

QUESTION 2

193079024

SARVESH KALE

Q2 a.)

We are given a care set $A = x_1.x_2 + x_3.x_4$, we first construct the characteristic equation of the problem .

I am using +,.,^,~ to denote or , and , xor and negation

$Y_1 = x_1 \wedge x_2 \wedge x_3 \wedge x_4$ so this can be written in boolean form as xnor of y_1 and the expression on the right , $\sim(y_1 \wedge (x_1 \wedge x_2 \wedge x_3 \wedge x_4))$ similarly the other two equations $\sim(y_2 \wedge (x_1.x_2 \wedge x_2.x_3 \wedge x_3.x_4 \wedge x_1.x_4))$, $\sim(y_3 \wedge (x_1.x_2.x_3 \wedge x_2.x_3.x_4 \wedge x_3.x_1.x_4))$

The resultant characteristic equation will be the product of the three expression written above ,

$$\text{Let } X = \sim(y_1 \wedge (x_1 \wedge x_2 \wedge x_3 \wedge x_4)) \cdot \sim(y_2 \wedge (x_1.x_2 \wedge x_2.x_3 \wedge x_3.x_4 \wedge x_1.x_4)) \cdot \sim(y_3 \wedge (x_1.x_2.x_3 \wedge x_2.x_3.x_4 \wedge x_3.x_1.x_4))$$

Now we have to do there exist operation on $A.X$,because A is our care set and we have to find the image that is those points in output vector which are true under $A.X$ so after doing a there exist operation on x_1, x_2, x_3, x_4 ,we will obtain an expression which is a function of y_1, y_2, y_3 because the there exist operation eliminates the variables

So we first defined the variables for bdd ,and then constructed A ,and X then we constructed the bdd for $A.X$ and then we performed the there exist operation

$$\text{Image} = \text{there exist } x_4 (\text{there exist } x_3 (\text{there exist } x_2 (\text{there exist } x_1 (A.X))))$$

Where $A = x_1.x_2 + x_3.x_4$

$$X = \sim(y_1 \wedge (x_1 \wedge x_2 \wedge x_3 \wedge x_4)) \cdot \sim(y_2 \wedge (x_1.x_2 \wedge x_2.x_3 \wedge x_3.x_4 \wedge x_1.x_4)) \cdot \sim(y_3 \wedge (x_1.x_2.x_3 \wedge x_2.x_3.x_4 \wedge x_3.x_1.x_4))$$

The output we got is displayed below .

```
sarvesh:q2$ ./q2a
if var.4
  !var.5
else if !var.4
  if var.5
    !var.6
  else if !var.5
    var.6
  endif var.5
endif var.4
```

So according to the ordering of variables , var.4 is y1, var.5 is y2 , var.6 is y3.

Image = (1,0,1),(1,0,0),(0,1,0),(0,0,1) these are the output image points we obtain after traversing the above bdd .

Q2 b.)

Approach

The approach is also similar to the above question but instead of computing the image we have to compute the preimage that means the there exist operation will now be on the output variables y1,y2,y3 and we will get a bdd in terms of x1,x2,x3,x4 . here we are asked that what input points map to the given formula

$$B = y1.y2 + y2.y3$$

For preimage computation we do the following .

We change the association of the variable on which bdd_exists has to be performed .

Preimage = there exist y3 (there exist y2 (there exist y1(B.X)))

Where $X = \sim(y1 \wedge (x1 \wedge x2 \wedge x3 \wedge x4)) \vee \sim(y2 \wedge (x1.x2 \wedge x2.x3 \wedge x3.x4 \wedge x1.x4)) \vee \sim(y3 \wedge (x1.x2.x3 \wedge x2.x3.x4 \wedge x3.x1.x4))$

On constructing the bdd for the formula given by B , we do the exists operation .

We obtain the following result .

```
sarvesh:q2$ ./q2b  
0
```

That means there is no input combination for which this formula is true so we get 0 bdd as output .