

## MuMap\_Python

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# Chapter 1

## Namespace Index

### 1.1 Namespace List

Here is a list of all documented namespaces with brief descriptions:

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## Chapter 2

# Class Index

### 2.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

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## Chapter 3

# Namespace Documentation

### 3.1 mumap\_fwd Namespace Reference

#### Classes

- class [EOS](#)
- class [Melt](#)
- class [Poroelasticity](#)
- class [Solid](#)

#### Functions

- def [Moduli\\_to\\_Velocity](#) (G, K, rho)
- def [Velocity\\_to\\_Moduli](#) (vs, vp, rho)
- def [PREM\\_Profile](#) (depth)

#### 3.1.1 Detailed Description

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This module contains classes and functions relevant to calculate the effect of melting on the elastic moduli and seismic wave velocities in partially molten rocks. To run the demonstrations, a working version of Python 2.7.12 or higher, numpy, and matplotlib libraries are required.

Detailed description for each class is provided within the classes. This is an overview of the classes.

**EOS:** Contains functions for equations of state for solids and melts. This class also contains the PREM model of Dziewonski and Anderson (1984). To initiate this class for a given material known values of some parameters need to be provided. In most cases, this class will be initiated from either the Solid or the Melt class, which contain default values for the parameters.

**Solid:** This class contains a number of variables and functions relating to the properties of the solid. All of the parameters are provided with a default value. See the docstring for more details. By default, this class uses the PREM model to evaluate the elastic properties corresponding to the depth parameter provided during instantiation.

**Melt:** This class contains physical parameters for calculating the EOS of the melt. It also defaults to a dihedral angle of 15 degrees. The choice of parameters for the EOS are set by the variable `melt_comp`. Please see the docstring for `__init__` for a full description of the currently available choices.

**Poroelasticity:** This class contains functions for calculating effective elastic properties for a given melt fraction and physical properties of the solid and the melt, contained in those classes. This class contains three choices of contiguity models, see the docstrings for more information. The default model is von Bargen and Waff, which allows for variation in the dihedral angle. Do not use this model for higher melt fractions.

**Example 1:**

Plot Vinet equation of state of MORB using parameters from Guillot and Sator(2007), run `demo2.py` for more plots

```
>>> from mumap import *
>>> import matplotlib.pyplot as plt
>>> rho1=np.linspace(2800.0,4000.0)
>>> melt1=Melt(melt_comp=2,rho=rho1)
>>> melt1.Melt_EOS.Vinet()
>>> plt.plot(melt1.Melt_EOS.P/1.0e9,melt1.Melt_EOS.rho)
>>> plt.show()
```

**Example 2:**

Plot the  $V_s/V_0$  as a function of melt fraction. In this case all the melt resides in films of aspect ratio 0.01. This uses the formulation of Walsh, 1969

```
>>> from mumap import*
>>> import matplotlib.pyplot as plt
>>> phi=np.linspace(1.0e-3,0.15)
>>> rock=Poroelasticity(phi=phi)
>>> rock.Melt=Melt(rho=3200.0)
>>> rock.film(aspect=0.01)
>>> plt.plot(rock.meltfrac,rock.vs_over_v0)
>>> plt.show()
```

**Example 3:**

Plot  $V_s/V_0$  as a function of melt fraction. In this case, the melt geometry is calculated from von Bargen and Waff (1986) and the effective elastic moduli are calculated following Hier-Majumder et al. (2014). Run `demo4.py` for more information.

```
>>> from mumap import *
>>> import matplotlib.pyplot as plt
>>> phi=np.linspace(1.0e-3,0.15)
>>> rock=Poroelasticity(phi=phi)
>>> rock.tube()
>>> plt.show()
```

## 3.1.2 Function Documentation

### 3.1.2.1 `def mumap_fwd.Moduli_to_Velocity( G, K, rho )`

This function calculates  $V_s$  and  $V_p$  from elastic moduli. Please use SI units

**Args:**

G : Shear modulus in Pa  
K : Bulk modulus in Pa  
rho: Density in  $\text{kg/m}^3$

**Returns:**

vs : Shear wave speed in m/s  
vp : P wave speed in m/s

### 3.1.2.2 def mumap\_fwd.PREM\_Profile ( *depth* )

This function is used as the default EOS for solids, unless otherwise chosen. The values of *vs* and *vp* are calculated from the PREM model.

See Table 1 of Dziewonski and Anderson, 1981 for reference

Input:

*depth*: Desired depth ARRAY for calculation, in m

Returns:

*rho* : Density of the solid  
*vs* : Shear wave speed of the solid (m/s)  
*vp* : P wave velocity of the solid (m/s)  
*G* : Shear modulus of the solid (Pa)  
*K* : Bulk modulus of the solid (Pa)  
*nu* : Poisson's ratio of the solid

The returned variables are stored as class attributes

### 3.1.2.3 def mumap\_fwd.Velocity\_to\_Moduli ( *vs*, *vp*, *rho* )

This utility subroutine calculates shear modulus *G*, bulk modulus *K*, and Poisson's ratio *nu*, from known shear and P wave velocities. Please use SI units.

Args:

*vs* : Shear wave speed in m/s  
*vp* : P wave speed in m/s  
*rho*: Density in kg/m<sup>3</sup>

Returns:

*G* : Shear modulus in Pa  
*K* : Bulk modulus in Pa  
*nu*: Poisson's ratio



# Chapter 4

## Class Documentation

### 4.1 mumap\_fwd.EOS Class Reference

#### Public Member Functions

- def `__init__` (self, K0, rho, Kp, rho0)
- def `Vinet` (self)
- def `BM3` (self)
- def `PREM` (self, depth=60.0e3)

#### Public Attributes

- **K0**
- **rho**
- **Kp**
- **rho0**
- **P**
- **K**
- **vs**
- **vp**

#### 4.1.1 Detailed Description

This class contains equations of state to calculate density and elastic moduli of solids and melts

To initiate this class, the following parameters are needed  
Parameters:

K0 : Bulk modulus of the material at surface, in Pa  
rho : Density (kg/m<sup>3</sup>) at the desired condition can be an array  
Kp : Pressure derivative of the bulk modulus  
rho0 : Density (kg/m<sup>3</sup>) at surface

These parameters are used by Vinet and BM3 (Third order Birch-Murnaghan EOS), can be used for both solid and melt. The EOS PREM is for solids only. This class is instantiated within classes Melt and Solid

## 4.1.2 Constructor & Destructor Documentation

### 4.1.2.1 `def mumap_fwd.EOS.__init__( self, K0, rho, Kp, rho0 )`

Initiate the class with known values of density, rho, surface bulk modulus, K0, and the pressure derivative of the bulk modulus, Kp.

## 4.1.3 Member Function Documentation

### 4.1.3.1 `def mumap_fwd.EOS.BM3( self )`

This function uses the third order Birch-Murnaghan EOS to calculate the bulk modulus and pressure for a given density.

Inputs:

```
rho    : Density
rho0   : Surface density
Kp     : Pressure derivative of bulk modulus
K0     : Bulk modulus at surface
```

These inputs are created during instantiation of the class

Returns:

```
P      : Pressure in Pa
K      : Bulk modulus in Pa
```

Both of these are stored as public attributes

### 4.1.3.2 `def mumap_fwd.EOS.PREM( self, depth = 60.0e3 )`

This function is used as the default EOS for solids, unless otherwise chosen. The values of vs and vp are calculated from the PREM model.

See Table 1 of Dziewonski and Anderson, 1981 for reference

Input:

```
depth:  Desired depth for calculation, in m
```

Returns:

```
rho    : Density of the solid
vs     : Shear wave speed of the solid (m/s)
vp     : P wave velocity of the solid  (m/s)
G      : Shear modulus of the solid  (Pa)
K      : Bulk modulus of the solid  (Pa)
nu     : Poisson's ratio of the solid
```

The returned variables are stored as class attributes

### 4.1.3.3 `def mumap_fwd.EOS.Vinet( self )`

This function uses the Vinet EOS to calculate the bulk modulus and pressure for a given density.

Inputs:

```
rho    : Density
rho0   : Surface density
Kp     : Pressure derivative of bulk modulus
K0     : Bulk modulus at surface
```

These inputs are created during instantiation of the class

Returns:

```
P      : Pressure in Pa
K      : Bulk modulus in Pa
```

Both of these are stored as public attributes

The documentation for this class was generated from the following file:

- `/media/sash/23CD-8107/codes/sashcodes/MuMAP/python/mumap_fwd.py`

## 4.2 mumap\_fwd.Melt Class Reference

### Public Member Functions

- `def __init__` (self, theta=20.0, rho=3000.0, melt\_comp=1)

### Public Attributes

- **theta**
- **K0**
- **Kp**
- **rho0**
- **description**
- **rho**
- **Melt\_EOS**
- **P**

### 4.2.1 Detailed Description

This class contains functions and properties of the melt. To initiate the class, the following parameters are needed

Parameters:

```
theta      : degrees, solid-melt dihedral angle
rho        : Melt density (kg/m^3)
melt_comp  : Melt composition for the EOS
```

Pressure of the melt is calculated by using the EOS of choice using the melt\_comp variable.

### 4.2.2 Constructor & Destructor Documentation

#### 4.2.2.1 `def mumap_fwd.Melt.__init__( self, theta = 20.0, rho = 3000.0, melt_comp = 1 )`

This function sets the properties of the melt

See Table 1 of Wimert and Hier-Majumder(2012) for details  
The choices are

```
1 = peridotite melt, (2273 K) Guillot and Sator (2007)
2 = MORB, (2073 K) Guillot and Sator (2007)
3 = peridotite melt, Ohtani and Maeda (2001)
4 = MORB, Ohtani and Maeda (2001)
5 = peridotite+5%CO2 from Ghosh et al (2007)
```

Any other value defaults to 1

The optional value of dihedral angle  
is the second input.

The documentation for this class was generated from the following file:

- `/media/sash/23CD-8107/codes/sashcodes/MuMAP/python/mumap_fwd.py`

## 4.3 mumap\_fwd.Poroelasticity Class Reference

### Public Member Functions

- def [\\_\\_init\\_\\_](#) (self, theta=20.0, phi=0.15)
- def [WHM12](#) (self)
- def [HMRB06](#) (self)
- def [VBW86](#) (self)
- def [set\\_contiguity](#) (self, contiguity\_model=1)
- def [film](#) (self, aspect=0.01)
- def [tube](#) (self)
- def [HH2000\\_Film](#) (self)
- def [HH2000\\_combined](#) (self)

### Public Attributes

- **theta**
- **meltfrac**
- **Contiguity**
- **Melt**
- **Solid**
- **vs\_over\_v0**
- **vp\_over\_v0**
- **K\_over\_K0**
- **G\_over\_G0**
- **aspect**

#### 4.3.1 Detailed Description

This class contains functions and variables relevant to calculating the effective properties for different melt geometries. There are 3 different functions for calculating contiguity, the ratio between the area of grain-grain contact and the surface area of a grain. The result is saved in a variable, `self.Contiguity`.

On initiation, the following variables are created

Parameters

```

theta      : dihedral angle
meltfrac   : Melt volume fraction (between 0 and 1)
Contiguity : Area fraction of grain-grain contact
Melt       : Object melt is created with theta
Solid      : Object solid is created

```

#### 4.3.2 Constructor & Destructor Documentation

##### 4.3.2.1 `def mumap_fwd.Poroelasticity.__init__( self, theta = 20.0, phi = 0.15 )`

Initiates the melt geometry class  
theta is the dihedral angle



### 4.3.3 Member Function Documentation

#### 4.3.3.1 def mumap\_fwd.Poroelasticity.film ( self, aspect = 0.01 )

This function calculates  $V_s/V_{s0}$ ,  $V_p/V_{p0}$ ,  $K/K_0$ , and  $G/G_0$  Based on the model of Walsh, 1969. On input, the aspect ratio is the ratio between the minor and major axis of the elliptical melt inclusion. Subscript 1 is the stronger phase. On return, the four members in the array elastic\_melt are respectively  $V_s/V_{s0}$ ,  $V_p/V_{p0}$ ,  $K/K_0$ , and  $G/G_0$ . Please only enter SI units. Input:

```

    aspect          : Aspect ratio of melt film
Parameters
    self.Solid.K    : Solid bulk modulus
    self.Solid.G    : Solid shear modulus
    self.Solid.rho  : Density of the solid
    self.meltfrac   : Melt volume fraction
Returns:
    vs_over_v0     : Normalized shear velocity
    vp_over_v0     : Normalized P wave velocity
    K_over_K0      : Normalized bulk modulus
    G_over_G0      : Normalized shear modulus

```

#### 4.3.3.2 def mumap\_fwd.Poroelasticity.HH2000\_combined ( self )

This function calculates the S and P wave velocity reduction following the model of Paradigm 2 of Hammonds and Humphreys (2000) It assumes relaxed, random cusped melt geometry. See Table 2 of Hammond and Humphreys (2000) for details. Inputs:

```

    meltfrac       : Melt fraction in the rock
Returns:
    vs_over_v0     : Dimensionless normalized Vs
    vp_over_v0     : Dimensionless normalized vp

```

All variables are stored as public attributes to the class

#### 4.3.3.3 def mumap\_fwd.Poroelasticity.HH2000\_Film ( self )

This function calculates the S and P wave velocity reduction following the model of Paradigm 1 of Hammonds and Humphreys (2000) It assumes relaxed, random cusped melt geometry. See Table 2 of Hammond and Humphreys (2000) for details. Inputs:

```

    meltfrac       : Melt fraction in the rock
Returns:
    vs_over_v0     : Dimensionless normalized Vs
    vp_over_v0     : Dimensionless normalized vp

```

All variables are stored as public attributes to the class

#### 4.3.3.4 def mumap\_fwd.Poroelasticity.HMRB06 ( self )

This function returns the two dimensional measurement of contiguity from Hier-Majumder et al (2006). This is not recommended as it typically returns contiguity values higher than the 3D models. Parameters:

```

    meltfrac       : melt volume fraction
    theta          : semidihedral angle
Returns:
    Contiguity     : Fractional area of grain-grain contact

```

#### 4.3.3.5 `def mumap_fwd.Poroelasticity.set_contiguity ( self, contiguity_model = 1 )`

Calculates contiguity, default is VBW86

#### 4.3.3.6 `def mumap_fwd.Poroelasticity.tube ( self )`

This function calculates the S and P wave velocity reduction following the model of Hier-Majumder et al. (2014)

Inputs:

```
meltfrac      : Melt fraction in the rock
contiguity     : contiguity of the rock
Solid.K        : Bulk modulus of solid
Solid.G        : Shear modulus of solid
Solid.rho      : Density of the solid
Solid.nu       : Poisson's ratio of the Solid
Melt.Melt_EOS.K : Bulk modulus of the melt
Melt.Melt_EOS.rho : Density of the melt
```

Returns:

```
vs_over_v0     : Dimensionless normalized Vs
vp_over_v0     : Dimensionless normalized vp
K_over_K0      : Dimensionless normalized bulk modulus
G_over_G0      : Dimensionless normalized shear modulus
```

All variables are stored as public attributes to the class.

#### 4.3.3.7 `def mumap_fwd.Poroelasticity.VBW86 ( self )`

This function returns the contiguity of a partially molten unit cell as a function of melt volume fraction and dihedral angle, using the parametrization of von Bargen and Waff (1986). Notice that the parameter Agg shouldn't become zero at zero melt fraction, as erroneously indicated in their article. it is fixed by subtracting it from pi to match their Figure 10. Doesn't work beyond melt volume fraction fo 0.18.

Parameters:

```
meltfrac      : melt volume fraction
theta         : semidihedral angle
```

Returns:

```
Contiguity    : Fractional area of grain-grain contact
```

#### 4.3.3.8 `def mumap_fwd.Poroelasticity.WHM12 ( self )`

This function returns the contiguity as a function of melt fraction. The dihedral angle, even taken as an input is currently not used, as the model of Wimert and Hier-Majumder is valid for a constant dihedral angle of approximately 30 degrees. Doesn't work well beyond melt volume fraction of 0.25.

Parameters:

```
meltfrac      : melt volume fraction
```

Returns:

```
Contiguity    : Fractional area of grain-grain contact
```

The documentation for this class was generated from the following file:

- `/media/sash/23CD-8107/codes/sashcodes/MuMAP/python/mumap_fwd.py`

## 4.4 mumap\_fwd.Solid Class Reference

### Public Member Functions

- `def __init__(self, K0=126.3e9, Kp=4.28, G0=78.0e9, Gp=1.71, rho0=2600.0, depth=60.0e3)`

### Public Attributes

- `K0`
- `K`
- `Kp`
- `G0`
- `G`
- `rho0`
- `rho`
- `depth`
- `Solid_EOS`
- `nu`

#### 4.4.1 Detailed Description

This class contains functions and properties of the solid.  
To initiate this class, the following parameters are needed  
Parameters:

```
K0      : Bulk modulus of the material at surface, in Pa
Kp      : Pressure derivative of the bulk modulus
G0      : Shear modulus of the material at surface, in Pa
Gp      : Pressure derivative of the shear modulus
rho0    : Density (kg/m^3) at surface
depth   : m, below the surface
```

By default, solid parameters are evaluated using the PREM model.

#### 4.4.2 Constructor & Destructor Documentation

**4.4.2.1** `def mumap_fwd.Solid.__init__( self, K0=126.3e9, Kp=4.28, G0=78.0e9, Gp=1.71, rho0=2600.0, depth=60.0e3 )`

initiates the class, assigns the values of K0,Kp,G0, and Gp from Abramson et al (1997), Table 4.1 of Poirier's Introduction to the physics of the Earth's interior 2nd ed.  
rho0 is from Prem model. Depth is given 60 km by default  
On initiation, K,G, and nu are given surface values

The documentation for this class was generated from the following file:

- `/media/sash/23CD-8107/codes/sashcodes/MuMAP/python/mumap_fwd.py`



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