

**Anhanguera Educacional LTDA**

**Curso:** Ciência da Computação

**Matéria:** Linguagens Formais e Autômatos

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**Respostas dos Pós-aulas 1, 2, 3, 4 e 5.**

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## Lista1 – Revisão de Conjuntos

### A.

- 1-)  $A \cup B = \{0, 1, 2, 3\}$
- 2-)  $A \cap B = \{2\}$
- 3-)  $A - B = \{0, 1\}$
- 4-)  $A' = \{3, 4, 5, 6, 7, 8, 9, 10\}$
- 5-)  $2A = \{\{\}, \{1\}, \{2\}, \{0, 1\}, \{0, 2\}, \{1, 2\}\}$
- 6-)  $A \times B = \{(0, 2), (0, 3), (1, 2), (1, 3), (2, 2), (2, 3)\}$
- 7-)  $B \cup C = \{2, 3, 4, 5\}$
- 8-)  $B \cap C = \{\}$
- 9-)  $B - C = \{2, 3\}$
- 10-)  $B' = \{0, 1, 4, 5, 6, 7, 8, 9, 10\}$
- 11-)  $2B = \{\{\}, \{2\}, \{3\}, \{0, 2\}, \{0, 3\}, \{2, 3\}\}$
- 12-)  $B \times C = \{(2, 4), (2, 5), (3, 4), (3, 5)\}$
- 13-)  $C \cup D = \{2, 4, 5, 7, 8\}$
- 14-)  $C \cap D = \{5\}$
- 15-)  $C - D = \{4\}$
- 16-)  $C' = \{0, 1, 2, 3, 6, 7, 8, 9, 10\}$
- 17-)  $2C = \{\{\}, \{4\}, \{5\}, \{0, 4\}, \{0, 5\}, \{4, 5\}\}$
- 18-)  $C \times D = \{(4, 2), (4, 5), (4, 7), (4, 8), (5, 2), (5, 5), (5, 7), (5, 8)\}$
- 19-)  $D \cup A = \{0, 1, 2, 5, 7, 8\}$
- 20-)  $D \cap A = \{2\}$
- 21-)  $D - A = \{5, 7, 8\}$
- 22-)  $D' = \{0, 1, 3, 4, 6, 9, 10\}$
- 23-)  $2D = \{\{\}, \{2\}, \{5\}, \{7\}, \{8\}, \{0, 2\}, \{0, 5\}, \{0, 7\}, \{0, 8\}, \{2, 5\}, \{2, 7\}, \{2, 8\}, \{5, 7\}, \{5, 8\}, \{7, 8\}\}$
- 24-)  $D \times A = \{(2, 0), (2, 1), (2, 2), (5, 0), (5, 1), (5, 2), (7, 0), (7, 1), (7, 2), (8, 0), (8, 1), (8, 2)\}$
- 25-)  $A^2 = A \times A = \{(0, 0), (0, 1), (0, 2), (1, 0), (1, 1), (1, 2), (2, 0), (2, 1), (2, 2)\}$
- 26-)  $D^2 = D \times D = \{(2, 2), (2, 5), (2, 7), (2, 8), (5, 2), (5, 5), (5, 7), (5, 8), (7, 2), (7, 5), (7, 7), (7, 8), (8, 2), (8, 5), (8, 7), (8, 8)\}$
- 27-)  $A \cup (B \cup C) = \{0, 1, 2, 3, 4, 5\}$
- 28-)  $A \cap (B \cup C) = \{2\}$
- 29-)  $A \cap (B \cap C) = \{\}$
- 30-)  $C \cup (B \cup D) = B \cup D = \{2, 3, 5, 7, 8\} \rightarrow C \cup (B \cap D) = \{2, 3, 4, 5, 7, 8\}$
- 31-)  $C \cap (B \cup D) = \{5\}$
- 32-)  $C \cap (B \cap D) = B \cap D = \{2\} \rightarrow C \cap (B \cap D) = \{\}$
- 33-)  $D \cup (A \cup C) = A \cup C = \{0, 1, 2, 4, 5\} \rightarrow D \cup (A \cap C) = \{0, 1, 2, 4, 5, 7, 8\}$
- 34-)  $D \cap (A \cup C) = \{2, 5\}$
- 35-)  $D \cap (A \cap C) = A \cap C = \{\} \rightarrow D \cap (A \cap C) = \{\}$
- 36-)  $A \cup (B \cup C)' = (B \cup C)' = \{0, 1, 6, 7, 8, 9, 10\} \rightarrow A \cup (B \cap C)' = \{0, 1, 2, 6, 7, 8, 9, 10\}$
- 37-)  $D \cup (A \cap C)' = (A \cap C)' = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\} \rightarrow D \cup (A \cap C)' = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$
- 38-)  $A \times D' = \{(0, 0), (0, 1), (0, 3), (0, 4), (0, 6), (0, 9), (0, 10), (1, 0), (1, 1), (1, 3), (1, 4), (1, 6), (1, 9), (1, 10), (2, 0), (2, 1), (2, 3), (2, 4), (2, 6), (2, 9), (2, 10)\}$
- 39-)  $D \times (C')' = \{(2, 4), (2, 5), (5, 4), (5, 5), (7, 4), (7, 5), (8, 4), (8, 5)\}$
- 40-)  $B \cup (B')' = \{2, 3\}$

**B.**

$A \times A = \{(1,1), (1,2), (1,3), (1,5), (1,7), (2,1), (2,2), (2,3), (2,5), (2,7), (3,1), (3,2), (3,3), (3,5), (3,7), (5,1), (5,2), (5,3), (5,5), (5,7), (7,1), (7,2), (7,3), (7,5), (7,7)\}$

Gráfico =  $\{(1,1), (2,3), (3,5), (5,1), (7,7)\}$

Resposta: d)  $(2,3) \in R$ ,  $(3,5) \in R$ ,  $(7,7) \in R$

**C.**

$A \times B = \{(2,1), (2,3), (2,5), (2,7), (4,1), (4,3), (4,5), (4,7), (6,1), (6,3), (6,5), (6,7), (8,1), (8,3), (8,5), (8,7)\}$

Gráfico =  $\{(2,1), (4,3), (6,5), (8,7)\}$

- a) V
- b) F
- c) V
- d) F
- e) V

**D.**

$A \times B = \{(1,1), (1,3), (1,4), (1,5), (2,1), (2,3), (2,4), (2,5), (3,1), (3,3), (3,4), (3,5)\}$

$$y = 2x1 - 1 = 1$$

$$y = 2x2 - 1 = 3$$

$$y = 2x3 - 1 = 5$$

Resposta: a)

**Lista 2 – ER**

1

- a) Todas as palavras de “a” geradas, tal que  $a^n$ , e  $n \geq 1$
- b) Todas as palavras de “a” geradas, tal que  $a^n$ , e  $n \geq 2$
- c) Todas as palavras de “012” geradas, tal que  $0^n, 1^m$ , 2 e  $n, m \geq 0$
- d) Todas as palavras de “ab” geradas, tal que  $a^n b$ , e  $n \geq 0$
- e) Todas as palavras de “ab” geradas, tal que  $(a^n b^m)^o$ , e  $m, n, o \geq 0$

2

- a)  $\{ab, aab, abb, aaab, abbb, \dots\}$
- b)  $\{aaab, aaaaaabb, aaaaaaaaabbb, aaaaaaaaaaabb, \dots\}$
- c)  $\{ab, aabb, aaabbb, aaaabbb, \dots\}$
- d)  $\{aaab, aaabb, aaabbb, aaabbbb, \dots\}$
- e)  $\{aa, bb, aaaa, bbbb, \dots\}$

3

As alternativas verdadeiras são: b (Uma vez que uma intersecção deve-se haver pertencentes nos ambos conjuntos, e união ou em um ou em outro. Logo, como em ambos há “a” e “b”, a afirmação é

verdadeira.). E c (Para uma intersecção deve-se haver pertencentes em ambos conjuntos, e como são elementos distintos, não há intersecção, ou seja, é vazia.).

4

- a) F
- b) F
- c) F
- d) F
- e) F

5

$a^n, n/2 \equiv 0 \pmod{2}$

6

$(01)^*$

### Lista 3 - GR

1-) Dada a gramática  $G = (V, T, P, X)$  onde:

$V = \{X\}$

$T = \{a, b\}$

$P = \{X \rightarrow aX, X \rightarrow b\}$

- a) A palavra *abb* é gerada pela gramática G?
- b) A palavra *aba* é gerada pela gramática G?
- c) A palavra *ba* é gerada pela gramática G?
- d) A palavra *aaab* é gerada pela gramática G?
- e) A palavra *aaaab* é gerada pela gramática G?

#### Resposta

**a) abb**

$X \rightarrow aX \rightarrow ab..$

Não é gerada

**b) aba**

$X \rightarrow aX \rightarrow ab$

Não é gerada

**c) ba**

$X \rightarrow b$

Não é gerada

**d)aaab**

$X \rightarrow aX \rightarrow aaX \rightarrow aaaX \rightarrow aaab$

$X^4 \rightarrow$

é Gerada

**e)aaab**

$X \rightarrow aX \rightarrow aaX \rightarrow aaaX \rightarrow aaaaX \rightarrow aaaab$

$X^5 \rightarrow aaaab$

**2-) Dada a gramática  $G = (V, T, P, A)$  onde:**

$V = \{A, B\}$

$T = \{0, 1\}$

$P = \{A \rightarrow 0A, A \rightarrow B, B \rightarrow 1B, B \rightarrow 1\}$

a) A palavra *010101* é gerada pela gramática  $G$ ?

b) A palavra *00110* é gerada pela gramática  $G$ ?

c) A palavra *110* é gerada pela gramática  $G$ ?

d) A palavra *00111* é gerada pela gramática  $G$ ?

**Resposta:**

**a)010101**

$A \rightarrow 0A \rightarrow 0B \rightarrow 01B..$

Não é gerada

**b)0011**

$A \rightarrow 0A \rightarrow 00A \rightarrow 00B \rightarrow 001B \rightarrow 0011$

Não é gerada

**c)110**

$A \rightarrow B \rightarrow 1B \rightarrow 11B \rightarrow ...$

Não é gerada

**d)00111**

$A \rightarrow 0A \rightarrow 00A \rightarrow 00B \rightarrow 001B \rightarrow 0011B \rightarrow 00111$

$S^6 \rightarrow 00111$

É gerada

**3-) Seja a gramática  $G = (V, T, P, S)$  onde:**

$V = \{S, B, C\}$

$T = \{a, b, c\}$

$P = \{S \rightarrow aSBC, S \rightarrow aBC, CB \rightarrow BC, aB \rightarrow ab, bB \rightarrow bb, bC \rightarrow bc, cC \rightarrow cc\}$

Apresente uma derivação para as palavras:

a) aabbcc

b) abbc

Resposta:

3-

a) aabbcc

$S \rightarrow aSBC \rightarrow aaBCBC \rightarrow aaBBCC \rightarrow aabBCC \rightarrow aabbCC \rightarrow aabbcc$

$S^6 \rightarrow aabbcc$

b) abbc

$S \rightarrow aBC \rightarrow abC \rightarrow abbc$

$S^3 \rightarrow abbc$

4-) Dada a gramática  $G = (V, T, P, S)$  onde:

$V = \{S, B, C, D\}$

$T = \{0, 1\}$

$P = \{S \rightarrow 0B, S \rightarrow 1C, S \rightarrow 0C, B \rightarrow 0S, B \rightarrow 1D, B \rightarrow 1B, \\ B \rightarrow \varepsilon, C \rightarrow 1S, C \rightarrow 0D, C \rightarrow \varepsilon, D \rightarrow 0C, D \rightarrow 1B\}$

Apresente uma derivação para as palavras:

a) 0111

b) 1101

c) 01110

d) 10011

**a)0111**

$S \rightarrow 0B \rightarrow 01B011B \rightarrow 0111B \rightarrow 0111\varepsilon$

$S^5 \rightarrow 0111$

**b)1101**

$B \rightarrow 1B \rightarrow 11B \rightarrow 110S \rightarrow 1101C \rightarrow 1101\varepsilon$

$S^5 \rightarrow 1101$

**c)01110**

$S \rightarrow 0B \rightarrow 01B \rightarrow 011B \rightarrow 0111D \rightarrow 01110C \rightarrow 01110\varepsilon$

$S^6 \rightarrow 01110$

**d)10011**

$S \rightarrow 1C \rightarrow 10D \rightarrow 100C \rightarrow 1001S \rightarrow 10011C \rightarrow 10011\varepsilon$

$S^6 \rightarrow 10011$

5-) Dada a gramática  $G = (V, T, P, INT)$  onde:

$V = \{DIG, INT\}$

$T = \{+, -, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}$

$P = \{INT \rightarrow +DIG \mid -DIG, DIG \rightarrow 0DIG \mid 1DIG \mid \dots \mid 9DIG \mid 0 \mid 1 \mid \dots \mid 9\}$

a) A palavra  $0 + 1$  é gerada pela gramática  $G$ ?

b) A palavra  $- 0 + 1$  é gerada pela gramática  $G$ ?

c) A palavra  $- 101$  é gerada pela gramática  $G$ ?

**a)0+1**

Não é gerado  
DIG- $\rightarrow$ 0DIG- $\rightarrow$ ...

**b)-0+1**

INT- $\rightarrow$ -DIG- $\rightarrow$ -0DIG- $\rightarrow$ ...

Não é gerado

**c)-101**

INT- $\rightarrow$ -DIG- $\rightarrow$ -1DIG- $\rightarrow$ -10DIG- $\rightarrow$  -101

É gerado

6-) Gere uma Gramática G, tal que tenhamos números pares de a validados.

$G = \{V, T, P, S\}$

$V = \{S, D\}$

$T = \{0, 2, 4, 6, 8, \epsilon\}$

$P = \{S \rightarrow D, S \rightarrow DS, D \rightarrow 0|1|2|4|6|8|\epsilon\}$

7-) Gere uma Gramática G, tal que tenhamos números 0 e 1 consecutivos: 01, 0011, 000111,

..., validados.

$G = \{V, T, P, S\}$

$V = \{S, D\}$

$T = \{0, 1\}$

$P = \{S \rightarrow 0D, S \rightarrow 1D, D \rightarrow 1D, D \rightarrow 0D, D \rightarrow \epsilon\}$

8-) Gere uma Gramática G, tal que tenhamos os pares ( $a^n b^{n-1}$ ), ou seja,  $a\epsilon$ ,  $ab$ ,  $aab$ ,  $aaabb$ ,  $aaaabbb$ , ..., validados.

$G = \{V, T, P, S\}$

$V = \{S, B\}$

$T = \{a, b, \epsilon\}$

$P = \{S \rightarrow aB, B \rightarrow 1B, B \rightarrow S, B \rightarrow \epsilon\}$

9-) Gere uma Gramática G, tal que tenhamos uma palavra que seja identificador do C++ validada, ou seja, palavras formadas por uma ou mais letras e dígitos, sempre iniciando com uma letra.

$G = \{V, T, P, S\}$

$V = \{D, B, S\}$

$T = \{a, b, c, \dots, z, \epsilon, 0, 1, 2, 3, \dots, 9\}$

$P = \{S \rightarrow DB, D \rightarrow S, D \rightarrow B, B \rightarrow S, B \rightarrow D, D \rightarrow \epsilon, B \rightarrow \epsilon, D \rightarrow a|b|c|\dots|y|z|\epsilon, B \rightarrow 0|1|2|3|4|5|6|7|8|9|\epsilon\}$

10-) Gere uma Gramática G, tal que tenhamos um endereço de e-mail validado, ou seja,  $x@x$ , onde @ ocorre apenas uma vez.

$G = \{V, T, P, S\}$

$V = \{A, B, S, @\}$

$T = \{a, b, c, \dots, z, \epsilon, 0, 1, 2, 3, \dots, 9\}$

$P = \{S \rightarrow AA, S \rightarrow BA, A \rightarrow B, B \rightarrow A, A \rightarrow @, @ \rightarrow @A | @B, A \rightarrow a|b|c|\dots|y|z|\epsilon, B \rightarrow 0|1|2|3|4|5|6|7|8|9|\epsilon\}$

11-) Classifique as gramáticas dos exercícios 1 a 5 segundo a hierarquia de Chomsky.

1- GLC;

- 2- 2- GR;
- 3- 3-GSC;
- 4- 4-GI;
- 5- 5-GR.

12-) Gere uma Gramática Regular  $G_R$ , tal que tenhamos um número real negativo ou positivo validado, sendo que apenas o símbolo negativo deve estar representado.

$V=\{D,X\}$

$T=\{-,0,1,2,3,4,5,6,7,8,9\}$

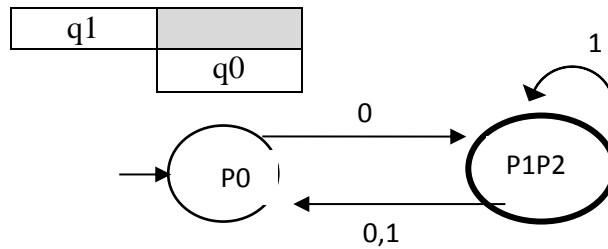
$P=\{X \rightarrow -D, D \rightarrow 0D, D \rightarrow |1D| \dots |9D|0|1| \dots |9\}$

## Lista 4 - AFD

1.

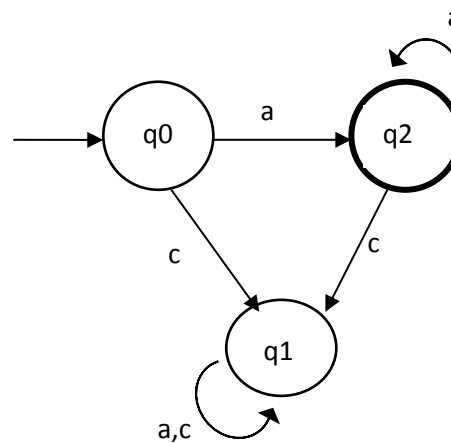
a)

P1	X	
P2	X	
	P0	P1

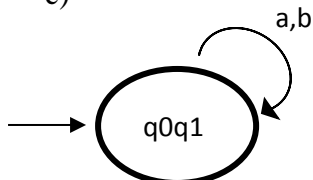


b)

q1	+	
q2	X	X
	q0	1



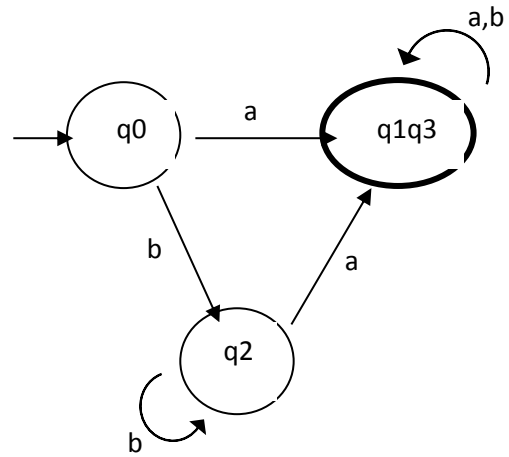
c)





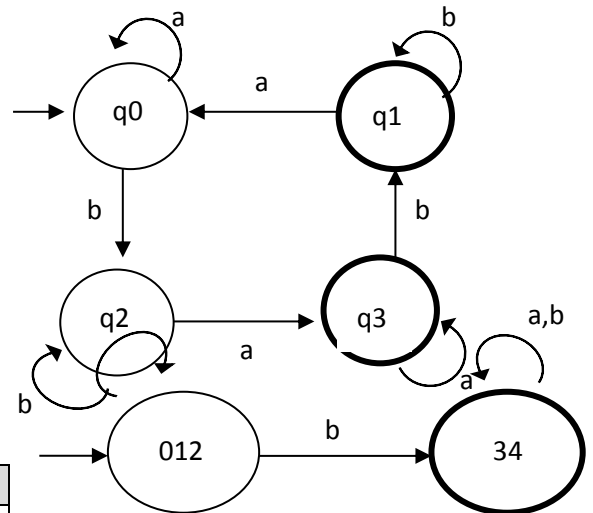
d)

q1	x		
q2	+	x	
q3	x		x
	q0	q1	q2



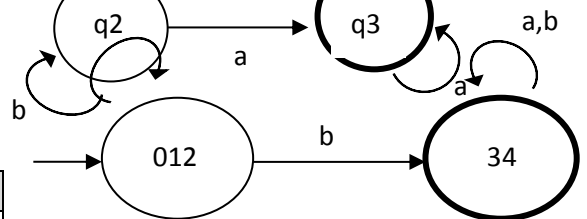
e)

q1	x		
q2	+	x	
q3	x	+	x
	q0	q1	q2



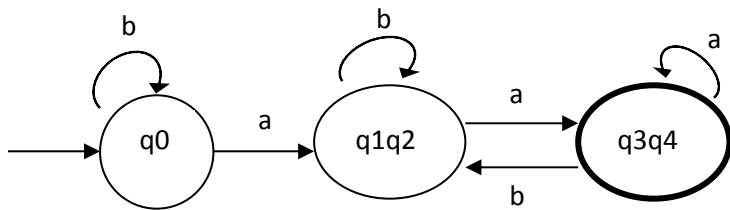
f)

1				
2				
3	x	x	x	
4	x	x	x	
	0	1	2	3



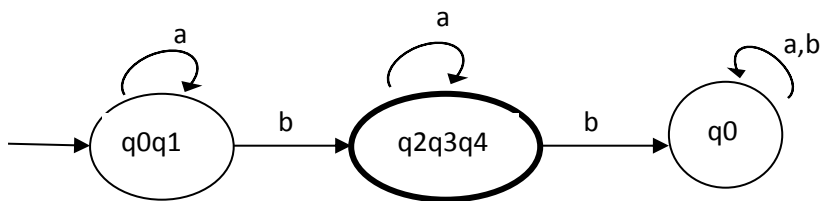
g)

q1	+			
q2	+			
q3	x	x	x	
q4	x	x	x	
	q0	q1	q2	q3

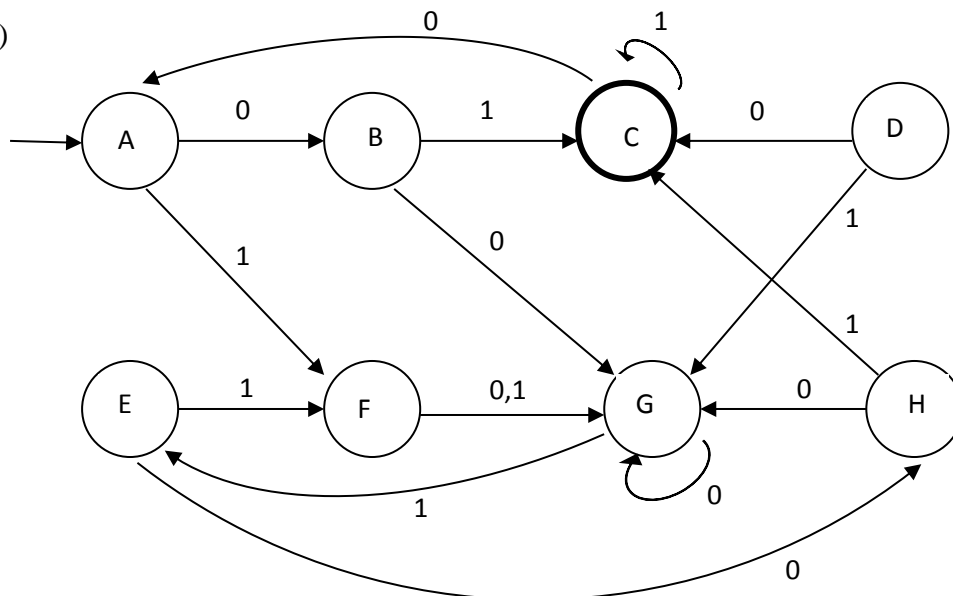


h)

q1					
q2	X	x			
q3	X	x			
q4	X	x			
q5	+	+	x	x	x
	q0	q1	q2	q3	q4



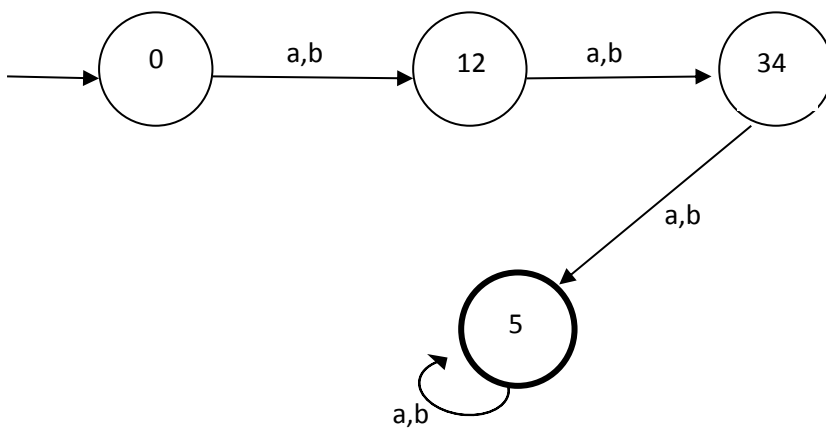
i)



Não é possível a minimização, pois o D é inacessível.

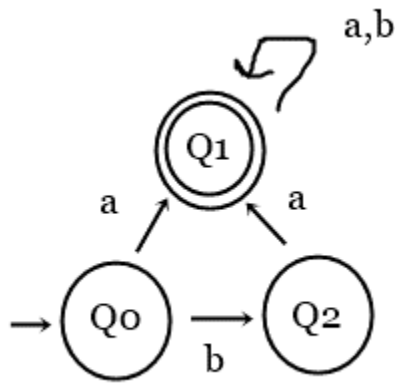
j)

1	+				
2	+				
3	+	+	+		
4	+	+	+		
5	x	x	X	x	x
	0	1	2	3	4



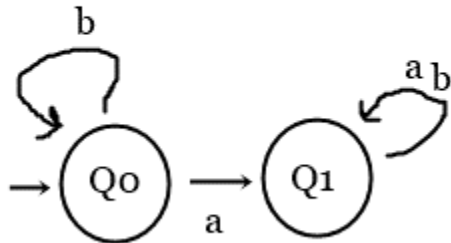
## Lista 5 - AFND

$$\begin{aligned}
 A- \\
 \delta'(<q0>,a) &= \delta(\{q0\},a) = <q1> \\
 ) \\
 \delta'(<q0>,b) &= \delta(\{q0\},b) = <q0q1> \\
 \delta'(<q1>,a) &= \delta(\{q1\},a) = <q1> \\
 \delta'(<q1>,b) &= \delta(\{q1\},b) = <q1> \\
 \delta'(<q0q1>,a) &= \delta(\{q0\},a) \cup \delta(\{q1\},a) = \{q1\} \cup \{q1\} = <q1> \\
 >,a) \\
 \delta'(<q0q1>,b) &= \delta(\{q0\},b) \cup \delta(\{q1\},b) = \{q0q1\} \cup \{q1\} = <q0q1> \\
 >,b)
 \end{aligned}$$



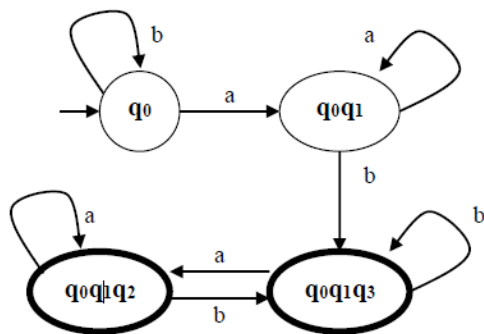
B-

$$\begin{aligned}
 \delta'(<q0>,a) &= \delta(\{q0\},a) = \{q1q2\} \\
 \delta'(<q0>,b) &= \delta(\{q0\},b) = \{q0\} \\
 \delta'(<q1q2>,a) &= \delta(\{q1\},a) \cup \delta(\{q2\},a) = \{q1\} \cup \{q2\} = \{q1q2\} \\
 \delta'(<q1q2>,b) &= \delta(\{q1\},b) \cup \delta(\{q2\},b) = \{q1\} \cup \{q2\} = \{q1q2\} \\
 \Sigma &\rightarrow \{a,b\} \\
 Q &\rightarrow \{<q0>, <q1q2>\} \\
 \delta &\rightarrow \\
 q0 &\rightarrow \{<q0>\} \\
 F &\rightarrow \{<q1>\}
 \end{aligned}$$



C-

$$\begin{aligned}
 \delta'(<q0>,a) &= \delta(\{q0\},a) = \{q0q1\} \\
 \delta'(<q0>,b) &= \delta(\{q0\},b) = \{q0\} \\
 \delta'(<q0q1>,a) &= \delta(\{q0\},a) \cup \delta(\{q1\},a) = \{q0q1\} \cup \{q1\} = \{q0q1q3\} \\
 \delta'(<q0q1>,b) &= \delta(\{q0\},b) \cup \delta(\{q1\},b) = \{q0\} \cup \{q1\} = \{q0q1q3\} \\
 \delta'(<q0q1q3>,a) &= \delta(\{q0\},a) \cup \delta(\{q1\},a) \cup \delta(\{q3\},a) = \{q0q1\} \cup \{q1\} \cup \{q3\} = \{q0q1q3\} \\
 \delta'(<q0q1q3>,b) &= \delta(\{q0\},b) \cup \delta(\{q1\},b) \cup \delta(\{q3\},b) = \{q0\} \cup \{q1\} \cup \{q3\} = \{q0q1q3\} \\
 \delta'(<q0q1q2>,a) &= \delta(\{q0\},a) \cup \delta(\{q1\},a) \cup \delta(\{q2\},a) = \{q0q1\} \cup \{q1\} \cup \{q2\} = \{q0q1q3\} \\
 \delta'(<q0q1q2>,b) &= \delta(\{q0\},b) \cup \delta(\{q1\},b) \cup \delta(\{q2\},b) = \{q0\} \cup \{q1\} \cup \{q2\} = \{q0q1q3\} \\
 \Sigma &\rightarrow \{a,b\} \\
 Q &\rightarrow \{<q0>, <q0q1>, <q0q1q3>, <q0q1q2>\} \\
 \delta &\rightarrow \\
 q0 &\rightarrow \{<q0>\} \\
 &\rightarrow
 \end{aligned}$$



D-

$\delta'(<q0>,a)$

=

$\delta =$

$(\{q0\}, a)$

$<q0>$

$\delta'(<q0>,b)$

=

$\delta(\{q0\},b)$

$<q0q1>$

$\delta'(<q0q1>,a)$

=

$\delta(\{q0\},a)$

$\cup$

$\{q0\} \cup \{q0q1\}$

$<q0q1q2>$

$\delta'(<q0q1>,b)$

=

$\delta(\{q0\},b)$

$\cup$

$\{q0q1\} \cup \{q0q1q2\}$

$<q0q1q2>$

$\delta'(<q0q1q2>,a)$

=

$\delta(\{q0\},a)$

$\cup$

$\delta(\{q1\},a)$

$\cup$

$\delta(\{q2\},a)$

=

$\{q0\} \cup \{q0q1\} \cup \{q0q1q2\}$

$<q0q1q2>$

$\delta'(<q0q1q2>,b)$

=

$\delta(\{q0\},b)$

$\cup$

$\delta(\{q1\},b)$

$\cup$

$\delta(\{q2\},b)$

=

$\{q0\} \cup \{q0q1\} \cup \{q0q1q2\}$

$<q0q1q2>$

$\delta'(<q0q1q2>,a)$

=

$\delta(\{q0\},a)$

$\cup$

$\delta(\{q1\},a)$

$\cup$

$\delta(\{q2\},a)$

=

$\{q0\} \cup \{q0q1\} \cup \{q0q1q2\}$

$<q0q1q2>$

$\delta'(<q0q1q2>,b)$

=

$\delta(\{q0\},b)$

$\cup$

$\delta(\{q1\},b)$

$\cup$

$\delta(\{q2\},b)$

=

$\{q0\} \cup \{q0q1\} \cup \{q0q1q2\}$

$<q0q1q2>$

$\Sigma \rightarrow \{a,b\}$

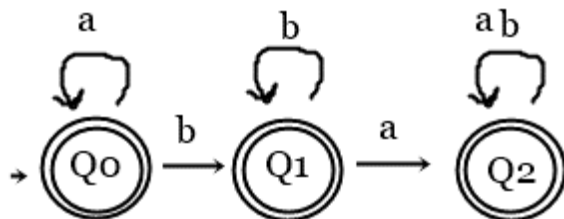
$Q \rightarrow \{<q0>, <q0q1>, <q0q1q2>\}$

$\delta \rightarrow$

$q0 \rightarrow \{<q0>\}$

$\rightarrow$

$F \rightarrow \{<q0>, <q0q1>, <q0q1q2>\}$



E-

$\delta'(<A>,0)$

=

$\delta(\{A\},0)$

=

$<BC>$

$\delta'(<A>,1)$

=

$\delta(\{A\},1)$

=

$<BC>$

$\delta'(<BC>,0)$

=

$\delta(\{B\},0)$

$\cup$

$\delta(\{C\},0)$

=

$\{C\} \cup \emptyset$

=

$<C>$

$\delta'(<BC>,1)$

=

$\delta(\{B\},1)$

$\cup$

$\delta(\{C\},1)$

=

$\{C\} \cup \emptyset$

=

$<C>$

$\delta'(<C>,0)$

=

$\emptyset$

$\delta'(<C>,1)$

=

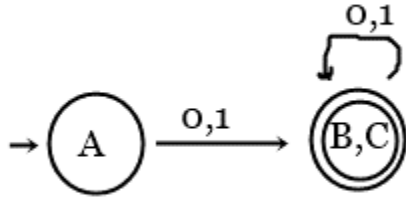
$\emptyset$

$\Sigma \rightarrow \{0,1\}$

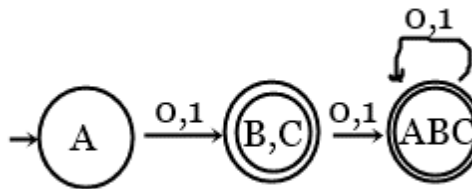
$Q \rightarrow \{<BC>\}$

$\delta \rightarrow$

$q_0 \rightarrow \{<A>\}$   
 $F \rightarrow \{<BC>\}$



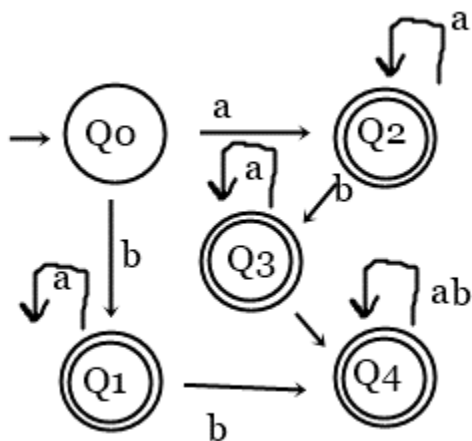
**F-**  
 $\delta'(<A>, 0) = \delta(\{A\}, 0) = \{<BC>\}$   
 $\delta'(<A>, 1) = \delta(\{A\}, 1) = \{<BC>\}$   
 $\delta'(<BC>, 0) = \delta(\{B\}, 0) \cup \delta(\{C\}, 0) = \{AC\} \cup \{AB\} = \{<ABC>\}$   
 $\delta'(<BC>, 1) = \delta(\{B\}, 1) \cup \delta(\{C\}, 1) = \{AC\} \cup \{AB\} = \{<ABC>\}$   
 $\delta'(<AB>, 0) = \delta(\{A\}, 0) \cup \delta(\{B\}, 0) \cup \delta(\{C\}, 0) = \{BC\} \cup \{AC\} \cup \{AB\} = \{<ABC>\}$   
 $\delta'(<AB>, 1) = \delta(\{A\}, 1) \cup \delta(\{B\}, 1) \cup \delta(\{C\}, 1) = \{BC\} \cup \{AC\} \cup \{AB\} = \{<ABC>\}$   
 $\Sigma \rightarrow \{0,1\}$   
 $Q \rightarrow \{<BC>\}$   
 $\delta \rightarrow$   
 $q_0 \rightarrow \{<A>\}$   
 $F \rightarrow \{<BC>, <ABC>\}$



**G-**  
 $\delta'(<q_0>, a) = \delta(\{q_0\}, a) = \{<q_0q_1q_2>\}$   
 $\delta'(<q_0>, b) = \delta(\{q_0\}, b) = \{<q_1q_2>\}$   
 $\delta'(<q_1q_2>, a) = \delta(\{q_1\}, a) \cup \delta(\{q_2\}, a) = \{q_1\} \cup \{q_2\} = \{<q_1q_2>\}$   
 $\delta'(<q_1q_2>, b) = \delta(\{q_1\}, b) \cup \delta(\{q_2\}, b) = \{q_1\} \cup \{q_3\} = \{<q_1q_3>\}$

$\delta'(<q1q3>,a)$	=	$\delta(\{q1\},a)$	$\cup$	$\delta(\{q3\},a)$	=	$\{q1\} \cup \{q3\}$	=	$<q1q3>$
$\delta'(<q1q3>,b)$	=	$\delta(\{q1\},b)$	$\cup$	$\delta(\{q3\},b)$	=	$\{q1\} \cup \{q3\}$	=	$<q1q3>$
$\delta'(<q0q1q2>,a)$	=	$\delta(\{q0\},a)$	$\cup$	$\delta(\{q1\},a)$	$\cup$	$\delta(\{q2\},a)$	=	$\{q0q1q2\} \cup \{q1q2\} \cup \{q1\} \cup \{q3\} = <q0q1q2>$
$\delta'(<q0q1q2>,b)$	=	$\delta(\{q0\},b)$	$\cup$	$\delta(\{q1\},b)$	$\cup$	$\delta(\{q2\},b)$	=	$\{q1q2\} \cup \{q1\} \cup \{q3\} = <q1q2q3>$
$\delta'(<q1q2q3>,a)$	=	$\delta(\{q1\},a)$	$\cup$	$\delta(\{q2\},a)$	$\cup$	$\delta(\{q3\},a)$	=	$\{q1\} \cup \{q2\} \cup \{q3\} = <q1q2q3>$
$\delta'(<q1q2q3>,b)$	=	$\delta(\{q1\},b)$	$\cup$	$\delta(\{q2\},b)$	$\cup$	$\delta(\{q3\},b)$	=	$\{q1\} \cup \{q3\} \cup \{q3\} = <q1q3>$

$\Sigma \rightarrow \{a,b\}$   
 $Q \rightarrow \{<q0>, <q1q2>, <q1q3>, <q0q1q2>, <q1q2q3>\}$   
 $\delta \rightarrow$   
 $q0 \rightarrow \{<q0>\}$   
 $\rightarrow$   
 $F \rightarrow \{<q1q2>, <q1q3>, <q0q1q2>, <q1q2q3>\}$

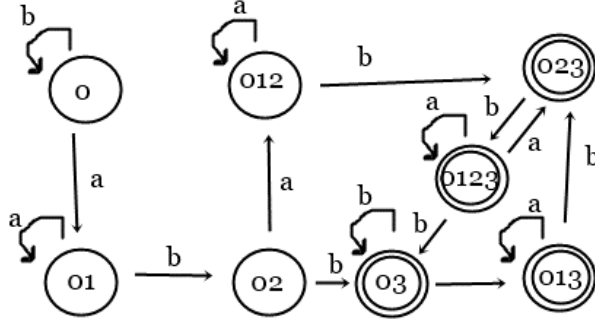


$H-$									
$\delta'(<0>,a)$	=		$\delta(\{0\},a)$	=		$<01>$			
$\delta'(<0>,b)$	=		$\delta(\{0\},b)$	=		$<0>$			
$\delta'(<01>,a)$	=	$\delta(\{0\},a)$	$\cup$	$\delta(\{1\},a)$	=	$\{01\} \cup \{1\}$	=	$<01>$	
$\delta'(<01>,b)$	=	$\delta(\{0\},b)$	$\cup$	$\delta(\{1\},b)$	=	$\{0\} \cup \{2\}$	=	$<02>$	
$\delta'(<02>,a)$	=	$\delta(\{0\},a)$	$\cup$	$\delta(\{2\},a)$	=	$\{01\} \cup \{2\}$	=	$<012>$	
$\delta'(<02>,b)$	=	$\delta(\{0\},b)$	$\cup$	$\delta(\{2\},b)$	=	$\{0\} \cup \{3\}$	=	$<03>$	
$\delta'(<03>,a)$	=	$\delta(\{0\},a)$	$\cup$	$\delta(\{3\},a)$	=	$\{01\} \cup \{3\}$	=	$<013>$	
$\delta'(<03>,b)$	=	$\delta(\{0\},b)$	$\cup$	$\delta(\{3\},b)$	=	$\{0\} \cup \{3\}$	=	$<03>$	
$\delta'(<012>,a)$	=	$\delta(\{0\},a)$	$\cup$	$\delta(\{1\},a)$	$\cup$	$\delta(\{2\},a)$	=	$\{01\} \cup \{1\} \cup \{2\} = <012>$	
$\delta'(<012>,b)$	=	$\delta(\{0\},b)$	$\cup$	$\delta(\{1\},b)$	$\cup$	$\delta(\{2\},b)$	=	$\{0\} \cup \{2\} \cup \{3\} = <023>$	
$\delta'(<013>,a)$	=	$\delta(\{0\},a)$	$\cup$	$\delta(\{1\},a)$	$\cup$	$\delta(\{3\},a)$	=	$\{01\} \cup \{1\} \cup \{3\} = <013>$	
$\delta'(<013>,b)$	=	$\delta(\{0\},b)$	$\cup$	$\delta(\{1\},b)$	$\cup$	$\delta(\{3\},b)$	=	$\{0\} \cup \{2\} \cup \{3\} = <023>$	
$\delta'(<023>,a)$	=	$\delta(\{0\},a)$	$\cup$	$\delta(\{2\},a)$	$\cup$	$\delta(\{3\},a)$	=	$\{01\} \cup \{2\} \cup \{3\} = <0123>$	
$\delta'(<023>,b)$	=	$\delta(\{0\},b)$	$\cup$	$\delta(\{2\},b)$	$\cup$	$\delta(\{3\},b)$	=	$\{0\} \cup \{3\} \cup \{3\} = <03>$	
$\delta'(<0123>,a)$	=	$\delta(\{0\},a)$	$\cup$	$\delta(\{1\},a)$	$\cup$	$\delta(\{2\},a)$	$\cup$	$\delta(\{3\},a)$	= $\{01\} \cup \{1\} \cup \{2\} \cup \{3\} = <0123>$

$$\begin{aligned} \delta' &= \delta \cup \delta(\{1\}, b) \cup \delta \cup \delta = \{0\} \cup \{2\} = \langle 023 \rangle \\ (\langle 0123 \rangle, b) &= (\{0\}, b) \cup \delta(\{1\}, b) \cup \delta(\{2\}, b) \cup \delta(\{3\}, b) = \{0\} \cup \{2\} \cup \{3\} = \langle 023 \rangle \\ \Sigma \rightarrow & \end{aligned}$$

H-

$$\begin{aligned} \delta'(\langle 0 \rangle, a) &= \delta(\{0\}, a) = \delta(\{0\}, a) = \langle 01 \rangle \\ \delta'(\langle 0 \rangle, b) &= \delta(\{0\}, b) = \delta(\{0\}, b) = \langle 0 \rangle \\ \delta'(\langle 01 \rangle, a) &= \delta(\{0\}, a) \cup \delta(\{1\}, a) = \{0\} \cup \{1\} = \langle 01 \rangle \\ \delta'(\langle 01 \rangle, b) &= \delta(\{0\}, b) \cup \delta(\{1\}, b) = \{0\} \cup \{2\} = \langle 02 \rangle \\ \delta'(\langle 02 \rangle, a) &= \delta(\{0\}, a) \cup \delta(\{2\}, a) = \{0\} \cup \{2\} = \langle 012 \rangle \\ \delta'(\langle 02 \rangle, b) &= \delta(\{0\}, b) \cup \delta(\{2\}, b) = \{0\} \cup \{3\} = \langle 03 \rangle \\ \delta'(\langle 03 \rangle, a) &= \delta(\{0\}, a) \cup \delta(\{3\}, a) = \{0\} \cup \{3\} = \langle 013 \rangle \\ \delta'(\langle 03 \rangle, b) &= \delta(\{0\}, b) \cup \delta(\{3\}, b) = \{0\} \cup \{3\} = \langle 03 \rangle \\ \delta'(\langle 012 \rangle, a) &= \delta(\{0\}, a) \cup \delta(\{1\}, a) \cup \delta(\{2\}, a) = \{0\} \cup \{1\} \cup \{2\} = \langle 012 \rangle \\ \delta'(\langle 012 \rangle, b) &= \delta(\{0\}, b) \cup \delta(\{1\}, b) \cup \delta(\{2\}, b) = \{0\} \cup \{2\} \cup \{3\} = \langle 023 \rangle \\ \delta'(\langle 013 \rangle, a) &= \delta(\{0\}, a) \cup \delta(\{1\}, a) \cup \delta(\{3\}, a) = \{0\} \cup \{1\} \cup \{3\} = \langle 013 \rangle \\ \delta'(\langle 013 \rangle, b) &= \delta(\{0\}, b) \cup \delta(\{1\}, b) \cup \delta(\{3\}, b) = \{0\} \cup \{2\} \cup \{3\} = \langle 023 \rangle \\ \delta'(\langle 023 \rangle, a) &= \delta(\{0\}, a) \cup \delta(\{2\}, a) \cup \delta(\{3\}, a) = \{0\} \cup \{2\} \cup \{3\} = \langle 0123 \rangle \\ \delta'(\langle 023 \rangle, b) &= \delta(\{0\}, b) \cup \delta(\{2\}, b) \cup \delta(\{3\}, b) = \{0\} \cup \{3\} \cup \{3\} = \langle 03 \rangle \\ \delta'(\langle 0123 \rangle, a) &= \delta(\{0\}, a) \cup \delta(\{1\}, a) \cup \delta(\{2\}, a) \cup \delta(\{3\}, a) = \{0\} \cup \{1\} \cup \{2\} \cup \{3\} = \langle 0123 \rangle \\ \delta'(\langle 0123 \rangle, b) &= \delta(\{0\}, b) \cup \delta(\{1\}, b) \cup \delta(\{2\}, b) \cup \delta(\{3\}, b) = \{0\} \cup \{2\} \cup \{3\} \cup \{3\} = \langle 023 \rangle \\ \Sigma \rightarrow & \{a, b\} \\ Q \rightarrow & \{\langle 0 \rangle, \langle 01 \rangle, \langle 02 \rangle, \langle 03 \rangle, \langle 012 \rangle, \langle 013 \rangle, \langle 023 \rangle, \langle 0123 \rangle\} \\ \delta \rightarrow & \\ q0 \rightarrow & \{\langle q0 \rangle\} \\ F \rightarrow & \{\langle 03 \rangle, \langle 012 \rangle, \langle 013 \rangle, \langle 023 \rangle\} \end{aligned}$$



I-

$$\begin{aligned} \delta'(\langle q0 \rangle, a) &= \delta(\{q0\}, a) = \{q1\} \cup \{q4\} = \langle q1q4 \rangle \\ \delta'(\langle q0 \rangle, b) &= \delta(\{q0\}, b) = \{q1\} \cup \{q4\} = \langle q1q4 \rangle \\ \delta'(\langle q1q4 \rangle, a) &= \delta(\{q1\}, a) \cup \delta(\{q4\}, a) = \{q2\} \cup \{q4\} = \langle q2q4 \rangle \\ \delta'(\langle q1q4 \rangle, b) &= \delta(\{q1\}, b) \cup \delta(\{q4\}, b) = \{q2\} \cup \{q4\} = \langle q2q4 \rangle \\ \delta'(\langle q2q4 \rangle, a) &= \delta(\{q2\}, a) \cup \delta(\{q4\}, a) = \{q3\} \cup \{q4\} = \langle q3q4 \rangle \\ \delta'(\langle q2q4 \rangle, b) &= \delta(\{q2\}, b) \cup \delta(\{q4\}, b) = \{q3\} \cup \{q4\} = \langle q3q4 \rangle \end{aligned}$$



$\delta'$	=	$\delta$	$\cup$	$\delta$	=	$\{q3\} \cup$	=	$\langle q3q4$
$(\langle q3q4 \rangle, a)$		$(\{q3\}, a)$		$(\{q4\}, a)$		$\{q4\}$		$\rangle$
$\delta'$	=	$\delta$	$\cup$	$\delta$	=	$\{q5\} \cup$	=	$\langle q4q5$
$(\langle q3q4 \rangle, b)$		$(\{q3\}, b)$		$(\{q4\}, b)$		$\{q4\}$		$\rangle$
$\delta'$	=	$\delta$	$\cup$	$\delta$	=	$\{q4\} \cup$	=	$\langle q4q5$
$(\langle q4q5 \rangle, a)$		$(\{q4\}, a)$		$(\{q5\}, a)$		$\{q5\}$		$\rangle$
$\delta'$	=	$\delta$	$\cup$	$\delta$	=	$\{q4\} \cup$	=	$\langle q4q5$
$(\langle q4q5 \rangle, b)$		$(\{q4\}, b)$		$(\{q5\}, b)$		$\{q4q5\}$		$\rangle$
$\Sigma \rightarrow$		$\{a, b\}$						
$Q \rightarrow$		$\{\langle q0 \rangle, \langle q1q4 \rangle, \langle q2q4 \rangle, \langle q3q4 \rangle, \langle q4q5 \rangle\}$						
$\delta \rightarrow$								
$q0 \rightarrow$		$\{\langle q0 \rangle\}$						
$F \rightarrow$		$\{\langle q1q4 \rangle, \langle q2q4 \rangle, \langle q3q4 \rangle, \langle q4q5 \rangle\}$						

