WEEK 3

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Questions

This test exercise is of an applied nature and uses data that are available in the data file TestExer3. We consider the so-called Taylor rule for setting the (nominal) interest rate. This model describes the level of the nominal interest rate that the central bank sets as a function of equilibrium real interest rate and inflation, and considers the current level of inflation and production. Taylor (1993) considers the model:

$$i_t = r^* + \pi_t + 0.5(\pi_t - \pi^*) + 0.5g_t$$

 $it = r^* + \pi t + 0.5(\pi t - \pi^*) + 0.5g_t$

with i_t it the Federal funds target interest rate at time t, r^*r^* the equilibrium real federal funds rate, $\pi_t\pi t$ a measure of inflation, $\pi^*\pi^*$ the target inflation rate and g_t gt the output gap (how much actual output deviates from potential output). We simplify the Taylor rule in two manners. First, we avoid determining r^*r^* and $\pi^*\pi^*$ and simply add an intercept to the model to capture these two variables (and any other deviations in the means). Second, we consider production y_v yy rather than the output gap. In this form the Taylor rule is

$$\begin{aligned} i_t &= \beta_1 + \beta_2 \pi_t + \beta_3 y_t + \epsilon_t \\ it &= \beta 1 + \beta 2 \pi t + \beta 3 y t + \epsilon t (1) \end{aligned}$$

Monthly data are available for the USA over the period 1960 through 2014 for the following variables:

- . INTRATE: Federal funds interest rate
- INFL: Inflation
 PROD: Production
- **PROD**: Production
- UNEMPL: Unemployment
 COMMPRI: Commodity price
- **COMMPRI**: Commodity prices
- PCE: Personal consumption expenditure
- PERSINC: Personal incomeHOUST: Housing starts

Exercise initialization

Loading data...

```
660 obs. of 11 variables:
## 'data.frame':
   $ OBS : Factor w/ 660 levels "1960:1", "1960:10",...: 1 5 6 7 8 9 10 11 12 2 ...
   $ INTRATE: num 3.99 3.97 3.84 3.92 3.85 3.32 3.23 2.98 2.6 2.47 ...
          : num 1.24 1.41 1.52 1.93 1.83 ...
   $ PROD : num 10.037 6.962 4.497 1.506 -0.114 ...
   $ UNEMPL : num 3.42 3.47 2.72 2.8 1.73 ...
##
   $ COMMPRI: num 7.95 -8.56 -16.84 -5.03 -12.44 ...
##
           : num 5.71 5.06 5.56 7.77 4.39 ...
##
   $ PERSINC: num 1.684 1.331 0.892 0.676 0.337 ...
   $ HOUST : num -11.89 -9.84 -31.54 -18.93 -15.15 ...
##
           ##
   $ Month : int 1 2 3 4 5 6 7 8 9 10 ...
```

```
OBS
                  INTRATE
                                   INFL
                                                  PROD
##
   1960:1: 1 Min.: 0.070 Min.:-1.959 Min.:-15.0610
   1960:10: 1 1st Qu.: 3.000 1st Qu.: 1.954 1st Qu.: 0.7964
##
   1960:11: 1
              Median : 5.220 Median : 3.173
                                             Median : 3.3541
##
   1960:12: 1
##
               Mean : 5.348
                              Mean : 3.920
                                             Mean : 2.9246
##
   1960:2: 1
               3rd Qu.: 7.122
                              3rd Qu.: 4.729
                                              3rd Qu.: 5.9683
##
   1960:3 : 1
               Max. :19.100
                              Max.
                                    :14.592
                                             Max.
                                                   : 13.3821
   (Other):654
##
                     COMMPRI
                                       PCE
                                                     PERSTNC
      UNEMPL
##
##
        :-4.9497 Min. :-73.529 Min. :-3.368 Min. :-4.9073
##
   1st Qu.: 0.6991 1st Qu.:-16.926
                                  1st Qu.: 5.031 1st Qu.: 0.9854
##
   Median : 2.0054
                  Median : 1.609
                                  Median : 6.518 Median : 2.1287
##
                  Mean : 4.694
                                   Mean : 6.853 Mean : 2.1392
   Mean : 1.7747
##
   3rd Qu.: 3.0386
                   3rd Qu.: 20.859
                                   3rd Qu.: 8.876
                                                  3rd Qu.: 3.2992
##
                  Max. :241.667
                                   Max.
                                        :13.574 Max. : 7.3561
##
##
      HOUST
                       Year
                                    Month
##
  Min. :-54.797 Min. :1960 Min. : 1.00
   1st Qu.:-11.180 1st Qu.:1973 1st Qu.: 3.75
```

```
## Median: 1.472 Median:1987 Median: 6.50

## Mean: 1.809 Mean:1987 Mean: 6.50

## 3rd Qu:: 13.327 3rd Qu::2001 3rd Qu:: 9.25

## Max.: 96.189 Max.:2014 Max.:12.00

##
```

(a) General-to-specific model

(a) Use general-to-specific to come to a model. Start by regressing the federal funds rate on the other 7 variables and eliminate 1 variable at a time.

General-to-specific regression runs results.

Variable name	regression round #1	regression round #2	regression round #3	
(Constant)	-0.221	-0.291	-0.240	
	se= 0.245	se= 0.236	se= 0.230	
	t= -0.903	t= -1.232	t= -1.042	
	p= 0.367	p= 0.218	p= 0.298	
INFL	0.696	0.693	0.718	
	se= 0.062	se= 0.062	se= 0.057	
	t= 11.185	t= 11.150	t= 12.555	
	p= 0.000	p= 0.000	p= 0.000	
DDOD	0.050	0.005		
PROD	-0.058 se= 0.040	-0.025 se= 0.026		
	t= -1.447	t= -0.989		
	r= -1.447 p= 0.148	p= 0.323		
	ρ- 0.146	ρ- 0.323		
UNEMPL	0.102			
	se= 0.097			
	t= 1.059			
	p= 0.290			
COMMPRI	-0.006	-0.007	-0.008	
	se= 0.003	se= 0.002	se= 0.003	
	t= -1.857	t= -2.308	t= -2.841	
	p= 0.064	p= 0.021	p= 0.005	
PCE	0.344	0.369	0.341	
	se= 0.069	se= 0.066	se= 0.059	
	t= 4.958	t= 5.618	t= 5.756	
	p= 0.000	p= 0.000	p= 0.000	
PERSINC	0.247	0.252	0.240	
	se= 0.061	se= 0.060	se= 0.059	
	t= 4.077	t= 4.162	t= 4.048	
	p= 0.000	p= 0.000	p= 0.000	

Variable name	regression round #1	regression round #2	regression round #3	
HOUST	-0.019 se= 0.005 t= -4.155 p= 0.000	-0.021 se= 0.004 t= -4.760 p= 0.000	-0.021 se= 0.004 t= -4.678 p= 0.000	
R ²	0.6385	0.6379	0.637	
AIC			1.581	
BIC			1.615	

[..] you start with the most general model, including as many variables as are at hand. Then, check whether one or more variables can be removed from the model. This can be based on individual t-tests, or a joint F-test in case of multiple variables. In case you remove one variable at a time, the variable with the lowest absolute t-value is removed from the model. The model is estimated again without that variable, and the procedure is repeated. The procedure continues until all remaining variables are significant.

Variables elimination after regression, one at a time, produced the following results:

- After regression round #1: UNEMPL UNEMPL variable was chosen to be removed,
- After regression round #2: PROD PROD variable was chosen to be removed,
- · After regression round #3: all remaining variables were found to be significant; variables removal stops here.
- (*) The results of all regressions performed during this step, are shown in Appendix A.

Calculating model AIC and BIC:

```
model <- lm(INTRATE ~ INFL + COMMPRI + PCE + PERSINC + HOUST, data = dat)
s <- sqrt(deviance(model)/df.residual(model))
k <- length(model$coefficients) - 1
n <- nrow(dat)
AIC <- log(s^2) + 2 * k / n
BIC <- log(s^2) + k * log(n) / n
print(round(c(AIC, BIC), 4))</pre>
```

```
Conclusion:
```

[1] 1.581 1.615

The general-to-specific process produced the following reduced model:

```
INTRATE = -0.240
+0.718 \cdot INFL
-0.008 \cdot COMMPRI
+0.341 \cdot PCE
+0.240 \cdot PERSINC
-0.021 \cdot HOUST
```

INTRATE=-0.240+0.718·INFL-0.008·COMMPRI+0.341·PCE+0.240·PERSINC-0.021·HOUST

Model characteristics: $R^2 = 0.637$, AIC = 1.581, BIC = 1.615.

(b) Specific-to-general model

(b) Use specific-to-general to come to a model. Start by regressing the federal funds rate on only a constant and add 1 variable at a time. Is the model the same as in (a)?

Specific-to-general regression runs results.

Variable	regressions	regressions	regressions	regressions	regressions	regressions	regression
name	set round #1	set round #2	set round #3	set round #4	set round #5	set round #6	round #7
(Constant)	(different	(different	(different	(different	(different	(different	-0.240
	value per,	value per,	value per,	value per,	value per,	value per,	se= 0.230
	each other	each other	each other	each other	each other	each other	t= -1.042
	variable)	variable)	variable)	variable)	variable)	variable)	p= 0.298
INFL	0.946	(different	(different	(different	(different	(different	0.718
	se= 0.033	value per,	value per,	value per,	value per,	value per,	se= 0.057
	t= 28.93	each other	each other	each other	each other	each other	t= 12.555
	p= 0.000	variable)	variable)	variable)	variable)	variable)	p= 0.000
PROD	-0.016 se= 0.030 t= -0.537 p= 0.592	0.094 se= 0.020 t= 4.805 p= 0.000	0.006 se= 0.022 t= 0.296 p= 0.767	-0.037 se= 0.026 t= -1.506 p= 0.133	-0.046 se= 0.024 t= -1.923 p= 0.055	-0.025 se= 0.026 t= -0.989 p= 0.323	
UNEMPL	0.452 se= 0.070 t= 6.447 p= 0.000	0.336 se= 0.046 t= 7.235 p= 0.000	0.142 se= 0.054 t= 2.638 p= 0.009	0.072 se= 0.061 t= 1.184 p= 0.237	-0.015 se= 0.063 t= -0.239 p= 0.811	-0.004 se= 0.063 t= -0.072 p= 0.943	
COMMPRI	-0.012	-0.005	-0.006	-0.008	-0.008	(different	-0.008
	se= 0.004	se= 0.003	se= 0.003	se= 0.003	se= 0.003	value per,	se= 0.003
	t= -2.75	t= -1.654	t= -2.257	t= -3.173	t= -2.841	each other	t= -2.841
	p= 0.006	p= 0.099	p= 0.024	p= 0.002	p= 0.005	variable)	p= 0.005
PCE	0.829	0.356	0.181	(different	(different	(different	0.341
	se= 0.038	se= 0.041	se= 0.053	value per,	value per,	value per,	se= 0.059
	t= 21.832	t= 8.590	t= 3.412	each other	each other	each other	t= 5.756
	p= 0.000	p= 0.000	p= 0.001	variable)	variable)	variable)	p= 0.000
PERSINC	0.104	0.436	(different	(different	(different	(different	0.240
	se= 0.072	se= 0.046	value per,	value per,	value per,	value per,	se= 0.059
	t= 1.451	t= 9.478	each other	each other	each other	each other	t= 4.048
	p= 0.147	p= 0.000	variable)	variable)	variable)	variable)	p= 0.000
HOUST	-0.031	-0.004	-0.011	-0.022	(different	(different	-0.0210
	se= 0.006	se= 0.004	se= 0.004	se= 0.004	value per,	value per,	se= 0.004
	t= -5.106	t= -0.911	t= -2.733	t= -4.893	each other	each other	t= -4.678
	p= 0.000	p= 0.362	p= 0.006	p= 0.000	variable)	variable)	p= 0.000
R ²							0.637
AIC							1.581
BIC							1.615

The specific to general approach follows the same logic [as the general to specific approach], but starts with a very small model, sometimes even only consisting of the constant term. Variables get added one at a time, choosing the one that has the largest absolute t-statistic. This procedure is repeated until no significant variables can be added anymore.

Variables inclusion (one at a time) after regressions (all possible combinations), produced the following results:

- After regressions set round #1 (with each candidate variable, individually): INFL INFL variable was chosen to be included,
- After regressions set round #2 (with INFL INFL and each other candidate variable combination): PERSINC PERSINC variable was
 chosen to be included as well,
- After regressions set round #3 (with INFL INFL, PERSINC PERSINC and each other candidate variable combination):
 PCE PCE variable was chosen to be included as well,
- After regressions set round #4 (with INFL INFL, PERSINC PERSINC, PCE PCE and each other candidate variable combination): HOUST HOUST variable was chosen to be included as well,
- After regressions set round #5 (with INFL INFL, PERSINC PERSINC, PCE PCE, HOUST HOUST and each other candidate variable combination): COMMPRI COMMPRI variable was chosen to be included as well,
- After regressions set round #6 (with INFL INFL, PERSINC PERSINC, PCE PCE, HOUST HOUST, COMMPRI COMMPRI and
 each other candidate variable combination): all remaining variables (PROD PROD and UNEMPL UNEMPL) were found to be
 insignificant; variables inclusion stops here.
- A final single regression round #7 with all selected variables (INFL INFL, PERSINC PERSINC, PCE PCE, HOUST HOUST, COMMPRI COMMPRI) was run in order to determine the concluded reduced model parameters.
- (*) The results of all regressions performed during this step, are shown in Appendix B.

Calculating model AIC and BIC:

```
model <- lm(INTRATE ~ INFL + PERSINC + PCE + HOUST + COMMPRI, data = dat)
s <- sqrt(deviance(model)/df.residual(model))
k <- length(model$coefficients) - 1
n <- nrow(dat)
AIC <- log(s^2) + 2 * k / n
BIC <- log(s^2) + k * log(n) / n
print(round(c(AIC, BIC), 4))</pre>
```

```
## [1] 1.581 1.615
```

*Conclusion:**

The specific-to-general process produced the following reduced model:

```
INTRATE = -0.240
+0.718 \cdot INFL
-0.008 \cdot COMMPRI
+0.341 \cdot PCE
+0.240 \cdot PERSINC
-0.021 \cdot HOUST
```

INTRATE=-0.240+0.718·INFL-0.008·COMMPRI+0.341·PCE+0.240·PERSINC-0.021·HOUST

Model characteristics: $R^2 = 0.637$, AIC = 1.581, BIC = 1.615.

This is the same reduced model produced with the general-to-specific process, in (a).

(c) Models comparison

(c) Compare your model from (a) and the Taylor rule of equation (1). Consider R^2R2 , AIC AIC and BIC BIC. Which of the models do you prefer?

(*) The results of Taylor rule regression performed during this step, are shown in Appendix C.

Reduced model (a) vs. Taylor rule model.

Variable Reduced model name (a) Talor rule model

Variable	Reduced model	
name	(a)	Talor rule model
(Constant)	-0.240	1.249
	se= 0.230	se= 0.176
	t= -1.042	t= 7.088
	p= 0.298	p= 0.000
INITI	0.740	0.075
INFL	0.718	0.975
	se= 0.057 t= 12.555	se= 0.033 t= 29.785
	p= 0.000	p= 0.000
	ρ- 0.000	μ= 0.000
PROD		0.095
		se= 0.020
		t= 4.805
		p= 0.000
UNEMPL		
COMMPRI	-0.008	
	se= 0.003	
	t= -2.841	
	p= 0.005	
DOE	0.341	
PCE	0.341 se= 0.059	
	t= 5.756	
	p= 0.000	
	ρ- 0.000	
PERSINC	0.240	
	se= 0.059	
	t= 4.048	
	p= 0.000	
HOUST	-0.021	
	se= 0.004	
	t= -4.678	
	p= 0.000	
R ²	0.637	0.575
AIC	1.581	1.727
BIC	1.615	1.740

When comparing models, a lower value of the information criteria is preferred, as we aim for a low standard error of the regression.

Conclusion:

Based on the lower AIC and BIC of the reduced model (a), it is considered better than the Taylor rule model. The reduced model (a) has also a greater R² value than the Taylor rule model, which confirms the conclusion.

(d) Models testing

(d) Test the Taylor rule of equation (1) using the RESET test, Chow break and forecast test (with in both tests as break date January 1980) and a Jarque-Bera test. What do you conclude?

(*) The results of each Taylor rule regression test performed during this step, are shown in Appendix D.

Taylor rule model regression tests.

Test name	Test statistic	p-value	F distribution degr. of freedom	Test result
RESET	F= 2 , 537	0.112	F(1/656)	H_{0} H0: Not rejected
Chow-break	F= 28,735	0.000	F(3/654)	H_0 H0: Rejected
Chow-forecast	F= 5,511	0.000	F(420/237)	H ₀ H0: Rejected
Jarque-Bera	JB= 12,444	0.002	X ² (2)	H ₀ H0: Rejected

^(*) For the Chow tests, year 1980 is used as break-point, because it has been noted (lecture 3.1) that the book-to-market seems to behave somewhat differently after this year.

Conclusion:

The RESET test did not rejected the null hypothesis of correct model specification, however the Chow tests and the Jarque-Bera test rejected the null hypothesis of stability and normality of the residuals.

Conclusively, the Taylor rule model does NOT seem to fit the data very well.

Appendix A

General-to-specific approach regressions run

Results of regression round #1 (with all variables):

```
##
## Call:
## lm(formula = INTRATE ~ INFL + PROD + UNEMPL + COMMPRI + PCE +
##
     PERSINC + HOUST, data = dat)
##
## Residuals:
           1Q Median
##
    Min
                       30
## -7.4066 -1.4340 -0.1175 1.3555 7.7386
##
## Coefficients:
           Estimate Std. Error t value Pr(>|t|)
##
0.102481 0.096757 1.059 0.2899
## UNEMPL
## COMMPRI -0.005521 0.002974 -1.857 0.0638 .
           ## PERSINC
           0.246999 0.060590 4.077 5.13e-05 ***
## HOUST
          ## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.188 on 652 degrees of freedom
## Multiple R-squared: 0.6385, Adjusted R-squared: 0.6346
## F-statistic: 164.5 on 7 and 652 DF, p-value: < 2.2e-16
```

Results of regression round #2 (with UNEMPL UNEMPL variable removed):

```
##
## Call:
## lm(formula = INTRATE ~ INFL + PROD + COMMPRI + PCE + PERSINC +
     HOUST, data = dat)
##
## Residuals:
##
             1Q Median
## -7.5322 -1.4982 -0.1005 1.3882 7.6954
##
## Coefficients:
            Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) -0.290851 0.236016 -1.232 0.2183
## INFL 0.693309 0.062180 11.150 < 2e-16 ***
         ## PROD
## COMMPRI
## PCE
## PERSINC 0.251581 0.060441 4.162 3.57e-05 ***
           ## HOUST
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.188 on 653 degrees of freedom
## Multiple R-squared: 0.6379, Adjusted R-squared: 0.6346
## F-statistic: 191.7 on 6 and 653 DF, p-value: < 2.2e-16
```

Results of regression round #3 (with UNEMPL UNEMPL and PROD PROD variables removed):

```
## Call:
## lm(formula = INTRATE ~ INFL + COMMPRI + PCE + PERSINC + HOUST,
##
     data = dat)
##
## Residuals:
##
     Min
             1Q Median
                          3Q
## -7.1631 -1.5244 -0.1125 1.3715 7.6725
##
## Coefficients:
             Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.240119   0.230366  -1.042   0.29764
            0.717527 0.057152 12.555 < 2e-16 ***
-0.007501 0.002640 -2.841 0.00464 **
## INFL
                       0.059156
             0.340525
                                 5.756 1.32e-08 ***
             ## PERSINC
           ## HOUST
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.188 on 654 degrees of freedom
## Multiple R-squared: 0.6374, Adjusted R-squared: 0.6346
## F-statistic: 229.9 on 5 and 654 DF, p-value: < 2.2e-16
```

Appendix B

Specific-to-general approach regression sets run

Results of regressions set round #1 (with each candidate variable, individually):

```
##
## Call:
## lm(formula = INTRATE ~ INFL, data = dat)
##
## Residuals:
## Min 1Q Median 3Q Max
```

```
## -5.9947 -1.5592 0.0603 1.4990 8.2910

##

## Coefficients:

## Estimate Std. Error t value Pr(>|t|)

## (Intercept) 1.64209 0.15863 10.35 <2e-16 ***

## INFL 0.94534 0.03268 28.93 <2e-16 ***

## ---

## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

##

## Residual standard error: 2.403 on 658 degrees of freedom

## Multiple R-squared: 0.5598, Adjusted R-squared: 0.5591

## F-statistic: 836.6 on 1 and 658 DF, p-value: < 2.2e-16
```

```
## Call:
## lm(formula = INTRATE ~ PROD, data = dat)
## Residuals:
## Min
            1Q Median
                           3Q
                                  Max
## -5.4733 -2.3293 -0.1199 1.8050 13.7859
##
## Coefficients:
##
            Estimate Std. Error t value Pr(>|t|)
## (Intercept) 5.39419 0.16551 32.592 <2e-16 ***
            -0.01592
                      0.02966 -0.537 0.592
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.621 on 658 degrees of freedom
## Multiple R-squared: 0.0004375, Adjusted R-squared: -0.001082
## F-statistic: 0.288 on 1 and 658 DF, p-value: 0.5917
```

```
##
## Call:
## lm(formula = INTRATE ~ UNEMPL, data = dat)
## Residuals:
##
  Min
             1Q Median
                            3Q
                                   Max
## -5.4502 -2.3216 -0.4573 1.9157 14.4183
##
## Coefficients:
##
       Estimate Std. Error t value Pr(>|t|)
## (Intercept) 4.54462 0.18496 24.571 < 2e-16 ***
             0.45247
                       0.07018 6.447 2.21e-10 ***
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.513 on 658 degrees of freedom
## Multiple R-squared: 0.05942,
                                Adjusted R-squared: 0.05799
## F-statistic: 41.57 on 1 and 658 DF, p-value: 2.206e-10
```

```
## Call:
## lm(formula = INTRATE ~ COMMPRI, data = dat)
##
## Residuals:
             1Q Median
                             30
## -6.0892 -2.4343 -0.2646 1.9122 13.8328
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 5.401743 0.141559 38.16 < 2e-16 ***
## COMMPRI -0.011526 0.004191 -2.75 0.00613 **
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.601 on 658 degrees of freedom
## Multiple R-squared: 0.01136, Adjusted R-squared: 0.009859
## F-statistic: 7.562 on 1 and 658 DF, p-value: 0.006125
```

```
##
## Call:
## lm(formula = INTRATE ~ PCE, data = dat)
##
## Residuals:
             1Q Median
                             30
##
    Min
## -6.0034 -2.2094 -0.1965 1.6315 10.9790
##
## Coefficients:
##
             Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.33613   0.28161 -1.194   0.233
                        0.03799 21.832 <2e-16 ***
## PCE
              0.82938
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.758 on 658 degrees of freedom
## Multiple R-squared: 0.4201, Adjusted R-squared: 0.4192
## F-statistic: 476.6 on 1 and 658 DF, p-value: < 2.2e-16
```

```
##
## Call:
## lm(formula = INTRATE ~ PERSINC, data = dat)
## Residuals:
             1Q Median
                             30
##
   Min
## -5.6152 -2.2902 -0.2105 1.7326 13.9662
##
## Coefficients:
##
            Estimate Std. Error t value Pr(>|t|)
## (Intercept) 5.12454 0.20844 24.586 <2e-16 ***
                        0.07186 1.451
            0.10429
                                           0.147
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.616 on 658 degrees of freedom
## Multiple R-squared: 0.003191, Adjusted R-squared: 0.001676
## F-statistic: 2.106 on 1 and 658 DF, p-value: 0.1472
```

```
##
## Call:
## lm(formula = INTRATE ~ HOUST, data = dat)
##
## Residuals:
          1Q Median
##
   Min
                       3Q
                              Max
## -6.950 -2.223 -0.156 1.833 14.152
##
## Coefficients:
             Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 5.403640 0.138710 38.956 < 2e-16 ***
            ## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.552 on 658 degrees of freedom
## Multiple R-squared: 0.03811,
                               Adjusted R-squared: 0.03665
## F-statistic: 26.07 on 1 and 658 DF, p-value: 4.317e-07
```

Results of regressions set round #2 (with INFL INFL and each other candidate variable combination):

```
##
## Call:
## lm(formula = INTRATE ~ INFL + UNEMPL, data = dat)
## Residuals:
              1Q Median
##
  Min
                             30
## -5.1135 -1.7040 -0.0674 1.2620 8.4818
## Coefficients:
##
             Estimate Std. Error t value Pr(>|t|)
                       0.16879 6.653 6.05e-11 ***
## (Intercept) 1.12297
## INFL
              0.92573
                         0.03159 29.300 < 2e-16 ***
                       0.04642 7.235 1.30e-12 ***
## UNEMPL
              0.33581
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.315 on 657 degrees of freedom
## Multiple R-squared: 0.5922, Adjusted R-squared: 0.591
## F-statistic: 477.1 on 2 and 657 DF, p-value: < 2.2e-16
```

```
##
## Call:
## lm(formula = INTRATE ~ INFL + COMMPRI, data = dat)
##
## Residuals:
             1Q Median
                            3Q
##
   Min
## -6.2351 -1.5814 0.0128 1.4972 8.3501
## Coefficients:
             Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 1.682029 0.160251 10.496 <2e-16 ***
                                          <2e-16 ***
              0.940702
                        0.032760 28.715
             -0.004637 0.002803 -1.654 0.0986 .
## COMMPRI
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.4 on 657 degrees of freedom
## Multiple R-squared: 0.5616, Adjusted R-squared: 0.5602
## F-statistic: 420.8 on 2 and 657 DF, p-value: < 2.2e-16
```

```
##
## Call:
## lm(formula = INTRATE ~ INFL + PCE, data = dat)
##
## Residuals:
              10 Median
##
   Min
                             30
## -5.8640 -1.7141 -0.0637 1.5733 7.8959
##
## Coefficients:
             Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 0.10125 0.23417 0.432
                                         0.666
## INFL
              0.71575
                         0.04094 17.483
                                          <2e-16 ***
                       0.04146 8.590 <2e-16 ***
## PCE
              0.35616
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.28 on 657 degrees of freedom
## Multiple R-squared: 0.6042, Adjusted R-squared: 0.603
## F-statistic: 501.5 on 2 and 657 DF, p-value: < 2.2e-16
```

```
## ## Call:
```

```
## lm(formula = INTRATE ~ INFL + PERSINC, data = dat)
## Residuals:
              1Q Median
##
     Min
                             30
## -7.4839 -1.4786 -0.1279 1.4757 7.8344
## Coefficients:
##
             Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.44720 0.19510 2.292 0.0222
                         0.03148 32.156
## INFL
              1.01224
                                         <2e-16 ***
## PERSINC
              0.43597
                        0.04600 9.478
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.256 on 657 degrees of freedom
## Multiple R-squared: 0.6127, Adjusted R-squared: 0.6115
## F-statistic: 519.7 on 2 and 657 DF, p-value: < 2.2e-16
```

```
##
## Call:
## lm(formula = INTRATE ~ INFL + HOUST, data = dat)
##
## Residuals:
               10 Median
##
      Min
                                 30
                                        Max
## -6.1362 -1.5837 0.1037 1.4405 8.2763
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 1.676666 0.163125 10.278 <2e-16 ***
## INFL 0.938290 0.033590 27.934 <2e-16 ***
               -0.003841 0.004215 -0.911
## HOUST
                                                0.362
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.404 on 657 degrees of freedom
## Multiple R-squared: 0.5603, Adjusted R-squared: 0.559
## F-statistic: 418.6 on 2 and 657 DF, p-value: < 2.2e-16
```

Results of regressions set round #3 (with INFL INFL, PERSINC PERSINC and each other candidate variable combination):

```
##
## Call:
## lm(formula = INTRATE ~ INFL + PERSINC + PROD, data = dat)
## Residuals:
           1Q Median
##
                          30
    Min
                                Max
## -7.354 -1.492 -0.136 1.450 7.817
##
## Coefficients:
             Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 0.442226   0.195958   2.257   0.0244 *
             1.013042 0.031616 32.042 < 2e-16 ***
## PERSINC
             0.428021 0.053304 8.030 4.53e-15 ***
             0.006446 0.021800 0.296 0.7675
## PROD
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.257 on 656 degrees of freedom
## Multiple R-squared: 0.6128, Adjusted R-squared: 0.611
## F-statistic: 346 on 3 and 656 DF, p-value: < 2.2e-16
```

```
##
## Call:
## lm(formula = INTRATE ~ INFL + PERSINC + UNEMPL, data = dat)
##
## Residuals:
## Min 1Q Median 3Q Max
## -6.4139 -1.4914 -0.1884 1.3693 7.9992
##
```

```
## Coefficients:
             Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.44625 0.19422 2.298 0.02190 *
                       0.03230 30.705 < 2e-16 ***
## TNFI 0.99164
## PERSINC
             0.35595
                      0.05493 6.480 1.8e-10 ***
             0.14249 0.05402 2.638 0.00854 **
## UNEMPL
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.246 on 656 degrees of freedom
## Multiple R-squared: 0.6168, Adjusted R-squared: 0.615
## F-statistic: 351.9 on 3 and 656 DF, p-value: < 2.2e-16
```

```
## Call:
## lm(formula = INTRATE ~ INFL + PERSINC + COMMPRI, data = dat)
## Residuals:
## Min 1Q Median
                    3Q
## -7.810 -1.438 -0.141 1.448 7.904
##
## Coefficients:
##
           Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.483740 0.195167 2.479 0.0134 *
          1.007126 0.031464 32.009 <2e-16 ***
## PERSINC
           ## COMMPRT
          ## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.249 on 656 degrees of freedom
## Multiple R-squared: 0.6157, Adjusted R-squared: 0.6139
## F-statistic: 350.3 on 3 and 656 DF, p-value: < 2.2e-16
```

```
##
## Call:
## lm(formula = INTRATE ~ INFL + PERSINC + PCE, data = dat)
## Residuals:
##
             1Q Median
   Min
                            30
                                   Max
## -6.8267 -1.5734 -0.1168 1.4852 7.6214
##
## Coefficients:
           Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 0.02122 0.23031 0.092 0.926622
            0.87542
                       0.05083 17.224 < 2e-16 ***
             0.30541 0.05955 5.129 3.85e-07 ***
## PERSTNC
## PCE
             0.18118
                      0.05310 3.412 0.000684 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.238 on 656 degrees of freedom
## Multiple R-squared: 0.6195, Adjusted R-squared: 0.6177
## F-statistic: 356 on 3 and 656 DF, p-value: < 2.2e-16
```

```
##
## Call:
## lm(formula = INTRATE ~ INFL + PERSINC + HOUST, data = dat)
##
## Residuals:
##
           1Q Median
                       30
## -7.7516 -1.4280 -0.1377 1.3543 7.7685
##
## Coefficients:
           Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.482973 0.194586 2.482 0.01331 *
          ## TNFI
           ## PERSINC
## HOUST
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
```

```
## Residual standard error: 2.245 on 656 degrees of freedom
## Multiple R-squared: 0.6171, Adjusted R-squared: 0.6153
## F-statistic: 352.4 on 3 and 656 DF, p-value: < 2.2e-16
```

Results of regressions set round #4 (with INFL INFL, PERSINC PERSINC, PCE PCE and each other candidate variable combination):

```
## Call:
## lm(formula = INTRATE ~ INFL + PERSINC + PCE + PROD, data = dat)
##
## Residuals:
##
     Min
              1Q Median
                           3Q
## -7.4144 -1.5287 -0.1259 1.5313 7.6676
##
## Coefficients:
            Estimate Std. Error t value Pr(>|t|)
0.05645 14.849 < 2e-16 ***
## INFL
             0.83827
## PERSINC
             0.31987
                       0.06026
                                5.308 1.52e-07 ***
## PCE
              0.22432
                       0.06029
                                3.720 0.000216 ***
## PROD
             -0.03694
                       0.02454 -1.506 0.132675
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.236 on 655 degrees of freedom
## Multiple R-squared: 0.6208, Adjusted R-squared: 0.6185
## F-statistic: 268.1 on 4 and 655 DF, p-value: < 2.2e-16
```

```
##
## lm(formula = INTRATE ~ INFL + PERSINC + PCE + UNEMPL, data = dat)
##
## Residuals:
##
              10 Median
                            30
     Min
  -6.4059 -1.5649 -0.1561 1.5020 7.7442
##
## Coefficients:
            Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 0.09932
                      0.23950 0.415 0.6785
## INFL
              0.89023
                       0.05232 17.013 < 2e-16 ***
                      0.06113 4.727 2.79e-06 ***
## PERSINC
             0.28896
             ## PCE
             0.07218 0.06094 1.184
## UNEMPL
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.237 on 655 degrees of freedom
## Multiple R-squared: 0.6203, Adjusted R-squared: 0.618
## F-statistic: 267.5 on 4 and 655 DF, p-value: < 2.2e-16
```

```
##
## Call:
## lm(formula = INTRATE ~ INFL + PERSINC + PCE + COMMPRI, data = dat)
## Residuals:
##
    Min
            1Q Median
                         30
## -7.1468 -1.4614 -0.1224 1.5219 7.6744
##
## Coefficients:
##
            Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.021050 0.229123 -0.092 0.92683
            0.837752   0.051854   16.156   < 2e-16 ***
## INFL
## PERSINC
            ## PCE
           ## COMMPRT
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.222 on 655 degrees of freedom
```

```
## Multiple R-squared: 0.6252, Adjusted R-squared: 0.6229
## F-statistic: 273.2 on 4 and 655 DF, p-value: < 2.2e-16
```

```
## Call:
## lm(formula = INTRATE ~ INFL + PERSINC + PCE + HOUST, data = dat)
##
## Residuals:
     Min
           1Q Median
                        30
## -6.8827 -1.5365 -0.1099 1.3049 7.7022
##
## Coefficients:
##
           Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.213571   0.231416   -0.923   0.356
           ## INFL
           ## PERSINC
           ## HOUST
           ## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.2 on 655 degrees of freedom
## Multiple R-squared: 0.6329, Adjusted R-squared: 0.6306
## F-statistic: 282.3 on 4 and 655 DF, p-value: < 2.2e-16
```

Results of regressions set round #5 (with INFL INFL, PERSINC PERSINC, PCE PCE, HOUST HOUST and each other candidate variable combination):

```
##
## Call:
## lm(formula = INTRATE ~ INFL + PERSINC + PCE + HOUST + PROD, data = dat)
## Residuals:
##
     Min
               1Q Median
                              3Q
## -7.6237 -1.4669 -0.1326 1.3547 7.7370
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) -0.312558   0.236607   -1.321   0.1870
## TNFI
              ## PERSINC
              0.273587
                        0.059881 4.569 5.86e-06 ***
                        0.065818 5.610 2.99e-08 ***
0.004403 -5.039 6.07e-07 ***
## PCE
              0.369249
              -0.022185
## HOUST
              -0.046477 0.024167 -1.923 0.0549
## PROD
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.195 on 654 degrees of freedom
## Multiple R-squared: 0.6349, Adjusted R-squared: 0.6322
## F-statistic: 227.5 on 5 and 654 DF, p-value: < 2.2e-16
```

```
##
## Call:
## lm(formula = INTRATE ~ INFL + PERSINC + PCE + HOUST + UNEMPL,
##
    data = dat)
##
## Residuals:
          1Q Median
                     30
## -6.9710 -1.5410 -0.1044 1.3203 7.7000
##
## Coefficients:
##
          Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.233338  0.245864 -0.949  0.343
          ## INFL
          ## PERSINC
          ## HOUST
          ## UNEMPL
          -0.015013 0.062716 -0.239
                               0.811
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 2.201 on 654 degrees of freedom
## Multiple R-squared: 0.6329, Adjusted R-squared: 0.6301
## F-statistic: 225.5 on 5 and 654 DF, p-value: < 2.2e-16
```

```
##
## Call:
## lm(formula = INTRATE ~ INFL + PERSINC + PCE + HOUST + COMMPRI,
      data = dat)
##
## Residuals:
              1Q Median
##
    Min
                           30
  -7.1631 -1.5244 -0.1125 1.3715 7.6725
##
## Coefficients:
             Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) -0.240119   0.230366  -1.042   0.29764
            ## PERSINC
             0.340525 0.059156 5.756 1.32e-08 ***
## PCE
            -0.020530 0.004389 -4.678 3.52e-06 ***
-0.007501 0.002640 -2.841 0.00464 **
## HOUST
## COMMPRI
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.188 on 654 degrees of freedom
## Multiple R-squared: 0.6374, Adjusted R-squared: 0.6346
## F-statistic: 229.9 on 5 and 654 DF, p-value: < 2.2e-16
```

Results of regressions set round #6 (with INFL INFL, PERSINC PERSINC, PCE PCE, HOUST HOUST, COMMPRI COMMPRI and each other candidate variable combination):

```
##
## Call:
## lm(formula = INTRATE ~ INFL + PERSINC + PCE + HOUST + COMMPRI +
##
    PROD, data = dat)
##
## Residuals:
    Min
            10 Median
                        3Q
##
## -7.5322 -1.4982 -0.1005 1.3882 7.6954
##
## Coefficients:
           Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) -0.290851  0.236016 -1.232  0.2183
         ## INFL
           ## PERSINC
           ## HOUST
          ## COMMPRI -0.006514 0.002822 -2.308 0.0213 *
## PROD
           -0.025460 0.025752 -0.989 0.3232
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.188 on 653 degrees of freedom
## Multiple R-squared: 0.6379, Adjusted R-squared: 0.6346
## F-statistic: 191.7 on 6 and 653 DF, p-value: < 2.2e-16
```

```
##
## Call:
## lm(formula = INTRATE ~ INFL + PERSINC + PCE + HOUST + COMMPRI +
##
     UNEMPL, data = dat)
##
## Residuals:
##
   Min
             1Q Median
                           3Q
## -7.1891 -1.5245 -0.1037 1.3731 7.6719
## Coefficients:
##
            Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.245982 0.244598 -1.006 0.3150
## INFL
```

```
## PERSINC
            0.343138
                    0.069508
                             4.937 1.01e-06 ***
           ## HOUST
           -0.007489 0.002647 -2.830 0.0048 **
## COMMPRT
           -0.004483 0.062494 -0.072 0.9428
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.19 on 653 degrees of freedom
## Multiple R-squared: 0.6374, Adjusted R-squared: 0.634
## F-statistic: 191.3 on 6 and 653 DF, p-value: < 2.2e-16
```

Results of regressions set round #7 (with INFL INFL, PERSINC PERSINC, PCE PCE, HOUST HOUST, COMMPRI COMMPRI included variables):

```
## Call:
## lm(formula = INTRATE ~ INFL + PERSINC + PCE + HOUST + COMMPRI,
     data = dat)
##
## Residuals:
##
           10 Median
    Min
                       30
##
  -7.1631 -1.5244 -0.1125 1.3715 7.6725
##
## Coefficients:
           Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) -0.240119   0.230366  -1.042   0.29764
           ## PFRSTNC
           ## PCE
          ## HOUST
## COMMPRI
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.188 on 654 degrees of freedom
## Multiple R-squared: 0.6374, Adjusted R-squared: 0.6346
## F-statistic: 229.9 on 5 and 654 DF, \, p-value: < 2.2e-16
```

Appendix C

Taylor rule regression run

```
model <- lm(INTRATE ~ INFL + PROD, data = dat)
summary(model)</pre>
```

```
## Call:
## lm(formula = INTRATE ~ INFL + PROD, data = dat)
##
## Residuals:
##
               1Q Median
## -5.1592 -1.6762 0.0141 1.3730 7.9203
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1.24890 0.17619 7.088 3.51e-12 ***
## TNFI
               0.97498
                         0.03273 29.785 < 2e-16 ***
## PROD
               0.09472
                         0.01971
                                   4.805 1.92e-06 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.364 on 657 degrees of freedom
## Multiple R-squared: 0.5747, Adjusted R-squared: 0.5734
## F-statistic: 443.9 on 2 and 657 DF, p-value: < 2.2e-16
```

Calculating Taylor rule AIC and BIC:

```
s <- sqrt(deviance(model)/df.residual(model))
k <- length(model$coefficients) - 1
n <- nrow(dat)
AIC <- log(s^2) + 2 * k / n
BIC <- log(s^2) + k * log(n) / n
print(round(c(AIC, BIC), 4))</pre>
```

```
## [1] 1.7267 1.7403
```

Appendix D

Taylor rule regression tests run

```
model <- lm(INTRATE ~ INFL + PROD, data = dat)
summary(model)</pre>
```

```
##
## Call:
## lm(formula = INTRATE ~ INFL + PROD, data = dat)
##
## Residuals:
            1Q Median
##
     Min
                          30
## -5.1592 -1.6762 0.0141 1.3730 7.9203
##
## Coefficients:
           Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 1.24890 0.17619 7.088 3.51e-12 ***
            ## PROD
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.364 on 657 degrees of freedom
## Multiple R-squared: 0.5747, Adjusted R-squared: 0.5734
## F-statistic: 443.9 on 2 and 657 DF, p-value: < 2.2e-16
```

```
# RESET testing
library(lmtest)
resettest(model, power = 2, type = "fitted", data = dat)
```

```
##
## RESET test
##
## data: model
## RESET = 2.5371, df1 = 1, df2 = 656, p-value = 0.1117
```

```
# Chow break testing
library(gap)
grp <- dat[dat$Year < 1980, ]
x1 <- grp[, c("INFL", "PROD")]; y1 <- data.frame( INTRATE = grp["INTRATE"] )
grp <- dat[dat$Year >= 1980, ]
x2 <- grp[, c("INFL", "PROD")]; y2 <- data.frame( INTRATE = grp["INTRATE"] )
#chow.test
chow.test(y1, x1, y2, x2)</pre>
```

```
## F value d.f.1 d.f.2 P value
## 2.873501e+01 3.000000e+00 6.540000e+02 1.836802e-17
```

- End of document -