three types of failure modes is beyond the scope here. Only the salient points needed for the routine design of beams in shear are presented here.

## **Shear Stress**

The distribution of shear stress in reinforced concrete rectangular, T and L-beams of uniform and varying depths depends on the distribution of the normal stress. However, for the sake of simplicity the nominal shear stress  $\tau_{\nu}$  is considered which is calculated as follows (IS 456, cls. 40.1 and 40.1.1):

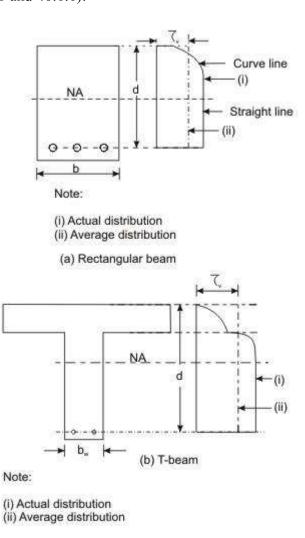


Figure 1.11: Distribution of shear stress and average shear stress

(i) In beams of uniform depth (Figs. 1.11a and b):

$$\tau_{v} = \frac{V_{u}}{bd} \tag{13}$$

where V = shear force due to design loads,

b = breadth of rectangular beams and breadth of the web  $b_{w}$  for flanged beams, and

d = effective depth.

(ii) In beams of varying depth:

$$\tau_{v} = \frac{V_{u} \pm \frac{M_{u}}{d} \tan \beta}{bd} \tag{14}$$

where  $\tau_v$ , Vu, b or  $b_w$  and d are the same as in (i),

 $M_u$  = bending moment at the section, and

 $\beta$  = angle between the top and the bottom edges.

The positive sign is applicable when the bending moment  $M_u$  decreases numerically in the same direction as the effective depth increases, and the negative sign is applicable when the bending moment  $M_u$  increases numerically in the same direction as the effective depth increases.

## **Design Shear Strength of Reinforced Concrete**

Recent laboratory experiments confirmed that reinforced concrete in beams has shear strength even without any shear reinforcement. This shear strength ( $\tau_c$ ) depends on the grade of concrete and the percentage of tension steel in beams. On the other hand, the shear strength of reinforced concrete with the reinforcement is restricted to some maximum value  $\tau_{cmax}$  depending on the grade of concrete. These minimum and maximum shear strengths of reinforced concrete (IS 456, cls. 40.2.1 and 40.2.3, respectively) are given below:

#### Design shear strength without shear reinforcement (IS 456, cl. 40.2.1)

Table 19 of IS 456 stipulates the design shear strength of concrete  $\tau_c$  for different grades of concrete with a wide range of percentages of positive tensile steel reinforcement. It is worth mentioning that the reinforced concrete beams must be provided with the minimum shear reinforcement as per cl. 40.3 even when  $\tau_c$  is less than  $\tau_c$  given in Table 3.

Table 3 Design shear strength of concrete,  $\tau_c$  in N/mm<sup>2</sup>

$100A_{\rm s}$ / $bd$	Grade of concrete						
3	M 20	M 25	M 30	M 35	M40 and		
					above		
≤ 0.15	0.28	0.29	0.29	0.29	0.30		
0.25	0.36	0.36	0.37	0.37	0.38		
0.50	0.48	0.49	0.50	0.50	0.51		
0.75	0.56	0.57	0.59	0.59	0.60		

1.00	0.62	0.64	0.66	0.67	0.68
1.25	0.67	0.70	0.71	0.73	0.74
1.50	0.72	0.74	0.76	0.78	0.79
1.75	0.75	0.78	0.80	0.82	0.84
2.00	0.79	0.82	0.84	0.86	0.88
2.25	0.81	0.85	0.88	0.90	0.92
2.50	0.82	0.88	0.91	0.93	0.95
2.75	0.82	0.90	0.94	0.96	0.98
≥ 3.00	0.82	0.92	0.96	0.99	1.01

In Table 3,  $A_s$  is the area of longitudinal tension reinforcement which continues at least one effective depth beyond the section considered except at support where the full area of tension reinforcement may be used provided the detailing is as per IS 456, cls. 26.2.2 and 26.2.3.

# Maximum shear stress $\tau_{cmax}$ with shear reinforcement (cls. 40.2.3, 40.5.1 and 41.3.1)

Table 20 of IS 456 stipulates the maximum shear stress of reinforced concrete in beams  $\tau_{cmax}$  as given below in Table 6.2. Under no circumstances, the nominal shear stress in beams  $\tau_{v}$  shall exceed  $\tau_{cmax}$  given in Table 6.2 for different grades of concrete.

Table 4 Maximum shear stress,  $\tau_{cmax}$  in N/mm<sup>2</sup>

Grade of	M 20	M 25	M 30	M 35	M 40 and
concrete					above
$\tau_{c,\text{max}} \text{ N/mm}^2$	2.8	3.1	3.5	3.7	4.0

#### **Critical Section for Shear**

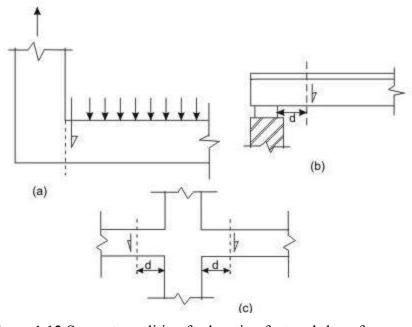


Figure 1.12 Support condition for locating factored shear force

Clauses 22.6.2 and 22.6.2.1 stipulate the critical section for shear and are as follows:

For beams generally subjected to uniformly distributed loads or where the principal load is located further than 2d from the face of the support, where d is the effective depth of the beam, the critical sections depend on the conditions of supports as shown in Figs. 1.12 a, b and c and are mentioned below.

- (i) When the reaction in the direction of the applied shear introduces tension (Fig. 1.12a) into the end region of the member, the shear force is to be computed at the face of the support of the member at that section.
- (ii) When the reaction in the direction of the applied shear introduces compression into the end region of the member (Figs. 1.12b and c), the shear force computed at a distance d from the face of the support is to be used for the design of sections located at a distance less than d from the face of the support. The enhanced shear strength of sections close to supports, however, may be considered as discussed in the following section.

# Minimum Shear Reinforcement (cls. 40.3, 26.5.1.5 and 26.5.1.6 of IS 456)

Minimum shear reinforcement has to be provided even when  $\tau_v$  is less than  $\tau_c$  given in Table 3 as recommended in cl. 40.3 of IS 456. The amount of minimum shear reinforcement, as given in cl. 26.5.1.6, is given below.

The minimum shear reinforcement in the form of stirrups shall be provided such that:

$$\frac{A_{sv}}{bs_v} \ge \frac{0.4}{0.87f_v} \tag{15}$$

where  $A_{sv}$  = total cross-sectional area of stirrup legs effective in shear,

 $s_{y} =$ stirrup spacing along the length of the member,

b =breadth of the beam or breadth of the web of the web of flanged beam  $b_{w}$ , and

 $f_y$  = characteristic strength of the stirrup reinforcement in N/mm<sup>2</sup> which shall not be taken greater than 415 N/mm<sup>2</sup>.

The above provision is not applicable for members of minor structural importance such as lintels where the maximum shear stress calculated is less than half the permissible value.

The minimum shear reinforcement is provided for the following:

- (i) Any sudden failure of beams is prevented if concrete cover bursts and the bond to the tension steel is lost.
- (ii) Brittle shear failure is arrested which would have occurred without shear reinforcement.

- (iii) Tension failure is prevented which would have occurred due to shrinkage, thermal stresses and internal cracking in beams.
- (iv) To hold the reinforcement in place when concrete is poured.
- (v) Section becomes effective with the tie effect of the compression steel.

Further, cl. 26.5.1.5 of IS 456 stipulates that the maximum spacing of shear reinforcement measured along the axis of the member shall not be more than 0.75 d for vertical stirrups and d for inclined stirrups at  $45^{\circ}$ , where d is the effective depth of the section. However, the spacing shall not exceed 300 mm in any case.

## Design of Shear Reinforcement (cl. 40.4 of IS 456)

When  $\tau_{v}$  is more than  $\tau_{c}$  given in Table 6.1, shear reinforcement shall be provided in any of the three following forms:

- (a) Vertical stirrups,
- (b) Bent-up bars along with stirrups, and
- (c) Inclined stirrups.

In the case of bent-up bars, it is to be seen that the contribution towards shear resistance of bent-up bars should not be more than fifty per cent of that of the total shear reinforcement.

The amount of shear reinforcement to be provided is determined to carry a shear force  $V_{us}$  equal to

$$V_{us} = V_u - \tau_c bd \tag{16}$$

where b is the breadth of rectangular beams or  $b_{w}$  in the case of flanged beams.

The strengths of shear reinforcement  $V_{us}$  for the three types of shear reinforcement are as follows:

(a) Vertical stirrups:

$$V_{us} = \frac{0.87 f_y A_{sv} d}{s_v} \tag{17}$$

(b) For inclined stirrups or a series of bars bent-up at different cross-sections:

$$V_{us} = \frac{0.87 f_y A_{sv} d}{s_v} (\sin \alpha + \cos \alpha) \tag{18}$$

(c) For single bar or single group of parallel bars, all bent-up at the same cross-section:

$$V_{us} = 0.87 f_y A_{sv} d \sin \alpha \tag{19}$$

where  $A_{sy}$  = total cross-sectional area of stirrup legs or bent-up bars within a distance  $s_{sy}$ ,

 $s_{ij}$  = spacing of stirrups or bent-up bars along the length of the member,

 $\tau$  = nominal shear stress,

 $\tau$  = design shear strength of concrete,

- b =breadth of the member which for the flanged beams shall be taken as the breadth of the web  $b_{...}$ ,
- $f_y$  = characteristic strength of the stirrup or bent-up reinforcement which shall not be taken greater than 415 N/mm<sup>2</sup>,
- $\alpha$  = angle between the inclined stirrup or bent-up bar and the axis of the member, not less than 45 $^{\circ}$ , and

d =effective depth.

The following two points are to be noted:

- (i) The total shear resistance shall be computed as the sum of the resistance for the various types separately where more than one type of shear reinforcement is used.
- (ii) The area of stirrups shall not be less than the minimum specified in cl. 26.5.1.6.

#### **Curtailment of Tension Reinforcement in Flexural Members (cl. 26.2.3.2 of IS 456)**

Curtailment of tension reinforcement is done to provide the required reduced area of steel with the reduction of the bending moment. However, shear force increases with the reduction of bending moment. Therefore, it is necessary to satisfy any one of following three conditions while terminating the flexural reinforcement in tension zone:

(i) The shear stress  $\tau_{\nu}$  at the cut-off point should not exceed two-thirds of the permitted value which includes the shear strength of the web reinforcement. Accordingly,

$$\tau_v \le (2/3)(\tau_c + V_{us}/bd)$$
or  $V_{us} \ge (1.5\tau_v - \tau_c)bd$ 

(ii) For each of the terminated bars, additional stirrup area should be provided over a distance of three-fourth of effective depth from the cut-off point. The additional stirrup area shall not be less than  $0.4 \ b \ s/f_y$ , where b is the breadth of rectangular beams and is replaced by  $b_w$ , the breadth of the web for flanged beams, s = spacing of additional stirrups and  $f_y$  is the characteristic strength of stirrup reinforcement in N/mm. The value of s shall not exceed d/(8)