STAT 333

Day 1

Basic Review

Conditional probability:

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$
$$P(A \cap B) = P(A|B)P(B)$$

Law of total probability:

$$P(A) = \sum_{i=1}^{n} P(A|B_i)P(B_i)$$

Baye's Rule:

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 $P(B \mid A) = \frac{P(A \mid B)P(B)}{P(A)}$

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$$P(B|A) = \frac{P(A|B)P(B)}{P(A)}$$

$$P(B|A) = \frac{P(A|B)P(B)}{P(A)}$$

Example 1.2

Show that when n is large and p is small, the BIN(n,p) distribution may be approximated by a $POI(\lambda)$ distribution where $\lambda=np$.

$$egin{aligned} \lim_{n o\infty}\lim_{p o0}BIN(n,p)&=\lim_{n o\infty}\lim_{p o0}inom{n}{x}(p)^x(1-p)^{n-x} \ &=\lim_{n o\infty}\lim_{p o0}rac{n(n-1)\dots(n-x+1)}{x!}(rac{\lambda}{n})^x(1-rac{\lambda}{n})^{n-x} \ &=\lim_{n o\infty}\lim_{p o0}rac{n(n-1)\dots(n-x+1)}{n^x}rac{\lambda^x}{x!}rac{(1-rac{\lambda}{n})^n}{(1-rac{\lambda}{n})^x} \ &=rac{\lambda^x}{x!}e^{-\lambda} \ &\lambda=np\implies \lim_{n o\infty}\lim_{p o0}BIN(n,p)=POI(\lambda) \end{aligned}$$