

Lab 2 – DT system applications

Objectives: In this lab we will learn to build simple discrete time (DT) systems to perform some tasks and recognize the patterns of pole-zero, ROC properties, and impulse response of a second order system.

2.1. A **Moving Average** (MA) system is used to detect trends from a given signal. It is related to the accumulator. It finds the average of the signal over the past few samples.

$$\text{Accumulator: } y[n] = \sum_{k=-\infty}^n x[k] \quad \text{Moving average system: } y[n] = \frac{1}{N} \sum_{k=n-N+1}^n x[k]$$

- Write a Matlab script to implement the above MA system.
- Test the system with a unit step function ($u[n]$) as input.
- Find the trend of the given test sequence $s[n]$, the signal is provided in q1.mat file.
- Experiment with different values for N and find the value appropriate for $s[n]$. Why do you think it is appropriate?
- Find the impulse response of the MA system and implement it using convolution. Find the trend of $s[n]$ using this implementation. Is there any difference in the result? What are the pros and cons of the two implementations?

2.2. An **Upsampler** is a system which increases the length of a given sequence and interpolates to find the values of the new samples. A popular application of upsampling is magnifying/zooming an image.

Upsampling step 1:

$$y[n] = \frac{n}{M} \text{ if } n \text{ is an integer multiple of } M > 1$$

= 0 otherwise

Upsampling step 2: Estimate the value of the newly inserted samples, i.e. do interpolation.

- Write a script to implement the upsampler with $M = 2$ and 3. Experiment with zero order hold and linear interpolation.
- Upsample the given test sequences present in q2_1.mat and q2_2.mat files. What do you observe?

2.3. A **digital differentiator** is given as $y[n] = x[n] - x[n-1]$. Write a script to implement this system and find the output of this system for the following three inputs. Plot the input and output sequences.

- $x[n] = 5(u[n] - u[n - 20])$
- $x[n] = n(u[n] - u[n - 10]) + (20 - n)(u[n - 10] - u[n - 20])$
- $x[n] = \sin[\frac{\pi}{25}](u[n] - u[n - 100])$

2.4. A finite difference equation can be written as,

$$\sum_{k=0}^N a_k y[n - k] = \sum_{m=0}^M b_m x[n - m]$$

The solution for this equation can be found numerically using the *filter* function in Matlab.

Matlab code:

```
y = filter(b,a,x)
```

```
b = [b0, b1, b2.. bM]; a = [a0, a1, a2.. aN].
```

Note that you have to choose $a_0 \neq 0$; Output $y[n]$ is same length as $x[n]$.

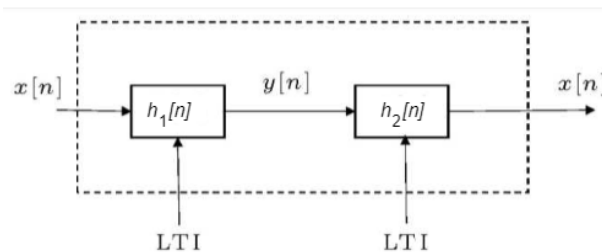
To find the impulse response $h[n]$

```
h = impz(b,a,n)
```

2.4.1. A second order feedback system is given as $y[n] + \alpha y[n-1] + \beta y[n-2] = x[n]$. Plot the impulse response $h[n]$ for this system (using the above code) for different coefficient values, i.e. α and β .

- $\alpha = -1$ and $\beta = 0.9$
- Find the coefficients for the system such that $h[n]$ decays monotonically.
- Find the coefficients such that $h[n]$ diverges monotonically.
- Find coefficients such that $h[n]$ grows initially and then decays as n increases to ∞ .
- Find the coefficients such that $h[n]$ oscillates for all n .

2.5. Consider the **digital differentiator** system **S** from 2.3. Find the difference equation for a system **S*** such that it acts as the inverse of the digital differentiator system. Thus, the cascade connection of **S** and **S*** acts like an identity system as shown below.



2.5.1 Derive and write a Matlab code to implement the **S*** system. Make subplots for $x[n]$, $y[n]$ at the input and output of each system.

2.5.2 Find the impulse response of the systems h_1 and h_2 and compare their plots.

2.5.3 Comment on the result of convolution of the systems h_1 and h_2