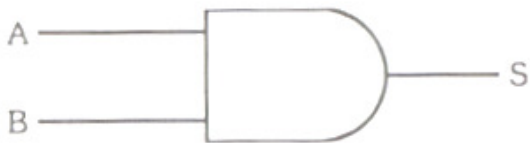
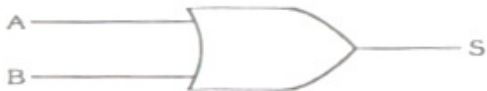


CIRCUITOS DIGITAIS




Funções e expressões lógicas



Prof. Rogério Moreira







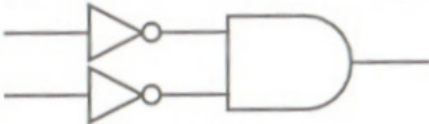

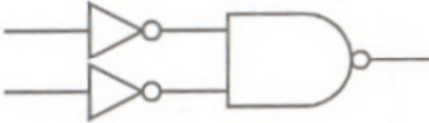
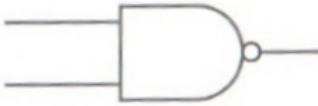
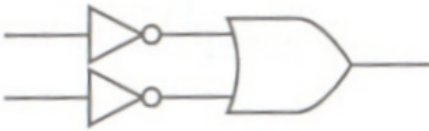
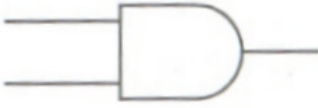
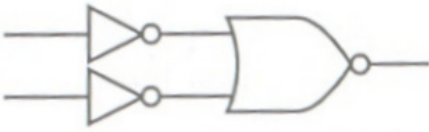
BLOCOS LÓGICOS BÁSICOS

BLOCOS LÓGICOS BÁSICOS																			
Porta	Símbolo Usual	Tabela da Verdade	Função Lógica	Expressão															
E AND		<table><tr><th>A</th><th>B</th><th>S</th></tr><tr><td>0</td><td>0</td><td>0</td></tr><tr><td>0</td><td>1</td><td>0</td></tr><tr><td>1</td><td>0</td><td>0</td></tr><tr><td>1</td><td>1</td><td>1</td></tr></table>	A	B	S	0	0	0	0	1	0	1	0	0	1	1	1	Função E: assume 1 quando todas as variáveis forem 1 e 0 nos outros casos.	$S = AB$
A	B	S																	
0	0	0																	
0	1	0																	
1	0	0																	
1	1	1																	
OU OR		<table><tr><th>A</th><th>B</th><th>S</th></tr><tr><td>0</td><td>0</td><td>0</td></tr><tr><td>0</td><td>1</td><td>1</td></tr><tr><td>1</td><td>0</td><td>1</td></tr><tr><td>1</td><td>1</td><td>1</td></tr></table>	A	B	S	0	0	0	0	1	1	1	0	1	1	1	1	Função OU: assume 0 quando todas as variáveis forem 0 e 1 nos outros casos.	$S = A + B$
A	B	S																	
0	0	0																	
0	1	1																	
1	0	1																	
1	1	1																	

BLOCOS LÓGICOS BÁSICOS

Porta	Símbolo Usual	Tabela da Verdade	Função Lógica	Expressão															
NÃO NOT INVERSOR		<table><tr><th>A</th><th>S</th></tr><tr><td>0</td><td>1</td></tr><tr><td>1</td><td>0</td></tr></table>	A	S	0	1	1	0	Função NÃO: inverte a variável aplicada à sua entrada.	$S = \overline{A}$									
A	S																		
0	1																		
1	0																		
NE NAND		<table><tr><th>A</th><th>B</th><th>S</th></tr><tr><td>0</td><td>0</td><td>1</td></tr><tr><td>0</td><td>1</td><td>1</td></tr><tr><td>1</td><td>0</td><td>1</td></tr><tr><td>1</td><td>1</td><td>0</td></tr></table>	A	B	S	0	0	1	0	1	1	1	0	1	1	1	0	Função NE: inverso da função E.	$S = \overline{AB}$
A	B	S																	
0	0	1																	
0	1	1																	
1	0	1																	
1	1	0																	
NOU NOR		<table><tr><th>A</th><th>B</th><th>S</th></tr><tr><td>0</td><td>0</td><td>1</td></tr><tr><td>0</td><td>1</td><td>0</td></tr><tr><td>1</td><td>0</td><td>0</td></tr><tr><td>1</td><td>1</td><td>0</td></tr></table>	A	B	S	0	0	1	0	1	0	1	0	0	1	1	0	Função NOU: inverso da função OU.	$S = \overline{A + B}$
A	B	S																	
0	0	1																	
0	1	0																	
1	0	0																	
1	1	0																	

BLOCOS LÓGICOS BÁSICOS																			
Porta	Símbolo Usual	Tabela da Verdade	Função Lógica	Expressão															
<div>OU</div> <div>EXCLUSIVO</div> <div>EXCLUSIVE</div> <div>OR</div>		<table><tr><th>A</th><th>B</th><th>S</th></tr><tr><td>0</td><td>0</td><td>0</td></tr><tr><td>0</td><td>1</td><td>1</td></tr><tr><td>1</td><td>0</td><td>1</td></tr><tr><td>1</td><td>1</td><td>0</td></tr></table>	A	B	S	0	0	0	0	1	1	1	0	1	1	1	0	<div>Função OU</div> <div>Exclusivo:</div> <div>assume 1</div> <div>quando as</div> <div>variáveis</div> <div>assumirem</div> <div>valores</div> <div>diferentes</div> <div>entre si.</div>	<div>$S = \overline{A} \cdot B + A \cdot \overline{B}$</div> <div>$S = A \oplus B$</div>
A	B	S																	
0	0	0																	
0	1	1																	
1	0	1																	
1	1	0																	
<div>NOU</div> <div>EXCLUSIVO</div> <div>EXCLUSIVE</div> <div>NOR</div> <div>COINCIDÊNCIA</div>		<table><tr><th>A</th><th>B</th><th>S</th></tr><tr><td>0</td><td>0</td><td>1</td></tr><tr><td>0</td><td>1</td><td>0</td></tr><tr><td>1</td><td>0</td><td>0</td></tr><tr><td>1</td><td>1</td><td>1</td></tr></table>	A	B	S	0	0	1	0	1	0	1	0	0	1	1	1	<div>Função</div> <div>Coincidência:</div> <div>assume 1</div> <div>quando</div> <div>houver</div> <div>coincidência</div> <div>entre os</div> <div>valores das</div> <div>variáveis.</div>	<div>$S = \overline{A} \cdot \overline{B} + A \cdot B$</div> <div>$S = A \odot B$</div>
A	B	S																	
0	0	1																	
0	1	0																	
1	0	0																	
1	1	1																	

BLOCO LÓGICO	BLOCO EQUIVALENTE
	   
	
	
	
	

AND – Logical AND

Description:

Performs the logical *AND* between the contents of register Rd and register Rr and places the result in the destination register Rd.

Operation:

{i} $Rd \leftarrow Rd \bullet Rr$

Syntax:

{i} **AND Rd,Rr**

Operands:

$0 \leq d \leq 31, 0 \leq r \leq 31$

Program Counter:

$PC \leftarrow PC + 1$

16-bit Opcode:

0010	00rd	ddd0	rrrr
------	------	------	------

Status Register (SREG) and Boolean Formula:

I	T	H	S	V	N	Z	C
–	–	–	\leftrightarrow	0	\leftrightarrow	\leftrightarrow	–

S: $N \oplus V$, For signed tests.

V: 0
Cleared

N: R7
Set if MSB of the result is set; cleared otherwise.

Z: $\overline{R7} \bullet \overline{R6} \bullet \overline{R5} \bullet \overline{R4} \bullet \overline{R3} \bullet \overline{R2} \bullet \overline{R1} \bullet \overline{R0}$
Set if the result is \$00; cleared otherwise.

R (Result) equals Rd after the operation.

Example:

```
and r2,r3      : Bitwise and r2 and r3, result in r2
ldi r16,1      : Set bitmask 0000 0001 in r16
and r2,r16     : Isolate bit 0 in r2
```

Words: 1 (2 bytes)

Cycles: 1

ANDI – Logical AND with Immediate

Description:

Performs the logical AND between the contents of register Rd and a constant and places the result in the destination register Rd.

Operation:

() $Rd \leftarrow Rd \bullet K$

Syntax:

() ANDI Rd,K

Operands:

$16 \leq d \leq 31$, $0 \leq K \leq 255$

Program Counter:

$PC \leftarrow PC + 1$

16-bit Opcode:

0111	EEEE	GGGG	EEEE
------	------	------	------

Status Register (SREG) and Boolean Formula:

I	T	H	S	V	N	Z	C
–	–	–	\oplus	0	\oplus	\oplus	–

S: $N \oplus V$, For signed tests.

V: 0
Cleared

N: R7
Set if MSB of the result is set; cleared otherwise.

Z: $\overline{R7} \bullet \overline{R6} \bullet \overline{R5} \bullet \overline{R4} \bullet \overline{R3} \bullet \overline{R2} \bullet \overline{R1} \bullet \overline{R0}$
Set if the result is \$00; cleared otherwise.

R (Result) equals Rd after the operation.

Example:

```
andi r17,$0F ; Clear upper nibble of r17
andi r18,$10 ; Isolate bit 4 in r18
andi r19,$AA ; Clear odd bits of r19
```

Words: 1 (2 bytes)

Cycles: 1

EOR – Exclusive OR

Description:

Performs the logical EOR between the contents of register Rd and register Rr and places the result in the destination register Rd.

Operation:

(i) $Rd \leftarrow Rd \oplus Rr$

Syntax:

(i) EOR Rd,Rr

Operands:

$0 \leq d \leq 31, 0 \leq r \leq 31$

Program Counter:

$PC \leftarrow PC + 1$

16-bit Opcode:

0010	01rd	ddd	rrrr
------	------	-----	------

Status Register (SREG) and Boolean Formula:

I	T	H	S	V	N	Z	C
–	–	–	\leftrightarrow	0	\leftrightarrow	\leftrightarrow	–

S: $N \oplus V$, For signed tests.

V: 0
Cleared

N: R7
Set if MSB of the result is set; cleared otherwise.

Z: $R7 \bullet R6 \bullet R5 \bullet R4 \bullet R3 \bullet R2 \bullet R1 \bullet R0$
Set if the result is \$00; cleared otherwise.

R (Result) equals Rd after the operation.

Example:

```
eor    r4,r4        ; Clear r4
eor    r8,r32        ; Bitwise exclusive or between r8 and r32
```

Words: 1 (2 bytes)

Cycles: 1

OR – Logical OR

Description:

Performs the logical OR between the contents of register Rd and register Rr and places the result in the destination register Rd.

Operation:
(i) $Rd \leftarrow Rd \vee Rr$

Syntax: OR Rd,Rr **Operands:** $0 \leq d \leq 31, 0 \leq r \leq 31$ **Program Counter:** $PC \leftarrow PC + 1$

16-bit Opcode:

0010	10rd	0000	rrrr
------	------	------	------

Status Register (SREG) and Boolean Formula:

I	T	H	S	V	N	Z	C
–	–	–	\leftrightarrow	0	\leftrightarrow	\leftrightarrow	–

S: $N \oplus V$, For signed tests.

V: 0
Cleared

N: R7
Set if MSB of the result is set; cleared otherwise.

Z: $R7 \bullet R6 \bullet R5 \bullet R4 \bullet R3 \bullet R2 \bullet R1 \bullet R0$
Set if the result is \$00; cleared otherwise.

R (Result) equals Rd after the operation.

Example:

```
or      r15,r16      ; Do bitwise or between registers
bst     r15,6         ; Store bit 6 of r15 in T Flag
brts    ok            ; Branch if T Flag set
...
ok:     nop           ; branch destination (do nothing)
```

Words: 1 (2 bytes)

Cycles: 1

ORI – Logical OR with Immediate

Description:

Performs the logical OR between the contents of register Rd and a constant and places the result in the destination register Rd.

Operation:
(()) $Rd \leftarrow Rd \vee K$

Syntax: ORI Rd,K **Operands:** $16 \leq d \leq 31, 0 \leq K \leq 255$ **Program Counter:** $PC \leftarrow PC + 1$

16-bit Opcode:

0110	EEEE	0000	EEEE
------	------	------	------

Status Register (SREG) and Boolean Formula:

I	T	H	S	V	N	Z	C
–	–	–	\leftrightarrow	0	\leftrightarrow	\leftrightarrow	–

S: $N \oplus V$, For signed tests.

V: 0
Cleared

N: R7
Set if MSB of the result is set; cleared otherwise.

Z: $\overline{R7} \bullet \overline{R6} \bullet \overline{R5} \bullet \overline{R4} \bullet \overline{R3} \bullet \overline{R2} \bullet \overline{R1} \bullet \overline{R0}$
Set if the result is \$00; cleared otherwise.

R (Result) equals Rd after the operation.

Example:

```
ori    r16,$F0    ; Set high nibble of r16
ori    r17,1       ; Set bit 0 of r17
```

Words: 1 (2 bytes)

Cycles: 1

Exercício

- Desenhe o sinal na saída S do circuito da Figura 2.58.

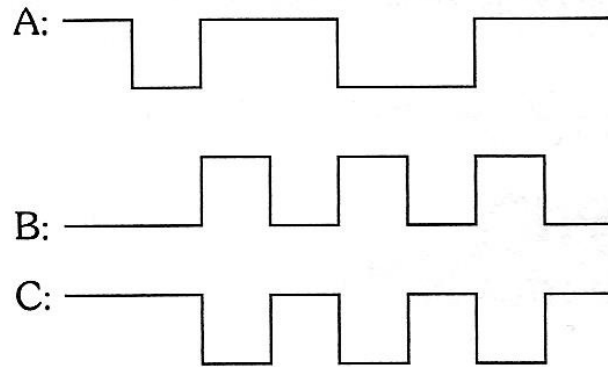
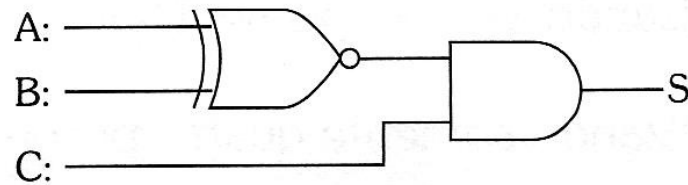
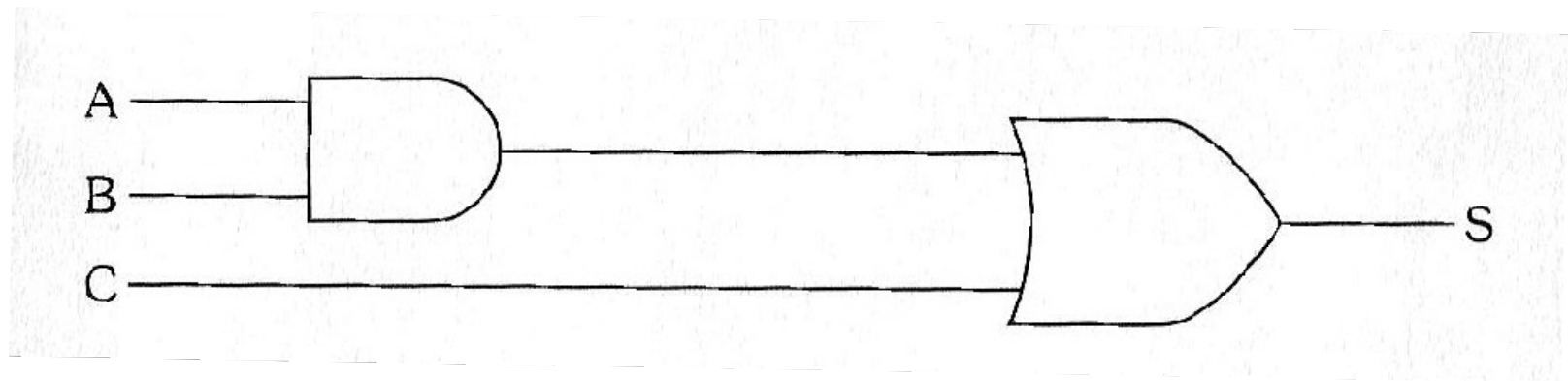
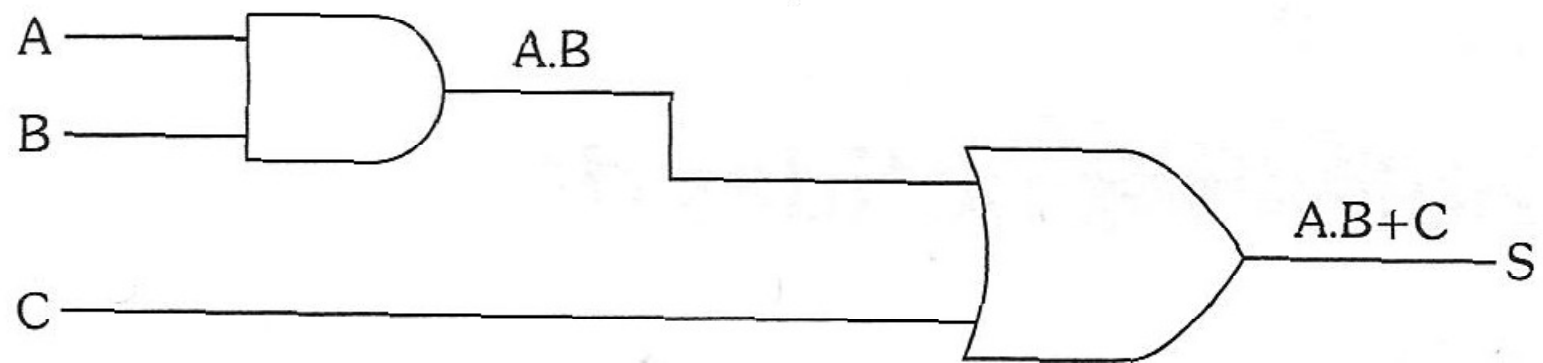


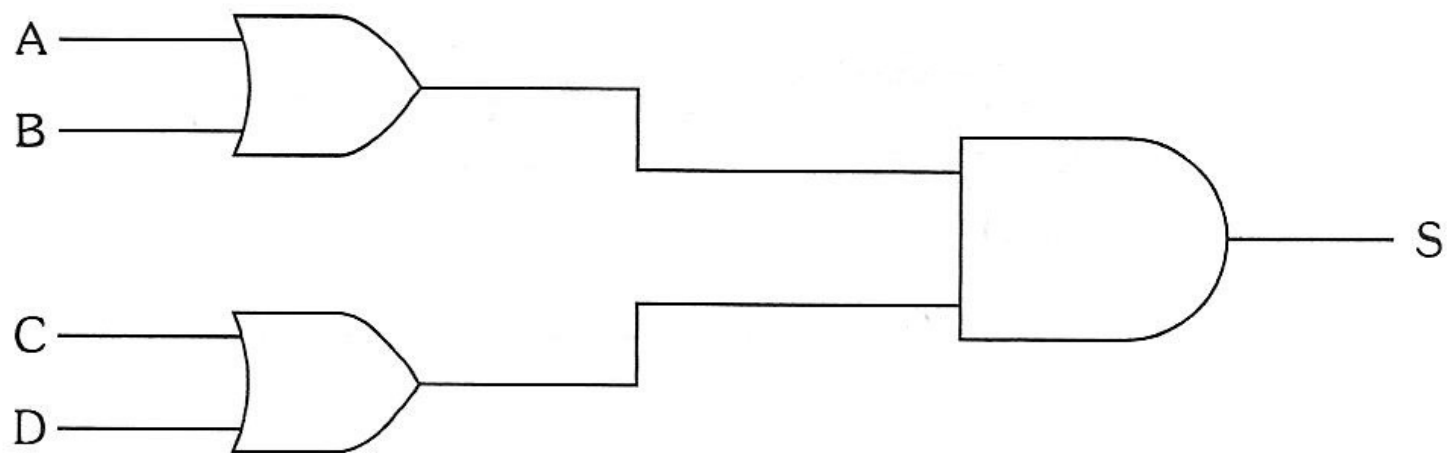
Figura 2.58

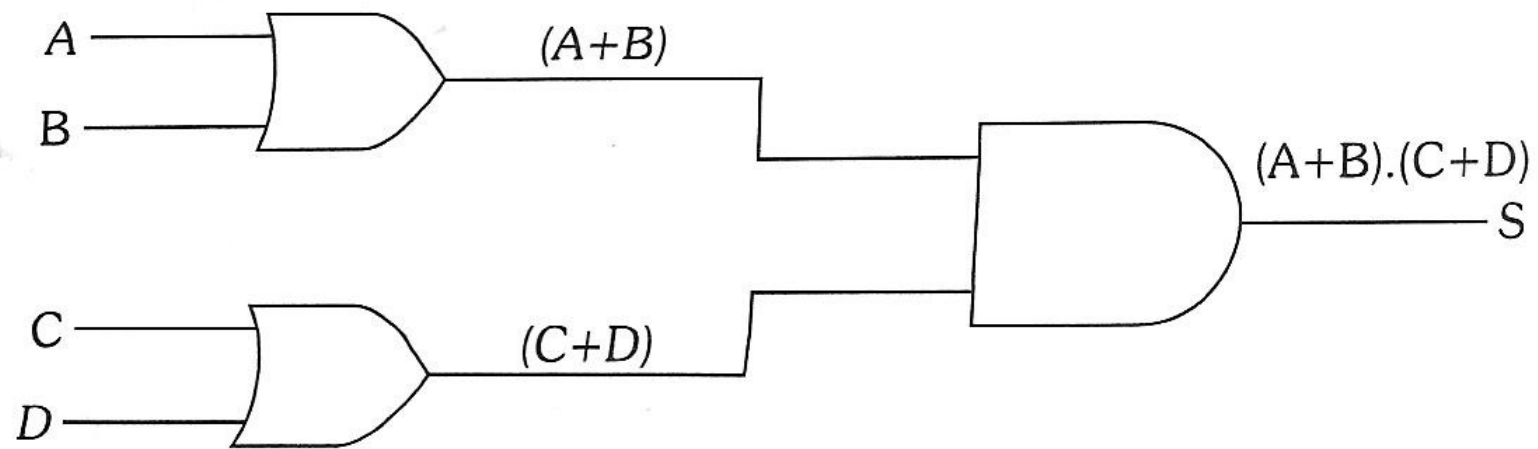
1. Expressões booleanas obtidas de circuitos lógicos
2. Circuitos lógicos obtidos de expressões booleanas
3. Tabelas verdade obtidas de expressões booleanas
4. Expressões booleanas obtidas de tabelas verdade

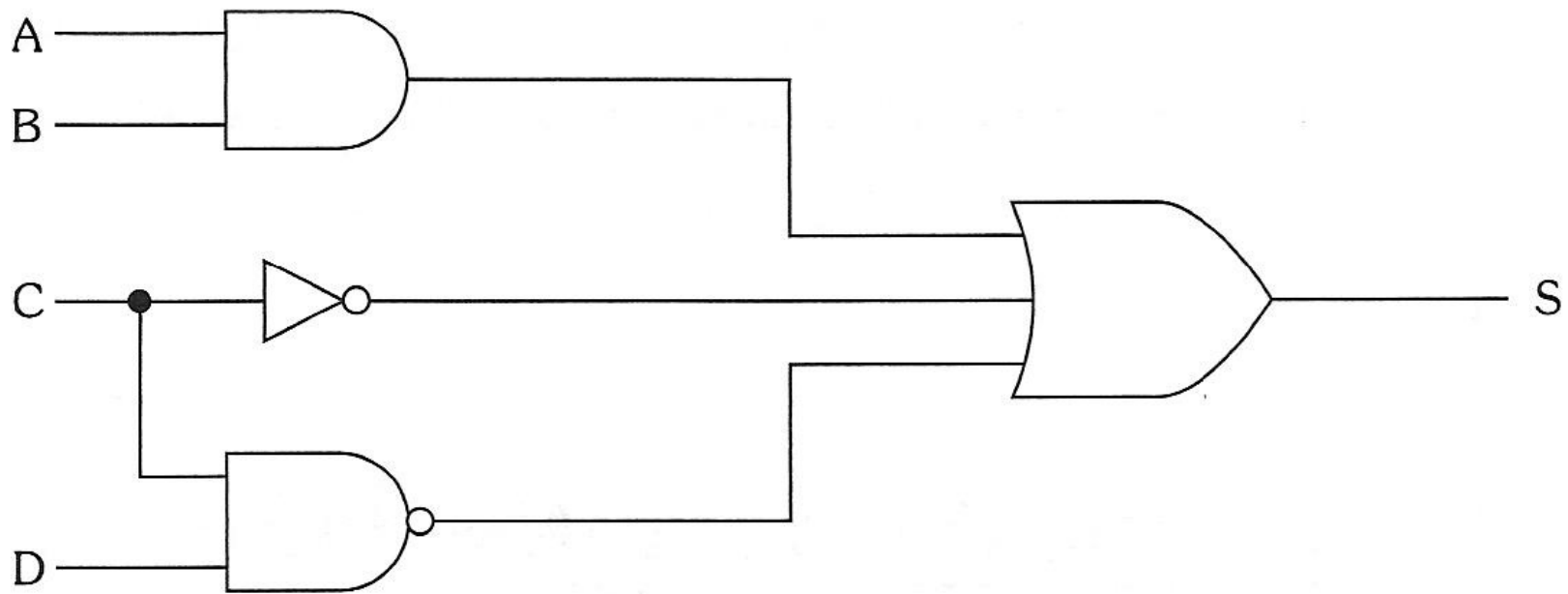
- 1. Expressões booleanas obtidas de circuitos lógicos**
2. Circuitos lógicos obtidos de expressões booleanas
3. Tabelas verdade obtidas de expressões booleanas
4. Expressões booleanas obtidas de tabelas verdade

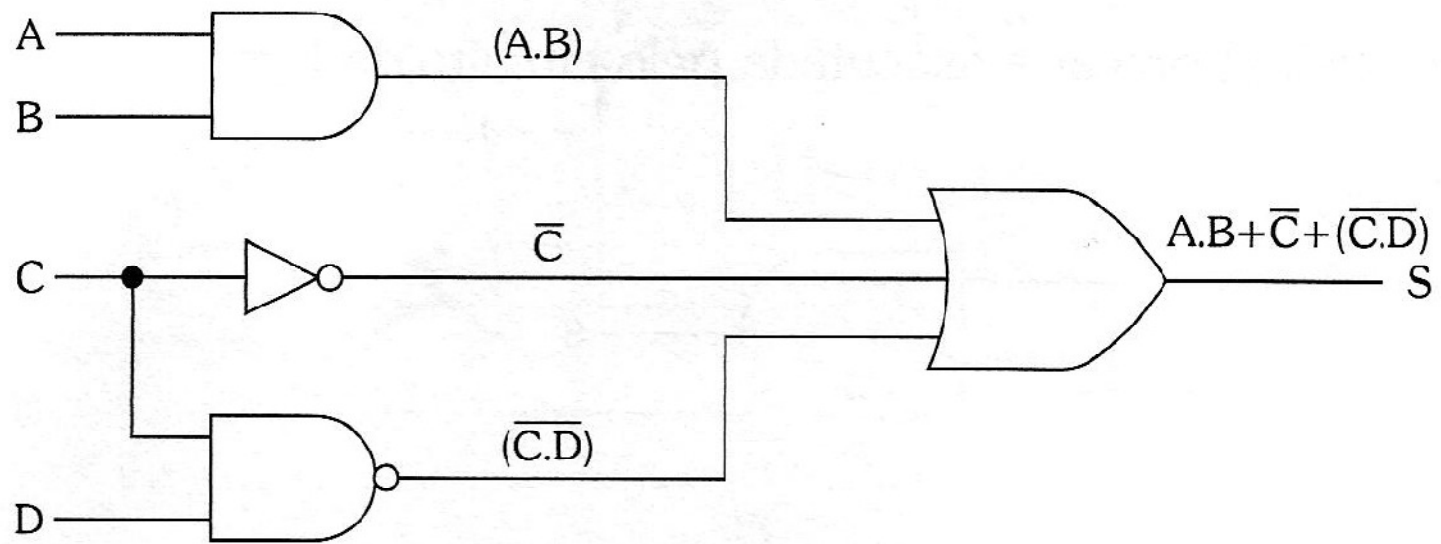


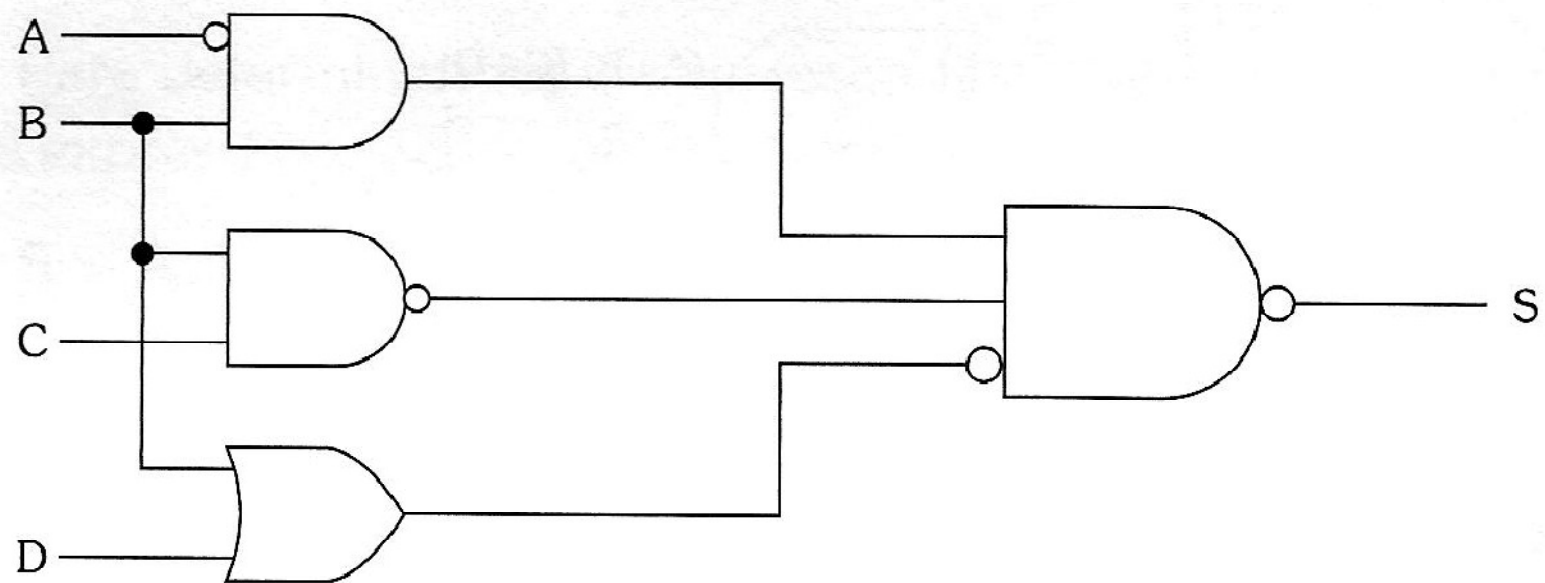


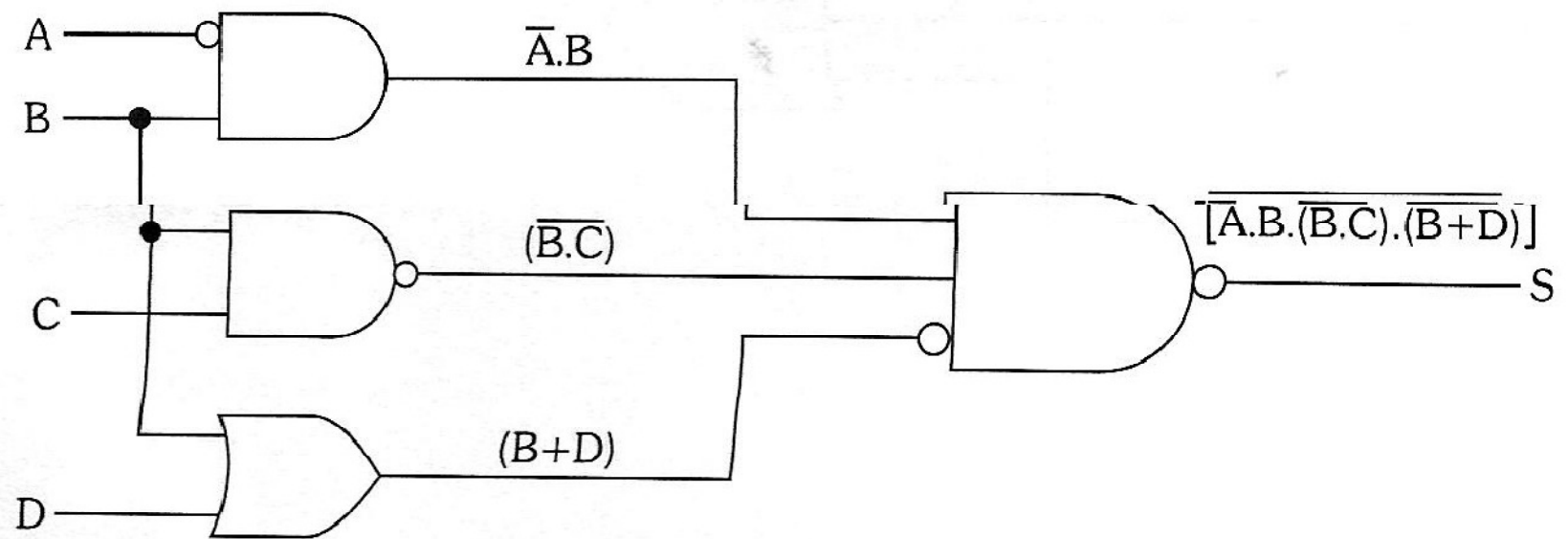








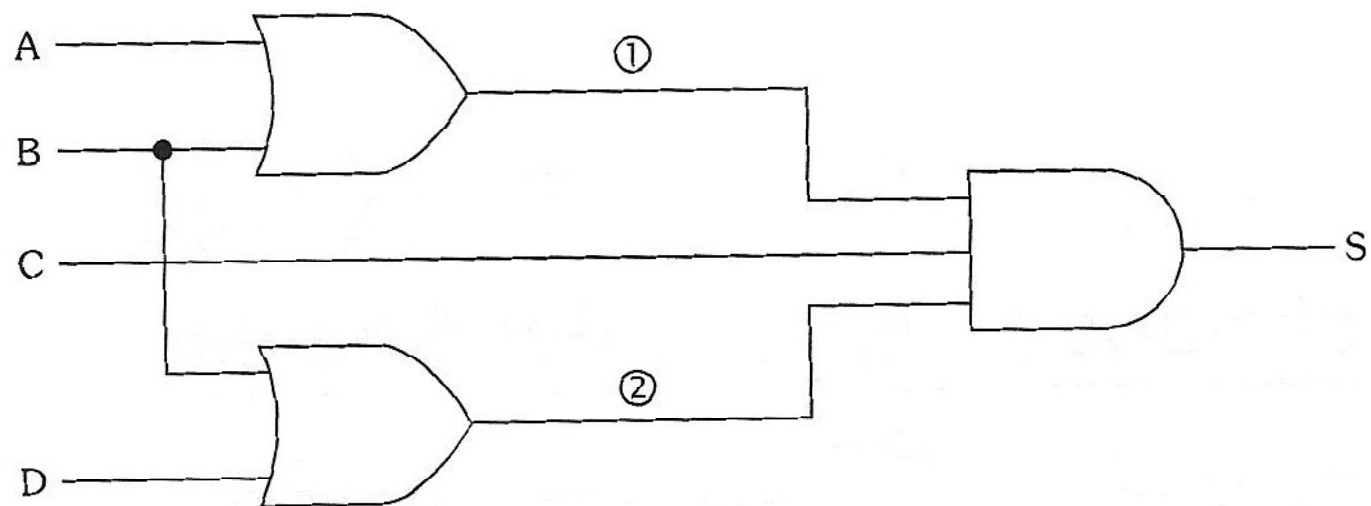




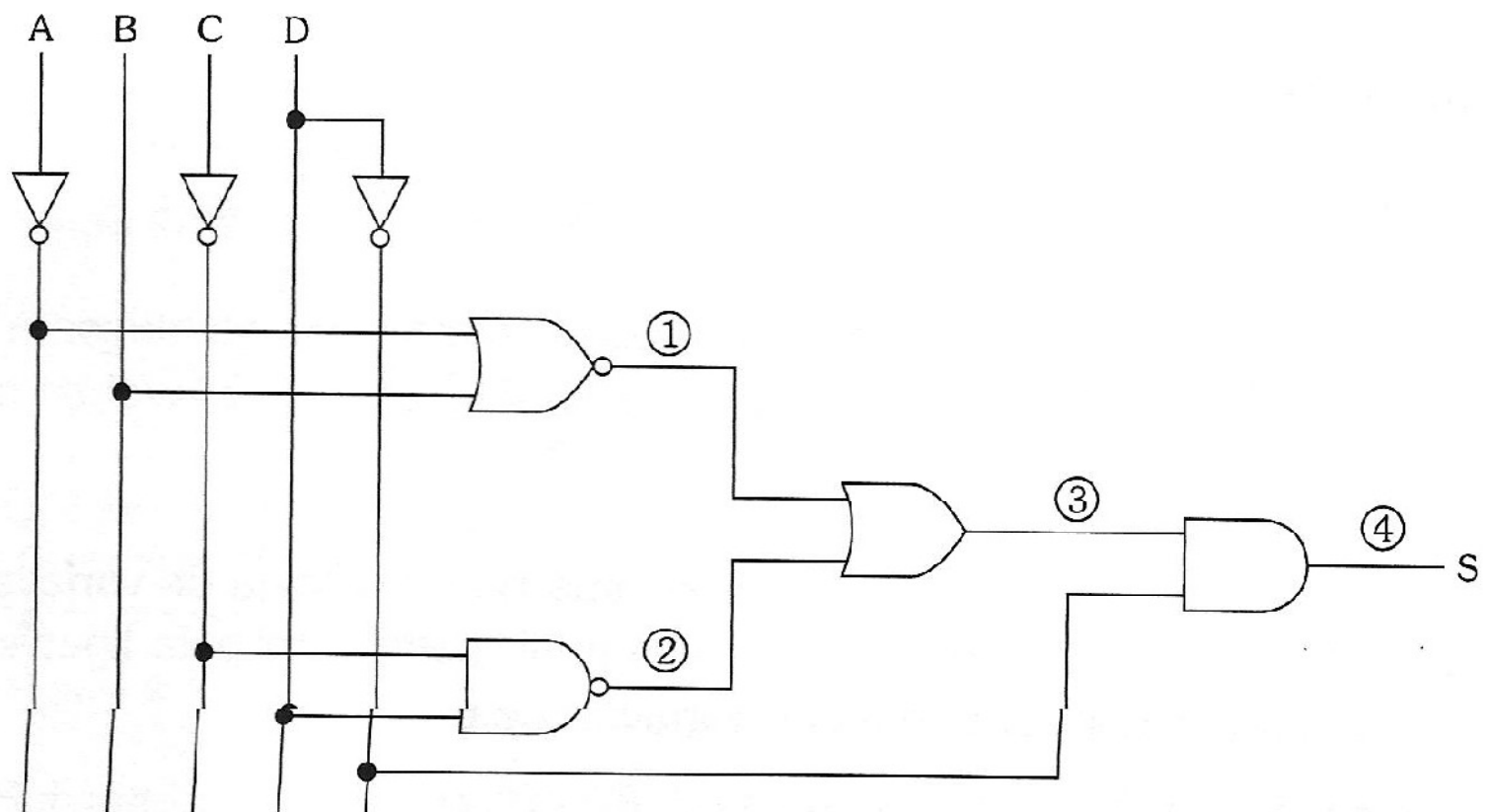
$$\therefore S = \left[\overline{A.B.(B.C).(B+D)} \right]$$

1. Expressões booleanas obtidas de circuitos lógicos
2. **Circuitos lógicos obtidos de expressões booleanas**
3. Tabelas verdade obtidas de expressões booleanas
4. Expressões booleanas obtidas de tabelas verdade

$$S = (A + B) \cdot C \cdot (B + D)$$



$$S = \overline{(\overline{A+B} + \overline{\overline{C}.D})} . \overline{D}$$



1. Expressões booleanas obtidas de circuitos lógicos
2. Circuitos lógicos obtidos de expressões booleanas
3. **Tabelas verdade obtidas de expressões booleanas**
4. Expressões booleanas obtidas de tabelas verdade

$$S = A \cdot \overline{B} \cdot C + A \cdot \overline{D} + \overline{A} \cdot B \cdot D.$$

A	B	C	D	1º miembro $A \cdot \bar{B} \cdot C$	2º miembro $A \cdot \bar{D}$	3º miembro $\bar{A} \cdot B \cdot D$	Resultado final S
0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	0
0	0	1	0	0	0	0	0
0	0	1	1	0	0	0	0
0	1	0	0	0	0	0	0
0	1	0	1	0	0	1	1
0	1	1	0	0	0	0	0
0	1	1	1	0	0	1	1
1	0	0	0	0	1	0	1
1	0	0	1	0	0	0	0
1	0	1	0	1	1	0	1
1	0	1	1	1	0	0	1
1	1	0	0	0	1	0	1
1	1	0	1	0	0	0	0
1	1	1	0	0	1	0	1
1	1	1	1	0	0	0	0

1. Expressões booleanas obtidas de circuitos lógicos
2. Circuitos lógicos obtidos de expressões booleanas
3. Tabelas verdade obtidas de expressões booleanas
- 4. Expressões booleanas obtidas de tabelas verdade**

#	A	B	S
0	0	0	1
1	0	1	0
2	1	0	1
3	1	1	1

Caso 00: $S = 1$ quando $A = 0$ e $B = 0$ ($\bar{A} = 1$ e $\bar{B} = 1$) $\Rightarrow \bar{A} \cdot \bar{B}$

Caso 10: $S = 1$ quando $A = 1$ e $B = 0$ ($A = 1$ e $\bar{B} = 1$) $\Rightarrow A \cdot \bar{B}$

Caso 11: $S = 1$ quando $A = 1$ e $B = 1 \Rightarrow A \cdot B$

$$\therefore S = \bar{A} \cdot \bar{B} + A \cdot \bar{B} + A \cdot B$$

#	A	B	C	S
0	0	0	0	1
1	0	0	1	0
2	0	1	0	1
3	0	1	1	0
4	1	0	0	0
5	1	0	1	0
6	1	1	0	1
7	1	1	1	1

Para solucionar, extraímos os casos em que a expressão é verdadeira ($S = 1$): 000 ou 010 ou 110 ou 111.

$$\therefore S = \overline{A}.\overline{B}.\overline{C} + \overline{A}.B.\overline{C} + A.B.\overline{C} + A.B.C$$