

# Heisenberg Uncertainty

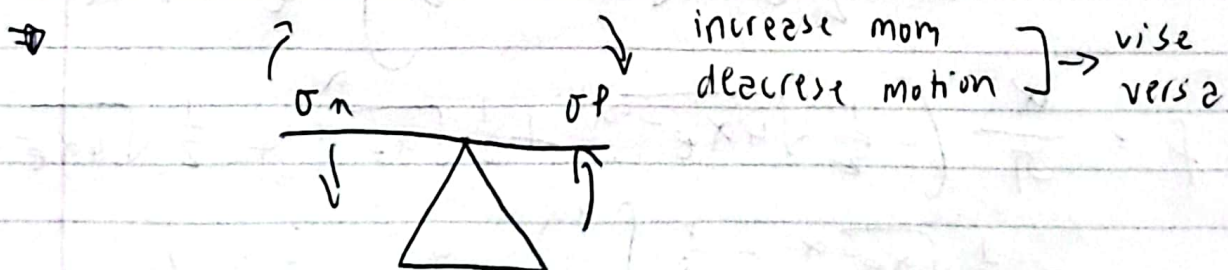
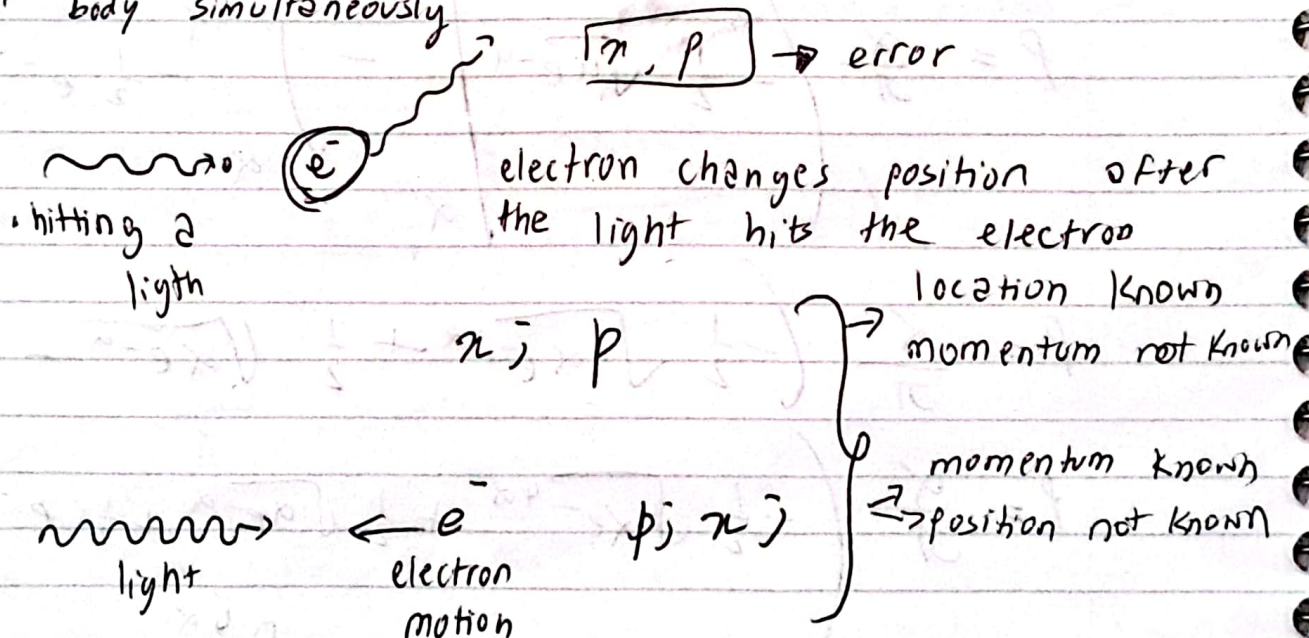
$$\hbar = 10^{-34} \text{ J}\cdot\text{s}$$

$$\sigma_x \sigma_p \geq \frac{\hbar}{2} ; \Delta x \Delta p \geq \frac{\hbar}{2}$$

- 1) Heisenberg uncertainty principle has nothing to do with the measurement of  $(x, p)$

measurement  $\neq$  theory

- 2) It's impossible to know the exact position & momentum of body simultaneously



⇒ heisenberg uncertainty only applicable in the quantum world not classical world.

$$\Delta x \Delta p \geq \frac{h}{2} ; \Delta t \Delta E \geq \frac{h}{2}$$

Subatomic particles

⇒ Because SAP like electrons have wave - particle duality,

↳ hard to find exact location

(a) hard to find the momentum

↳ hard to distinguish between electron & wave

Wave function :  $\psi$  [because the subatomic particle behaves as wave HUP exists]

$$\int_{-\infty}^{+\infty} |\psi|^2 dx = 1 \quad \left[ \begin{array}{l} \text{Because particle} \\ \text{exists 100\% from} \\ -\infty \text{ to } +\infty \end{array} \right]$$

⇒  $p \propto \frac{1}{\lambda}$  [wave] :  $\lambda$  : localise particle

⇒ to find position, we must localise the particle by summing up all the particle

$$\Delta x \Delta p \geq \frac{h}{2} \quad \therefore \lambda \Rightarrow p = \hbar K = \frac{h}{\lambda}$$

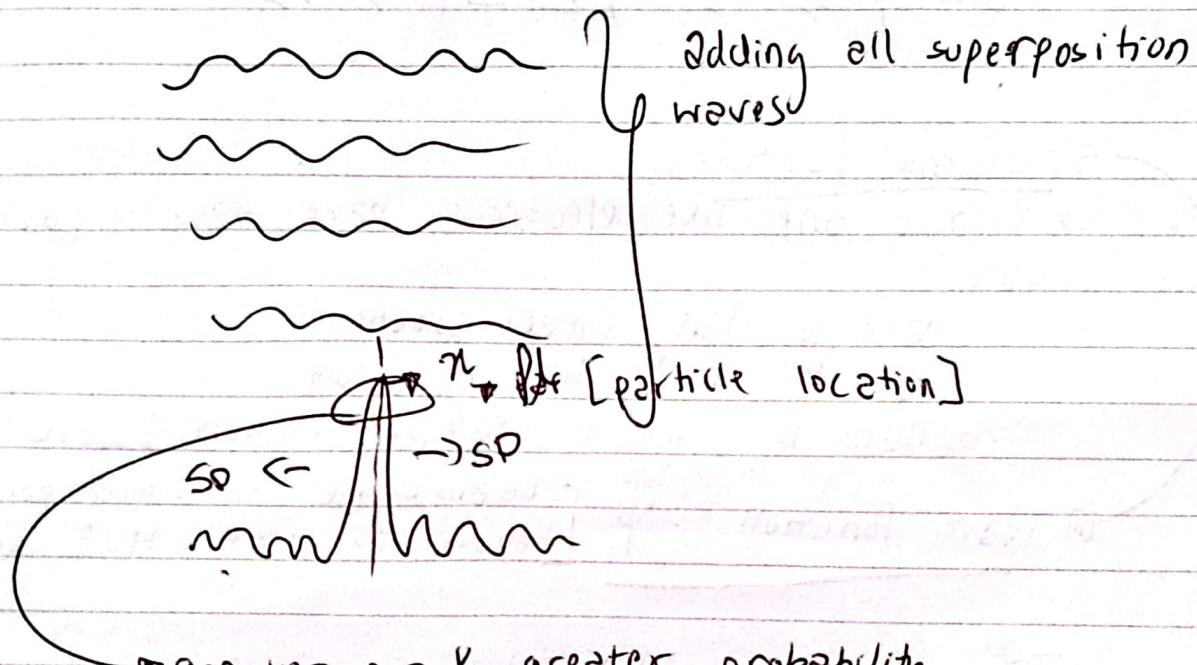
$\downarrow$        $\downarrow$   
 particle   wave

[if i know the  $\lambda$ , i know the momentum]

⇒ Based on wavelength we can get momentum



⇒ To localize the location of particle, we must add all the superposition waves



→ greater  $p$  & greater probability

→ we know the probability of where the particle may exist

$\lambda$  being single wave leading to not finding momentum because we cannot find the momentum of a single wave

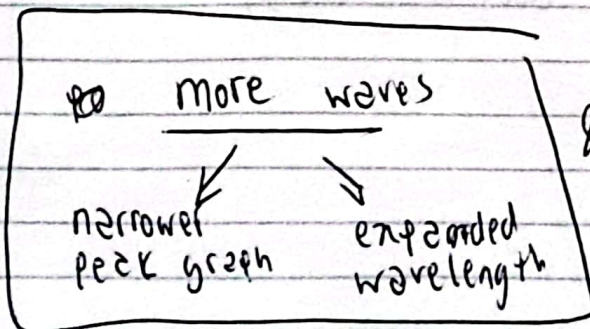
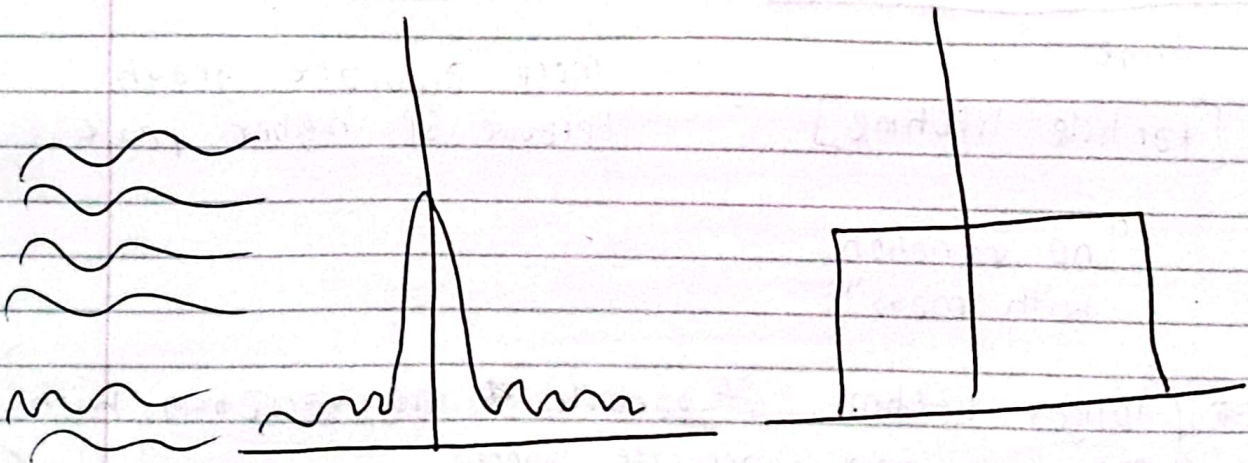
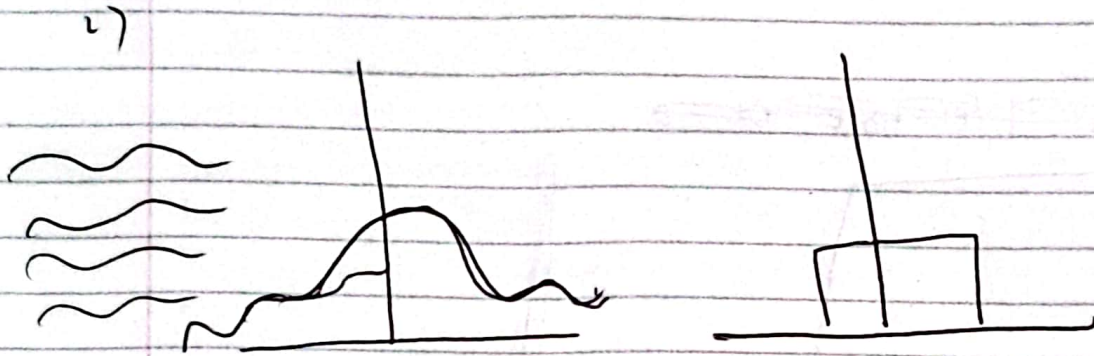
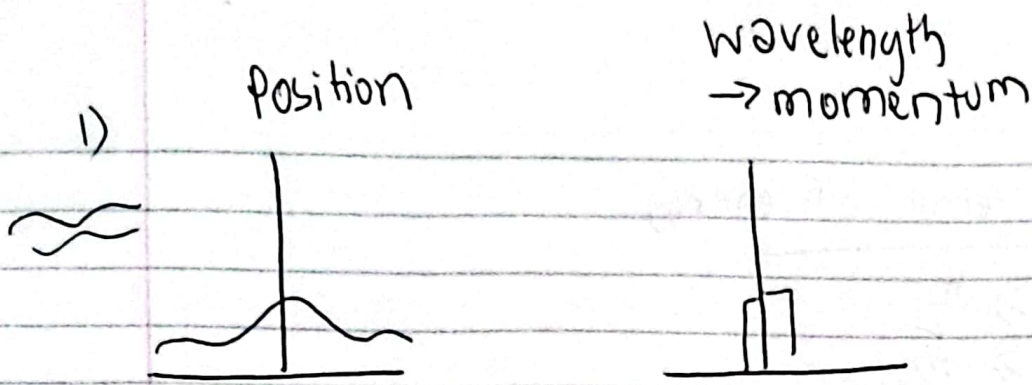
$$\boxed{\sigma x \sigma p \geq \hbar/2} \text{ HUP}$$

$$\sigma x = \sqrt{\langle x^2 \rangle - \langle x \rangle^2}$$

= standard deviation [location]

$$\sigma p = \sqrt{\langle p^2 \rangle - \langle p \rangle^2}$$

= SD [momentum]



& vice versa for less waves

$\Rightarrow$  Adding more waves gives us the probability of where the particle exists but momentum graph is so expanded that we cannot find the momentum of the particle at a ~~spot~~ "almost" specified location