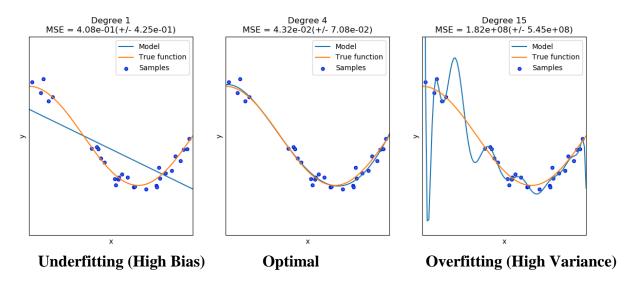
Q1. Explain Underfitting and Overfitting in Brief.

Underfitting:

- (a) A statistical model or a machine learning algorithm is said to have underfitting when it cannot capture the underlying trend of the data. It has poor performance on the training data and *poor generalization* to other data.
- (b) Underfitting destroys the accuracy of our machine learning model.
- (c) Its occurrence simply means that our model or the algorithm does not fit the data well eno ugh.
- (d) It usually happens when we have less data to build an accurate model and also when we try to build a linear model with a non-linear data.
- (e) In such cases the rules of the machine learning model are too easy and flexible to be applied on such a minimal data and therefore the model will probably make a lot of wrong predictions.
- (f) Underfitting can be avoided by using more data and also reducing the features by feature selection.

For example, when a given model yields a large training MSE and a large test MSE, we are said to be underfitting the data



Overfitting:

- (a) A statistical model is said to be overfitted, when we train it with a lot of data. It has good performance on the training data, *poor generliazation* to other data
- (b) When a model gets trained with so much of data, it starts learning from the noise and ina ccurate data entries in our data set.
- (c) Then the model does not categorize the data correctly, because of too much of details and noise. Thus model has *high Variance*.
- (d) The causes of overfitting are the non-parametric and non-linear methods because these ty pes of machine learning algorithms have more freedom in building the model based on the dataset and therefore they can really build unrealistic models.
- (e) Overfitting can be avoided by using methodologies like cross-validation, early stopping, pruning, regularization.

For example, when a given model yields a small training MSE but a large test MSE, we are said to be overfitting the data

Q3.What is Regularization? When you will use it? Effect of choosing different values of Lambda during Regression?

- a) Overfitting or high variance is caused by hypothesis function that fits the trained data but does not generalize well to predict new data. It is usually caused by a complicated function that creates a lot of unnecessary curves and angles unrelated to the data.
- b) Regularization takes care of the overfitting by keeping all the features but reducing the magnitude of parameters θ_i .
- c) Regularization tries to push the coefficients for many variables to zero and hence reduce cost term.
- d) The genral formula for regularization is as follows:

$$J(\theta) = \frac{1}{2} \left[\sum_{i=1}^{m} \left(h_{\theta} \left(x^{(i)} \right) - y^{(i)} \right)^{2} \right] + \lambda \sum_{j=1}^{n} \left(\theta_{j}^{2} \right)$$

Where λ is the regularization parameter. It determines how much the costs of our theta parameters are inflated

The effect of different values of lambda on regression

Linear regression with regularization

$$\begin{split} \text{Model:} \ \ h_{\theta}(x) &= \theta_0 + \theta_1 x + \theta_2 x^2 + \theta_3 x^3 + \theta_4 x^4 \\ J(\theta) &= \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2 + \frac{\lambda}{2m} \sum_{j=1}^m \theta_j^2 \end{split}$$

The equation above describes fitting a high order polynomial with regularization (used to keep parameter values small)

Consider three cases

$\lambda = large$

All θ values are heavily penalized

So most parameters end up being close to zero

So hypothesis ends up being close to 0

So high bias --- underfitting data

λ = intermediate

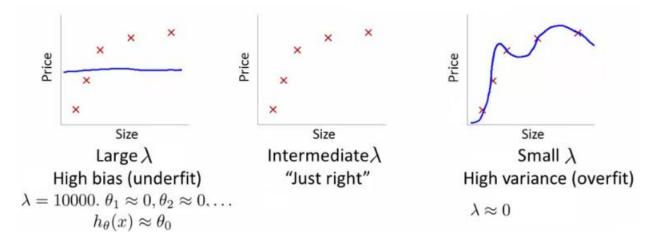
Only this values gives the fitting which is reasonable

$\lambda = small$

Lambda = 0

So we make the regularization term 0

So high variance ---- overfitting data



The effect of lambda on cross validation error and training error can be shown by the following graph

