

## ASSIGNMENT 6

### Resolution QUESTION

- (a) Marcus was a man.
- (b) Marcus was a Roman.
- (c) All men are people.
- (d) Caesar was a ruler.
- (e) All Romans were either loyal to Caesar or hated him (or both).
- (f) Everyone is loyal to someone.
- (g) People only try to assassinate rulers they are not loyal to.
- (h) Marcus tried to assassinate Caesar

QUERY:.....

Who hated Caesar?

### First order logic

- |  |   |
|--|---|
| (a) Marcus was a man.  | $\Rightarrow M(\text{Marcus})$  |
| (b) Marcus was a Roman.  | $\Rightarrow R(\text{Marcus})$  |
| (c) All men are people.  | $\Rightarrow \forall x (M(x) \rightarrow P(x))$   |
| (d) Caesar was a ruler.  | $\Rightarrow \text{Ruler}(\text{Caesar})$   |
| (e) All Romans were either loyal to Caesar or hated him (or both). | $\Rightarrow \forall x R(x) \rightarrow \text{Loyal}(x, \text{Caesar}) \vee \text{Hated}(x, \text{Caesar})$ |
| (f) Everyone is loyal to someone.                                  | $\Rightarrow \forall x \exists y \text{Loyal}(x, y)$  |
| (g) People only try to assassinate rulers they are not loyal to.   | $\forall x \Rightarrow \forall x \forall y (\text{Assassinate}(x, y) \rightarrow \neg \text{Loyal}(x, y))$  |
| (h) Marcus tried to assassinate Caesar                             | $\Rightarrow \text{Assassinate}(\text{Marcus}, \text{Caesar})$  |

Now,

Let  $\neg \text{Hated}(\text{Marcus}, \text{Caesar})$

$\text{Loyal}(x, \text{Caesar}) \vee \text{Hated}(x, \text{Caesar})$

$\neg \text{Hated}(\text{Marcus}, \text{Caesar})$

$\text{Loyal}(\text{Marcus}, \text{Caesar})$

$\text{Assassinate}(\text{Marcus}, \text{Caesar}) \rightarrow \neg \text{Assassinate}(\text{Marcus}, \text{Caesar})$

Contradiction

So, Marcus hates Caesar.

Q. Consider the following paragraph:

"anything anyone eats are called food. Milka likes all kind of food. Bread is a food. Mango is a food. Alka eats pizza. Alka eats everything milka eats."

Translate the following sentences into (WFF) in predicate logic and then into set of clauses. Using resolution principle answer the following:

1. Does Milka like pizza?
2. what food Alka eats [Question answering]

1. Anything anyone eats are called food

$\forall x: \forall y: \text{eats}(x, y) \rightarrow \text{food}(y)$

$\forall x: \forall y: \neg \text{eats}(x, y) \vee \text{food}(y)$

$\Rightarrow \neg \text{eats}(x, y) \vee \text{food}(y)$

2. Milka likes all kind of food

$\forall y: \text{Food}(y) \rightarrow \text{like}(\text{Milka}, y)$

$\forall y: \neg \text{Food}(y) \vee \text{like}(\text{Milka}, y)$

$\Rightarrow \neg \text{Food}(y) \vee \text{like}(\text{Milka}, y)$

3. Bread is a food

$\Rightarrow \text{food}(\text{Bread})$

4. Mango is a food

$\Rightarrow \text{food}(\text{Mango})$

5. Alka eats pizza

$\Rightarrow \text{eats}(\text{Alka}, \text{pizza})$

6. Alka eats everything milka eats

$\forall x: \forall y: \text{eats}(\text{Milka}, x) \rightarrow \text{eats}(\text{Alka}, x)$

$\forall x: \forall y: \neg \text{eats}(\text{Milka}, x) \vee \text{eats}(\text{Alka}, x)$

$\Rightarrow \neg \text{eats}(\text{Milka}, x) \vee \text{eats}(\text{Alka}, x)$

i> Does Milka like pizza?

Assume, Milka doesn't like pizza

$\neg \text{like}(\text{Milka}, \text{pizza})$

$\neg \text{like}(\text{Milka}, \text{pizza}) \quad \neg \text{food}(y) \vee \text{like}(\text{Milka}, y)$

$\text{eats}(x, y) \vee \text{food}(y) \quad \neg \text{food}(\text{pizza})$

$\text{eats}(\text{Alka}, \text{pizza}) \quad \neg \text{eats}(x, \text{pizza})$

Failed assumption

Since  $\neg \text{like}(\text{Milka}, \text{pizza})$  is contradiction  
 $\text{like}(\text{Milka}, \text{pizza})$  is true.

2. What food Alka eats

$\exists x: \text{eats}(\text{Alka}, x)$

Assume: Alka doesn't eats anything

$\neg (\exists x_2: \text{eats}(\text{Alka}, x_2))$

$\forall x_2: \neg \text{eats}(\text{Alka}, x_2)$

$\Rightarrow \neg \text{eats}(\text{Alka}, x_2)$

$\neg \text{eats}(\text{Alka}, x_2) \quad \text{eats}(\text{Alka}, \text{pizza})$

Assumption failed

So, Alka eats anything is true, Alka eats pizza.

Q. Consider the following axioms:

1. Every child loves Santa.

Represent these axioms in predicate calculus; skolemize as necessary and convert each formula to clause form. (Note: 'has a red nose' can be a single predicate. Remember to negate the conclusion.) Prove the unsatisfiability of the set of clauses by resolution.

1. Every child loves Santa.

$$\forall x(\text{child}(x) \rightarrow \text{love}(x, \text{Santa})) \Rightarrow \neg \text{child}(x) \vee \text{love}(x, \text{Santa})$$

2. Everyone who loves Santa loves any reindeer.

$$\forall x(\text{love}(x, \text{Santa})) \rightarrow \forall y(\text{reindeer}(y) \rightarrow \text{love}(x, y))$$

$$\Rightarrow \neg \text{love}(x, \text{Santa}) \vee (\neg \text{reindeer}(y) \vee \text{love}(x, y))$$

3. Rudolph is a reindeer, and Rudolph has a red nose.

$$\text{reindeer}(\text{Rudolph}) \wedge \text{rednose}(\text{Rudolph})$$

4. Anything which has a red nose is weird or is a clown.

$$\forall x (\text{rednose}(x) \rightarrow \text{weird}(x) \vee \text{clown}(x)) \quad \neg \text{rednose}(x) \vee (\text{weird}(x) \vee \text{clown}(x))$$

5. No reindeer is a clown.

$$\neg \exists x (\text{reindeer}(x) \wedge \text{clown}(x)) \quad \neg \text{reindeer}(x) \vee \neg \text{clown}(x)$$

6. Scrooge does not love anything which is weird.

$$\forall x (\text{weird}(x) \rightarrow \neg \text{love}(\text{Scrooge}, x)) \quad \neg \text{weird}(x) \vee \neg \text{love}(\text{Scrooge}, x)$$

7. (Conclusion) Scrooge is not a child.

$$\neg \text{child}(\text{Scrooge}) \quad \neg \text{child}(\text{Scrooge})$$

$$\neg \text{child}(x) \vee \text{love}(x, \text{Santa})$$

$$\neg \text{child}(\text{Scrooge})$$

$$\text{So, let: } \neg \text{child}(x) : \text{love}(\text{Scrooge}, \text{Santa})$$

$$\neg \text{love}(x, \text{Santa}) \vee (\neg \text{reindeer}(y) \vee \text{love}(x, y))$$

$$\text{love}(\text{Scrooge}, \text{Santa})$$

$$\neg \text{reindeer}(y) \vee \text{love}(\text{Scrooge}, y)$$

$$\neg \text{reindeer}(x) \vee \text{clown}(x)$$

$$\text{reindeer}(\text{Rudolph})$$

$$\neg \text{clown}(\text{Rudolph})$$

$$\neg \text{weird}(r) \vee \neg \text{love}(\text{Scrooge}, r)$$

$$\text{weird}(\text{Rudolph})$$

$$\neg \text{love}(\text{Scrooge}, \text{Rudolph})$$

$$\neg \text{clown}(\text{Rudolph})$$

$$\neg \text{love}(\text{Scrooge}, \text{Rudolph})$$

$$\neg \text{clown}(\text{Rudolph})$$

Contradiction

Hence, The set of clauses are unsatisfied.