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In[7]:= sol = DSolve[{
  ω'[t] == (Km i[t] - T - d ω[t]) / J,
  i'[t] == (V - Km ω[t] - R i[t]) / L,
  ω[0] == ω0,
  i[0] == i0
}, {ω[t], i[t]}, t] // First // Simplify;
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In[12]:= sol2 = sol /. {
   $\frac{\sqrt{d^2 L^2 + J^2 R^2 - 2 J L (2 K m^2 + d R)} t}{J L} \rightarrow \Omega t,$ 
   $\frac{\left(d L + J R + \sqrt{d^2 L^2 + J^2 R^2 - 2 J L (2 K m^2 + d R)}\right) t}{2 J L} \rightarrow \Gamma t,$ 
   $-\frac{\left(d L + J R + \sqrt{d^2 L^2 + J^2 R^2 - 2 J L (2 K m^2 + d R)}\right) t}{2 J L} \rightarrow -\Gamma t$ 
};
```

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sol2 //
Simplify
```

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Out[13]= {i[t] →  $\left( e^{-t \Gamma} \left( i_0 (K m^2 + d R) \right. \right.$ 
 $\left. \left( \left( 1 + e^{t \Omega} \right) J^2 R^2 + d L \left( d \left( 1 + e^{t \Omega} \right) L + \left( -1 + e^{t \Omega} \right) \sqrt{d^2 L^2 + J^2 R^2 - 2 J L (2 K m^2 + d R)} \right) - \right.$ 
 $\left. J \left( 4 \left( 1 + e^{t \Omega} \right) K m^2 L + 2 d \left( 1 + e^{t \Omega} \right) L R + \left( -1 + e^{t \Omega} \right) R \right. \right.$ 
 $\left. \left. \left. \sqrt{d^2 L^2 + J^2 R^2 - 2 J L (2 K m^2 + d R)} \right) \right) - \left( 1 - 2 e^{t \Gamma} + e^{t \Omega} \right) J^2 R^2 (K m T + d V) - \right.$ 
 $d L \left( d \left( 1 - 2 e^{t \Gamma} + e^{t \Omega} \right) L + \left( -1 + e^{t \Omega} \right) \sqrt{d^2 L^2 + J^2 R^2 - 2 J L (2 K m^2 + d R)} \right) (K m T + d V) +$ 
 $J \left( 2 K m^2 \left( 2 d \left( 1 - 2 e^{t \Gamma} + e^{t \Omega} \right) L + \left( -1 + e^{t \Omega} \right) \sqrt{d^2 L^2 + J^2 R^2 - 2 J L (2 K m^2 + d R)} \right) V + \right.$ 
 $d R \left( 2 d \left( 1 - 2 e^{t \Gamma} + e^{t \Omega} \right) L + \left( -1 + e^{t \Omega} \right) \sqrt{d^2 L^2 + J^2 R^2 - 2 J L (2 K m^2 + d R)} \right) V +$ 
 $2 K m^3 \left( 2 \left( 1 - 2 e^{t \Gamma} + e^{t \Omega} \right) L T - \left( -1 + e^{t \Omega} \right) \sqrt{d^2 L^2 + J^2 R^2 - 2 J L (2 K m^2 + d R)} \omega_0 \right) -$ 
 $K m R \left( -2 d \left( 1 - 2 e^{t \Gamma} + e^{t \Omega} \right) L T + \left( -1 + e^{t \Omega} \right) \sqrt{d^2 L^2 + J^2 R^2 - 2 J L (2 K m^2 + d R)} T + \right.$ 
 $\left. \left. \left. 2 d \left( -1 + e^{t \Omega} \right) \sqrt{d^2 L^2 + J^2 R^2 - 2 J L (2 K m^2 + d R)} \omega_0 \right) \right) \right) \right) /$ 
 $\left( 2 (K m^2 + d R) (d^2 L^2 + J^2 R^2 - 2 J L (2 K m^2 + d R)) \right), \omega[$ 
t] →
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$$\left(\begin{aligned} & e^{-t\Gamma} \left(2 (-1 + e^{t\Omega}) i0 Km L (Km^2 + d R) \sqrt{d^2 L^2 + J^2 R^2 - 2 J L (2 Km^2 + d R)} + \right. \\ & J^2 R^2 ((1 - 2 e^{t\Gamma} + e^{t\Omega}) RT - (1 - 2 e^{t\Gamma} + e^{t\Omega}) Km V + (1 + e^{t\Omega}) Km^2 \omega \theta + d (1 + e^{t\Omega}) R \omega \theta) - \\ & J \left(-4 (1 - 2 e^{t\Gamma} + e^{t\Omega}) Km^3 LV + \right. \\ & Km R \left(-2 d (1 - 2 e^{t\Gamma} + e^{t\Omega}) L + (-1 + e^{t\Omega}) \sqrt{d^2 L^2 + J^2 R^2 - 2 J L (2 Km^2 + d R)} \right) V + \\ & 4 (1 + e^{t\Omega}) Km^4 L \omega \theta + Km^2 R \left(4 (1 - 2 e^{t\Gamma} + e^{t\Omega}) LT + 6 d (1 + e^{t\Omega}) L \omega \theta - \right. \\ & \quad \left. (-1 + e^{t\Omega}) \sqrt{d^2 L^2 + J^2 R^2 - 2 J L (2 Km^2 + d R)} \omega \theta \right) - \\ & R^2 \left(-2 d (1 - 2 e^{t\Gamma} + e^{t\Omega}) LT + (-1 + e^{t\Omega}) \sqrt{d^2 L^2 + J^2 R^2 - 2 J L (2 Km^2 + d R)} T - \right. \\ & \quad \left. 2 d^2 (1 + e^{t\Omega}) L \omega \theta + d (-1 + e^{t\Omega}) \sqrt{d^2 L^2 + J^2 R^2 - 2 J L (2 Km^2 + d R)} \omega \theta \right) \Bigg) + \\ & L \left(-2 (-1 + e^{t\Omega}) Km^2 \sqrt{d^2 L^2 + J^2 R^2 - 2 J L (2 Km^2 + d R)} T + d^3 (1 + e^{t\Omega}) LR \omega \theta - \right. \\ & d (-1 + e^{t\Omega}) \sqrt{d^2 L^2 + J^2 R^2 - 2 J L (2 Km^2 + d R)} (RT + Km (V + Km \omega \theta)) + \\ & d^2 \left((1 - 2 e^{t\Gamma} + e^{t\Omega}) LRT - (-1 + e^{t\Omega}) R \sqrt{d^2 L^2 + J^2 R^2 - 2 J L (2 Km^2 + d R)} \omega \theta + \right. \\ & \quad \left. Km L (- (1 - 2 e^{t\Gamma} + e^{t\Omega}) V + (1 + e^{t\Omega}) Km \omega \theta) \right) \Bigg) \Bigg) / \\ & (2 (Km^2 + d R) (d^2 L^2 + J^2 R^2 - 2 J L (2 Km^2 + d R))) \Bigg\} \end{aligned} \right.$$