text{max}}}{d} = 0.48$

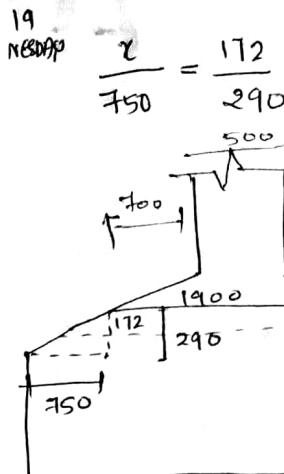
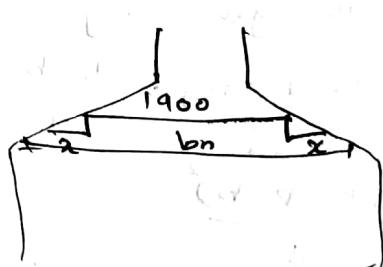
If the section is under reinforced $\frac{x_d}{d}$ must be less than $\frac{x_{\text{max}}}{d}$

Adopt a value $x_d = 0.4$
 $x_d = 0.4d' = 0.4 \times 430 = 172 \text{ mm}$
width of the section

@ neutral axis

$$1900 + x + x = b_n$$

width b_n



$$\frac{x}{750} = \frac{172}{290}$$

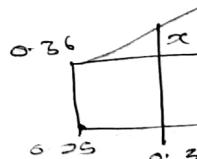
$$x = 445$$

width b_n @ the section
 $x + 1900 = 445 + 1900$

$$T_v = \frac{V_u}{b_n d'} = 0.$$

Assume 0.36 reinforcement

Table 19.



$$x = 0.36$$

$$T_c = 0.36 +$$

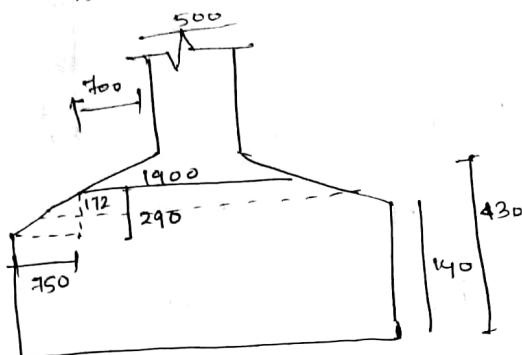
$$T_v < K T_c$$

$$D = 760 \text{ mm}$$

cl. 40.2.1.

L12.19
H0 N8D9P

$$\frac{x}{750} = \frac{172}{290}$$

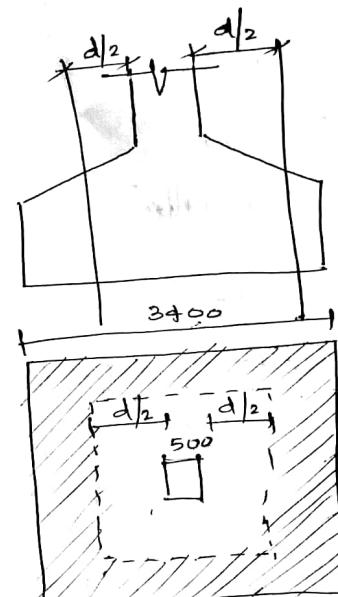


$D = 300$ or more $K = 1$
 $K = 1$ ($760 = D$)

$$K T_c = 0.384$$

$$T_v < K T_c$$

Hence safe
CHECK FOR 2 WAY SHEAR /
PUNCHING SHEAR



$$100 + 500 = 1200$$

Section lies @ $d/2$ distance
from the column face
Punching shear stress = $\frac{\text{force}}{\text{area}}$

stress \times Area

$$= 103.8 \left[\pi \cdot B^2 - B_0^2 \right]$$

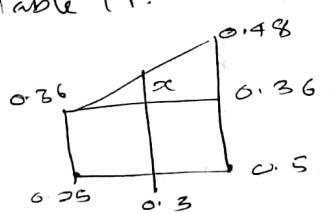
$$\sqrt{=} 103.8 \left[3.4^2 - 1.2^2 \right]$$

$$= 103.8 [10.12]$$

$$= 1050.456 \text{ kN}$$

$$V_u = 1050.456 \times 1.5 \\ = 1575.684 \text{ kN}$$

$$T_v = \frac{V_u}{4 \times b \times d}$$



$$x = 0.024$$

$$T_c = 0.36 + x = 0.384$$

$$T_v < K T_c$$

$$D = 760 \text{ mm}$$

(cl. 40.2.1.)

$$T_u = \frac{V_u}{4 B_{od}}$$

$$= \frac{15 + 5.684 \times 10^3}{4 \times 1200 \times 700}$$

$$= 0.468 \text{ N/mm}^2$$

ALLOWABLE SHEAR STRESS $\tau_s = K_s T_c$

$$T_c = 0.25 \sqrt{f_{ck}}$$

$$= 0.25 \sqrt{50}$$

$$= 1.118 \text{ N/mm}^2$$

$$K_s = 0.5 + \beta_c$$

β_c = Ratio of longer side to shorter side of column.

$$\therefore \beta_c = \frac{600}{500} = 1.2$$

$$K_s = 0.5 + 1 = 1.5$$

K_s subjected to a max of 1
Take $K_s = 1$

$$K_s T_c = 1.118 \text{ N/mm}^2$$

$$T_u < K_s T_c$$

Hence safe

DESIGN OF STEEL REINFORCEMENT

Annexe G)

$$M_u = 0.87 f_y A_{st} d \left[1 - \frac{A_{st} f_y}{bd f_{ck}} \right]$$

$$556.5 \times 10^6 = 0.87 \times 415 \times A_{st} \times 700$$

$$\left[1 - \frac{A_{st} \times 415}{500 \times 100 \times 415} \right]$$

$1390 > L_d$

Hence safe.

$$2201.9 = A_{st} - A_{st}^2 \approx 2.85 \times 10^{-3} \text{ TRANSFER OF LOAD BASE}$$

$$A_{st} = 2215.8, 348661.2, 0.1344$$

$$A_{st} = 2215.8 \text{ mm}^2 \quad \text{permissible area} = 0.45 \text{ F}$$

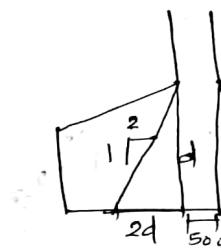
No. of bars:-

$$\frac{A_{st}}{\text{Area of 1 bar}} =$$

$$A_2 = \text{loaded area} = 500 \times 500$$

$$\frac{2215.8}{\frac{\pi}{4} \times 12^2} = 19.5 \approx 20 \text{ No.s.}$$

Hence provide 12mm dia 20 nos 12mm Ø bars uniformly spaced in each direction



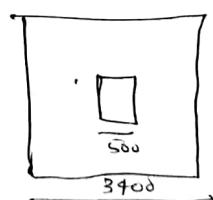
CHECK FOR DEVELOPMENT LENGTH

Min development length

$$= 47 \times \phi$$

$$= 47 \times 12 = 564 \text{ mm}$$

Available length



$$\frac{3900 - 500}{2} - 60 = 1340$$

$$\sqrt{\frac{A_1}{A_2}} = 6.6$$

\therefore It is greater than permissible

adopt max permissible

$$= 0.45 \times f_{ck}$$

$$= 0.45 \times 20$$

$$= 18 \text{ N/mm}^2$$

$$\begin{bmatrix} 715 \times A + 700 \\ \times 416 \\ 00 \times 415 \end{bmatrix}$$

$$+ 2 \times 2.85 \times 10^6$$

$$, 348661.24$$

mm²

$$1390 > L_d$$

Hence safe.

TRANSFER OF LOAD AT COLUMN BASE

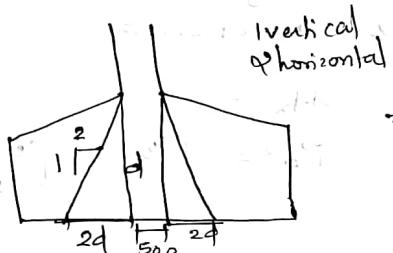
$$C1-34-4 Pg: 65$$

permissible bearing stress

$$= 0.45 f_{ck} \sqrt{\frac{A_1}{A_2}}$$

A_2 = loaded area of column

$$= 500 \times 500 = 250000$$



$$\begin{aligned} A_1 &= (2d + 500 + 2d)^2 \\ &= (2 \times 100 + 500 + 2 \times 100)^2 \\ &= 10890000 \\ &= 1089 \times 10^4 \text{ mm}^2 \end{aligned}$$

$$\sqrt{\frac{A_1}{A_2}} = 6.6$$

\therefore It is greater than 2
adopt max value 2

Permissible bearing stress

$$\begin{aligned} &= 0.45 \times f_{ck} \sqrt{\frac{A_1}{A_2}} \\ &= 0.45 \times 20 \times 2 \\ &= 18 \text{ N/mm}^2 \end{aligned}$$

length

$$= 564 \text{ mm}$$

length



$$100 - 60 = 1390$$

Actual bearing pressure =

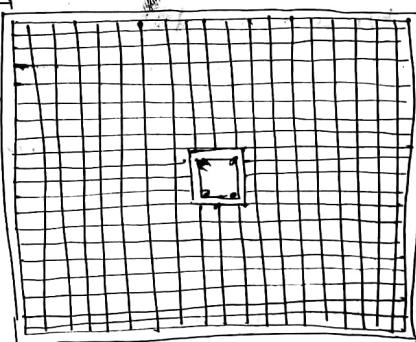
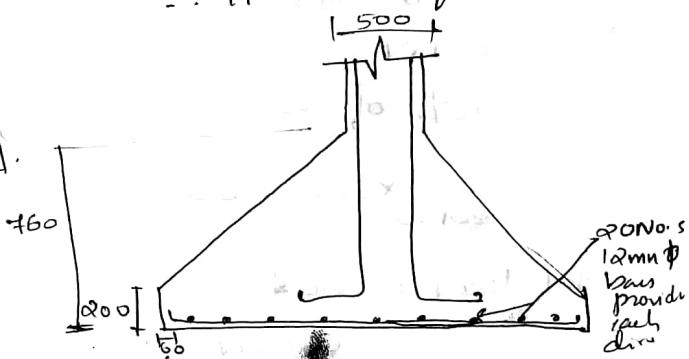
$$\frac{F.O.S \times \text{Load}}{\text{Area}}$$

$$= \frac{1.5 \times 1200 \times 10^3}{500 \times 500}$$

$$= 7.2 \text{ N/mm}$$

Actual bearing pressure < Permissible bearing pressure

\therefore It is safe.



Q: Isolated rectangular footing of uniform thickness for RC column bearing a vertical load of 600 KN and having a base size 400x600mm with a safe bearing capacity is taken as 60 kN/m². Use M20 concrete and Fe 415 steel

16.12.19
MONDAY

$$W = 600 \text{ kN}$$

Size of column =

$$400 \times 600 \text{ mm}$$

$$q_o = 120 \text{ kN/m}^2$$

$$f_{ck} = 20 \text{ N/mm}^2$$

$$f_y = 415 \text{ N/mm}^2$$

Step 1: Dimensions of the footing

$$W = 600 \text{ kN}$$

say $w^1 = 10\%$ of W

$$= \frac{10}{100} \times 600 = 60$$

$$\text{Total load} = 600 + 60$$

$$= 660 \text{ kN}$$

Area = $\frac{\text{load}}{\text{pressure}}$

$$= \frac{660}{120} = 5.5 \text{ m}^2$$

column and same ratio

Ratio of breadth to length
of footing = $\frac{400}{600} = \frac{2}{3}$

$$\text{Area} = 5.5 \text{ m}^2$$

$$L \times B = 5.5$$

$$L \times \frac{2}{3} L = 5.5$$

$$L = 2.87$$

$$L = 2.9 \text{ mm} \approx 3 \text{ mm}$$

$$B = 1.9 \text{ mm} \approx 2 \text{ mm}$$

Provide a footing of
length $3m \times 3m$.

Net upward pressure

$$= \frac{600}{2 \times 3} = 100 \text{ kN/m}^2$$

Step 2: Design of sections

D Depth on the basis of
bending compression

Max bending moment occurs
@ the face of the column
bending moment about
xx direction =

$$BM_{xx} =$$

$$P_o \times 2 \times \left(\frac{3-0.6}{2} \right) \left(\frac{3-0.6}{4} \right)$$

$$= 100 \times 2 \left(\frac{3-0.6}{2} \right) \left(\frac{3-0.6}{4} \right)$$

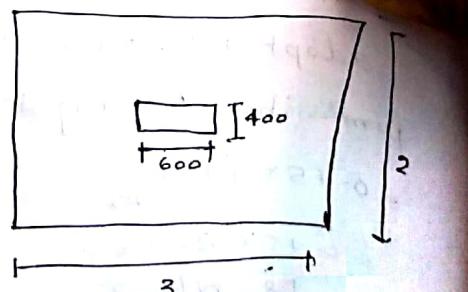
$$= 144 \text{ kNm}$$

$$M_{4xx} = 216 \text{ kNm}$$

$$BM_{yy} = 100 \times 3 \times \left(\frac{0-0.4}{2} \right) \left(\frac{0-0.4}{4} \right)$$

$$M_{yy} = 96 \text{ kNm}$$

$$M_{4yy} = 144 \text{ kNm}$$



(highest value
is considered
the depth of
Annexue 6)
 $M_u / \text{limit} = 0.36 \frac{x}{c}$

$$916 \times 10^6 = 0.36 \times 0.4 \times 2000$$

$$d = 197.8$$

Take effective

$$D = 197$$

$$= 0.95$$

$$\approx 260$$

18.12.19
Wednesday

(2) Depth of
beam s

For beam sh
is considered
fr

(highest value of moment is considered for finding the depth of footing)

Annexure 6)

$$M_u/\text{limit} = 0.86 \frac{x_{\max}}{d} \left[1 - 0.42 \frac{d_{\max}}{d} \right] b d^2 f_{ck}$$

$$976 \times 10^6 = 0.36 \times 0.48 \left[1 - 0.42 \times 0.48 \right] \times 2000 \times d^2 \times 20$$

$$d = 197.8$$

Take effective cover = 60mm

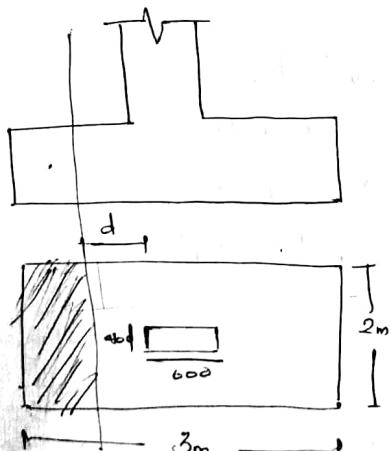
$$D = 197.8 + 60 \\ = 257.8 \text{ mm}$$

$$\approx 260$$

$$18.10.19 \\ d = 260 - 60 = 200 \text{ mm}$$

Wednesday.
(2) Depth on the basis of beam shear / one way.

for beam shear, the sectⁿ is considered at d distance from face of column.



Shear force

$$V = P_o B \left[\frac{3-0.6}{2} - d \times 10^{-3} \right]$$

$$= 100 \times 2 \left[\frac{3-0.6}{2} - d \times 10^{-3} \right]$$

$$V_u = 100 \times 2 \times 1.5 \left[\frac{3-0.6}{2} - d \times 10^{-3} \right]$$

$$V_u = 360 - 0.3d$$

$$T_v = \frac{V_u}{bd}$$

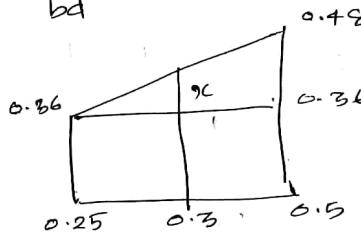
$$= \frac{(360 - 0.3d) 10^3}{2000 \times d}$$

T_{cv}

$$T_w = k T_c$$

Assume $P_E = 0.3\%$ for M_{20} concrete.

$$\frac{100 A_s}{bd} = P_E = 0.3\%$$



$$\frac{0.48 - 0.36}{x} = \frac{0.5 - 0.25}{0.3 - 0.25}$$

$$x = 0.024$$

$$T_c = 0.384 \text{ N/mm}^2$$

Value of K

$$D = 200 \text{ mm} \quad k = 1.2 \text{ mm}$$

$$T_v = k T_c$$

$$\frac{(360 - 0.3d) 10^3}{2000 d} = 1.2 \times 0.384$$

$$d = 294.69 \text{ mm}$$

$$\approx 300 \text{ mm}$$

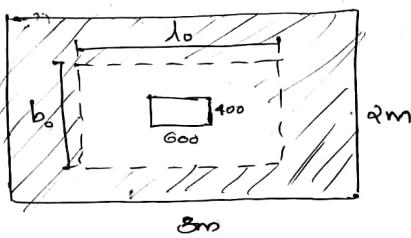
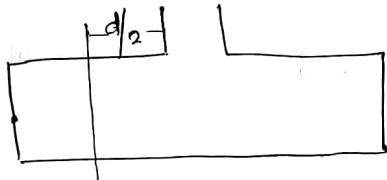
Effective depth in other direction = $300 - 12 = \underline{288 \text{ mm}}$

will take 300 (greater than 288)
 $\therefore d = 300$

3) Check for 2 way shear

For 2 way shear section lies at $d/2$ distance from flange of the column.

Adopt $d = 300 \text{ mm}$



$$l_o = 0.6 + 0.3 = 0.9 \text{ m}$$

$$b_o = 0.4 + 0.3 = 0.7 \text{ m}$$

$$\text{Area} = l \times b - l_o b_o$$

$$= 5.37 \text{ m}^2$$

Shear force:

$V = \text{Stress} \times \text{area}$

$$= 100 \times 5.37$$

$$= 537 \text{ kN}$$

$$V_u = 537 \times 1.5 = 805.5 \text{ kN}$$

$$T_v = \frac{V_u}{\text{Perimeter}}$$

$$T_v = \frac{V_u}{\text{Perimeter} \times d}$$

$$= \frac{V_u}{2(l_o + b_o) \times d}$$

$$= \frac{805.5 \times 10^3}{2(0.9 + 0.7) \times 300}$$

$$= 839.0625$$

$$= 0.839 \text{ N/mm}^2$$

Allowable stress = $k_s T_c$

C1 ~~31.6.3.1~~ 31.6.3.1

Pg: 59

Step 3: Design

$$I_u = 0.84 f_y$$

$$\times 10^8 = 0.84 \times 4$$

(1 -

$$A_{st} = 2154$$

$$\text{No. of bars} = \frac{2154}{414 \times 4}$$

Ast in other

$$M_u = 0.87 f_y$$

$$T_c = 0.25 \sqrt{F_{ck}} = 1.11 \text{ kN}^{1/2} \times 10^6 = 0.87 \times$$

$$k_s = 0.5 + \beta_c$$

$$= 0.5 + \frac{100}{600}$$

$$= 1.16$$

$$\text{Adopt } k_s = 1$$

$$k_s T_c = 1.11 \times 1$$

$$= 1.11 \text{ N/mm}^2$$

$$T_v < K_s T_c$$

\therefore Section is safe in 2 way shear.

Effective depth 288 mm is safe.

Step 5: cl

min dev

L_d =

Length of

=

Step 3: Design for Reinforcement

$$M_u = 0.87 f_y A_{st} d \left(1 - \frac{A_{st} f_y}{bd f_{ck}}\right)$$

length of bars in other direction

$$\left\{ \frac{3000 - 400}{2} \right\} - 60$$

$$= 740 \text{ mm} > L_d$$

$$216 \times 10^6 = 0.87 \times 415 A_{st} \times 300$$

$$\left(1 - \frac{A_{st} + 15}{3000 \times 300 \times 20}\right)$$

$$A_{st} = 2154$$

$$\text{No. of bars} = \frac{2154}{\pi/4 \times 12^2} = 19.04 \approx 20 \text{ Nos}$$

A_{st} in other direction

$$M_u = 0.87 f_y A_{st} d \left[1 - \frac{A_{st} f_y}{bd f_{ck}}\right]$$

$$144 \times 10^6 = 0.87 \times 415 \times A_{st} \times 288$$

$$\left[1 - \frac{A_{st} + 15}{3000 \times 288 \times 20}\right]$$

$$A_{st} = 1433.3 \text{ mm}^2$$

$$\text{No. of bars} = \frac{1433.3}{\pi/4 \times 12^2} \\ = 12.6 \approx 13 \text{ Nos.}$$

Step 5: Check for development length

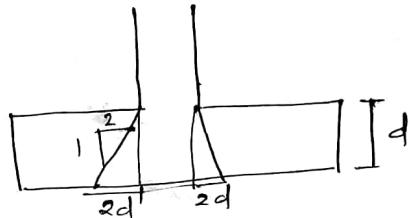
min development length

$$L_d = 41 \times \phi \\ = 41 \times 12 \\ = 564 \text{ mm}$$

$$\text{length of bars} = \left\{ \frac{3000 - 600}{2} \right\} - 60$$

$$= 1140 \text{ mm} > L_d$$

Step 6: Transfer of load
② column base.



Permissible stress = 0.45

$$0.45 f_{ck} \sqrt{\frac{A_1}{A_2}}$$

A_2 = loaded area of column

$$A_2 = 400 \times 800 = 240000$$

$$A_1 = (2d + 600 + 2d)^2$$

$$= (600 + 600 + 600)^2 \\ = 3240000$$

$$\sqrt{\frac{A_1}{A_2}} = 3.67$$

$$\text{Adopt } \sqrt{\frac{A_1}{A_2}} = 2$$

$$\text{Permissible stress} = 0.45 \times 2072 \\ = 18 \text{ N/mm}^2$$

$$\text{Actual bearing stress} = \frac{1.5 \times 600}{\text{Area}} = \frac{1.5 \times 600}{400 \times 600} \\ = 3.75 \text{ N/mm}^2$$

\therefore Actual bearing pressure < Permissible stress
 \therefore Bonding is safe.

Design a footing for circular column 560mm dia transmitting an axial load of 1200kN. The column is reinforced with 8 bars with 10mm dia. Safe bearing capacity of soil is 120 kN/m². Use M20 concrete & Fe415 steel.

Given: $w = 1200 \text{ kN}$

$$\phi_{\text{column}} = 560 \text{ mm}$$

$$q_o = 120 \text{ kN/m}^2$$

$$f_{ck} = 20 \text{ N/mm}^2$$

$$f_y = 415$$

Step 1 Size of footing

$$W_l = 1200 \text{ kN}$$

$$w' = 10\% \text{ of } W$$

$$= \frac{10}{100} \times 1200 = 120 \text{ kN}$$

$$\text{Total load} = 1200 + 120 = 1320$$

$$\text{Area of footing} = \frac{1320 \text{ kN}}{120 \text{ kN/mm}^2} = 11 \text{ m}^2$$

$$\pi R^2 = 11 \text{ m}^2$$

$$R = \sqrt{\frac{11}{\pi}} = 1.87$$

$$R = 1.9 \text{ m}$$

$$\phi = 3.8 \text{ m}$$

Length of one side of equivalent square,

$$2\pi R = 4a$$

$$\frac{2\pi R}{4} = a$$

$$\frac{2 \times \pi \times 1.9}{4} = a$$

$$a = 2.98 \text{ m}$$

Rest same as b4

Q. Isolated footing subjected to eccentric load

Q. Design an isolated unisymmetric square footing for a column 500x500 transmitting a load of 600kN and a moment of 30kNm. The safe bearing capacity of soil is 120kN. Use M20 concrete Fe415 steel.

Given: $w = 600 \text{ kN}$

$$M = 30 \text{ kNm}$$

Size of column = 500x500 mm

$$q_o = 120 \text{ kN/m}^2$$

$$f_{ck} = 20$$

$$f_y = 415$$

$$W_l = 1200 \text{ kN}$$

$$w' = \frac{10 \times 600}{100}$$

$$w' = 60 \text{ kN}$$

$$\text{Total } w + w' = 660 \text{ kN}$$

Area of footing

$$a^2 = 5.5$$

$$a = 2.345$$

$$a = 2.4$$

Provide a footing
Net upward press

$$= \frac{600}{2.4 \times 2.4}$$

$$= 104.1$$

$$\text{Moment} = \text{load} \times$$

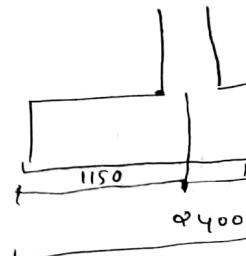
$$M = P \times e$$

$$e = \frac{M}{P}$$

$$\text{eccentricity} = \frac{M}{F}$$

$$= 0.0$$

$$= 50 \text{ mm}$$



e side of
uare,

$$W = 600 \text{ kN}$$

$$W' = \frac{10 \times 600}{100} = 60 \text{ kN}$$

$$W'' = 60 \text{ kN}$$

$$\text{Total } W + W' = 660 \text{ kN}$$

$$\text{Area of footing} = \frac{660}{120} = 5.5 \text{ m}^2$$

$$a^2 = 5.5 \text{ m}^2$$

$$a = 2.345$$

$$a = 2.4 \text{ m}$$

Provide a footing of size
Net upward pressure 2.4×2.4

$$= \frac{600}{2.4 \times 2.4}$$

$$= 104.16 \text{ kN/m}^2$$

Moment = Load \times distance

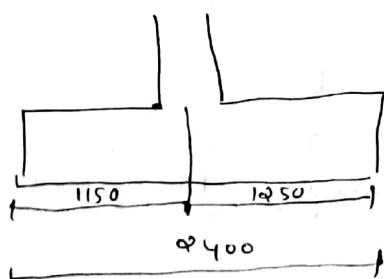
$$M = P \times e$$

$$e = \frac{M}{P}$$

$$\text{eccentricity} = \frac{M}{P} = \frac{300}{600} = 0.5 \text{ m}$$

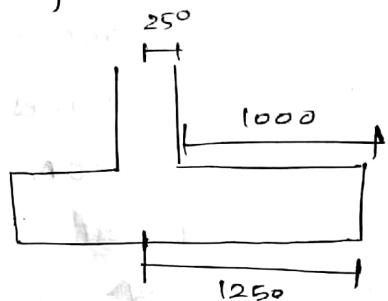
$$= 0.05 \text{ m}$$

$$= 50 \text{ mm}$$



Step 2: Design of section

D Depth on the basis of bending compression
(Highest eccentricity)



Cantilever length / length from
face of column =

$$1250 - 250 = 1000 \text{ mm} = 1 \text{ m}$$

$$M = P_o B \left(\frac{B-b}{2} \right) \left(\frac{B-b}{2} \right) = 1000$$

$$= P_o B \times 1 \times \frac{1}{2}$$

$$= 104.16 \times 2.4 \times \frac{1}{2}$$

$$M = 124.9 \times 1.5$$

$$M_u = 124.9 \times 1.5 = 187.48 \text{ kNm}$$

(Same as b4)

Take larger distance for
one way shear.