#### **Exercises**

# **Introduction to Verification**

### Exercise Sheet 4 (for 2.5.2023)

### Exercise 4.1

Prove that the language noncontainment problem for finite automata ("Given two finite automata  $\mathcal{A}$  and  $\mathcal{B}$ , does  $L(\mathcal{A}) \not\subseteq L(\mathcal{B})$  hold?") is PSPACE-hard.

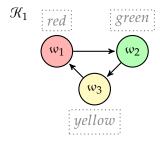
### Exercise 4.2

Prove that the language nonequivalence problem for finite automata ("Given two finite automata  $\mathcal{A}$  and  $\mathcal{B}$ , does  $L(\mathcal{A}) \neq L(\mathcal{B})$  hold?") is PSPACE-complete.

### Exercise 4.3

Consider the following regular properties for *finite paths* of the Kripke structure  $\mathcal{K}_1$  shown below.

- (i) When the traffic light is green, then it will *finally* be red.
- (ii) When the traffic light is green, then it will be red after exactly two steps.
- (iii) Everytime the traffic light is red, it was preceded by a yellow phase.



- (a) For each of the properties (i), (ii), and (iii), give a corresponding finite automaton over the alphabet  $\mathcal{P}(\mathbb{P})$  that expresses the property, where  $\mathbb{P} = \{red, green, yellow\}$ .
- (b) Can you give an algorithm that decides whether some finite path of  $\mathcal{K}_1$  starting in  $\omega_2$  satisfies these properties?
- (c) Do all finite paths of  $\mathcal{K}_1$  starting in  $\omega_2$  satisfy these properties?

# Exercise 4.4

Consider the Kripke structure  $\mathcal{R}_3$  over  $\mathbb{P} = \{p, q, r\}$  depicted below. For the following statements, can you give an algorithm that decides whether  $\mathcal{R}_3$  satisfies them?

- (i) In every path of  $\mathcal{R}_3$ , the propositional variable p always holds true.
- (ii) There is some path in  $\mathcal{K}_3$ , where p is as often true as q is true.
- (iii) It is *always possible* to reach a world where r holds in  $\mathcal{K}_3$ .

