

CMPE 256 Assignment

Starbucks Assignment

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Points	Co-ordinates	Points	Co-ordinates
P ₀	(1, 5)	P ₁₀	(4, 8)
P ₁	(1, 7)	P ₁₁	(4, 8)
P ₂	(2, 6)	P ₁₂	(5, 4)
P ₃	(2, 9)	P ₁₃	(5, 7)
P ₄	(3, 3)	P ₁₄	(6, 9)
P ₅	(3, 6)	P ₁₅	(7, 2)
P ₆	(3, 8)	P ₁₆	(7, 3)
P ₇	(3, 8)	P ₁₇	(7, 9)
P ₈	(3, 9)	P ₁₈	(8, 1)
P ₉	(4, 5)	P ₁₉	(8, 7)

⇒ We will form 3 clusters with points P₀, P₈, P₁₈.
in all the 3 clusters

	Cluster 1 (C ₁)	Cluster 2 (C ₂)	Cluster (C ₃)
Centroid	(1, 5)	(3, 9)	(8, 1)

⇒ Let's take a point P₁ (1, 7)

$$\text{Distance from } C_1 = \sqrt{(1-1)^2 + (5-7)^2} = 2 = D_1$$

$$\text{Distance from } C_2 = \sqrt{(3-1)^2 + (9-7)^2} = \sqrt{4+4} = \sqrt{8} = D_2$$

$$\text{Distance from } C_3 = \sqrt{(8-1)^2 + (1-7)^2} = \sqrt{85} = D_3$$

⇒ D₁ is less, Point P₁ will be in Cluster C₁

Centroid C_1 $(1, 6)$ C_2 $(\frac{3}{4}, \frac{9}{4})$ C_3 $(8, 1)$

⇒ Let's take point P_2 $(2, 8)$

Distance $D_1 = \sqrt{(2-1)^2 + 0^2} = 1$

Distance $D_2 = \sqrt{(4-\frac{3}{4})^2 + (6-\frac{9}{4})^2} = \sqrt{5}$

Distance $D_3 = \sqrt{(\frac{8-4}{2})^2 + (1-\frac{9}{4})^2} = \sqrt{37}$

Distance $D_2 = \sqrt{(3-2)^2 + (9-6)^2} = \sqrt{10}$

Distance $D_1 = \sqrt{(2-1)^2 + (6-9)^2} = 1$

Distance $D_3 = \sqrt{(8-2)^2 + (6-1)^2} = \sqrt{61}$

⇒ D_1 is less, P_2 will be in cluster C_1 .

Centroid C_1 $(1.5, 6)$ C_2 $(\frac{3}{4}, \frac{9}{4})$ C_3 $(8, 1)$

⇒ Point P_3 $(2, 9)$

$D_1 = \sqrt{(2-1.5)^2 + (9-6)^2} = \sqrt{9.25} = 3.04$

$D_2 = \sqrt{(3-2)^2 + (9-9)^2} = 1$

$D_3 = \sqrt{(8-2)^2 + (9-1)^2} = 10$

⇒ D_2 is less, P_3 will be in cluster C_2 .

C_1 C_2 C_3
 $(1.5, 6)$ $(2.5, 9)$ $(8, 1)$

⇒ Point $P_4(3, 3)$

$$D_1 = \sqrt{(3-1.5)^2 + (6-3)^2} = \sqrt{11.25}$$

$$D_2 = \sqrt{(3-2.5)^2 + (9-3)^2} = \sqrt{36.25}$$

$$D_3 = \sqrt{(8-3)^2 + (3-1)^2} = \sqrt{29}$$

⇒ D_1 is less, P_4 will be in cluster C_1 .

C_1 C_2 C_3
 $(2, 2, 4.5)$ $(2.5, 9)$ $(8, 1)$

⇒ Point $P_5(3, 6)$

$$D_1 = \sqrt{(3-2)^2 + (6-4.5)^2} = \sqrt{2.89}$$

$$D_2 = \sqrt{(3-2.5)^2 + (9-6)^2} = \sqrt{9.25}$$

$$D_3 = \sqrt{(8-3)^2 + (6-1)^2} = \sqrt{50}$$

⇒ D_1 is less, P_5 will be in cluster C_1 .

C_1 C_2 C_3
 $(2, 6, 5.2)$ $(2.5, 9)$ $(8, 1)$

⇒ Point $P_6(3, 8)$

$$D_1 = \sqrt{(3-2.6)^2 + (8-5.2)^2} = \sqrt{8}$$

$$D_2 = \sqrt{(3-2.5)^2 + (8-7)^2} = \sqrt{10.25} \approx 3.2$$

$$D_3 = \sqrt{(8-3)^2 + (1-8)^2} = \sqrt{74}$$

⇒ D_2 is less, P_6 will be included in C_2

⇒ $C_1 = (2.6, 5.2)$ $C_2 = (2.7, 8.5)$ $C_3 = (8, 1)$

⇒ Point $P_7(3, 8)$

$$D_1 = \sqrt{(2.6-3)^2 + (8-5.2)^2} = \sqrt{8}$$

$$D_2 = \sqrt{(3-2.7)^2 + (8-8.5)^2} = \sqrt{0.34} \approx 0.58$$

$$D_3 = \sqrt{(8-3)^2 + (1-8)^2} = \sqrt{74}$$

⇒ D_2 is less, P_7 will be in cluster C_2

⇒ $C_1 = (2.6, 5.2)$ $C_2 = (2.7, 8.5)$ $C_3 = (8, 1)$

⇒ Point $P_9(4, 5)$

$$D_1 = \sqrt{(4-2.6)^2 + (5-5.2)^2}$$

$$D_2 = \sqrt{(4-2.7)^2 + (5-8.5)^2}$$

$$D_3 = \sqrt{(8-4)^2 + (5-1)^2}$$

→ ~~D1~~ ~~is~~ ~~less~~, Point P_9 will be in Cluster C1.

$$\begin{array}{ccc} C_1 & C_2 & C_3 \\ (3.3, 5.1) & (2.8, 8.2) & (8.1) \end{array}$$

⇒ Point $P_{10} (4.8)$

$$D_1 = \sqrt{(4-3.3)^2 + (8-5.1)^2} = \sqrt{8.9}$$

$$D_2 = \sqrt{(4-2.8)^2 + (8-8.2)^2} = \sqrt{1.48}$$

$$D_3 = \sqrt{(8-4)^2 + (8-1)^2} = \sqrt{65}$$

→ D_2 is less, P_{10} will be in cluster C2

$$\begin{array}{ccc} C_1 & C_2 & C_3 \\ (3.3, 5.1) & (3.4, 8.1) & (8.1) \end{array}$$

⇒ Point $P_{11} (4.8)$

$$D_1 = \sqrt{(4-3.3)^2 + (8-5.1)^2} = \sqrt{8.9}$$

$$D_2 = \sqrt{(4-3.4)^2 + (8-8.1)^2} = \sqrt{0.37}$$

$$D_3 = \sqrt{(8-4)^2 + (8-1)^2} = \sqrt{65}$$

→ D_2 is less, P_{11} will be in cluster C2

\Rightarrow

C_1	C_2	C_3
$(3.3, 5.1)$	$(3.7, 8)$	$(8, 1)$

\Rightarrow Point $P_{12} (5, 4)$

$$D_1 = \sqrt{(5-3.3)^2 + (5-4)^2}$$

$$D_2 = \sqrt{(5-3.7)^2 + (8-4)^2}$$

$$D_3 = \sqrt{(8-5)^2 + (1-4)^2}$$

$\Rightarrow D_1$ is less, P_{12} will be in cluster C_1 .

\Rightarrow

C_1	C_2	C_3
$(4.1, 4.5)$	$(3.7, 8)$	$(8, 1)$

\Rightarrow Point $P_{13} (5, 7)$

$$D_1 = \sqrt{(5-4.1)^2 + (4.5-7)^2} = \sqrt{7.41}$$

$$D_2 = \sqrt{(5-3.7)^2 + (8-7)^2} = \sqrt{2.69}$$

$$D_3 = \sqrt{(8-5)^2 + (1-7)^2} = \sqrt{45}$$

$\Rightarrow D_2$ is less, P_{13} will be in cluster C_2

\Rightarrow

C_1	C_2	C_3
$(4.1, 4.5)$	$(4.4, 7.5)$	$(8, 1)$

⇒ Point $P_{14} (6, 9)$

$$D_1 = \sqrt{(6-4.1)^2 + (9-4.5)^2} = (1.1, 4.5) \quad 10$$

$$D_2 = \sqrt{(6-5.2)^2 + (9-8.9)^2} = (5.2, 8.9) \quad 20$$

$$D_3 = \sqrt{(6-8)^2 + (9-1)^2} = (8, 1) \quad 20$$

⇒ D_2 is less, P_{14} will be in cluster 2

$C_1 (4.1, 4.5)$

$C_2 (5.2, 8.9)$

$C_3 (8, 1)$

$(4.1, 4.5)$

$(5.2, 8.9)$

$(8, 1)$

⇒ Point $P_{15} (7, 2)$

$$D_1 = \sqrt{(7-4.1)^2 + (2-4.5)^2} = (4.1, 4.5) \quad 10$$

$$D_2 = \sqrt{(7-5.2)^2 + (2-8.9)^2} = (5.2, 8.9) \quad 20$$

$$D_3 = \sqrt{(7-8)^2 + (2-1)^2} = (8, 1) \quad 20$$

⇒ D_3 is less, P_{15} will be in cluster 3.

$C_1 (4.1, 4.5)$

$C_2 (5.2, 8.2)$

$C_3 (7.5, 1.5)$

$(4.1, 4.5)$

$(5.2, 8.2)$

$(7.5, 1.5)$

→ Point $P_{18} (7, 3)$

$$D_1 = \sqrt{(7-4.1)^2 + (3-4.5)^2}$$

$$D_2 = \sqrt{(7-5.2)^2 + (3-8.2)^2}$$

$$D_3 = \sqrt{(7-7.5)^2 + (3-1.5)^2}$$

→ D_3 is less, P_{18} will be in cluster 3

C1	C2	C3
(4.1, 4.5)	(5.2, 8.2)	(7.2, 2.2)
(4.1, 4.5)	(5.2, 8.2)	(7.2, 2.2)

→ Point $P_{19} (7, 9)$

$$D_1 = \sqrt{(7-4.1)^2 + (9-4.5)^2}$$

$$D_2 = \sqrt{(7-5.2)^2 + (9-8.2)^2}$$

$$D_3 = \sqrt{(7.2-7)^2 + (2.2-9)^2}$$

→ D_2 is less, P_{19} will be in cluster 2

C1	C2	C3
(4.1, 4.5)	(6.1, 8.1)	(7.2, 2.2)
(4.1, 4.5)	(6.1, 8.1)	(7.2, 2.2)

→ $P_{19} (8, 7)$

$$D_1 = \sqrt{(8-4.1)^2 + (7-4.5)^2}$$

$$D_2 = \sqrt{(8-6)^2 + (7-8)^2}$$

$$D_3 = \sqrt{(8-7.2)^2 + (2.2-7)^2}$$

$\Rightarrow D_2$ is less. P_{19} will be in cluster C_2

C_1	C_2	C_3
$(4.1, 4.5)$	$(7, 7.1)$	$(7.2, 2.2)$

\Rightarrow Cluster $C_1 \Rightarrow \{P_0, P_1, P_2, P_4, P_5, P_9, P_{12}\}$

\Rightarrow Cluster $C_2 \Rightarrow \{P_3, P_6, P_7, P_8, P_{10}, P_{11}, P_{13}, P_{14}, P_{17}, P_{19}\}$

\Rightarrow Cluster $C_3 = \{P_{16}, P_{15}, P_{18}\}$