

ATIVIDADE EXTRA-CLASSE

4 – Conversão $AF_{\epsilon} \rightarrow AFND$

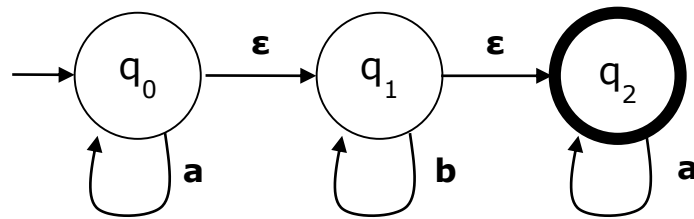
Data de Entrega: (até 08/05/2016)

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Grupo: ≤ 4 alunos

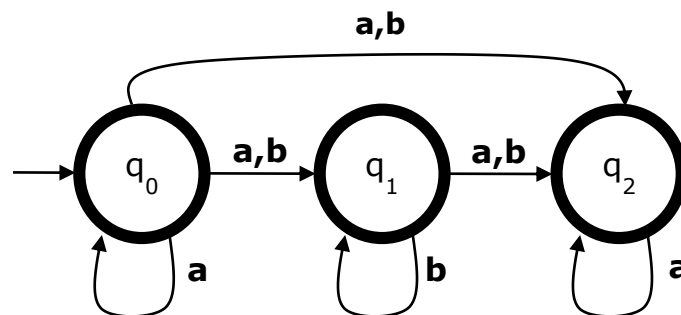
Exemplo: Dado o $AF_{\epsilon} M = (\{a,b\}, \{q_0, q_1, q_2\}, \delta, \{q_0\}, F)$



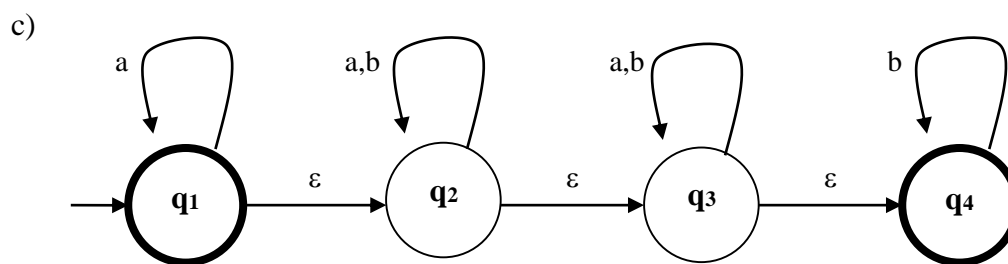
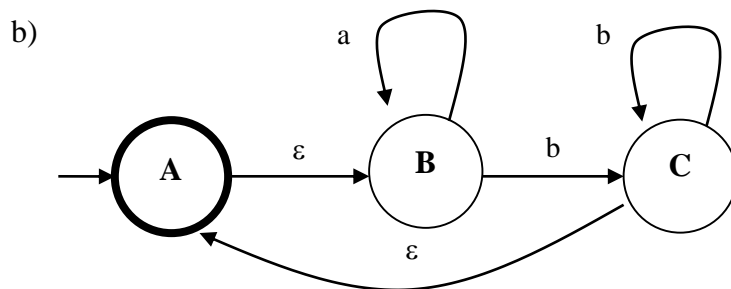
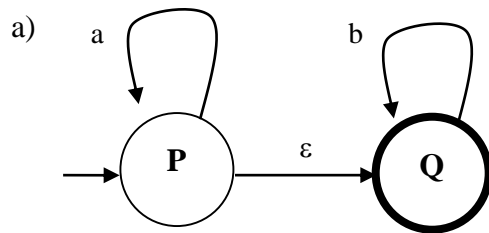
- Existe um AFND $M' = (\{a,b\}, \{q_0, q_1, q_2\}, \delta', \{q_0\}, F')$ equivalente.
- F' é retirado da função Fecho Vazio (F_{ϵ}).
 - $F' = \{q_0, q_1, q_2\}$, pois:
 - $F_{\epsilon}(q_0) = \{q_0\} \cup \delta(q_0, \epsilon) \cup \delta(\delta(q_0, \epsilon), \epsilon) =$
 $= \{q_0\} \cup \{q_1\} \cup \{q_2\}$
 $= \{q_0, q_1, q_2\}$
 - $F_{\epsilon}(q_1) = \{q_1\} \cup \delta(q_1, \epsilon) =$
 $= \{q_1\} \cup \{q_2\}$
 $= \{q_1, q_2\}$
 - $F_{\epsilon}(q_2) = \{q_2\}$
 - Como todos tem $\{q_2\}$, todos os estados são finais no AFND.
- δ' é retirado da função Programa Estendida ($\underline{\delta}$).
 - $\delta'(q_0, \epsilon) = \underline{\delta}(q_0, \epsilon) = F_{\epsilon}(q_0) = \{q_0, q_1, q_2\}$
 - $\delta'(q_0, a) = \underline{\delta}(q_0, a) = F_{\epsilon}(\{r \mid r \in \delta(s, a) \text{ e } s \in \underline{\delta}(q_0, \epsilon)\})$
 $= F_{\epsilon}(\{r \mid r \in \delta(s, a) \text{ e } s \in \{q_0, q_1, q_2\}\})$
 $= F_{\epsilon}(\{\delta(q_0, a) \cup \delta(q_1, a) \cup \delta(q_2, a)\})$
 $= F_{\epsilon}(\{q_0 \cup \emptyset \cup q_2\})$
 $= F_{\epsilon}(\{q_0, q_2\})$
 $= F_{\epsilon}(q_0) \cup F_{\epsilon}(q_2) = \{q_0, q_1, q_2\}$
 - $\delta'(q_0, b) = \underline{\delta}(q_0, b) = F_{\epsilon}(\{r \mid r \in \delta(s, b) \text{ e } s \in \underline{\delta}(q_0, \epsilon)\})$
 $= F_{\epsilon}(\{r \mid r \in \delta(s, b) \text{ e } s \in \{q_0, q_1, q_2\}\})$
 $= F_{\epsilon}(\{\delta(q_0, b) \cup \delta(q_1, b) \cup \delta(q_2, b)\})$
 $= F_{\epsilon}(\{\emptyset \cup q_1 \cup \emptyset\})$
 $= F_{\epsilon}(\{q_1\}) = \{q_1, q_2\}$

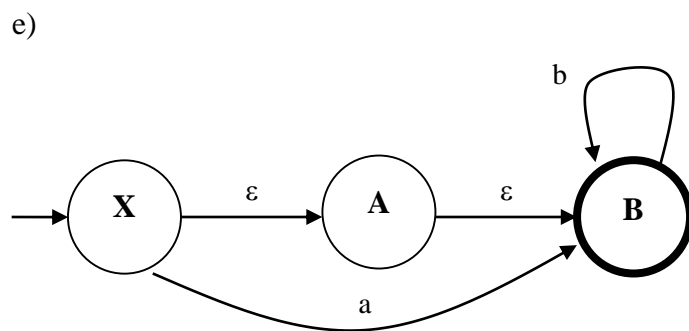
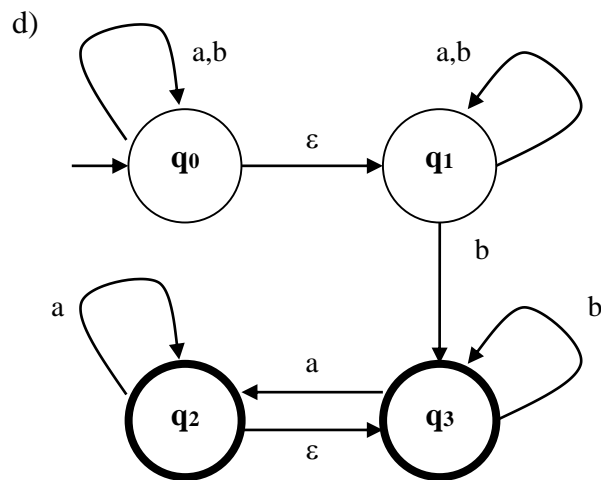
- $\delta'(q_1, \varepsilon) = \underline{\delta}(q_1, \varepsilon) = F\varepsilon(q_1) = \{q_1, q_2\}$
- $\delta'(q_1, a) = \underline{\delta}(q_1, a) = F\varepsilon(\{r \mid r \in \delta(s, a) \text{ e } s \in \underline{\delta}(q_1, \varepsilon)\})$
 $= F\varepsilon(\{r \mid r \in \delta(s, a) \text{ e } s \in \{q_1, q_2\}\})$
 $= F\varepsilon(\{\delta(q_1, a) \cup \delta(q_2, a)\})$
 $= F\varepsilon(\{\emptyset \cup q_2\})$
 $= F\varepsilon(\{q_2\}) = \{q_2\}$
- $\delta'(q_1, b) = \underline{\delta}(q_1, b) = F\varepsilon(\{r \mid r \in \delta(s, b) \text{ e } s \in \underline{\delta}(q_1, \varepsilon)\})$
 $= F\varepsilon(\{r \mid r \in \delta(s, b) \text{ e } s \in \{q_1, q_2\}\}) =$
 $= F\varepsilon(\{\delta(q_1, b) \cup \delta(q_2, b)\})$
 $= F\varepsilon(\{q_1 \cup \emptyset\})$
 $= F\varepsilon(\{q_1\}) = \{q_1, q_2\}$
- $\delta'(q_2, \varepsilon) = \underline{\delta}(q_2, \varepsilon) = F\varepsilon(q_2) = \{q_2\}$
- $\delta'(q_2, a) = \underline{\delta}(q_2, a) = F\varepsilon(\{r \mid r \in \delta(s, a) \text{ e } s \in \underline{\delta}(q_2, \varepsilon)\})$
 $= F\varepsilon(\{r \mid r \in \delta(s, a) \text{ e } s \in \{q_2\}\}) =$
 $= F\varepsilon(\{\delta(q_2, a)\})$
 $= F\varepsilon(\{q_2\}) = \{q_2\}$
- $\delta'(q_2, b) = \underline{\delta}(q_2, b) = F\varepsilon(\{r \mid r \in \delta(s, b) \text{ e } s \in \underline{\delta}(q_2, \varepsilon)\}) =$
 $= F\varepsilon(\{r \mid r \in \delta(s, b) \text{ e } s \in \{q_2\}\}) =$
 $= F\varepsilon(\{\delta(q_2, b)\})$
 $= F\varepsilon(\{\emptyset\}) = \emptyset$

- δ' equivalente:



1-) Converta os AFe's abaixo para seus equivalentes AFND's.





2-) Converta o AF ϵ abaixo para seu AFD mínimo equivalente, se possível.

