

The Basics of Integration

Basic Rules in Integration

Power Rule: For any function $f(x) = x^r$, the integral is:

$$\int x^n\,dx=rac{x^{n+1}}{n+1}+C\quad (n
eq -1)$$

Example: $\int x^2 dx = \frac{x^3}{3} + C$.



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Sum Rule: The integral of a sum of functions is the sum of their integrals:

$$\int [f(x)+g(x)]\,dx = \int f(x)\,dx + \int g(x)\,dx$$

Example:
$$\int (x^2 + 2x) \, dx = \frac{x^3}{3} + x^2 + C$$
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Constant Rule: The integral of a constant times a function is the constant times the integral of the function:

$$\int c \cdot f(x) \, dx = c \int f(x) \, dx$$

Example:
$$\int 3x^2\,dx = 3\cdot \tfrac{x^3}{3} = x^3.$$



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Definite Integral: The integral between two bounds 'a' and 'b' is:

$$\int_a^b f(x)\,dx = F(b) - F(a)$$

Where F(x) is the antiderivative of f(x).