

## ARRAYED\_HEAP+

### feature --Commands

insert+ (new\_key: INTEGER) --Add new key into the heap if it does not exist

#### require

*non\_existing\_key*:  $\forall j: 1 \leq j \leq \text{array.count}: \text{array}[j] \neq \text{new\_key}$

#### ensure

*size\_incremented*:  $\text{array.count} = \text{old array.count} + 1$

*others\_unchanged*:  $\forall j: 1 \leq j \leq \text{array.count}: \text{array}[j] \neq \text{new\_key} \Rightarrow (\text{old array}).\text{has}(j)$

remove\_maximum+ --Remove the maximum key from the heap if it is not empty

#### require

*non\_empty\_heap*:  $\text{array.count} \neq 0$

#### ensure

*size\_decremented*:  $\text{array.count} = \text{old array.count} - 1$

*others\_unchanged\_except\_max*:  $\forall j: 1 \leq j \leq \text{array.count}: (\text{old array}).\text{has}(j)$

### feature --Queries

key\_exists+ (a\_key: INTEGER): BOOLEAN -- Does 'a\_key' exist in the current heap?

#### require

*--No precondition is needed*

#### ensure

*correct\_result*:  $\exists j: 1 \leq j \leq \text{array.count}: \text{array}[j] \sim \_key$

### feature -- { NONE }

-- array representation of the heap

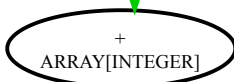
array: ARRAY[INTEGER]

### invariant

*all\_positive\_keys*:  $\forall j: 1 \leq j \leq \text{array.count}: \text{array}[j] > 0$

*max\_heap\_property*:  $\forall j: 1 \leq j \leq \text{array.count}: \text{array}[j] > \text{children\_of}(j)$

array+



## SCHEDULER+

### feature --Queries

priority\_exists (priority: INTEGER): BOOLEAN

-- Does the priority value exist for a given task?

### feature --Commands

add\_task (new\_task: TUPLE[task: TASK; priority: INTEGER])

--Add 'new\_task' to the scheduler,  
--given the priority does not exist'

#### require

*non\_existing\_priority*:  $\exists j: \text{tasks.current\_keys}:$

*priority\_exists*(new\_task.priority)

### feature -- { NONE }

-- A mapping from a priority value to a task object

tasks: HASH\_TABLE[TASK, INTEGER]

--A priority queue implemented using the array based heap

pq: ARRAYED\_HEAP

### invariant

*equal\_counts*:  $\text{tasks.count} = \text{pq.count}$

*consistent\_key\_priorities*:

$\forall j: \text{tasks.current\_keys}: \text{pq.key\_exists}(j)$

pq+

tasks+

