

## 1) Recursive language.

A language is Recursive language if there exists a Turing machine, such that the Turing machine accepts all strings in language  $L$  and rejects those strings that are not in language  $L$ . If the string  $w$  is in  $L$ , then it accepts and therefore the Turing machine halts.

- If  $w$  is not in the language  $L$ , then halts without entering the accepting state.
- So any problem on language  $L$  is decidable if it is a recursive language.
- And any language is undecidable if it is not a recursive language.

## 2) Recursive enumerable language

Recursive language or type-0 languages are Recursive languages generated by type-0 grammars. An RE Language can be accepted or recognized by Turing machine which means it will enter into final state for the strings of language and may or may not enter into rejecting state for the strings which are not part of the language.

It means TM can stop for the strings which are not part of the language. Recursive enumerable languages are also called as Turing decidable language.



### 3) Diagonalization language

The diagonalization language, denoted by  $w$  is the set of the strings  $w$ , such that  $w$ , is not in LCM. This  $w$ , consists of all the strings  $w$  such that by Turing machine code  $w$ .

In the given table, if Turing machine accept the string in the  $i$ th row and  $j$ th column in the language (LCM), that means row represents the string that are member of language we will complement the binary string along diagonal and if we add this string is 1000 This and there is now 20300 This would contain  $\epsilon$ .

		1	2	3	4	...
i	1	0	1	1	0	
2	1	1	0	0		
3	0	0	1	1		
4	0	1	0	1		
...	...	...	...	...	...	...



#### 4) Halt problem

The output of TM can be

- Halt the machine will halt state of the machine & finish number of state
- No halt the machine will never halt state no matter how long it was.

Input A Turing machine and on input string a problem. Does the Turing machine finish ~~completing~~ of the string

Proof: At first we will assume that such a Turing machine exists to solve a problem and this machine controls itself we will this Turing machine the output comes ~~out~~ 'yes' otherwise a 'no'

input string	→	Halt Turing machine	yes	[halt]
			No	[no halt]

#### 5) Rice theorem

Theorem

Every non trivial property of recursively enumerable language is undecidable

Proof:

properties of a language is a set of strings for which that Turing machine can be shown which is ultimately non-trivial class for example & property of count all the codes



for the Turing machine such that all  $L(n)$  are  
 context free language it has the property not at  
 least on language and not having the property  
 P. as P is not decidable there should  
 some language L having property P and  
 therefore there must a context Turing  
 Machine accepted language  $L_1$  to  $L_n$  and on the  
 is undecidable if it also Turing Machine  
 The Turing Machine the following thing  
 There exists the most effective machine do  
 next.

