

$$\tau_c = 0.67 + x$$

$$= 0.68 \text{ N/mm}^2$$

$$\tau_{cmax} = 2.8 \text{ N/mm}^2$$

$$\tau_v > \tau_c > \tau_{cmax}$$

Provide design shear reinforcement in the form of vertical stirrups

$$V_{us} = \frac{0.87 f_y A_{sv} d}{S_v}$$

$$V_{us} = V_u - \tau_c b d$$

$$= 150 \times 10^3 - 0.68 \times 250 \times 450$$

$$= 73500 \text{ N}$$

2 legged -  $\phi 8 \text{ mm}$

$$73500 = \frac{0.87 \times 415 \times 2 \times \frac{\pi}{4} \times 8^2 \times 450}{S_v}$$

$$S_v = 222.22 \text{ mm} = 220$$

Check for spacing of shear reinforcement

Cl 26.5.1.5 of IS 456:2000

$$(i) 222.22 = 220$$

$$(ii) 0.75d = 0.75 \times 450 = 337.5$$

$$(iii) 300$$

So provide 2 legged stirrup of  $8 \text{ mm } \phi$

@  $220 \text{ mm c/c}$

### STEP 7 CHECK FOR DEFLECTION

$$\frac{l}{d} = \frac{5000}{450} = 11.11$$

$\therefore$  safe

### STEP 8 CHECK FOR DEVELOPMENT LENGTH

$$Cl-26.2.1$$

$$L_d = \frac{\phi \sigma_s}{4 \tau_{bd}}$$

$$= \frac{25 \times 0.87 \times 415}{4 \times 1.2}$$

$$= 1880.46 \text{ mm}$$

23.10.19 Wednesday SLAB MODULE '3'

### ONE WAY SLAB

$\frac{L}{l}$  (larger span by shorter span) always greater than 2

- Slab is supported only on 2 opposite sides
- Since the ratio of longer span to shorter span is greater than 2 the load distribution takes place in the shorter direction
- The main reinforcement is provided only in one direction.

### TWO WAY SLAB

The ratio of long to shorter span is less than 2 and the distribution takes place in both direction

The main reinforcement is provided in both direction

Slab is supported on the 4 sides

2. Design a reinforced concrete slab for having inside a

3x7 m thickness

supporting wall

Slab carries 75

lime mortar at

The unit rate

by  $20 \text{ kN/m}^3$

on the slab

Assume the slab

simply supported

ends. Use M20

Fe 415 steel.

$$L = 7 \text{ m}$$

$$l = 3 \text{ m}$$

thickness of slab = 300 mm

Finishing load = 20 kN/m<sup>2</sup>

$$L.L = 2 \text{ kN/m}^2$$

FOR

## TWO WAY SLAB

The ratio of longer span to shorter span is less than 2 and the load distribution takes place in both direction

The main reinforcement is provided in both direction  
Slab is supported on all the 4 sides

Q: Design a reinforced concrete slab for a room having inside dimension 3x7 m thickness of the supporting wall is 300mm slab carries 75mm thick lime mortar at its top  
The unit rate is given by 20 kN/m<sup>3</sup> live load on the slab is 2 kN/m  
Assume the slab to be simply supported at the ends. Use M20 concrete & Fe 415 steel.

$$L = 7m$$

$$l = 3m$$

thickness of support = 300mm

$$\text{Finishing load} = 20 \text{ kN/m}^3$$

$$L.L = 2 \text{ kN/m}$$

Finishing load =

$$[75 \text{ mm thick lime mortar unit wt} = 20 \text{ kN/m}^3]$$

$$= 1 \times 75 \times 20$$

$$= 1500$$

length is always 1m

$$f_{ck} = 20 \text{ N/mm}^2$$

$$f_y = 415 \text{ N/mm}^2$$

STEP 1: CHECK FOR ONE WAY SLAB

$$\frac{L}{l} = \frac{7}{3} = 2.33$$

$$> 2$$

∴ It is one way slab

STEP 2: SLAB DIMENSIONS

pg: 38

$$\frac{d}{d} = 20 \times M.F. \text{ modification factor}$$

Assume Percentage tension reinforcement = 0.35

Modification factor = 1.4

From Fig 4 of IS 456:2000

$$\frac{d}{d} = 20 \times 1.4$$

$$\frac{3000}{d} = 20 \times 1.4$$

$$d = \frac{3000}{20 \times 1.4} = 107.14 \text{ mm}$$

Assume clear cover = 30

$$D = d + c + \phi/2$$

$$c = 30$$

$$\phi = 12$$

max upto 16

$$= 107.14 + 30 + 12/2$$

$$= 143.14$$

$$\approx 150 \text{ mm}$$

$$d = 150 - 30 - 6 = 114 \text{ mm} \quad b = 1m$$

Effective span [cl 21.2.1]

$$(i) c/c = 3300 (3000 + 300)$$

$$(ii) l + d = 3000 + 114 = 3114$$

$\therefore$  effective span = 3114 mm

STEP 3: COMPUTATION OF BENDING MOMENT & LOAD

$$L.L = 2 \text{ kN/m}$$

$$D.L = c/s \text{ Area} \times \text{unit wt}$$

$$= 0.15 \times 1 \times 25$$

$$= 3.75 \text{ kN/m}$$

$$FL = 0.075 \times 1 \times 20$$

$$= 1.5 \text{ kN/m}$$

$$\text{Total DL} = 3.75 + 1.5$$

$$= 5.25 \text{ kN/m}$$

$$\text{Total Load} = L.L + D.L$$

$$= 2 + 5.25$$

$$= 7.25 \text{ kN/m}$$

$$M = \frac{wl^2}{8} = \frac{7.25 \times 3.114^2}{8}$$

$$M_u = \frac{7.25 \times 3.114^2}{8} \times 1.5$$

$$= 13.18 \text{ kNm}$$

STEP 4:

DEPTH OF NEUTRAL AXIS

$$M_u = 0.36 \frac{x_u}{d} \left[ 1 - 0.42 \frac{x_u}{d} \right] b d^2 f_{ck}$$

$$13.18 \times 10^6 = 0.36 \frac{x_u}{d} \left[ 1 - 0.42 \frac{x_u}{d} \right] 1000 \times 114^2 \times 20$$

$$\frac{x_u}{d} = 0.15 \quad \frac{0.0149}{2.234}$$

$$\frac{x_{u\max}}{d} = 0.48$$

[cl. 38.1 of IS 456:2000]

$$\frac{x_u}{d} < \frac{x_{u\max}}{d}$$

$\therefore$  under reinforced

STEP 5: COMPUTATION OF  $A_{st}$

$$M_u = 0.87 f_y A_{st} d \left[ 1 - \frac{A_{st} f_y}{b d f_{ck}} \right]$$

$$13.18 \times 10^6 = 0.87 \times 415 \times A_{st} \times 114$$

$$\left[ 1 - \frac{A_{st} \times 415}{1000 \times 114 \times 20} \right]$$

$$320.21 = A_{st} - A_{st}^2 \times 1.82 \times 10^{-4}$$

$$x = 341.3, 5153.20$$

$$A_{st} = 341.3 \text{ mm}^2 \rightarrow \text{main bar}$$

from Cl. 26.5.2.1

$$A_{st\min} = 0.12\% \text{ c/s area}$$

$$= \frac{0.12 b D}{100} \text{ HSD}$$

$$= \frac{0.12 \times 1000 \times 150}{100}$$

$$= 180 \text{ mm}^2 \rightarrow \text{for distribution bar.}$$

SPACING OF MAIN BAR

$$= \frac{100 \text{ breadth} \times \text{Area of 1 bar}}{A_{st}}$$

$$= \frac{1000 \times \frac{\pi}{4} \times 12^2}{341.431}$$

$$= 331.24 \text{ mm}$$

check for spacing  
cl. 26.3.3 b of

$$(i) 331.24$$

$$(ii) 3 \times d = 3 \times 114 = 342$$

$$(iii) 300$$

So provide

@ 300 mm c/s  
main rein.

DISTRIBUTION

$$\text{Spacing} = 1000 \times \frac{A_{st\min}}{A_{st}}$$

Assume  $\phi$

$$8 \text{ mm} =$$

$$1000 \times$$

$$= 279$$

check for spacing  
distribution

$$(i) 279 \approx 280$$

$$(ii) 3 \times d = 3 \times 114 = 342$$

$$(iii) 450$$

provide

@ 270 mm  
distrib

$$= \frac{1000 \times \frac{\pi}{4} \times 12^2}{341.431}$$

$$= 331.24 \text{ mm}^2$$

check for spacing

cl 20.3.3b of IS 456:2000

$$(i) 331.24$$

pg. 46

$$(ii) 3x d = 3 \times 114 = 342$$

$$(iii) 300$$

So provide 12mm  $\phi$  bar

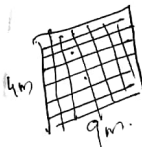
@ 300mm c/c as main reinforcement

DISTRIBUTION REINFORCEMENT

$$\text{Spacing} = \frac{1000 \times \text{Area of 1 bar}}{A_{st \text{ min}}}$$

Assume  $\phi$  of bars as 8mm =

$$\frac{1000 \times \frac{\pi}{4} \times 8^2}{180}$$



$$= 279 \text{ mm}^2$$

Check for spacing of distribution bars

$$(i) 279 \approx 270 \text{ mm}$$

$$(ii) 5d = 5 \times 114 = 570$$

$$(iii) 450$$

Provide 8mm  $\phi$  bars

@ 270mm c/c as distribution bars

STEP 6: CHECK FOR SHEAR

$$cl. 40.1$$

$$\tau_v < k \tau_c$$

$$\tau_v = \frac{V_u}{bd}$$

$$V_u = \frac{wl}{2} \times 1.5$$

$$= \frac{7.25 \times 3.114}{2} \times 1.5$$

$$= 16.93 \text{ kN}$$

$$\tau_v = \frac{16.93 \times 10^3}{1000 \times 114}$$

$$= 0.148 \text{ N/mm}^2$$

$$\tau_c \Rightarrow 100 \frac{A_s}{bd}$$

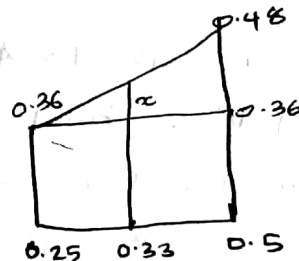
$$A_s = \frac{1000 \times \text{Area of 1 bar}}{\text{Spacing}}$$

$$= \frac{1000 \times \frac{\pi}{4} \times 12^2}{300}$$

$$= 376.99 \text{ mm}^2$$

$$100 \frac{A_s}{bd} = \frac{100 \times 376.99}{1000 \times 114}$$

$$= 0.33$$



$$\frac{0.5 - 0.25}{0.33 - 0.25} = \frac{0.48 - 0.36}{x}$$

$$x = 0.0384$$

$$\tau_c = 0.36 + 0.0384$$

$$= 0.3984$$

From Cl. A02.1.1 of IS 456: 2000

$$k = 1.30$$

$$k \tau_c = 1.3 \times 0.3984$$

$$= 0.507$$

$$\therefore \tau_v < 0.148 < 0.507$$

$$\tau_v < k \tau_c$$

$\therefore$  The slab is safe in shear

STEP 7: CHECK FOR DEVELOPMENT LENGTH [Cl. 26.2]

$$L_d = \frac{\phi \sigma_s}{4 \tau_{bd}}$$

$$= \frac{12 \times 0.87 \times 415}{4 \times 1.2}$$

$$= 902.62 \text{ mm}$$

Q: Design a slab  $9 \times 4 \text{ m}$  supported on brick wall 300 mm which is independent to be a floor of a library and is supposed to have a

live load  $5 \text{ kN/m}$  Use M20 concrete Fe 415

$$L = 9 \text{ m}$$

$$l = 4 \text{ m}$$

Support 300 mm

$$\text{L.L.} = 5 \text{ kN/m}$$

$$\text{F.L.} = 1 \text{ kN/m}$$

$$f_{ck} = 20 \text{ N/mm}^2$$

$$f_y = 415 \text{ N/mm}^2$$

STEP 1: CHECK FOR ONE WAY SLAB

$$\frac{L}{l} = \frac{9}{4} = 2.25 > 2$$

It is one way slab

STEP 2: SLAB DIMENSIONS

$$\frac{l}{d} = 20 \times \text{MF}$$

$$\frac{4000}{d} = 20 \times 1.4$$

$$d = 142.85$$

$$D = d + c + \phi/2$$

$$= 142.85 + 30 + 12/2$$

$$= 178.85$$

$$\approx 200 \text{ mm}$$

$$d = 200 - 30 - 6$$

$$= 164 \text{ mm}$$

$$b = 1 \text{ m}$$

Effective span

$$c/c = 4000 +$$

$$l + d = 4000$$

effective span

STEP 3: COM BENDING

LOAD

$$\text{L.L.} = 5$$

$$\text{D.L.} = 0.2$$

$$= 5$$

$$\text{F.L.} = 1$$

$$\text{TL} = \text{L.L.} +$$

$$= 11$$

$$m = \frac{w l^2}{8}$$

$$= 2$$

$$M_u =$$

STEP 4: D NE

$$M_u = 0.36 \frac{x_u}{d}$$

$$35.161 \times 10^6 =$$

$$\frac{x_u}{d} =$$

$$\frac{x_u}{d} =$$

$$\frac{x_u}{d} =$$

N/m Use  
Fe 415 HYS

(i)  $c/c = 4000 + 300 = 4300$   
 $l+d = 4000 + 164 = 4164$   
 effective span = 4164 mm

STEP 3: COMPUTATION OF  
BENDING MOMENT &  
LOAD.

L.L = 5 kN/m  
 D.L =  $0.2 \times 1 \times 25$   
 = 5

F.L = 1 kN/m

TL = L.L + D.L + F.L  
 = 11 kN/m

$M = \frac{w l^2}{8} = \frac{11 \times 4.164^2}{8}$

= 23.84

$M_u = M \times 1.5$   
 = 35.761 kNm

STEP 4: DEPTH OF  
NEUTRAL AXIS

$M_u = 0.36 \frac{x_u}{d} \left[ 1 - 0.42 \frac{x_u}{d} \right] b d^2 f_{ck}$

$35.761 \times 10^6 = 0.36 \frac{x_u}{d} \left[ 1 - 0.42 \frac{x_u}{d} \right] 1000 \times 164^2 \times 20$

$\frac{x_u}{d} - 0.42 \frac{x_u^2}{d} = 0.1846$

$x = 0.201, 2.179$

$\frac{x_u}{d} = 0.201$

$\frac{x_u}{d} < \frac{x_{u,max}}{d}$  under reinforced

STEP 5: COMPUTATION OF  
 $A_{st}$

$M_u = 0.87 f_y A_{st} d \left[ 1 - \frac{A_{st} f_y}{b d f_{ck}} \right]$

$35.761 \times 10^6 = 0.87 \times 415 \times A_{st} \times 164$

$\left[ 1 - \frac{A_{st} \times 415}{1000 \times 164 \times 20} \right]$

$608.94 = A_{st} - A_{st}^2 \times 1.2 \times 10^{-4}$   
 $A_{st} = 655.5$  7692

from Cl. 26.5.2.1

$A_{st,min} = 0.12\% \text{ c/s area}$

$= \frac{0.12 b D}{100}$

$= \frac{0.12 \times 1000 \times 200}{100}$

= 240 mm<sup>2</sup>

SPACING OF MAIN BAR

=  $1000 \times \frac{\text{Area of 1 bar}}{A_{st}}$

=  $1000 \times \frac{\pi/4 \times 12^2}{655.5}$

= 172.53 mm<sup>2</sup>

check for spacing

Cl. 26.3.3.b of IS 456:2000

(i)  $172.53 \approx 170$

(ii)  $s_d = 3 \times 164 = 492$

(iii) 800

So provide 12mm  $\phi$  bar

② 172.53 mm c/c as main reinforcement

## DISTRIBUTION REINFORCEMENT

$$\text{Spacing} = \frac{1000 \times \text{Area of 1 bar}}{A_{st \min}}$$

Assume  $\phi = 8 \text{ mm}$

$$\frac{1000 \times \pi/4 \times 8^2}{240}$$

$$= 209.43 \text{ mm}^2$$

check for spacing

$$(i) 209.43 \approx 200$$

$$(ii) 5d = 5 \times 164 = 820$$

$$(iii) 450$$

provide 8mm  $\phi$  bar at 200 mm c/c as distribution bars.

STEP 6: CHECK FOR SHEAR (cl. 40.1)

$$\tau_v < k \tau_c$$

$$\tau_v = \frac{V_u}{bd}$$

$$V_u = \frac{wL}{2} \times 1.5$$

$$= \frac{11 \times 4.164 \times 1.5}{2}$$

$$= 34.353$$

$$\tau_v = \frac{34.353 \times 10^3}{1000 \times 164}$$

$$= 0.209$$

$$\tau_c = 100 \frac{A_s}{bd}$$

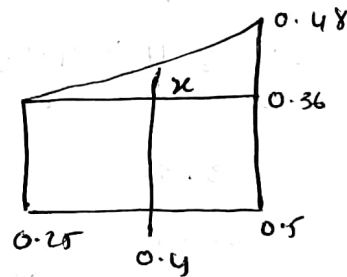
$$A_s = \frac{1000 \times \text{Area of 1 bar}}{\text{Spacing}}$$

$$= \frac{1000 \times \pi/4 \times 12^2}{170}$$

$$= 665.278$$

$$\tau_c = \frac{100 A_s / bd}{1000 \times 164}$$

$$= 0.405$$



$$\frac{0.5 - 0.25}{0.5 - 0.4} = \frac{0.5 - 0.36}{x}$$

$$x = 0.056$$

$$\tau_c = x + 0.36$$

$$= 0.416$$

From cl. 40.2.1.1

$$k = 1.3$$

$$k \tau_c = 1.3 \times 0.416$$

$$= 0.499$$

$$\tau_v < k \tau_c$$

slab is 8  
shear

STEP 7: CH  
DEVELOP  
cl. 26.

$$L_d = \frac{\phi \sigma_s}{4 \tau_b}$$

$$= 12$$

$$=$$

MODUL

DESIGN OF

A member ca  
axial load  
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slab is safe in shear.

### STEP 7: CHECK FOR DEVELOPMENT LENGTH cl. 26.2.1

$$L_d = \frac{\phi \sigma_s}{4 \tau_{bd}}$$

$$= \frac{12 \times 0.87 \times 415}{4 \times 1.2}$$

$$= 902.62 \text{ mm}$$

## MODULE 4

### DESIGN OF COLUMNS

A member carrying direct axial load is called as column, the effective length of which exceeds 3 times of its lateral dimensions.

- If the compression member carrying the load is inclined or horizontal it is termed as strut.
- The columns may be various shapes such as circular, rectangular, square etc.
- The longitudinal reinforcement bars in the columns are tied by laterally ties of suitable columns are tied by or stirrups laterally ties of suitable intervals, so that the bars does not buckle.

### FUNCTIONS OF LONGITUDINAL REINFORCEMENT

- To share the vertical compressive load
- To provide ductility to the column.
- To resist the tensile stresses due to eccentric load, moment or transverse load.
- To reduce the effect of creep and shrinkage.
- To prevent brittle failure.

### FUNCTIONS OF TRANSVERSE REINFORCEMENT

- To prevent brittle failure
- To provide ductility to column
- To confine the concrete thereby preventing longitudinal splitting.
- To resist diagonal tension caused due to transverse shear.
- To prevent longitudinal buckling of the longitudinal reinforcement.

### SHORT COLUMNS AND LONG COLUMNS

A compression member is considered as short when the slenderness ratio ( $l/d$ ) is less than 12 and if the slenderness ratio ( $l/d$ )