Econometrics Test Exercise 4

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Questions

A challenging and very relevant economic problem is the measurement of the returns to schooling. In this question we will use the following variables on 3010 US men:

- logw: log wage
- · educ: number of years of schooling
- age: age of the individual in years
- exper: working experience in years
- smsa: dummy indicating whether the individual lived in a metropolitan area
- . south: dummy indicating whether the individual lived in the south
- nearc: dummy indicating whether the individual lived near a 4-year college
- daded: education of the individual's father (in years)
- momed: education of the individual's mother (in years)

This data is a selection of the data used by D. Card (1995)

(a) Use OLS to estimate the parameters of the model

$$logw = \beta_1 + \beta_2 * educ + \beta_3 * exper + \beta_4 * exper^2 + \beta_5 * smsa + \beta_6 * south + \epsilon.$$

Give an interpretation to the estimated β_2 coefficient.

- **(b)** OLS may be inconsistent in this case as educ and exper may be endogenous. Give a reason why this may be the case. Also indicate whether the estimate in part (a) is still useful.
- (c) Give a motivation why age and age^2 can be used as instruments for exper and $exper^2$.
- (d) Run the first-stage regression for educ for the two-stage least squares estimation of the parameters in the model above when $age, age^2, nearc, daded$, and momed are used as additional instruments. What do you conclude about the suitability of these instruments for schooling?
- **(e)** Estimate the parameters of the model for log wage using two-stage least squares where you correct for the endogeneity of education and experience. Compare your result to the estimate in part (a).
- (f) Perform the Sargan test for validity of the instruments. What is your conclusion?

Exercise initialization

Loading data...

```
dat <- read.csv("../TestExer4_Wage-round1.txt")
#dat
dat$nbr <- 1:nrow(dat)
dat$exper2 <- dat$exper^2
dat$age2 <- dat$age^2
str(dat)</pre>
```

```
## 'data.frame':
                   3010 obs. of 12 variables:
           : num 6.31 6.18 6.58 5.52 6.59 ...
   $ logw
   $ educ
           : int
                  7 12 12 11 12 12 18 14 12 12 ...
                  29 27 34 27 34 26 33 29 28 29 ...
##
   $ age
           : int
   $ exper : int
                  16 9 16 10 16 8 9 9 10 11 ...
##
   $ smsa : int
                  1 1 1 1 1 1 1 1 1 1 ...
   $ south : int 00000000000...
   $ nearc : int
##
                  0001111111...
                  9.94 8 14 11 8 9 14 14 12 12 ...
##
   $ daded : num
   $ momed : num
                 10.2 8 12 12 7 ...
##
   $ nbr
           : int
                  1 2 3 4 5 6 7 8 9 10 ...
                  256 81 256 100 256 64 81 81 100 121 ...
   $ exper2: num
   $ age2 : num 841 729 1156 729 1156 ...
```

```
summary(dat)
```

```
##
         logw
                          educ
                                           age
                                                           exper
           :4.605
                            : 1.00
                                             :24.00
##
   Min.
                     Min.
                                     Min.
                                                      Min.
                                                             : 0.000
##
   1st Qu.:5.977
                     1st Qu.:12.00
                                     1st Qu.:25.00
                                                      1st Qu.: 6.000
   Median :6.287
                     Median :13.00
                                     Median :28.00
                                                      Median : 8.000
##
   Mean
           :6.262
                     Mean
                            :13.26
                                     Mean
                                             :28.12
                                                      Mean
                                                              : 8.856
    3rd Qu.:6.564
                     3rd Qu.:16.00
                                     3rd Qu.:31.00
                                                      3rd Qu.:11.000
##
##
                                                              :23.000
   Max.
           :7.785
                     Max.
                            :18.00
                                             :34.00
                                     Max.
                                                      Max.
##
         smsa
                         south
                                           nearc
                                                             daded
   Min.
                                                                : 0.000
##
           :0.000
                    Min.
                            :0.0000
                                      Min.
                                              :0.0000
                                                        Min.
##
   1st Qu.:0.000
                     1st Qu.:0.0000
                                      1st Qu.:0.0000
                                                        1st Qu.: 8.000
   Median :1.000
                     Median :0.0000
                                      Median :1.0000
                                                        Median : 9.940
##
##
   Mean
           :0.713
                     Mean
                            :0.4037
                                              :0.6821
                                                                : 9.989
                                      Mean
                                                        Mean
##
   3rd Qu.:1.000
                     3rd Qu.:1.0000
                                      3rd Qu.:1.0000
                                                        3rd Qu.:12.000
                            :1.0000
##
   Max.
           :1.000
                     Max.
                                      Max.
                                              :1.0000
                                                        Max.
                                                                :18.000
##
        momed
                          nbr
                                           exper2
                                                              age2
   Min.
           : 0.00
                                              : 0.00
                                                                : 576.0
##
                     Min.
                            :
                                1.0
                                      Min.
                                                        Min.
                     1st Qu.: 753.2
                                      1st Qu.: 36.00
                                                        1st Qu.: 625.0
   1st Qu.: 9.00
##
   Median :11.00
                    Median :1505.5
                                      Median : 64.00
                                                        Median : 784.0
##
##
   Mean
           :10.34
                    Mean
                            :1505.5
                                      Mean
                                              : 95.58
                                                        Mean
                                                                : 800.5
   3rd Qu.:12.00
##
                     3rd Qu.:2257.8
                                      3rd Qu.:121.00
                                                        3rd Qu.: 961.0
##
   Max.
           :18.00
                     Max.
                            :3010.0
                                      Max.
                                              :529.00
                                                        Max.
                                                                :1156.0
```

(a) OLS estimation

(a) Use OLS to estimate the parameters of the model

```
logw = eta_1 + eta_2 * educ + eta_3 * exper + eta_4 * exper^2 + eta_5 * smsa + eta_6 * south + \epsilon.
```

Give an interpretation to the estimated β_2 coefficient.

logw variable regression results (see also Appendix A).

| Variable | Coefficient | Standard Error | t-statistic |
|------------|-------------|----------------|-------------|
| (Constant) | 4.611 | 0.0679 | 67.914 |

| Variable | Coefficient | Standard Error | t-statistic |
|--------------------|-------------|----------------|-------------|
| educ | 0.082 | 0.0035 | 23.315 |
| exper | 0.084 | 0.0068 | 12.377 |
| exper ² | -0.002 | 0.0003 | -6.800 |
| smsa | 0.151 | 0.0158 | 9.523 |
| south | -0.175 | 0.0146 | -11.959 |
| | | | |
| R^2 | 0.2632 | | |

Conclusion:

OLS estimates the following model:

$$logw = 4.611 \\ + 0.082 \cdot educ \\ + 0.084 \cdot exper \\ - 0.002 \cdot exper^{2} \\ + 0.151 \cdot smsa \\ - 0.175 \cdot south$$

Model characteristics: $R^2 = 0.2632$

Estimated β_2 coefficient interpretation:

The 0.082 educ coefficient means that with each additional year of schooling, the log wage increases by about 0.082.

Therefore, with each additional year of schooling the wage increases by about exp(0.082), or by 1.085 or ~8.5%.

(b) Endogeneity insight

(b) OLS may be inconsistent in this case as educ and exper may be endogenous. Give a reason why this may be the case. Also indicate whether the estimate in part (a) is still useful.

It is possible the wage, experience and education variables to be affected by some other variable (i.e. ability, social class, family support, etc.) in a way, such as, a higher ability to lead to a higher wage, longer education and less experience (due to long education) and vice versa.

In this case, these variables would be endogenous and the OLS estimates would be biased and inconsistent, therefore not useful anymore.

(c) Instrument variables motivation

(c) Give a motivation why age and age^2 can be used as instruments for exper and $exper^2$.

Age is obviously exogenous as it cannot be influenced by the people, and it is also obviously related to experience as younger people cannot have a very long experience.

So it's a good instrument for the experience variable. And the same applies for their squared values.

(d) First-stage regression

(d) Run the first-stage regression for educ for the two-stage least squares estimation of the parameters in the model above when $age, age^2, nearc, daded$, and momed are used as additional instruments. What do you conclude about the suitability of these instruments for schooling?

educ variable regression results (see also Appendix B).

| Variable | Coefficient | Standard Error | t-statistic |
|------------------|-------------|----------------|-------------|
| (Constant) | -5.652 | 3.976 | -1.421 |
| age | 0.990 | 0.279 | 3.551 |
| age ² | -0.017 | 0.005 | -3.518 |
| smsa | 0.530 | 0.102 | 5.217 |
| south | -0.425 | 0.091 | -4.667 |
| nearc | 0.265 | 0.099 | 2.670 |
| daded | 0.190 | 0.016 | 12.199 |
| momed | 0.235 | 0.017 | 13.773 |
| | | | |
| R ² | 0.2466 | | |

Conclusions:

First-stage regression is giving the following model:

```
educ = -5.652 \ +0.990 \cdot age \ -0.017 \cdot age^2 \ +0.530 \cdot smsa \ -0.425 \cdot south \ +0.265 \cdot nearc \ +0.190 \cdot daded \ +0.235 \cdot momed
```

Model characteristics: $R^2 = 0.2466$

The additional instruments (age, age^2 , nearc, daded, and momed) are significantly correlated with the education. This is especially true about the later two (daded and momed) due to their high t-statistics, which makes perfect sense as highly educated parents are more likely to support and promote their children education as well.

So, the instrument variables and the endogenous variable educ are significantly related.

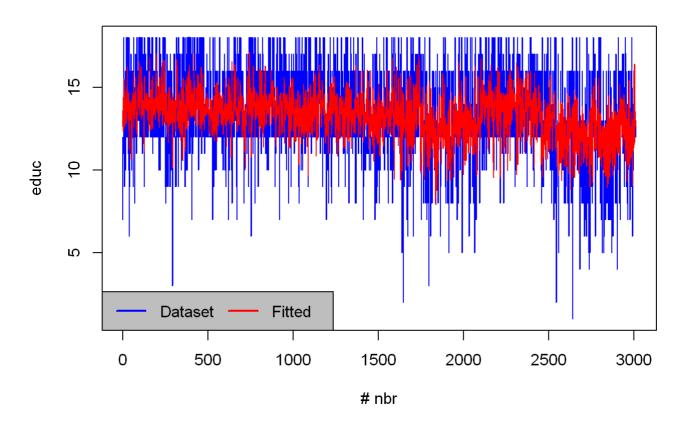
We can use the model estimated in order to compute its fitted values for education, like this:

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 1.00 12.00 13.00 13.26 16.00 18.00
```

summary(dat\$educFIT)

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 7.891 12.560 13.410 13.290 14.170 17.130
```

Education values



(e) Two-stage least squares correction

(e) Estimate the parameters of the model for log wage using two-stage least squares where you correct for the endogeneity of education and experience. Compare your result to the estimate in part (a).

We already run the first-stage regression and estimated fitted values for the educ variable, in (d). We can repeat that process for the exper and $exper^2$ variables:

exper and exper² variables regressions results (see also Appendix C).

| (Constant) -0.348 3.976 -0.087 681.383 84.845 8.031 | |
|---|---|
| | |
| age 0.010 0.279 0.037 -54.065 5.947 -9.091 | |
| age ² 0.017 0.005 3.518 1.280 0.103 12.39 |) |
| smsa -0.530 0.102 -5.217 -11.803 2.166 -5.450 | |
| south 0.425 0.091 4.667 10.615 1.943 5.464 | |
| nearc -0.265 0.099 -2.670 -5.780 2.114 -2.734 | |
| daded -0.190 0.016 -12.199 -3.314 0.333 -9.949 | |
| momed -0.235 0.017 -13.773 -4.733 0.3633 -13.02 | 8 |

| Variable | exper Coefficient | Std.Error | t-stat | exper Coefficient | Std.Error | t-stat |
|----------|----------------------|-----------|--------|----------------------|-----------|--------|
| | | | | | | |
| R^2 | 0.6853 | | | 0.6567 | | |

Conclusions:

First-stage regressions are giving the following models:

exper =
$$-0.348$$

 $+0.010 \cdot age$
 $+0.017 \cdot age^2$
 $-0.530 \cdot smsa$
 $+0.425 \cdot south$
 $-0.265 \cdot nearc$
 $-0.190 \cdot daded$
 $-0.235 \cdot momed$
 $exper^2 = 681.383$
 $-54.065 \cdot age$
 $+1.280 \cdot age^2$
 $-11.803 \cdot smsa$
 $+10.615 \cdot south$
 $-5.780 \cdot nearc$
 $-3.314 \cdot daded$
 $-4.733 \cdot momed$

We can use these models estimated in order to compute their fitted values for exper and $exper^2$, like this:

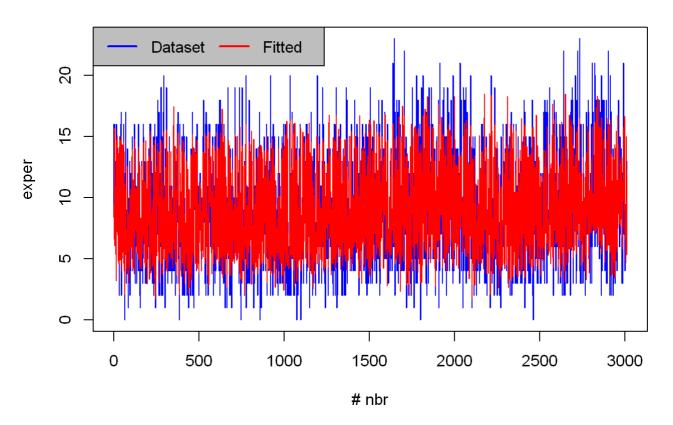
```
dat$experFIT <- -0.348 + 0.010 * dat$age + 0.017 * dat$age2 - 0.530 * dat$smsa +
                 0.425 * dat$south - 0.265 * dat$nearc - 0.190 * dat$daded - 0.235 * dat$mome
summary(dat$exper)
```

```
##
     Min. 1st Qu. Median
                              Mean 3rd Qu.
                                              Max.
##
    0.000
             6.000
                     8.000
                             8.856 11.000 23.000
```

```
summary(dat$experFIT)
```

```
##
     Min. 1st Qu. Median
                             Mean 3rd Qu.
                                            Max.
    1.709
            6.098
                    8.260
                            8.828 11.360 18.470
##
```

Experience values



Then we can perform **the second stage regression**, by replacing the dataset with the fitted values for the variables $e\hat{duc}$, $ex\hat{p}er$ and $ex\hat{p}er^2$ (denoted by the hat symbol):

logw second stage regression results (see also Appendix C).

| Variable | Coefficient | Standard Error | t-statistic |
|-----------------|-------------|----------------|-------------|
| (Constant) | 4.417 | 0.1179 | 37.460 |
| $e \hat{du} c$ | 0.100 | 0.0067 | 14.894 |
| $ex\hat{p}er$ | 0.073 | 0.0171 | 4.255 |
| $\hat{exper^2}$ | -0.002 | 0.0009 | -1.910 |
| smsa | 0.135 | 0.0171 | 7.879 |
| south | -0.159 | 0.0160 | -9.925 |
| | | | |

| Variable | Coefficient | Standard Error | t-statistic |
|----------------|-------------|----------------|-------------|
| R ² | 0.2192 | | |

Conclusion:

2SLS with endogeneity correction for the education and experience, estimates the following model:

$$logw = 4.417 \\ + 0.100 \cdot educ \\ + 0.073 \cdot exper \\ - 0.002 \cdot exper^{2} \\ + 0.135 \cdot smsa \\ - 0.159 \cdot south$$

Model characteristics: $R^2 = 0.2192$

Comparison with part (a) OLS model:

Part (a) OLS model was:

$$egin{aligned} logw = &4.611 \ &+ 0.082 \cdot educ \ &+ 0.084 \cdot exper \ &- 0.002 \cdot exper^2 \ &+ 0.151 \cdot smsa \ &- 0.175 \cdot south \end{aligned}$$

We can see that both models look a bit similar, and that both education and experience still have a positive effect while the squared experience still has a negative effect to logw.

The 2SLS education estimated effect size of about 10% is a bit larger than the OLS estimation of about 8.2%, while the 2SLS experience estimated effect size of about 7.3% is a bit smaller than the OLS estimation of about 8.4%. And both 2SLS and OLS estimated a (small) negative 0.2% effect size for the squared experience variable.

(f) Sargan validity testing

(f) Perform the Sargan test for validity of the instruments. What is your conclusion?

In order to perform the Sargan test, we need to calculate the 2SLS residuals using the original dataset values (not the fitted ones).

```
#model <- lm(formula = logw ~ educ + exper + exper2 + smsa + south, data = dat)
#dat$res2SLS = model$residuals
dat$logw2SLS = 4.417 + 0.100 * dat$educ + 0.073 * dat$exper - 0.002 * dat$exper2 + 0.135 * da
t$smsa - 0.159 * dat$south
dat$res2SLS = dat$logw - dat$logw2SLS
summary(dat$res2SLS)</pre>
```

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## -1.68300 -0.20390 0.05577 0.03108 0.28010 1.35000
```

```
# Store the model coefficients for later usage
model <- lm(formula = logw ~ educFIT + experFIT + exper2FIT + smsa + south, data = dat)
coefs2SLS <- matrix(summary(model)$coefficients[,1])

X = cbind(1, dat$educ, dat$exper, dat$exper2, dat$smsa, dat$south)
colnames(X) <- c('(Intersept)', 'educ', 'exper', 'exper2', 'smsa', 'south')
dat$logw2SLS <- X %*% coefs2SLS
dat$res2SLS = dat$logw - dat$logw2SLS
summary(dat$res2SLS)</pre>
```

```
## V1
## Min. :-1.7486969
## 1st Qu.:-0.2357908
## Median : 0.0270949
## Mean : 0.0005503
## 3rd Qu.: 0.2502512
## Max. : 1.3471109
```

2SLS residuals regression results (see also Appendix D).

| Variable | Coefficient | Standard Error | t-statistic |
|------------------|-------------|----------------|-------------|
| (Constant) | 0.1218 | 0.6568 | 0.185 |
| smsa | -0.0033 | 0.0168 | -0.199 |
| south | 0.0022 | 0.0150 | 0.147 |
| age | -0.0090 | 0.0460 | -0.196 |
| age ² | 0.0002 | 0.0008 | 0.193 |
| nearc | 0.0135 | 0.0164 | 0.825 |
| daded | -0.0041 | 0.0026 | -1.594 |
| momed | 0.0041 | 0.0028 | 1.461 |
| | | | |
| R^2 | 0.00123 | | |

Then, the Sargan test statistic is calculated by multiplying the size of the dataset with the 2SLS residuals regression's R^2 :

```
model <- lm(formula = res2SLS ~ smsa + south + age + age2 + nearc + daded + momed, data = dat
)
sargan.tstat = nrow(dat) * summary(model)$r.squared
sargan.tstat</pre>
```

```
## [1] 3.70242
```

Appendix A

(a) OLS estimation

logw variable regression results:

```
model <- lm(formula = logw ~ educ + exper + exper2 + smsa + south, data = dat)
summary(model)</pre>
```

```
##
## Call:
## lm(formula = logw ~ educ + exper + exper2 + smsa + south, data = dat)
## Residuals:
##
      Min
               1Q
                  Median
                               3Q
## -1.71487 -0.22987 0.02268 0.24898 1.38552
##
## Coefficients:
             Estimate Std. Error t value Pr(>|t|)
## (Intercept) 4.6110144 0.0678950 67.914 < 2e-16 ***
## educ
            0.0815797 0.0034990 23.315 < 2e-16 ***
             ## exper
## exper2
            ## smsa
             0.1508006 0.0158360 9.523 < 2e-16 ***
            -0.1751761 0.0146486 -11.959 < 2e-16 ***
## south
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.3813 on 3004 degrees of freedom
## Multiple R-squared: 0.2632, Adjusted R-squared: 0.2619
## F-statistic: 214.6 on 5 and 3004 DF, p-value: < 2.2e-16
```

Appendix B

(d) First-stage regression

educ variable regression results:

```
model <- lm(formula = educ ~ age + age2 + smsa + south + nearc + daded + momed, data = dat)
summary(model)</pre>
```

```
##
## Call:
## lm(formula = educ ~ age + age2 + smsa + south + nearc + daded +
     momed, data = dat)
##
## Residuals:
      Min
##
              1Q
                  Median
                            3Q
                                  Max
## -11.2777 -1.5450 -0.2224
                         1.6957
                                7.2250
## Coefficients:
            Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) -5.652354 3.976343 -1.421 0.155277
            0.989610 0.278714 3.551 0.000390 ***
## age
## age2
           ## smsa
            -0.424851 0.091037 -4.667 3.19e-06 ***
## south
## nearc
           0.264554 0.099085 2.670 0.007626 **
## daded
           ## momed
            ## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.326 on 3002 degrees of freedom
## Multiple R-squared: 0.2466, Adjusted R-squared: 0.2448
## F-statistic: 140.4 on 7 and 3002 DF, p-value: < 2.2e-16
```

Appendix C

(e) Two-stage least squares correction

exper variable regression results:

```
model <- lm(formula = exper ~ age + age2 + smsa + south + nearc + daded + momed, data = dat)
summary(model)</pre>
```

```
##
## Call:
## lm(formula = exper ~ age + age2 + smsa + south + nearc + daded +
     momed, data = dat)
##
## Residuals:
##
     Min
            1Q Median
                         3Q
                              Max
## -7.2250 -1.6957 0.2224 1.5450 11.2777
##
## Coefficients:
##
            Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.347646 3.976343 -0.087 0.930337
            0.010390 0.278714 0.037 0.970266
## age
## age2
            0.017019 0.004838 3.518 0.000441 ***
## smsa
           0.424851 0.091037 4.667 3.19e-06 ***
## south
           ## nearc
## daded
           ## momed
           ## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.326 on 3002 degrees of freedom
## Multiple R-squared: 0.6853, Adjusted R-squared: 0.6845
## F-statistic: 933.7 on 7 and 3002 DF, p-value: < 2.2e-16
```

exper^2 variable regression results:

```
model <- lm(formula = exper2 ~ age + age2 + smsa + south + nearc + daded + momed, data = dat)
summary(model)</pre>
```

```
##
## Call:
## lm(formula = exper2 \sim age + age2 + smsa + south + nearc + daded +
       momed, data = dat)
##
## Residuals:
      Min
               1Q Median
                              3Q
                                     Max
## -164.28 -27.39
                   -0.20
                           23.05 380.94
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 681.3828 84.8457
                                  8.031 1.38e-15 ***
## age
              -54.0654
                          5.9471 -9.091 < 2e-16 ***
                          0.1032 12.399 < 2e-16 ***
## age2
                1.2799
## smsa
              -11.8031
                          2.1659 -5.450 5.46e-08 ***
                          1.9425
                                  5.464 5.02e-08 ***
## south
               10.6147
               -5.7804
                          2.1142 -2.734 0.00629 **
## nearc
## daded
               -3.3142
                         0.3331 -9.949 < 2e-16 ***
                         0.3633 -13.028 < 2e-16 ***
## momed
               -4.7333
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 49.64 on 3002 degrees of freedom
## Multiple R-squared: 0.6567, Adjusted R-squared: 0.6559
## F-statistic: 820.4 on 7 and 3002 DF, p-value: < 2.2e-16
```

logw second stage regression results:

```
model <- lm(formula = logw ~ educFIT + experFIT + exper2FIT + smsa + south, data = dat)
summary(model)</pre>
```

```
##
## Call:
## lm(formula = logw ~ educFIT + experFIT + exper2FIT + smsa + south,
##
## Residuals:
       Min
                 1Q
                    Median
                                  3Q
                                          Max
## -1.67803 -0.23815 0.01704 0.26700 1.46758
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 4.4171884 0.1179164 37.460 < 2e-16 ***
## educFIT 0.0998308 0.0067029 14.894 < 2e-16 ***
## experFIT
             0.0727341 0.0170952
                                    4.255 2.16e-05 ***
## exper2FIT -0.0016340 0.0008557 -1.910 0.0563 .
               0.1349183 0.0171244
                                    7.879 4.59e-15 ***
## smsa
## south
              -0.1589739 0.0160172 -9.925 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.3925 on 3004 degrees of freedom
## Multiple R-squared: 0.2192, Adjusted R-squared: 0.2179
## F-statistic: 168.7 on 5 and 3004 DF, p-value: < 2.2e-16
```

```
# Store the model coefficients for later usage
coefs2SLS <- matrix(summary(model)$coefficients[,1])</pre>
```

Appendix D

(f) Sargan validity testing

2SLS residuals regression results:

```
model <- lm(formula = res2SLS ~ smsa + south + age + age2 + nearc + daded + momed, data = dat
)
summary(model)</pre>
```

```
##
## Call:
## lm(formula = res2SLS ~ smsa + south + age + age2 + nearc + daded +
      momed, data = dat)
##
## Residuals:
       Min
                1Q Median
                                 3Q
                                        Max
## -1.77692 -0.23319 0.02737 0.25027 1.34299
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.1217866 0.6568267 0.185 0.853
## smsa
            -0.0033287 0.0167668 -0.199 0.843
                                          0.883
## south
              0.0022077 0.0150378 0.147
## age
             -0.0090297 0.0460389 -0.196 0.845
              0.0001543 0.0007991 0.193
## age2
                                           0.847
## nearc
              0.0135069 0.0163672 0.825 0.409
## daded
             -0.0041105 0.0025788 -1.594 0.111
## momed
              0.0041103 0.0028127 1.461
                                         0.144
##
## Residual standard error: 0.3843 on 3002 degrees of freedom
## Multiple R-squared: 0.00123,
                               Adjusted R-squared: -0.001099
## F-statistic: 0.5282 on 7 and 3002 DF, p-value: 0.8138
```

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