

### What is Statistics?

Statistics is the study of collecting, analyzing, interpreting, and presenting data. It allows us to make sense of data and draw conclusions from it.

**Two Main Areas of Statistics:** 

- 1. Descriptive Statistics: Summarizing and organizing data to describe its key features.
- 2. Inferential Statistics: Drawing conclusions and making predictions about a population based on a sample of data.



### What is Statistics?

## **Descriptive Statistics Basics**

• Mean (Average):

 $\mathrm{Mean} = \frac{\mathrm{Sum\ of\ all\ values}}{\mathrm{Number\ of\ values}}$ 

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**Example: The mean of the numbers** 

$$\frac{2+4+6}{3}=4$$

• Median: The middle value when the data is ordered. Example: The median of 1,3,7,8,9 is 7 (the middle number).



### What is Statistics?

• Variance: A measure of how much the data values differ from the mean.

$$Variance = \frac{\sum (x_i - mean)^2}{n}$$

• Standard Deviation: The square root of the variance, indicating how spread out the data is.

Standard Deviation = 
$$\sqrt{\text{Variance}}$$



### What is Statistics?

#### **Inferential Statistics Basics**

Inferential statistics helps us make predictions or inferences about a population based on a sample of data.

### **Key Concepts:**

- 1. Population vs. Sample:
  - Population: The entire group of individuals or items we want to study.
  - Sample: A subset of the population used to make inferences.
- 1. Hypothesis Testing: A method to test if an assumption about a population is true, using sample data.
  - Null Hypothesis (H0H\_0H0): The default assumption (e.g., no effect or no difference).
  - Alternative Hypothesis (HAH\_AHA): The assumption we want to test (e.g., there is an effect or difference).



### What is Statistics?

## **Probability Distributions**

In statistics and machine learning, understanding probability distributions is critical for analyzing random variables and data behavior.

## **Types of Distributions:**

- 1. Discrete Probability Distributions: Deals with variables that take specific, distinct values.
  - Example: Binomial Distribution (number of successes in a fixed number of trials).
- 2. Continuous Probability Distributions: Deals with variables that can take any value within a range.
  - Example: Normal Distribution (bell-shaped curve, common in nature and machine learning).



What is Statistics?

**Normal Distribution (Gaussian Distribution):** 

The normal distribution is important in AI and statistics because many natural phenomena follow this pattern.

- It is symmetric around the mean.
- Most of the data falls within 1 standard deviation from the mean.

## **Example:**

In a normal distribution with mean 50 and standard deviation 5:

- About 68% of the data falls within 45 to 55 (1 standard deviation).
- About 95% of the data falls within 40 to 60 (2 standard deviations).