

# Recursion

- Concept in programming
  - Function calls itself to solve a problem
  - A problem can be solved by dividing into sub-problems
  - Why & When
    - ① Problem can be divided into sub problems.
    - ② Base case.
    - ③ Tree , Graph traversal.
    - ④ Backtracking.
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## ① Base condition

→ there is a simple solution of the problem that can be directly solved.

## ② Recursive call

→ We should be able to divide the problem.

## ③ Combine the results.

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Example :- Factorial of a number

$$\begin{aligned} \text{Eg } 5! &= 120 \\ &= 5 \times 4 \times 3 \times 2 \times 1 \end{aligned}$$

$$n! = n \times (n-1) \times (n-2) \dots \times 1$$

~~n!~~

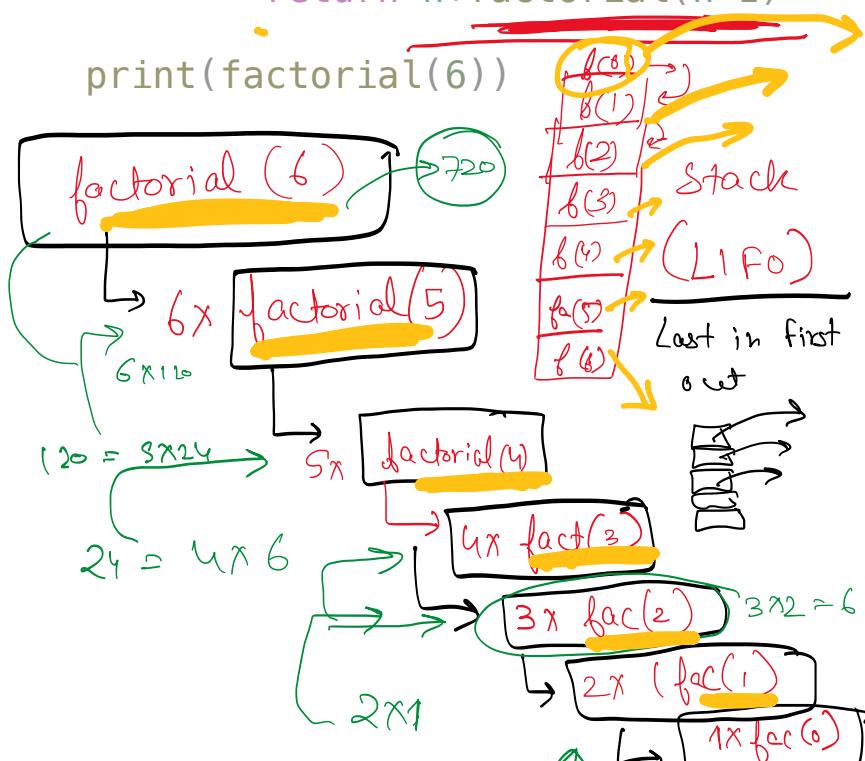
$$n! = n \times (n-1)! \rightarrow \text{divide}$$

$$(n-1)! = (n-1)(n-2)!$$

$$1! = 1$$

$$n=0 \Rightarrow 1 \quad \text{Base case.}$$

```
def factorial(n):
    # base condition
    if n==0:
        return 1
    else:
        return n*factorial(n-1)
```



$$1 \times 1 = 1$$

Fibonacci Series

$$F(n) = F(n-1) + F(n-2)$$

$$\begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & \dots \\ 0 & 1 & 1 & 2 & 3 & 5 & 8 & \dots \end{matrix}$$

Base condition:-

$$\left. \begin{array}{l} f(0) = 0 \\ f(1) = 1 \end{array} \right\}$$

$$f(n) = \underbrace{f(n-1)}_{\text{fibonacci}} + \underbrace{f(n-2)}_{\text{fibonacci}}$$

```
def fibonacci(n): # f(n) = f(n-1) +f(n-2)
    # base condition
    Box { if n<=1:
        return n
    else:
        return fibonacci(n-1) +fibonacci(n-2)}
```

fibonacci(6)

$$\begin{aligned} \underline{\underline{\text{fib}(4)}} &\xrightarrow{3} \\ \underline{\underline{\text{fib}(3) + \text{fib}(2)}} &\xrightarrow{2} \quad \xrightarrow{1} \end{aligned}$$

