Programming Assignment 1: Learning Distributed Word Representations

Version: 1.2

Changes by Version:

- (v1.1)
 - 1. Part 1 Description: indicated that each word is associated with two embedding vectors and two biases
 - 2. Part 1: Updated calculate log co occurence to include the last pair of consecutive words as well
 - 3. Part 2: Updated question description for 2.1
 - 4. Part 4: Updated answer requirement for 4.1
 - 5. (1.3) Fixed symmetric GLoVE gradient
 - 6. (1.3) Clarified that W_tilde and b_tilde gradients also need to be implemented
 - 7. (2) Removed extra space leading up to docstring for compute loss derivative
- (v1.2)
 - 1. (1.4) Updated the training function train_GLoVE to not use inplace update (e.g. W = W learning_rate * grad_W instead), so the initial weight variables are not overwritten between asymmetric and symmetric GLoVE models.
 - 2. (2) Noted that compute_loss_derivative input argument target_mask is 3D tensor with shape [batch_size x context len x 1]

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Due Date: Thursday, Feb. 4, at 11:59pm

Based on an assignment by George Dahl

For CSC413/2516 in Winter 2021 with Professor Jimmy Ba and Professor Bo Wang

Submission: You must submit two files through MarkUs:

- 1. [] A PDF file containing your writeup, titled *a1-writeup.pdf*, which will be the PDF export of this notebook (i.e., by printing this notebook webpage as PDF). Your writeup must be typed. There will be sections in the notebook for you to write your responses. Make sure that the relevant outputs (e.g. print gradients() outputs, plots, etc.) are included and clearly visible.
- 2. [] This al-code.ipynb iPython Notebook.

The programming assignments are individual work. See the Course Syllabus for detailed policies.

You should attempt all questions for this assignment. Most of them can be answered at least partially even if you were unable to finish earlier questions. If you think your computational results are incorrect, please say so; that may help you get partial credit.

The teaching assistants for this assignment are Harris Chan and Summer Tao. Send your email with subject "[CSC413] PA1" to mailto:csc413-2021-01-tas@cs.toronto.edu or post on Piazza with the tag pa1.

Introduction

In this assignment we will learn about word embeddings and make neural networks learn about words. We could try to match statistics about the words, or we could train a network that takes a sequence of words as input and learns to predict the word that comes next.

This assignment will ask you to implement a linear embedding and then the backpropagation computations for a neural language model and then run some experiments to analyze the learned representation. The amount of code you have to write is very short but each line will require you to think very carefully. You will need to derive the updates mathematically, and then implement them using matrix and vector operations in NumPy.

Starter code and data

First, perform the required imports for your code:

```
In [2]:
```

```
import collections
import pickle
import numpy as np
import os
```

```
from tqdm import tqdm
import pylab
from six.moves.urllib.request import urlretrieve
import tarfile
import sys

TINY = 1e-30
EPS = 1e-4
nax = np.newaxis
```

If you're using colaboratory, this following script creates a folder - here we used 'CSC413/A1' - in order to download and store the data. If you're not using colaboratory, then set the path to wherever you want the contents to be stored at locally.

You can also manually download and unzip the data from [http://www.cs.toronto.edu/~jba/a1_data.tar.gz] and put them in the same folder as where you store this notebook.

Feel free to use a different way to access the files data.pk, partially_trained.pk, and raw_sentences.txt.

The file *raw_sentences.txt* contains the sentences that we will be using for this assignment. These sentences are fairly simple ones and cover a vocabulary of only 250 words (+ 1 special [MASK] token word).

```
In [3]:
```

```
*******************************
# Setup working directory
# Change this to a local path if running locally
%mkdir -p /content/CSC413/A1/
%cd /content/CSC413/A1
# Helper functions for loading data
# adapted from
# https://github.com/fchollet/keras/blob/master/keras/datasets/cifar10.py
def get_file(fname,
          origin,
          untar=False,
          extract=False,
          archive_format='auto',
          cache dir='data'):
   datadir = os.path.join(cache dir)
   if not os.path.exists(datadir):
      os.makedirs(datadir)
      untar fpath = os.path.join(datadir, fname)
      fpath = untar fpath + '.tar.gz'
   else:
      fpath = os.path.join(datadir, fname)
   print('File path: %s' % fpath)
   if not os.path.exists(fpath):
      print('Downloading data from', origin)
      error msg = 'URL fetch failure on {}: {} -- {}'
      try:
         try:
             urlretrieve (origin, fpath)
          except URLError as e:
             raise Exception(error msg.format(origin, e.errno, e.reason))
          except HTTPError as e:
             raise Exception(error_msg.format(origin, e.code, e.msg))
      except (Exception, KeyboardInterrupt) as e:
         if os.path.exists(fpath):
             os.remove(fpath)
          raise
   if untar:
      if not os.path.exists(untar fpath):
          print('Extracting file.')
          with tarfile.open(fpath) as archive:
             archive.extractall(datadir)
      {\tt return} \ {\tt untar\_fpath}
      _extract_archive(fpath, datadir, archive_format)
   return fpath
      . /--------
```

```
In [4]:
```

```
File path: data/al_data.tar.gz
Downloading data from http://www.cs.toronto.edu/~jba/al_data.tar.gz
Extracting file.
```

We have already extracted the 4-grams from this dataset and divided them into training, validation, and test sets. To inspect this data, run the following:

```
In [5]:
```

```
data = pickle.load(open(data location, 'rb'))
 print(data['vocab'][0]) # First word in vocab is [MASK]
print(data['vocab'][1])
 print(len(data['vocab'])) # Number of words in vocab
 print(data['vocab']) # All the words in vocab
print(data['train inputs'][:10]) # 10 example training instances
 [MASK]
all
251
 ['[MASK]', 'all', 'set', 'just', 'show', 'being', 'money', 'over', 'both', 'years', 'four', 'through', 'du
ring', 'go', 'still', 'children', 'before', 'police', 'office', 'million', 'also', 'less', 'had', ',', 'in cluding', 'should', 'to', 'only', 'going', 'under', 'has', 'might', 'do', 'them', 'good', 'around', 'get',
 'very', 'big', 'dr.', 'game', 'every', 'know', 'they', 'not', 'world', 'now', 'him', 'school', 'several',
'like', 'did', 'university', 'companies', 'these', 'she', 'team', 'found', 'where', 'right', 'says', 'people', 'house', 'national', 'some', 'back', 'see', 'street', 'are', 'year', 'home', 'best', 'out', 'even', 'what', 'said', 'for', 'federal', 'since', 'its', 'may', 'state', 'does', 'john', 'between', 'new', ';', 'three', 'public', '?', 'be', 'we', 'after', 'business', 'never', 'use', 'here', 'york', 'members', 'percent', 'put', 'group', 'come', 'by', '$', 'on', 'about', 'last', 'her', 'of', 'could', 'days', 'against', 'time's', 'women', 'place', 'think', 'first', 'among', 'own', 'family', 'into', 'each', 'one', 'down', 'because'
   'long', 'another', 'such', 'old', 'next', 'your', 'market', 'second', 'city', 'little', 'from', 'would',
 'few', 'west', 'there', 'political', 'two', 'been', '.', 'their', 'much', 'music', 'too', 'way', 'white', ':', 'was', 'war', 'today', 'more', 'ago', 'life', 'that', 'season', 'company', '-', 'but', 'part', 'court
', 'dat', 'botton', 'general', 'with', 'than', 'those', 'he', 'me', 'high', 'made', 'this', 'work', 'up', 'us', 'until', 'will', 'ms.', 'while', 'officials', 'can', 'were', 'country', 'my', 'called', 'and', 'program', 'have', 'then', 'is', 'it', 'an', 'states', 'case', 'say', 'his', 'at', 'want', 'in', 'any', 'as', 'if', 'united', 'end', 'no', ')', 'make', 'government', 'when', 'american', 'same', 'how', 'mr.', 'other', 'take',
'which', 'department', '--', 'you', 'many', 'nt', 'day', 'week', 'play', 'used', "'s", 'though', 'our', 'w ho', 'yesterday', 'director', 'most', 'president', 'law', 'man', 'a', 'night', 'off', 'center', 'i', 'well
 ', 'or', 'without', 'so', 'time', 'five', 'the', 'left']
 [[ 28  26  90  144]
   [184 44 249 117]
  [183 32 76 122]
   [117 247 201 186]
   [223 190 249
                            61
   [ 42 74 26
  [242 32 223 32]
  [223 32 158 144]
   [ 74 32 221 32]
  [ 42 192 91 68]]
```

Now data is a Python dict which contains the vocabulary, as well as the inputs and targets for all three splits of the data.

data['vocab'] is a list of the 251 words in the dictionary; data['vocab'][0] is the word with index 0, and so on.

data['train_inputs'] is a 372,500 x 4 matrix where each row gives the indices of the 4 consecutive context words for one of the 372,500 training cases. The validation and test sets are handled analogously.

Even though you only have to modify two specific locations in the code, you may want to read through this code before starting the assignment.

Part 1: GLoVE Word Representations (2pts)

In this part of the assignment, you will implement a simplified version of the GLoVE embedding (please see the handout for detailed description of the algorithm) with the loss defined as

$$L(\{\mathbf{w}_{i}, \tilde{\mathbf{w}}_{i}, b_{i}, \tilde{b}_{i}\}_{i=1}^{V}) = \sum_{i,j=1}^{V} (\mathbf{w}_{i}^{\top} \tilde{\mathbf{w}}_{i} + b_{i} + \tilde{b}_{i} - \log X_{ii})^{2}$$

Note that each word is represented by two d-dimensional embedding vectors \mathbf{w}_i , $\tilde{\mathbf{w}}_i$ and two scalar biases b_i , \hat{b}_i .

Answer the following questions:

1.1. GLoVE Parameter Count [0pt]

Given the vocabulary size V and embedding dimensionality d, how many parameters does the GLoVE model have? Note that each word in the vocabulary is associated with 2 embedding vectors and 2 biases.

1.1 Answer: **TODO: Write Part 1.2 answer here**

1.2. Expression for gradient $\overline{\partial \mathbf{w}_i}$ [1pt]

Write the expression for ∂w_i , the gradient of the loss function L with respect to one parameter vector \mathbf{w}_i . The gradient should be a function of $\mathbf{w}, \tilde{\mathbf{w}}, b, b, X$ with appropriate subscripts (if any).

1.2 Answer: The gradient $\frac{\partial L}{\partial \mathbf{w}_i}$ is: $\sqrt{\frac{\partial L}{\partial \mathbf{w}_i}} = 2(\mathbf{w}_i \tilde{\mathbf{w}}_j + b_i + \tilde{b}_j - log X_{ij}) \tilde{\mathbf{w}}_j$

1.3. Implement the gradient update of GLoVE. [1pt]

See YOUR CODE HERE Comment below for where to complete the code

We have provided a few functions for training the embedding:

- calculate log co occurence computes the log co-occurrence matrix of a given corpus
- train GLoVE runs momentum gradient descent to optimize the embedding
- loss GLoVE:
 - INPUT $V \times d$ matrix W (collection of V embedding vectors, each d-dimensional); $V \times d$ matrix W tilde; $V \times 1$ vector D(collection of V bias terms); $V \times 1$ vector b tilde; $V \times V$ log co-occurrence matrix.
 - OUTPUT loss of the GLoVE objective
- grad GLoVE: TO BE IMPLEMENTED.
 - INPUT:
 - o $V \times d$ matrix W (collection of V embedding vectors, each d-dimensional), embedding for first word;
 - o $V \times d$ matrix W tilde, embedding for second word;
 - o $V \times 1$ vector b (collection of V bias terms);
 - o $V \times 1$ vector b tilde, bias for second word;
 - \circ $V \times V \log$ co-occurrence matrix.
 - OUTPUT:
 - $V \times d$ matrix grad W containing the gradient of the loss function w.r.t. W;
 - o $V \times d$ matrix $grad_{W_tilde}$ containing the gradient of the loss function w.r.t. W_tilde ;
 - o $V \times 1$ vector grad b which is the gradient of the loss function w.r.t. b.
 - o $V \times 1$ vector grad b tilde which is the gradient of the loss function w.r.t. b tilde.

Run the code to compute the co-occurence matrix. Make sure to add a 1 to the occurences, so there are no 0's in the matrix when we take the elementwise log of the matrix.

```
In [7]:
vocab size = len(data['vocab']) # Number of vocabs
def calculate_log_co_occurence(word data, symmetric=False):
  "Compute the log-co-occurence matrix for our data."
```

```
log_co_occurence = np.zeros((vocab_size, vocab_size))
for input in word data:
  # Note: the co-occurence matrix may not be symmetric
 log co occurence[input[0], input[1]] += 1
```

log_co_occurence[input[1], input[2]] += 1 log_co_occurence[input[2], input[3]] += 1

If we want symmetric co-occurence can also increment for these.

if symmetric:

```
log_co_occurence[input[1], input[0]] += 1
log_co_occurence[input[2], input[1]] += 1
log_co_occurence[input[3], input[2]] += 1
delta_smoothing = 0.5  # A hyperparameter. You can play with this if you want.
log_co_occurence += delta_smoothing  # Add delta so log doesn't break on 0's.
log_co_occurence = np.log(log_co_occurence)
return log_co_occurence
```

```
In [8]:
```

```
asym_log_co_occurence_train = calculate_log_co_occurence(data['train_inputs'], symmetric=False)
asym_log_co_occurence_valid = calculate_log_co_occurence(data['valid_inputs'], symmetric=False)
```

• [] TO BE IMPLEMENTED: Calculate the gradient of the loss function w.r.t. the parameters W, \hat{W} , b, and b. You should vectorize the computation, i.e. not loop over every word.

```
In [9]:
\label{eq:condition} \mbox{def loss\_GLoVE} \mbox{($W$, $W$\_tilde, b, b\_tilde, log\_co\_occurence):}
 "Compute the GLoVE loss."
 n_{,-} = log_co_occurence.shape
 if W tilde is None and b_tilde is None:
   return np.sum((W @ W.T + b @ np.ones([1,n]) + np.ones([n,1])@b.T - log co occurence)**2)
 else:
   return np.sum((W @ W_tilde.T + b @ np.ones([1,n]) + np.ones([n,1])@b_tilde.T - log_co_occurence)**2)
def grad GLoVE(W, W tilde, b, b tilde, log co occurence):
 "Return the gradient of GLoVE objective w.r.t W and b."
  "INPUT: W - Vxd; W tilde - Vxd; b - Vx1; b tilde - Vx1; log co occurence: VxV"
 "OUTPUT: grad W - Vxd; grad W tilde - Vxd, grad b - Vx1, grad b tilde - Vx1"
 n,_ = log_co_occurence.shape
 if not W tilde is None and not b tilde is None:
  grad_W = 2*(W @ W_tilde.T + b @ np.ones([1,n]) + np.ones([n,1])@b_tilde.T - log_co_occurence)@W_tild
   grad_W_tilde = 2*(W @ W_tilde.T + b @ np.ones([1,n]) + np.ones([n,1])@b_tilde.T - log_co_occurence)@
W
   s([n,1])
   grad b tilde = 2*(W @ W tilde.T + b @ np.ones([1,n]) + np.ones([n,1])@b tilde.T - log co occurence)@
np.ones([n,1])
  *****************
 else:
   loss = (\texttt{W @ W.T + b @ np.ones([1,n]) + np.ones([n,1])@b.T - 0.5*(log co occurence + log co occurence)})
.T))
   grad W = 4 * (W.T @ loss).T
   grad W tilde = None
   grad b = 4 * (np.ones([1,n]) @ loss).T
   grad b tilde = None
 return grad W, grad W tilde, grad b, grad b tilde
def train GLoVE(W, W tilde, b, b tilde, log co occurence train, log co occurence valid, n epochs, do prin
t=False):
 "Traing W and b according to GLoVE objective."
 n,_ = log_co_occurence_train.shape
 learning_rate = 0.05 / n # A hyperparameter. You can play with this if you want.
 for epoch in range(n_epochs):
   grad_W, grad_W_tilde, grad_b, grad_b_tilde = grad_GLoVE(W, W_tilde, b, b_tilde, log_co_occurence_trai
n)
   W = W - learning_rate * grad_W
   b = b - learning rate * grad b
   if not grad W tilde is None and not grad b tilde is None:
     W_tilde = W_tilde - learning_rate * grad_W_tilde
     b_tilde = b_tilde - learning_rate * grad_b_tilde
   train_loss, valid_loss = loss_GLoVE(W, W_tilde, b, b_tilde, log_co_occurence_train), loss_GLoVE(W, W_
tilde, b, b_tilde, log_co_occurence_valid)
   if do_print:
     print(f"Train Loss: {train loss}, valid loss: {valid loss}, grad norm: {np.sum(grad W**2)}")
 return W, W_tilde, b, b_tilde, train_loss, valid loss
```

1.4. Effect of embedding dimension d [Opt]

Train the both the symmetric and asymmetric GLoVe model with varying dimensionality d by running the cell below. Comment on:

- 1. Which d leads to optimal validation performance for the asymmetric and symmetric models?
- 2. Why does / doesn't larger d always lead to better validation error?

2. Willy does 7 does it larger a diways lead to be

1.4 Answer: **TODO: Write Part 1.4 answer here**

Train the GLoVE model for a range of embedding dimensions

```
In [10]:
```

```
np.random.seed(1)
n_epochs = 500 # A hyperparameter. You can play with this if you want.
embedding_dims = np.array([1, 2, 10, 128, 256])  # Play with this
# Store the final losses for graphing
asymModel_asymCoOc_final_train_losses, asymModel_asymCoOc_final_val_losses = [], []
symModel asymCoOc final train losses, symModel asymCoOc final val losses = [], []
Asym W final 2d, Asym b final 2d, Asym W tilde final 2d, Asym b tilde final 2d = None, None, None
W_final_2d, b final 2d = None, None
do print = False # If you want to see diagnostic information during training
for embedding_dim in tqdm(embedding_dims):
 init_variance = 0.1 # A hyperparameter. You can play with this if you want.
  W = init variance * np.random.normal(size=(vocab size, embedding dim))
 W_tilde = init_variance * np.random.normal(size=(vocab_size, embedding_dim))
 b = init variance * np.random.normal(size=(vocab size, 1))
 b tilde = init variance * np.random.normal(size=(vocab size, 1))
 if do print:
    print(f"Training for embedding dimension: {embedding dim}")
  # Train Asym model on Asym Co-Oc matrix
  Asym W final, Asym W tilde final, Asym b final, Asym b tilde final, train loss, valid loss = train GLoV
E(W, W_tilde, b, b_tilde, asym_log_co_occurence_train, asym_log_co_occurence_valid, n_epochs, do_print=do
_print)
 if embedding dim == 2:
    # Save a parameter copy if we are training 2d embedding for visualization later
   Asym W final 2d = Asym W final
   Asym_W_tilde_final_2d = Asym_W_tilde_final
   Asym_b_final_2d = Asym_b_final
   Asym b tilde final 2d = Asym b tilde final
  asymModel_asymCoOc_final_train_losses += [train_loss]
  asymModel asymCoOc final val losses += [valid loss]
  if do print:
   print(f"Final validation loss: {valid loss}")
  # Train Sym model on Asym Co-Oc matrix
  W_final, W_tilde_final, b_final, b_tilde_final, train_loss, valid_loss = train_GLoVE(W, None, b, None,
asym_log_co_occurence_train, asym_log_co_occurence_valid, n_epochs, do_print=do_print)
  if embedding dim == 2:
    # Save a parameter copy if we are training 2d embedding for visualization later
   W final 2d = W final
   b final 2d = b final
  symModel_asymCoOc_final_train_losses += [train loss]
  symModel_asymCoOc_final_val_losses += [valid loss]
  if do print:
    print(f"Final validation loss: {valid loss}")
100%| 5/5 [00:43<00:00, 8.62s/it]
```

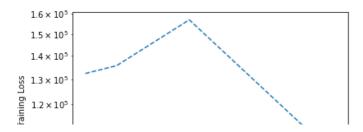
Plot the training and validation losses against the embedding dimension.

```
In [11]:
```

```
pylab.loglog(embedding_dims, asymModel_asymCoOc_final_train_losses, label="Asymmetric Model / Asymmetric
Co-Oc", linestyle="--")
pylab.loglog(embedding_dims, symModel_asymCoOc_final_train_losses, label="Symmetric Model / Asymmetric C
o-Oc")
pylab.xlabel("Embedding Dimension")
pylab.ylabel("Training Loss")
pylab.legend()
```

Out[11]:

<matplotlib.legend.Legend at 0x7f7a227789b0>



```
1.1 × 10<sup>3</sup>

10<sup>3</sup>

--- Asymmetric Model / Asymmetric Co-Oc
Symmetric Model / Asymmetric Co-Oc

10<sup>9</sup>

10<sup>1</sup>

10<sup>2</sup>

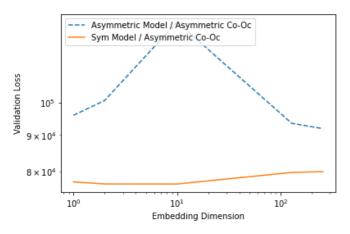
Embedding Dimension
```

In [12]:

```
pylab.loglog(embedding_dims, asymModel_asymCoOc_final_val_losses, label="Asymmetric Model / Asymmetric Co
-Oc", linestyle="--")
pylab.loglog(embedding_dims, symModel_asymCoOc_final_val_losses, label="Sym Model / Asymmetric Co-Oc")
pylab.xlabel("Embedding Dimension")
pylab.ylabel("Validation Loss")
pylab.legend(loc="upper left")
```

Out[12]:

<matplotlib.legend.Legend at 0x7f7a220f4c50>



Part 2: Network Architecture (2pts)

See the handout for the written questions in this part.

Answer the following questions

2.1. Number of parameters in neural network model [1pt]

Assume in general that we have V words in the dictionary and use the previous N words as inputs. Suppose we use a D-dimensional word embedding and a hidden layer with H hidden units. The trainable parameters of the model consist of 3 weight matrices and 2 sets of biases. What is the total number of trainable parameters in the model, as a function of V, V, D, F?

In the diagram given, which part of the model (i.e., <code>word_embbeding_weights</code>, <code>embed_to_hid_weights</code>, <code>hid_to_output_weights</code>, <code>hid_bias</code>, or <code>output_bias</code>) has the largest number of trainable parameters if we have the constraint that $V \ll H > D > N$? Note: The symbol <code>« means ``much greater than" Explain your reasoning.</code>

2.1 Answer: Number of parameters for each of the weight matrices and the 2 sets of biases are as follows: \ -> For word_embbeding_weights: VD parameters \ -> For embed_to_hid_weights: HND parameters \ -> For hid_to_output_weights: H parameters \ -> For output_bias: 1 parameter \

Total number of parameters to be learnt = VD + HND + 2H + 1

if we have the constraint that $V \ll H > D > N$, then, word_embedding_weights will have largest number of training parameters as word_embedding_weights is a $V \times D$ matrix, which tells us there are VD parameters to learn; comparing this to embed_to_hid_weights which has HND parameters to learn, we can see that VD > HND as V >> H > N, which implies V = V is 'much' larger than V = V is 'very' large and therfore, word_embedding_weights has largest number of trainable parameters when $V \ll H > D > N$

2.2 Number of parameters in n-gram model [1pt]

Another method for predicting the next words is an n-gram model, which was mentioned in Lecture 3. If we wanted to use an n-gram model with the same context length N as our network, we'd need to store the counts of all possible (N+1)-grams. If we stored all the counts explicitly, how many entries would this table have?

2.3. Comparing neural network and n-gram model scaling [0pt]

How do the parameters in the neural network model scale with the number of context words N versus how the number of entries in the n-gram model scale with N? [0pt]

2.3 Answer: **TODO: Write Part 2.3 answer here**

Part 3: Training the model (3pts)

We will modify the architecture slightly from the previous section, inspired by BERT \citep{devlin2018bert}. Instead of having only one output, the architecture will now take in N=4 context words, and also output predictions for N=4 words. See Figure 2 diagram in the handout for the diagram of this architecture.

During training, we randomly sample one of the N context words to replace with a <code>[MASK]</code> token. The goal is for the network to predict the word that was masked, at the corresponding output word position. In practice, this <code>[MASK]</code> token is assigned the index 0 in our dictionary. The weights $W^{(2)} = \text{hid_to_output_weights}$ now has the shape $NV \times H$, as the output layer has NV neurons, where the first V output units are for predicting the first word, then the next V are for predicting the second word, and so on. We call this as C output units across all word positions, i.e. the (j+nV)-th column is for the word j in vocabulary for the N-th output word position. Note here that the softmax is applied in chunks of N as well, to give a valid probability distribution over the N words. Only the output word positions that were masked in the input are included in the cross entropy loss calculation:

There are three classes defined in this part: Params, Activations, Model. You will make changes to Model, but it may help to read through Params and Activations first.

$$C = -\sum_{i}^{B} \sum_{n}^{N} \sum_{j}^{V} m_{n}^{(i)}(t_{n,j}^{(i)} \log y_{n,j}^{(i)}),$$

Where $y_{n,j}^{(i)}$ denotes the output probability prediction from the neural network for the i-th training example for the word j in the n-th output word, and $t_{n,j}^{(i)}$ is 1 if for the i-th training example, the word j is the n-th word in context. Finally, $m_n^{(i)} \in \{0,1\}$ is a mask that is set to 1 if we are predicting the n-th word position for the i-th example (because we had masked that word in the input), and 0 otherwise.

There are three classes defined in this part: Params , Activations , Model . You will make changes to Model , but it may help to read through Params and Activations first.

```
In [13]:
```

```
class Params (object):
    """A class representing the trainable parameters of the model. This class has five fields:
           word embedding weights, a matrix of size V x D, where V is the number of words in the vocabula
rv
                   and D is the embedding dimension.
           embed to hid weights, a matrix of size H x ND, where H is the number of hidden units. The first
                  columns represent connections from the embedding of the first context word, the next D
columns
                  for the second context word, and so on. There are N context words.
          hid bias, a vector of length H
          hid_to_output_weights, a matrix of size NV x H
          output bias, a vector of length NV"""
   def __init__(self, word_embedding_weights, embed_to_hid_weights, hid_to_output_weights,
                hid bias, output bias):
        self.word embedding weights = word embedding weights
        self.embed to hid weights = embed to hid weights
        self.hid to output weights = hid to output weights
        self.hid bias = hid bias
        self.output bias = output bias
    def copy(self):
        return self.__class__(self.word_embedding_weights.copy(), self.embed to hid weights.copy(),
                             self.hid to output weights.copy(), self.hid bias.copy(), self.output bias.
copy())
   @classmethod
    def zeros(cls, vocab size, context len, embedding dim, num hid):
        """A constructor which initializes all weights and biases to 0."""
```

```
word embedding weights = np.zeros((vocab_size, embedding_dim))
       embed to hid weights = np.zeros((num hid, context len * embedding dim))
       hid to output_weights = np.zeros((vocab_size * context_len, num_hid))
       hid bias = np.zeros(num hid)
       output bias = np.zeros(vocab size * context len)
       return cls(word embedding weights, embed to hid weights, hid to output weights,
                  hid bias, output bias)
   @classmethod
   def random_init(cls, init_wt, vocab_size, context_len, embedding_dim, num_hid):
        """A constructor which initializes weights to small random values and biases to 0."""
       word_embedding_weights = np.random.normal(0., init_wt, size=(vocab_size, embedding_dim))
       embed_to_hid_weights = np.random.normal(0., init_wt, size=(num_hid, context_len * embedding_dim)
       hid to output weights = np.random.normal(0., init wt, size=(vocab size * context len, num hid))
       hid bias = np.zeros(num hid)
       output bias = np.zeros(vocab size * context len)
       return cls(word embedding weights, embed to hid weights, hid to output weights,
                  hid bias, output bias)
   ###### The functions below are Python's somewhat oddball way of overloading operators, so that
    ###### we can do arithmetic on Params instances. You don't need to understand this to do the assignme
nt.
   def _mul__(self, a):
       return self. class (a * self.word embedding weights,
                             a * self.embed to hid weights,
                             a * self.hid to output weights,
                             a * self.hid bias,
                             a * self.output_bias)
   def __rmul__(self, a):
       return self * a
   def add (self, other):
       return self.__class__(self.word_embedding_weights + other.word_embedding_weights,
                             self.embed_to_hid_weights + other.embed_to_hid_weights,
                             self.hid to output weights + other.hid to output weights,
                             self.hid bias + other.hid bias,
                             self.output bias + other.output bias)
   def sub (self, other):
       return self + -1. * other
```

In [14]:

```
class Activations(object):
    """A class representing the activations of the units in the network. This class has three fields:
        embedding layer, a matrix of B x ND matrix (where B is the batch size, D is the embedding dimensio
n,
                and N is the number of input context words), representing the activations for the embeddi
ng
                layer on all the cases in a batch. The first D columns represent the embeddings for the
                first context word, and so on.
        hidden_layer, a B x H matrix representing the hidden layer activations for a batch
        output_layer, a B x V matrix representing the output layer activations for a batch"""
   def __init__(self, embedding_layer, hidden_layer, output_layer):
        self.embedding layer = embedding layer
        self.hidden_layer = hidden_layer
        self.output layer = output layer
def get batches(inputs, batch size, shuffle=True):
    """Divide a dataset (usually the training set) into mini-batches of a given size. This is a
    'generator', i.e. something you can use in a for loop. You don't need to understand how it
    works to do the assignment."""
    if inputs.shape[0] % batch size != 0:
        raise RuntimeError('The number of data points must be a multiple of the batch size.')
    num batches = inputs.shape[0] // batch size
    if shuffle:
        idxs = np.random.permutation(inputs.shape[0])
        inputs = inputs[idxs, :]
    for m in range(num_batches):
        yield inputs[m * batch size:(m + 1) * batch size, :]
```

- compute activations computes the activations of all units on a given input batch
 - compute loss computes the total cross-entropy loss on a mini-batch
 - evaluate computes the average cross-entropy loss for a given set of inputs and targets

You will need to complete the implementation of two additional methods which are needed for training, and print the outputs of the gradients.

3.1 Implement gradient with respect to output layer inputs [1pt]

compute_loss_derivative computes the derivative of the loss function with respect to the output layer inputs.

In other words, if C is the cost function, and the softmax computation for the j-th word in vocabulary for the n-th output word position is:

$$y_{n,j} = \frac{e^{z_{n,j}}}{\sum_{l} e^{z_{n,l}}}$$

This function should compute a $B \times NV$ matrix where the entries correspond to the partial derivatives $\partial C/\partial z_j^n$. Recall that the output units are concatenated across all positions, i.e. the (j + nV)-th column is for the word j in vocabulary for the n-th output word position.

3.2 Implement gradient with respect to parameters [1pt]

and initializes the biases to all zeros."""

and we set the entry to be 0.

def indicator_matrix(self, targets, mask_zero_index=True):

for example i is k, and all other entries are 0.

return Model (params, vocab)

In [38]:

class Model(object):

back_propagate is the function which computes the gradient of the loss with respect to model parameters using backpropagation. It uses the derivatives computed by *compute_loss_derivative*. Some parts are already filled in for you, but you need to compute the matrices of derivatives for <code>embed_to_hid_weights</code>, <code>hid_bias</code>, <code>hid_to_output_weights</code>, and <code>output_bias</code>. These matrices have the same sizes as the parameter matrices (see previous section).

In order to implement backpropagation efficiently, you need to express the computations in terms of matrix operations, rather than *for* loops. You should first work through the derivatives on pencil and paper. First, apply the chain rule to compute the derivatives with respect to individual units, weights, and biases. Next, take the formulas you've derived, and express them in matrix form. You should be able to express all of the required computations using only matrix multiplication, matrix transpose, and elementwise operations --- no *for* loops! If you want inspiration, read through the code for *Model.compute_activations* and try to understand how the matrix operations correspond to the computations performed by all the units in the network.

To make your life easier, we have provided the routine <code>checking.check_gradients</code>, which checks your gradients using finite differences. You should make sure this check passes before continuing with the assignment.

```
"""A class representing the language model itself. This class contains various methods used in trainin
the model and visualizing the learned representations. It has two fields:
   params, a Params instance which contains the model parameters
   vocab, a list containing all the words in the dictionary; vocab[0] is the word with index
           0, and so on."""
def init (self, params, vocab):
    self.params = params
    self.vocab = vocab
   self.vocab size = len(vocab)
    self.embedding dim = self.params.word embedding weights.shape[1]
    self.embedding_layer_dim = self.params.embed_to_hid_weights.shape[1]
    self.context len = self.embedding layer dim // self.embedding dim
    self.num_hid = self.params.embed_to_hid_weights.shape[0]
def copy(self):
   return self. class (self.params.copy(), self.vocab[:])
@classmethod
def random init(cls, init wt, vocab, context len, embedding dim, num hid):
    """Constructor which randomly initializes the weights to Gaussians with standard deviation init_wt
```

params = Params.random init(init wt, len(vocab), context len, embedding dim, num hid)

"""Construct a matrix where the (k + j*V)th entry of row i is 1 if the j-th target word

Note: if the j-th target word index is 0, this corresponds to the [MASK] token,

```
batch size, context len = targets.shape
        expanded targets = np.zeros((batch size, context len * len(self.vocab)))
        targets offset = np.repeat((np.arange(context len) * len(self.vocab))[np.newaxis, :], batch size
, axis=0) # [[0, V, 2V], [0, V, 2V], ...]
        targets += targets offset
        for c in range(context len):
          expanded_targets[np.arange(batch_size), targets[:,c]] = 1.
          if mask zero index:
            # Note: Set the targets with index 0, V, 2V to be zero since it corresponds to the [MASK] tok
en
           expanded targets[np.arange(batch size), targets offset[:,c]] = 0.
        return expanded targets
   def compute loss derivative (self, output activations, expanded target batch, target mask):
        """Compute the derivative of the multiple target position cross-entropy loss function \n"
            For example:
          [y_{\{0\}} \dots y_{\{V-1\}}] [y_{\{0\}}, \dots, y_{\{2*V-1\}}] [y_{\{2*V\}} \dots y_{\{i,3*V-1\}}] [y_{\{3*V\}} \dots y_{\{i,4*V-1\}}] 
         Where for colum j + n*V,
           y \{j + n*V\} = e^{z} \{j + n*V\} / \sum_{m=0}^{V-1} e^{z} \{m + n*V\}, \text{ for } n=0,...,N-1\}
        This function should return a dC / dz matrix of size [batch size x (vocab size * context len)],
        where each row i in dC / dz has columns 0 to V-1 containing the gradient the 1st output
        context word from i-th training example, then columns vocab_size to 2*vocab_size - 1 for the 2nd
        output context word of the i-th training example, etc.
        C is the loss function summed acrossed all examples as well:
            C = -\{sum\ \{i,j,n\}\ mask\ \{i,n\}\ (t\ \{i,\ j+n*V\}\ log\ y\ \{i,\ j+n*V\}),\ for\ j=0,...,V,\ and\ n=0,...,N
        where mask {i,n} = 1 if the i-th training example has n-th context word as the target,
        otherwise mask \{i,n\} = 0.
        The arguments are as follows:
            output_activations - A [batch_size x (context_len * vocab_size)] tensor,
                for the activations of the output layer, i.e. the y_j's.
            expanded_target_batch - A [batch_size (context_len * vocab_size)] tensor,
                where expanded\_target\_batch[i,n*V:(n+1)*V] is the indicator vector for
                the n-th context target word position, i.e. the (i, j + n*V) entry is 1 if the
                i'th example, the context word at position n is j, and 0 otherwise.
            target\ mask - A [batch size x context len x 1] tensor, where target\ mask[i,n] = 1
               if for the i'th example the n-th context word is a target position, otherwise 0
        Outputs:
            loss derivative - A [batch size x (context len * vocab size)] matrix,
                where loss derivative[i,0:vocab size] contains the gradient
                d\mathcal{C} / dz_0 for the i-th training example gradient for 1st output
                context\ word,\ and\ loss\_derivative [\textit{i,vocab\_size:2*vocab\_size}]\ for
                the 2nd output context word of the i-th training example, etc.
                                     ############################
        batch_size, N, _ = target_mask.shape
        V = self.vocab size
       dy t1 = (output activations[:,:, np.newaxis] - np.eye(N*V))
        \label{eq:mat_of_mat} \mbox{id\_mat\_of\_mat} = \mbox{np.repeat(np.eye(N), V, axis = 0), V, axis = 1)}
        dy = dy_t1 * id_mat_of_mat
       indicator mat gt = (expanded target batch * np.repeat(target mask.squeeze(), V, axis = 1))[:,:,
np.newaxis]
        loss_derivative_pre = np.matmul(dy, indicator_mat_gt)
        loss derivative = loss derivative pre.squeeze()
        return loss derivative
        def compute loss(self, output activations, expanded target batch):
        """Compute the total loss over a mini-batch. expanded_target_batch is the matrix obtained
        by calling indicator_matrix on the targets for the batch."""
        return -np.sum(expanded_target_batch * np.log(output_activations + TINY))
   def compute activations(self, inputs):
        """Compute the activations on a batch given the inputs. Returns an Activations instance.
        You should try to read and understand this function, since this will give you clues for
```

```
how to implement back propagate."""
       batch size = inputs.shape[0]
       if inputs.shape[1] != self.context len:
           raise RuntimeError('Dimension of the input vectors should be {}, but is instead {}'.format(
               self.context len, inputs.shape[1]))
       # Embedding layer
        # Look up the input word indies in the word_embedding_weights matrix
       embedding layer state = np.zeros((batch size, self.embedding layer dim))
       for i in range(self.context len):
           embedding layer state[:, i * self.embedding dim:(i + 1) * self.embedding dim] = \setminus
               self.params.word_embedding_weights[inputs[:, i], :]
        # Hidden layer
       inputs to hid = np.dot(embedding layer state, self.params.embed to hid weights.T) + \setminus
                       self.params.hid bias
        # Apply logistic activation function
       hidden_layer_state = 1. / (1. + np.exp(-inputs_to_hid))
        # Output layer
       inputs to softmax = np.dot(hidden layer state, self.params.hid to output weights.T) + \
                           self.params.output bias
       # Subtract maximum.
        # Remember that adding or subtracting the same constant from each input to a
        # softmax unit does not affect the outputs. So subtract the maximum to
        # make all inputs <= 0. This prevents overflows when computing their exponents.
       inputs to softmax -= inputs to softmax.max(1).reshape((-1, 1))
        # Take softmax along each V chunks in the output layer
       output_layer_state = np.exp(inputs_to_softmax)
       output_layer_state_shape = output_layer state.shape
       output_layer_state = output_layer_state.reshape((-1, self.context_len, len(self.vocab)))
       output layer state /= output layer state.sum(axis=-1, keepdims=True) # Softmax along each target
word
       output layer state = output layer state.reshape(output layer state shape) # Flatten back
       return Activations (embedding layer state, hidden layer state, output layer state)
   def back_propagate(self, input_batch, activations, loss_derivative):
        """Compute the gradient of the loss function with respect to the trainable parameters
       of the model. The arguments are as follows:
            input_batch - the indices of the context words
            activations - an Activations class representing the output of Model.compute_activations
            loss derivative - the matrix of derivatives computed by compute loss derivative
       Part of this function is already completed, but you need to fill in the derivative
       computations for hid_to_output_weights_grad, output_bias_grad, embed_to_hid_weights_grad,
       and hid bias grad. See the documentation for the Params class for a description of what
       these matrices represent."""
        # The matrix with values dC / dz_j, where dz_j is the input to the jth hidden unit,
        # i.e. h_j = 1 / (1 + e^{-z_j})
       hid deriv = np.dot(loss derivative, self.params.hid to output weights) \
                    * activations.hidden_layer * (1. - activations.hidden_layer)
       hid to output weights grad = np.matmul(np.transpose(loss derivative), activations.hidden layer)
       output bias grad = np.sum(loss derivative, axis = 0)
       embed to hid weights grad = np.matmul(np.transpose(hid deriv), activations.embedding layer)
       hid bias grad = np.sum(hid deriv, axis = 0)
        # The matrix of derivatives for the embedding layer
       embed deriv = np.dot(hid deriv, self.params.embed to hid weights)
        # Embedding layer
       word_embedding_weights_grad = np.zeros((self.vocab_size, self.embedding_dim))
       for w in range(self.context len):
           word embedding weights grad += np.dot(self.indicator matrix(input batch[:, w:w+1], mask zero
index=False).T,
                                                 embed deriv[:, w * self.embedding dim:(w + 1) * self
.embedding dim])
       return Params (word_embedding_weights_grad, embed_to_hid_weights_grad, hid_to_output_weights_grad,
                     hid bias grad, output bias grad)
   def sample input mask(self, batch size):
        """Samples a binary mask for the inputs of size batch size x context len
       For each row, at most one element will be 1.
```

```
mask_idx = np.random.randint(self.context_len, size=(batch_size,))
       mask = np.zeros((batch size, self.context len), dtype=np.int) # Convert to one hot B x N, B batch
size, N context len
       mask[np.arange(batch size), mask idx] = 1
       return mask
   def evaluate(self, inputs, batch_size=100):
        """Compute the average cross-entropy over a dataset.
            inputs: matrix of shape D x N"""
       ndata = inputs.shape[0]
       total = 0.
       for input batch in get batches(inputs, batch size):
           mask = self.sample input mask(batch size)
           input batch masked = input batch * (1 - mask)
           activations = self.compute_activations(input_batch_masked)
           target_batch_masked = input_batch * mask
           expanded target batch = self.indicator matrix(target batch masked)
           cross_entropy = -np.sum(expanded_target_batch * np.log(activations.output_layer + TINY))
           total += cross_entropy
       return total / float(ndata)
   def display nearest words(self, word, k=10):
        """List the k words nearest to a given word, along with their distances."""
       if word not in self.vocab:
           print('Word "{}" not in vocabulary.'.format(word))
        # Compute distance to every other word.
       idx = self.vocab.index(word)
       word rep = self.params.word embedding weights[idx, :]
       diff = self.params.word_embedding_weights - word_rep.reshape((1, -1))
       distance = np.sqrt(np.sum(diff ** 2, axis=1))
       # Sort by distance.
       order = np.argsort(distance)
       order = order[1:1+k] # The nearest word is the query word itself, skip that.
       for i in order:
           print('{}: {}'.format(self.vocab[i], distance[i]))
   def word distance(self, word1, word2):
        """Compute the distance between the vector representations of two words."""
       if word1 not in self.vocab:
           raise RuntimeError('Word "{}" not in vocabulary.'.format(word1))
       if word2 not in self.vocab:
           raise RuntimeError('Word "{}" not in vocabulary.'.format(word2))
       idx1, idx2 = self.vocab.index(word1), self.vocab.index(word2)
       word_rep1 = self.params.word_embedding_weights[idx1, :]
       word_rep2 = self.params.word_embedding_weights[idx2, :]
       diff = word rep1 - word rep2
       return np.sqrt(np.sum(diff ** 2))
```

3.3 Print the gradients [1pt]

To make your life easier, we have provided the routine <code>check_gradients</code>, which checks your gradients using finite differences. You should make sure this check passes before continuing with the assignment. Once <code>check_gradients()</code> passes, call <code>print gradients()</code> and include its output in your write-up.

```
In [39]:

def relative_error(a, b):
    return np.abs(a - b) / (np.abs(a) + np.abs(b))

def check_output_derivatives(model, input_batch, target_batch):
    def softmax(z):
        z = z.copy()
        z -= z.max(-1, keepdims=True)
        y = np.exp(z)
        y /= y.sum(-1, keepdims=True)
        return y

    batch_size = input_batch.shape[0]
    z = np.random.normal(size=(batch_size, model.context_len, model.vocab_size))
```

```
y = softmax(z).reshape((batch size, model.context len * model.vocab size))
    z = z.reshape((batch size, model.context len * model.vocab size))
    expanded target batch = model.indicator matrix(target batch)
    target mask = expanded target batch.reshape(-1, model.context len, len(model.vocab)).sum(axis=-1, kee
pdims=True)
   loss_derivative = model.compute_loss_derivative(y, expanded_target_batch, target_mask)
   if loss_derivative is None:
       print('Loss derivative not implemented yet.')
        return False
    if loss derivative.shape != (batch size, model.vocab size * model.context len):
       print('Loss derivative should be size {} but is actually {}.'.format(
            (batch size, model.vocab size), loss derivative.shape))
       return False
   def obj(z):
        z = z.reshape((-1, model.context_len, model.vocab_size))
        y = softmax(z).reshape((batch size, model.context len * model.vocab size))
        return model.compute_loss(y, expanded_target_batch)
    for count in range(1000):
        i, j = np.random.randint(0, loss derivative.shape[0]), np.random.randint(0, loss derivative.shap
e[1])
        z_plus = z.copy()
        z_plus[i, j] += EPS
        obj plus = obj(z plus)
        z_{minus} = z.copy()
        z_{minus[i, j]} -= EPS
       obj minus = obj(z minus)
       empirical = (obj plus - obj minus) / (2. * EPS)
       rel = relative error(empirical, loss derivative[i, j])
        if rel > 1e-4:
           print('The loss derivative has a relative error of {}, which is too large.'.format(rel))
           return False
    print('The loss derivative looks OK.')
    return True
def check_param_gradient(model, param_name, input_batch, target_batch):
    activations = model.compute_activations(input_batch)
    expanded target batch = model.indicator matrix(target batch)
    target_mask = expanded_target_batch.reshape(-1, model.context_len, len(model.vocab)).sum(axis=-1, kee
   loss derivative = model.compute loss derivative(activations.output layer, expanded target batch, targ
et mask)
   param gradient = model.back propagate(input batch, activations, loss derivative)
   def obj(model):
       activations = model.compute_activations(input_batch)
        return model.compute loss(activations.output layer, expanded target batch)
    dims = getattr(model.params, param name).shape
    is matrix = (len(dims) == 2)
    if getattr(param_gradient, param_name).shape != dims:
        print('The gradient for {} should be size {} but is actually {}.'.format(
           param name, dims, getattr(param gradient, param name).shape))
       return
    for count in range(1000):
        if is matrix:
           slc = np.random.randint(0, dims[0]), np.random.randint(0, dims[1])
        else:
           slc = np.random.randint(dims[0])
        model plus = model.copy()
        getattr(model_plus.params, param_name)[slc] += EPS
        obj plus = obj(model plus)
       model minus = model.copy()
        getattr(model_minus.params, param_name)[slc] -= EPS
        obj minus = obj (model minus)
        empirical = (obj_plus - obj_minus) / (2. * EPS)
        exact = getattr(param gradient, param name)[slc]
        rel = relative_error(empirical, exact)
        if rel > 3e-4:
```

```
import pdb; pdb.set_trace()
print('The loss derivative has a relative error of {}, which is too large for param {}.'.form
at(rel, param name))
             return False
    print('The gradient for {} looks OK.'.format(param name))
def load_partially_trained_model():
    obj = pickle.load(open(PARTIALLY TRAINED MODEL, 'rb'))
    params = Params(obj['word embedding weights'], obj['embed to hid weights'],
                                        obj['hid to output weights'], obj['hid bias'],
                                         obj['output bias'])
    vocab = obj['vocab']
    return Model(params, vocab)
def check gradients():
     """Check the computed gradients using finite differences."""
    np.random.seed(0)
    np.seterr(all='ignore') # suppress a warning which is harmless
    model = load partially trained model()
    data_obj = pickle.load(open(data_location, 'rb'))
    train inputs = data obj['train inputs']
    input batch = train inputs[:100, :]
    mask = model.sample_input_mask(input_batch.shape[0])
    input batch masked = input batch * (1 - mask)
    target_batch_masked = input_batch * mask
    if not check_output_derivatives(model, input_batch_masked, target_batch_masked):
    for param name in ['word embedding weights', 'embed to hid weights', 'hid to output weights',
                           'hid bias', 'output bias']:
         input_batch_masked = input_batch * (1 - mask)
         target batch masked = input batch * mask
         check_param_gradient(model, param_name, input_batch_masked, target_batch_masked)
def print gradients():
    """Print out certain derivatives for grading."""
    np.random.seed(0)
    model = load_partially_trained_model()
    data obj = pickle.load(open(data location, 'rb'))
    train_inputs = data_obj['train inputs']
    input batch = train inputs[:100, :]
    mask = model.sample input mask(input batch.shape[0])
    input batch masked = input batch * (1 - mask)
    activations = model.compute_activations(input_batch_masked)
    target_batch_masked = input_batch * mask
    expanded_target_batch = model.indicator_matrix(target_batch_masked)
    target mask = expanded target batch.reshape(-1, model.context len, len(model.vocab)).sum(axis=-1, kee
pdims=True)
    loss derivative = model.compute loss derivative(activations.output layer, expanded target batch, targ
et mask)
    param gradient = model.back propagate(input batch, activations, loss derivative)
    print('loss_derivative[2, 5]', loss_derivative[2, 5])
    print('loss_derivative[2, 121]', loss_derivative[2, 121])
print('loss_derivative[5, 33]', loss_derivative[5, 33])
print('loss_derivative[5, 31]', loss_derivative[5, 31])
    print()
    print('param_gradient.word_embedding_weights[27, 2]', param_gradient.word_embedding_weights[27, 2])
    print('param_gradient.word_embedding_weights[43, 3]', param_gradient.word_embedding_weights[43, 3])
print('param_gradient.word_embedding_weights[22, 4]', param_gradient.word_embedding_weights[22, 4])
print('param_gradient.word_embedding_weights[2, 5]', param_gradient.word_embedding_weights[2, 5])
    print('param_gradient.embed_to_hid_weights[10, 2]', param_gradient.embed_to_hid_weights[10, 2])
    print('param_gradient.embed_to_hid_weights[15, 3]', param_gradient.embed_to_hid_weights[15, 3])
print('param_gradient.embed_to_hid_weights[30, 9]', param_gradient.embed_to_hid_weights[30, 9])
print('param_gradient.embed_to_hid_weights[35, 21]', param_gradient.embed_to_hid_weights[35, 21])
    print('param_gradient.hid_bias[10]', param_gradient.hid_bias[10])
    print('param_gradient.hid_bias[20]', param_gradient.hid_bias[20])
    print('param gradient.output_bias[0]', param_gradient.output_bias[0])
    print('param gradient.output bias[1]', param gradient.output bias[1])
    print('param_gradient.output_bias[2]', param_gradient.output_bias[2])
    print('param_gradient.output_bias[3]', param_gradient.output_bias[3])
```

```
# Run this to check if your implement gradients matches the finite difference within tolerance
# Note: this may take a few minutes to go through all the checks
check_gradients()
The loss derivative looks OK.
The gradient for word embedding weights looks OK.
The gradient for embed_to_hid_weights looks OK.
The gradient for hid_to_output_weights looks OK.
The gradient for hid bias looks OK.
The gradient for output_bias looks OK.
In [19]:
# Run this to print out the gradients
print gradients()
loss_derivative[2, 5] 0.0
loss_derivative[2, 121] 0.0
loss_derivative[5, 33] 0.0
loss derivative[5, 31] 0.0
param gradient.word embedding weights[27, 2] 0.0
param gradient.word embedding weights[43, 3] 0.011596892511489458
param_gradient.word_embedding_weights[22, 4] -0.0222670623817297
param gradient.word embedding weights[2, 5] 0.0
param gradient.embed to hid weights[10, 2] 0.3793257091930164
param_gradient.embed_to_hid_weights[15, 3] 0.01604516132110917
param_gradient.embed_to_hid_weights[30, 9] -0.4312854367997419
param_gradient.embed_to_hid_weights[35, 21] 0.06679896665436337
param gradient.hid bias[10] 0.023428803123345148
param gradient.hid bias[20] -0.024370452378874197
param gradient.output bias[0] 0.000970106146902794
param gradient.output bias[1] 0.16868946274763222
param_gradient.output_bias[2] 0.0051664774143909235
param gradient.output bias[3] 0.15096226471814364
```

3.4 Run model trainin [0pt]

Once you've implemented the gradient computation, you'll need to train the model. The function *train* implements the main training procedure. It takes two arguments:

- embedding_dim: The number of dimensions in the distributed representation.
- num hid: The number of hidden units

As the model trains, the script prints out some numbers that tell you how well the training is going. It shows:

- The cross entropy on the last 100 mini-batches of the training set. This is shown after every 100 mini-batches.
- The cross entropy on the entire validation set every 1000 mini-batches of training.

At the end of training, this function shows the cross entropies on the training, validation and test sets. It will return a Model instance.

```
In [21]:
```

In [40]:

```
# cache the data so we don't keep reloading
   global train inputs, train targets, vocab
    if _train_inputs is None:
       data obj = pickle.load(open(data location, 'rb'))
       _vocab = data_obj['vocab']
        __train_inputs, _train_targets = data_obj['train_inputs'], data_obj['train_targets']
   if word1 not in _vocab:
       raise RuntimeError('Word "{}" not in vocabulary.'.format(word1))
    if word2 not in vocab:
       raise RuntimeError('Word "{}" not in vocabulary.'.format(word2))
    if word3 not in vocab:
       raise RuntimeError('Word "{}" not in vocabulary.'.format(word3))
    idx1, idx2, idx3 = _vocab.index(word1), _vocab.index(word2), _vocab.index(word3)
   idxs = np.array([idx1, idx2, idx3])
   matches = np.all( train inputs == idxs.reshape((1, -1)), 1)
   if np.any(matches):
       counts = collections.defaultdict(int)
        for m in np.where(matches)[0]:
           counts[ vocab[ train targets[m]]] += 1
        word counts = sorted(list(counts.items()), key=lambda t: t[1], reverse=True)
        print('The tri-gram "{} {} {}" was followed by the following words in the training set:'.format(
           word1, word2, word3))
        for word, count in word counts:
           if count > 1:
               print('
                           {} ({} times)'.format(word, count))
           else:
               print('
                         {} (1 time)'.format(word))
   else:
       print('The tri-gram "{} {} {}" did not occur in the training set.'.format(word1, word2, word3))
def train(embedding dim, num hid, config=DEFAULT TRAINING CONFIG):
    """This is the main training routine for the language model. It takes two parameters:
        embedding dim, the dimension of the embedding space
        num hid, the number of hidden units."""
    # For reproducibility
   np.random.seed(123)
    # Load the data
    data obj = pickle.load(open(data location, 'rb'))
   vocab = data_obj['vocab']
    train inputs = data obj['train inputs']
   valid_inputs = data_obj['valid_inputs']
    test inputs = data obj['test inputs']
    # Randomly initialize the trainable parameters
   model = Model.random init(config['init wt'], vocab, config['context len'], embedding dim, num hid)
    # Variables used for early stopping
   best valid CE = np.infty
    end training = False
    # Initialize the momentum vector to all zeros
   delta = Params.zeros(len(vocab), config['context len'], embedding dim, num hid)
    this chunk CE = 0.
   batch count = 0
    for epoch in range(1, config['epochs'] + 1):
       if end training:
           break
        print()
        print('Epoch', epoch)
        for m, (input batch) in enumerate(get batches(train inputs, config['batch size'])):
           batch count += 1
            # For each example (row in input batch), select one word to mask out
           mask = model.sample input mask(config['batch size'])
           input_batch_masked = input_batch * (1 - mask) # We only zero out one word per row
           target_batch_masked = input_batch * mask # We want to predict the masked out word
            # Forward propagate
           activations = model.compute activations(input batch masked)
           # Compute loss derivative
```

```
expanded target batch = model.indicator matrix(target batch masked)
            loss_derivative = model.compute_loss_derivative(activations.output_layer, expanded_target_bat
ch, mask[:,:, np.newaxis])
           loss derivative /= config['batch size']
            # Measure loss function
           cross_entropy = model.compute_loss(activations.output_layer, expanded_target_batch) / config
['batch size']
           this_chunk_CE += cross_entropy
           if batch_count % config['show_training_CE_after'] == 0:
                print('Batch {} Train CE {:1.3f}'.format(
                   batch_count, this_chunk_CE / config['show_training CE after']))
                this chunk CE = 0.
            # Backpropagate
           loss gradient = model.back propagate(input batch, activations, loss derivative)
            # Update the momentum vector and model parameters
           delta = config['momentum'] * delta + loss gradient
           model.params -= config['learning_rate'] * delta
            # Validate
           if batch_count % config['show_validation_CE_after'] == 0:
                print('Running validation...')
                cross_entropy = model.evaluate(valid_inputs)
               print('Validation cross-entropy: {:1.3f}'.format(cross entropy))
                if cross entropy > best valid CE:
                    print('Validation error increasing! Training stopped.')
                    end_training = True
                   break
                best valid CE = cross entropy
    train CE = model.evaluate(train inputs)
    print('Final training cross-entropy: {:1.3f}'.format(train CE))
    valid CE = model.evaluate(valid inputs)
   print('Final validation cross-entropy: {:1.3f}'.format(valid_CE))
    test CE = model.evaluate(test inputs)
    print('Final test cross-entropy: {:1.3f}'.format(test CE))
    return model
```

Run the training.

```
In [22]:
```

```
embedding_dim = 16
num hid = 128
trained model = train(embedding dim, num hid)
Epoch 1
Batch 100 Train CE 4.793
Batch 200 Train CE 4.645
Batch 300 Train CE 4.649
Batch 400 Train CE 4.629
Batch 500 Train CE 4.633
Batch 600 Train CE 4.648
Batch 700 Train CE 4.617
Batch 800 Train CE 4.607
Batch 900 Train CE 4.606
Batch 1000 Train CE 4.615
Running validation...
Validation cross-entropy: 4.615
Batch 1100 Train CE 4.615
Batch 1200 Train CE 4.624
Batch 1300 Train CE 4.608
Batch 1400 Train CE 4.595
Batch 1500 Train CE 4.611
Batch 1600 Train CE 4.598
Batch 1700 Train CE 4.577
Batch 1800 Train CE 4.578
Batch 1900 Train CE 4.568
Batch 2000 Train CE 4.589
Running validation...
Validation cross-entropy: 4.589
Batch 2100 Train CE 4.573
Batch 2200 Train CE 4.611
Batch 2300 Train CE 4.562
Batch 2400 Train CE 4.587
Batch 2500 Train CE 4.589
```

```
Batch 2600 Train CE 4.587
Batch 2700 Train CE 4.561
Batch 2800 Train CE 4.544
Batch 2900 Train CE 4.521
Batch 3000 Train CE 4.524
Running validation...
Validation cross-entropy: 4.496
Batch 3100 Train CE 4.504
Batch 3200 Train CE 4.449
Batch 3300 Train CE 4.384
Batch 3400 Train CE 4.352
Batch 3500 Train CE 4.324
Batch 3600 Train CE 4.261
Batch 3700 Train CE 4.267
Epoch 2
Batch 3800 Train CE 4.208
Batch 3900 Train CE 4.168
Batch 4000 Train CE 4.117
Running validation...
Validation cross-entropy: 4.112
Batch 4100 Train CE 4.105
Batch 4200 Train CE 4.049
Batch 4300 Train CE 4.008
Batch 4400 Train CE 3.986
Batch 4500 Train CE 3.924
Batch 4600 Train CE 3.897
Batch 4700 Train CE 3.857
Batch 4800 Train CE 3.790
Batch 4900 Train CE 3.796
Batch 5000 Train CE 3.773
Running validation...
Validation cross-entropy: 3.776
Batch 5100 Train CE 3.766
Batch 5200 Train CE 3.714
Batch 5300 Train CE 3.720
Batch 5400 Train CE 3.668
Batch 5500 Train CE 3.668
Batch 5600 Train CE 3.639
Batch 5700 Train CE 3.571
Batch 5800 Train CE 3.546
Batch 5900 Train CE 3.537
Batch 6000 Train CE 3.511
Running validation...
Validation cross-entropy: 3.531
Batch 6100 Train CE 3.494
Batch 6200 Train CE 3.495
Batch 6300 Train CE 3.477
Batch 6400 Train CE 3.455
Batch 6500 Train CE 3.435
Batch 6600 Train CE 3.446
Batch 6700 Train CE 3.411
Batch 6800 Train CE 3.376
Batch 6900 Train CE 3.419
Batch 7000 Train CE 3.375
Running validation...
Validation cross-entropy: 3.386
Batch 7100 Train CE 3.398
Batch 7200 Train CE 3.383
Batch 7300 Train CE 3.371
Batch 7400 Train CE 3.355
Epoch 3
Batch 7500 Train CE 3.320
Batch 7600 Train CE 3.315
Batch 7700 Train CE 3.342
Batch 7800 Train CE 3.293
Batch 7900 Train CE 3.285
Batch 8000 Train CE 3.296
Running validation...
Validation cross-entropy: 3.294
Batch 8100 Train CE 3.271
Batch 8200 Train CE 3.291
Batch 8300 Train CE 3.287
Batch 8400 Train CE 3.274
Batch 8500 Train CE 3.228
Batch 8600 Train CE 3.256
Batch 8700 Train CE 3.250
Batch 8800 Train CE 3.256
Batch 8900 Train CE 3.266
Batch 9000 Train CE 3.221
Running validation...
Validation cross-entropy: 3.233
```

```
Batch 9200 Train CE 3.229
Batch 9300 Train CE 3.223
Batch 9400 Train CE 3.215
Batch 9500 Train CE 3.208
Batch 9600 Train CE 3.199
Batch 9700 Train CE 3.200
Batch 9800 Train CE 3.229
Batch 9900 Train CE 3.189
Batch 10000 Train CE 3.179
Running validation...
Validation cross-entropy: 3.175
Batch 10100 Train CE 3.168
Batch 10200 Train CE 3.163
Batch 10300 Train CE 3.166
Batch 10400 Train CE 3.197
Batch 10500 Train CE 3.174
Batch 10600 Train CE 3.173
Batch 10700 Train CE 3.143
Batch 10800 Train CE 3.178
Batch 10900 Train CE 3.185
Batch 11000 Train CE 3.101
Running validation...
Validation cross-entropy: 3.146
Batch 11100 Train CE 3.159
Epoch 4
Batch 11200 Train CE 3.156
Batch 11300 Train CE 3.134
Batch 11400 Train CE 3.140
Batch 11500 Train CE 3.155
Batch 11600 Train CE 3.128
Batch 11700 Train CE 3.121
Batch 11800 Train CE 3.161
Batch 11900 Train CE 3.111
Batch 12000 Train CE 3.141
Running validation...
Validation cross-entropy: 3.121
Batch 12100 Train CE 3.136
Batch 12200 Train CE 3.132
Batch 12300 Train CE 3.120
Batch 12400 Train CE 3.105
Batch 12500 Train CE 3.078
Batch 12600 Train CE 3.136
Batch 12700 Train CE 3.120
Batch 12800 Train CE 3.125
Batch 12900 Train CE 3.080
Batch 13000 Train CE 3.107
Running validation...
Validation cross-entropy: 3.104
Batch 13100 Train CE 3.116
Batch 13200 Train CE 3.088
Batch 13300 Train CE 3.091
Batch 13400 Train CE 3.093
Batch 13500 Train CE 3.069
Batch 13600 Train CE 3.074
Batch 13700 Train CE 3.084
Batch 13800 Train CE 3.075
Batch 13900 Train CE 3.081
Batch 14000 Train CE 3.089
Running validation...
Validation cross-entropy: 3.088
Batch 14100 Train CE 3.090
Batch 14200 Train CE 3.108
Batch 14300 Train CE 3.127
Batch 14400 Train CE 3.075
Batch 14500 Train CE 3.073
Batch 14600 Train CE 3.132
Batch 14700 Train CE 3.104
Batch 14800 Train CE 3.076
Batch 14900 Train CE 3.076
Epoch 5
Batch 15000 Train CE 3.054
Running validation...
Validation cross-entropy: 3.056
Batch 15100 Train CE 3.088
Batch 15200 Train CE 3.065
Batch 15300 Train CE 3.087
Batch 15400 Train CE 3.099
Batch 15500 Train CE 3.055
Batch 15600 Train CE 3.075
Batch 15700 Train CE 3.071
Datab 15000 masta CE 3 076
```

Batch 9100 Train CE 3.24/

```
Batch 15000 Train CE 3.076
Batch 15900 Train CE 3.075
Batch 16000 Train CE 3.071
Running validation...
Validation cross-entropy: 3.087
Validation error increasing! Training stopped.
Final training cross-entropy: 3.071
Final validation cross-entropy: 3.081
Final test cross-entropy: 3.083
```

To convince us that you have correctly implemented the gradient computations, please include the following with your assignment submission:

- [] You will submit a1-code.ipynb through MarkUs. You do not need to modify any of the code except the parts we asked you to implement.
- [] In your writeup, include the output of the function <code>print_gradients</code>. This prints out part of the gradients for a partially trained network which we have provided, and we will check them against the correct outputs. Important: make sure to give the output of <code>print gradients</code>, not <code>check gradients</code>.

This is worth 4 points:

- 1 for the loss derivatives,
- 1 for the bias gradients, and
- 2 for the weight gradients.

Since we gave you a gradient checker, you have no excuse for not getting full points on this part.

Part 4: Arithmetics and Analysis (2pts)

In this part, you will perform arithmetic calculations on the word embeddings learned from previous models and analyze the representation learned by the networks with t-SNE plots.

4.1 t-SNE

You will first train the models discussed in the previous sections; you'll use the trained models for the remainder of this section.

Important: if you've made any fixes to your gradient code, you must reload the a1-code module and then re-run the training procedure. Python does not reload modules automatically, and you don't want to accidentally analyze an old version of your model.

These methods of the Model class can be used for analyzing the model after the training is done:

- tsne_plot_representation creates a 2-dimensional embedding of the distributed representation space using an algorithm called t-SNE. (You don't need to know what this is for the assignment, but we may cover it later in the course.) Nearby points in this 2-D space are meant to correspond to nearby points in the 16-D space.
- display_nearest_words lists the words whose embedding vectors are nearest to the given word
- word distance computes the distance between the embeddings of two words

Plot the 2-dimensional visualization for the trained model from part 3 using the method $tsne_plot_representation$. Look at the plot and find a few clusters of related words. What do the words in each cluster have in common? Plot the 2-dimensional visualization for the GloVe model from part 1 using the method $tsne_plot_GLoVe_representation$. How do the t-SNE embeddings for both models compare? Plot the 2-dimensional visualization using the method $plot_2d_GLoVe_representation$. How does this compare to the t-SNE embeddings? Please answer in 2 sentences for each question and show the plots in your submission.

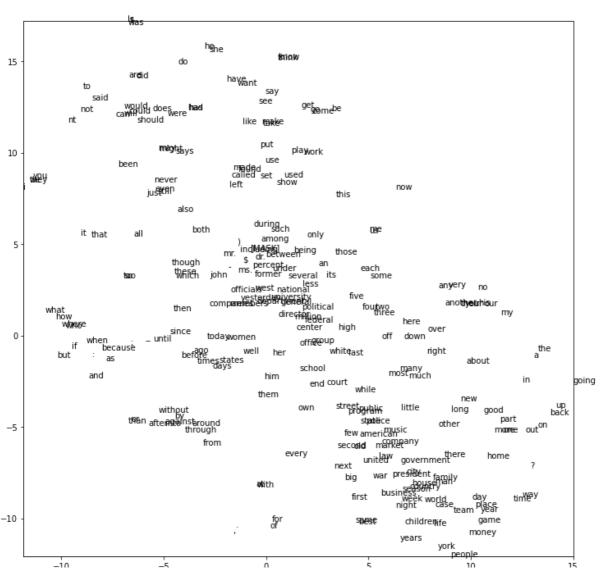
- 4.1 **Answer**: \ -> Words in each common cluster have similar semantic meaning/attributes. They are words that are 'more' likely to be used in similar context/to potray a similar meaning and in some cases, maybe even interchangably.
- -> We can see that tsne_plot_GLoVe_representation produces plots that seem to show a much less sense of semantic relation compared to the t-SNE plots generated using trained neural network model. In the GLoVe t-SNE plot, there seems to be a lack of word clusters and all words just seem scattered around; It can be seen that words that are not semantically similar seem to be close in distance, unlike plots generated by tsne_plot_representation.
- -> We can see that plot_2d_GLoVe_representation produces a plot that seems to not show semantic relation between words. The plot seems to be following an arbitrary distribution of words where they seem to be concentrated at bottom of plot and they scatter around resembling the idea of a 'blooming flower'. Compared to t-SNE, we see a much lower effect of relation of semantic meaning of words on the distribution of the plot.

```
def tsne plot representation(model):
    """Plot a 2-D visualization of the learned representations using t-SNE."""
    print(model.params.word_embedding_weights.shape)
    mapped X = TSNE(n components=2).fit transform(model.params.word embedding weights)
    pylab.figure(figsize=(12,12))
    for i, w in enumerate(model.vocab):
       pylab.text(mapped X[i, 0], mapped X[i, 1], w)
    pylab.xlim(mapped_X[:, 0].min(), mapped_X[:, 0].max())
    pylab.ylim(mapped_X[:, 1].min(), mapped_X[:, 1].max())
    pylab.show()
def tsne plot GLoVE representation(W final, b final):
    """Plot a 2-D visualization of the learned representations using t-SNE."""
    mapped X = TSNE(n components=2).fit transform(W final)
    pylab.figure(figsize=(12,12))
    data obj = pickle.load(open(data location, 'rb'))
    for i, w in enumerate(data_obj['vocab']):
        pylab.text(mapped_X[i, 0], mapped_X[i, 1], w)
    pylab.xlim(mapped_X[:, 0].min(), mapped_X[:, 0].max())
    pylab.ylim(mapped_X[:, 1].min(), mapped_X[:, 1].max())
    pylab.show()
def plot 2d GLoVE representation (W final, b final):
    """Plot a 2-D visualization of the learned representations."""
    mapped X = W final
    pylab.figure(figsize=(12,12))
    data obj = pickle.load(open(data location, 'rb'))
    for i, w in enumerate(data obj['vocab']):
        pylab.text(mapped_X[i, 0], mapped_X[i, 1], w)
    pylab.xlim(mapped_X[:, 0].min(), mapped_X[:, 0].max())
    pylab.ylim(mapped_X[:, 1].min(), mapped_X[:, 1].max())
    pylab.show()
```

In [25]:

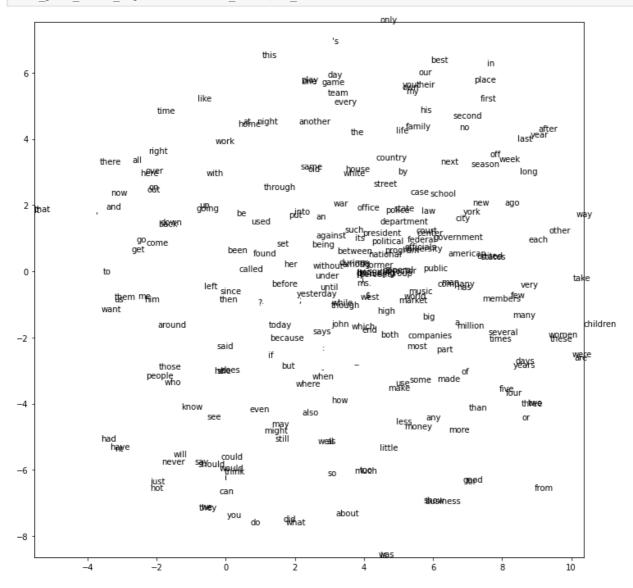
tsne plot representation(trained model)

(251, 16)



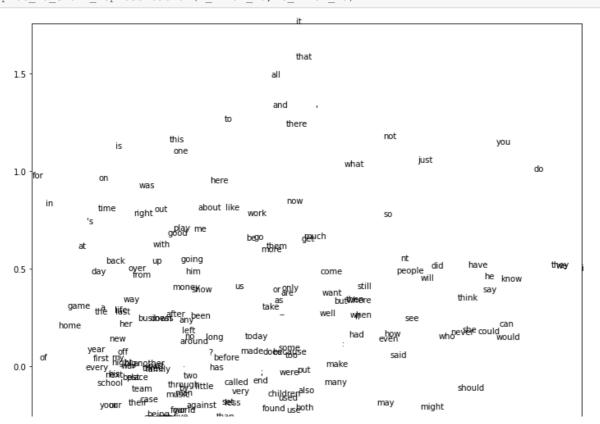
In [26]:

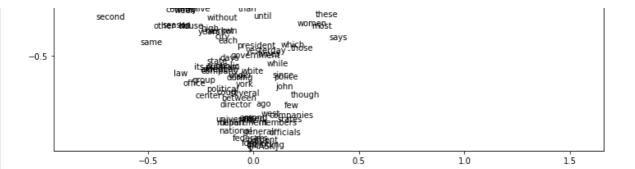
tsne_plot_GLoVE_representation(W_final, b_final)



In [27]:

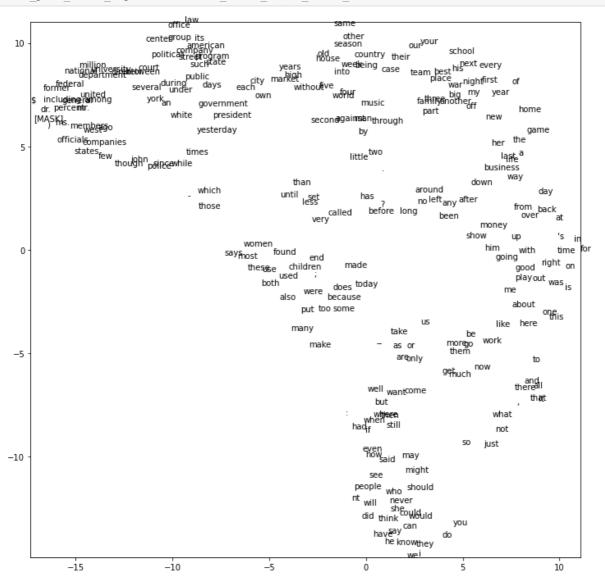
plot 2d GLoVE representation (W final 2d, b final 2d)





In [28]:

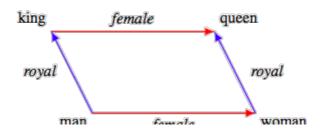
tsne plot GLoVE representation(W final 2d, b final 2d)



4.2 Word Embedding Arithmetic

A word analogy f is an invertible transformation that holds over a set of ordered pairs S iff $\forall (x, y) \in s$, $f(x) = y \land f^{-1}(y) = x$. When f is of the form $\vec{x} \to \vec{x} + \vec{r}$, it is a linear word analogy.

Arithmetic operators can be applied to vectors generated by language models. There is a famous example: $king - man + women \approx queen$. These linear word analogies form a parallelogram structure in the vector space (Ethayarajh, Duvenaud, \& Hirst, 2019).



In this section, we will explore a property of *linear word analogies*. A linear word analogy holds exactly over a set of ordered word

pairs S iff $\|\vec{x} - \vec{y}\|^2$ is the same for every word pair, $\|\vec{a} - \vec{x}\|^2 = \|\vec{b} - \vec{y}\|^2$ for any two word pairs, and the vectors of all words in S are coplanar.

We will use the embeddings from the symmetric, asymmetrical GloVe model, and the neural network model from part 3 to perform arithmetics. The method to perform the arithmetic and retrieve the closest word embeddings is provided in the notebook using the method <code>find_word_analogy</code>:

• find word analogy returns the closest word to the word embedding calculated from the 3 given words.

In [29]:

```
np.random.seed(1)
n_epochs = 500  # A hyperparameter. You can play with this if you want.
embedding_dims = 16

W_final_sym, W_tilde_final_asym, W_final_asym = None, None, None
init_variance = 0.1  # A hyperparameter. You can play with this if you want.
W = init_variance * np.random.normal(size=(vocab_size, embedding_dim))
W_tilde = init_variance * np.random.normal(size=(vocab_size, embedding_dim))
b = init_variance * np.random.normal(size=(vocab_size, 1))
b_tilde = init_variance * np.random.normal(size=(vocab_size, 1))

# Symmetric model
W_final_sym, _, b_final_sym, _ , _, _ = train_GLoVE(W, None, b, None, asym_log_co_occurence_train, asym_log_co_occurence_valid, n_epochs, do_print=do_print)
# Asymmetric model
W_final_asym, W_tilde_final_asym, b_final_asym, b_tilde_final_asym, _, _ = train_GLoVE(W, W_tilde, b, b_tilde, asym_log_co_occurence_train, asym_log_co_occurence_valid, n_epochs, do_print=do_print)
```

You will need to use different embeddings to evaluate the word analogy

```
In [30]:
```

```
def get_word_embedding(word, embedding_weights):
    assert word in data['vocab'], 'Word not in vocab'
    return embedding_weights[data['vocab'].index(word)]
```

In [33]:

```
# word4 = word1 - word2 + word3
def find_word_analogy(word1, word2, word3, embedding_weights):
    embedding1 = get_word_embedding(word1, embedding_weights)
    embedding2 = get_word_embedding(word2, embedding_weights)
    embedding3 = get_word_embedding(word3, embedding_weights)
    target_embedding = embedding1 - embedding2 + embedding3

# Compute distance to every other word.
diff = embedding_weights - target_embedding.reshape((1, -1))
distance = np.sqrt(np.sum(diff ** 2, axis=1))

# Sort by distance.
order = np.argsort(distance)[:10]
print("The top 10 closest words to emb({}) - emb({}) + emb({}) are:".format(word1, word2, word3))
for i in order:
    print('{}): {}'.format(data['vocab'][i], distance[i]))
```

In this part of the assignment, you will use the find_word_analogy function to analyze quadruplets from the vocabulary.

4.2.1 Specific example

Perform arithmetic on words *her*, *him*, *her*, using: (1) symmetric, (2) averaging asymmetrical GloVe embedding, (3) concatenating asymmetrical GloVe embedding, and (4) neural network word embedding from part 3. That is, we are trying to find the closet word embedding vector to the vector

```
emb(he) - emb(him) + emb(her)
```

For each sets of embeddings, you should list out: (1) what the closest word that is not one of those three words, and (2) the distance to that closest word. Is the closest word *she*? Compare the results with the tSNE plots.

- 4.2.1 Answer: 1) Symmetric GLoVe \ Closest word: she \ Distance to word: 1.48167433432594 \
- 2) Averaging asymmetrical GLoVe embedding \ Closest word: she \ Distance to word: 1.316107521673434 \

- 3) Concatenating asymmetrical GLoVe embedding \ Closest word: she \ Distance to word: 2.743710426392632 \
- 4) Neural network word embedding from part 3 \ Closest word: she \ Distance to word: 17.4415802699889 \

Looking at the results above, we can see that closest word, as seen in all 4 results, is 'she'. The results seem incosistent with t-SNE plots, as we can see that in the tSNE plots given above, the words in question are fairly far apart. This tells us that these 2D tSNE embeddings can be fairly misleading.

```
embeddings can be fairly misleading.
In [34]:
## GloVe embeddings
embedding weights = W final sym # Symmetric GloVe
find word analogy('he', 'him', 'her', embedding weights)
The top 10 closest words to emb(he) - emb(him) + emb(her) are:
he: 1.4213098857979793
she: 1.48167433432594
said: 2.1025960106397767
then: 2.2720425987761406
does: 2.301964867719902
says: 2.318047293286045
who: 2.328984314854128
where: 2.334702431567161
did: 2.353623598835888
should: 2.4126428205989865
In [35]:
# Concatenation of W_final_asym, W_tilde_final_asym
\verb|embedding_weights = | \verb|np.concatenate((W_tilde_final_asym, W_final_asym), axis=1)| \\
find word analogy('he', 'him', 'her', embedding weights)
The top 10 closest words to emb(he) - emb(him) + emb(her) are:
he: 2.1270210644154752
she: 2.743710426392632
program: 4.030317287577378
public: 4.056551077307381
man: 4.086155696766423
center: 4.224988323444584
company: 4.2310659574809275
law: 4.247390643502706
never: 4.262615166566255
government: 4.27818356729387
In [36]:
# Averaging asymmetric GLoVE vectors
embedding_weights = (W_final_asym + W_tilde_final_asym)/2
find word analogy('he', 'him', 'her', embedding weights)
The top 10 closest words to emb(he) - emb(him) + emb(her) are:
he: 0.9967970921235595
she: 1.316107521673434
public: 1.634008236168681
program: 1.6800867525990495
his: 1.7225233690904012
company: 1.7358722511164506
man: 1.7459906626391475
center: 1.7510274093532725
law: 1.790314100786874
each: 1.8017989344466716
In [37]:
## Neural Netework Word Embeddings
embedding weights = trained model.params.word embedding weights # Neural network from part3
find word analogy('he', 'him', 'her', embedding weights)
The top 10 closest words to emb(he) - emb(him) + emb(her) are:
he: 2.4284684644619032
she: 17.4415802699889
have: 25.921497697983263
they: 25.981587972296392
want: 26.437644546989542
we: 27.128094534488834
i: 27.215833550319473
```

but: 28.03028938337095 about: 28.163403568035555 this: 28.531350495330678

4.2.2 Finding another Quadruplet

Pick another quadruplet from the vocabulary which displays the parallelogram property (and also makes sense sementically) and repeat the above proceduces. Compare and comment on the results from arithmetic and tSNE plots.

4.2.2 Answer: **TODO: Write Part 4.1 answer here**

In []:

Repeat above with a different set of words

What you have to submit

For reference, here is everything you need to hand in. See the top of this handout for submission directions.

- A PDF file titled a1-writeup.pdf containing the following:
 - [] Part 1: Questions 1.1, 1.2, 1.3, 1.4. Completed code for grad_GLoVE function.
 - [] Part 2: Questions 2.1, 2.2, 2.3.
 - [] Part 3: Completed code for compute_loss_derivative() (3.1), back_propagate() (3.2) functions, and the output of print gradients() (3.3)
 - [] Part 4: Questions 4.1, 4.2.1, 4.2.2
- Your code file al-code.ipynb

In []: