

$$\frac{0.5 - 0.25}{0.33 - 0.25} = \frac{0.48 - 0.36}{x}$$

$$x = 0.0384$$

$$\tau_c = 0.36 + 0.0384$$

$$= 0.3984$$

From Cl. A.2.1.1 of IS 456: 2000

$$k = 1.30$$

$$k \tau_c = 1.3 \times 0.3984$$

$$= 0.507$$

$$\therefore \tau_v < 0.507$$

$$\tau_v < k \tau_c$$

\therefore The slab is safe in shear

STEP 1: CHECK FOR DEVELOPMENT LENGTH [Cl. 26.2.]

$$L_d = \frac{\phi \sigma_s}{4 \tau_{bd}}$$

$$= \frac{12 \times 0.87 \times 415}{4 \times 1.2}$$

$$= 902.62 \text{ mm}$$

Q: Design a slab $9 \times 4 \text{ m}$ supported on brick wall 300 mm which is independent to be a floor of a library and is supposed to have a

M20 concrete Fe 415 (IS 456)

$$L = 9 \text{ m}$$

$$l = 4 \text{ m}$$

Support 300 mm

$$L.L = 5 \text{ kN/m}$$

$$F.L = 1 \text{ kN/m}$$

$$f_{\text{ack}} = 20 \text{ N/mm}^2$$

$$f_y = 415 \text{ N/mm}^2$$

STEP 1: CHECK FOR ONE WAY SLAB

$$\frac{L}{l} = \frac{9}{4} = 2.25 > 2$$

It is one way slab

STEP 2: SLAB DIMENSIONS

$$\frac{L}{d} = 20 \times \text{MF}$$

$$\frac{4000}{d} = 20 \times 1.4$$

$$d = 142.85$$

$$D = d + c + \phi/2$$

$$= 142.85 + 30 + 12/2$$

$$= 178.85$$

$$\approx 200 \text{ mm}$$

$$d = 200 - 30 - 6$$

$$= 164 \text{ mm}$$

$$b = 1 \text{ m}$$

Effective span

$$① c/c = 4000 + 300 = 4300$$

$$l+d = 4000 + 164 = 4164$$

$$\text{effective span} = 4164 \text{ mm}$$

STEP 3: COMPUTATION OF BENDING MOMENT & LOAD.

$$L.L = 5 \text{ kN/m}$$

$$D.L = 0.2 \times 1 \times 25 = 5$$

$$F.L = 1 \text{ kN/m}$$

$$TL = L.L + D.L + F.L = 11 \text{ kN/m}$$

$$M = \frac{w l^2}{8} = \frac{11 \times 4.164^2}{8} = 23.84$$

$$M_u = M \times 1.5 = 35.761 \text{ kNm}$$

STEP 4: DEPTH OF NEUTRAL AXIS

$$M_u = 0.36 \frac{x_u}{d} \left[1 - 0.42 \frac{x_u}{d} \right] b d^2 f_{ck}$$

$$35.761 \times 10^6 = 0.36 \frac{x_u}{d} \left[1 - 0.42 \frac{x_u}{d} \right] 1000 \times 164^2 \times 20$$

$$\frac{x_u}{d} - 0.42 \frac{x_u^2}{d} = 0.1846$$

$$x = 0.201, 2.179$$

$$\frac{x_u}{d} = 0.201$$

$$\frac{x_u}{d} < \frac{x_{u\max}}{d} \text{ under reinforced}$$

STEP 5: COMPUTATION OF A_{st}

$$M_u = 0.87 f_y A_{st} d \left[1 - \frac{A_{st} f_y}{b d f_{ck}} \right]$$

$$35.761 \times 10^6 = 0.87 \times 415 \times A_{st} \times 164$$

$$603.94 = A_{st} - \frac{A_{st}^2 \times 415}{1000 \times 164 \times 20}$$

$$A_{st} = 655.5 \quad 7697$$

from Cl. 26.5.2.1

$$A_{st\min} = 0.12\% \text{ c/s area}$$

$$= \frac{0.12 b D}{100}$$

$$= \frac{0.12 \times 1000 \times 200}{100}$$

$$= 240 \text{ mm}^2$$

SPACING OF MAIN BAR

$$= 1000 \times \frac{\text{Area of 1 bar}}{A_{st}}$$

$$= \frac{1000 \times \frac{\pi}{4} \times 12^2}{655.5}$$

$$= 172.53 \text{ mm}^2$$

check for spacing

Cl. 26.3.3.b of IS 456:2000

$$(i) 172.53 \approx 170$$

$$(ii) 3d = 3 \times 164 = 492$$

$$(iii) 800$$

So provide 12mm ϕ bar

@ 170 mm c/c as main reinforcement

DISTRIBUTION REINFORCEMENT

$$\text{Spacing} = \frac{1000 \times \text{Area of 1 bar}}{A_{st \min}}$$

Assume $\phi = 8 \text{ mm}$

$$\frac{1000 \times \frac{\pi}{4} \times 8^2}{240} = 209.43 \text{ mm}^2$$

Check for spacing

$$(i) 209.43 \approx 200$$

$$(ii) 5d = 5 \times 164 = 820$$

$$(iii) 450$$

provide 8mm ϕ bar at 200 mm c/c as distribution bars.

STEP 6: CHECK FOR SHEAR (cl-40.1)

$$\tau_v < k \tau_c$$

$$\tau_v = \frac{V_u}{bd}$$

$$V_u = \frac{wL}{2} \times 1.5 = \frac{11 \times 4.164 \times 1.5}{2}$$

$$= 34.353$$

$$\tau_v = \frac{34.353 \times 10^3}{1000 \times 164} = 0.209$$

$$\tau_c = 100 \frac{f_{cs}}{bd}$$

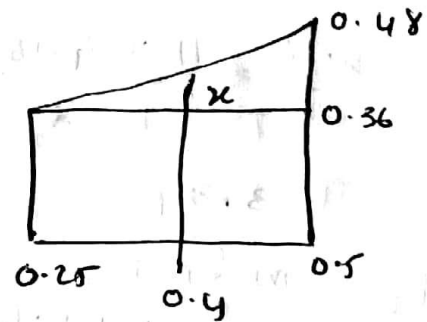
$$A_s = 1000 \frac{\text{Area of 1 bar}}{\text{Spacing}}$$

$$= \frac{1000 \times \frac{\pi}{4} \times 12^2}{170}$$

$$= 665.278$$

$$\frac{100 A_s}{b d} = \frac{100 \times 665.278}{1000 \times 164}$$

$$= 0.405$$



$$\frac{0.5 - 0.25}{0.5 - 0.4} = \frac{0.5 - 0.36}{x}$$

$$x = 0.056$$

$$\tau_c = x + 0.36 = 0.416$$

From cl-40.2.1.1

$$k = 1.3$$

$$k \tau_c = 1.3 \times 0.416 = 0.499$$

$$\tau_v < k \tau_c$$

slab is safe in
shear.

STEP 7: CHECK FOR
DEVELOPMENT LENGTH
cl. 26.2.1

$$L_d = \frac{\Phi \sigma_s}{4 \tau_{bd}}$$

$$= \frac{12 \times 0.87 \times 415}{4 \times 1.2}$$

$$= 902.62 \text{ mm}$$