

NEWTON INTERPOLATION METHOD:

- **FORWARD DIFFERENCE:**

Formula:

$$p = \frac{x - x_0}{h}$$

$$Y(x) = y_0 + p\Delta y_0 + \frac{p(p-1)}{2!} \cdot \Delta^2 y_0 + \frac{p(p-1)(p-2)}{3!} \cdot \Delta^3 y_0 + \frac{p(p-1)(p-2)(p-3)}{4!} \cdot \Delta^4 y_0 \dots$$

EXAMPLE:

Find solution using Newton's Forward Difference Formula

x	F(x)
1891	46
1901	66
1911	81
1921	93
1931	101

X=1895

SOLUTION:

The value of table for x and y

x	1891	1901	1911	1921	1931
y	46	66	81	93	101

Newton's forward difference table is

x	y	Δy	$\Delta^2 y$	$\Delta^3 y$	$\Delta^4 y$
1891	46				
		20			
1901	66		-5		
		15		2	
1911	81		-3		-3
		12		-1	
1921	93		-4		
		8			

1931	101				
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The value of x at you want to find the f(x):x=1895

$$h = x_1 - x_0$$

$$= 1901 - 1891 = 10$$

$$p = \frac{x - x_0}{h} = \frac{1895 - 1891}{10} = 0.4$$

Newton's forward difference interpolation formula is

$$y(x) = y_0 + p\Delta y_0 + \frac{p(p-1)}{2!} \cdot \Delta^2 y_0 + \frac{p(p-1)(p-2)}{3!} \cdot \Delta^3 y_0 + \frac{p(p-1)(p-2)(p-3)}{4!} \cdot \Delta^4 y_0$$

$$y(1895) = 46 + 0.4 \times 20 + \frac{0.4(0.4-1)}{2} \times -5 + \frac{0.4(0.4-1)(0.4-2)}{6} \times 2 + \frac{0.4(0.4-1)(0.4-2)(0.4-3) \times -3}{24}$$

$$y(1895) = 46 + 8 + 0.6 + 0.128 + 0.1248$$

$$y(1895) = 54.8528$$

Solution for newton's forward interpolation method $y(1895) = 54.8528$