

# Approximation of Pi

## Compute $\pi$ value using $p$ processors.

### Integration to evaluate $\pi$

Computer approximations to  $\pi$  by using numerical integration

Know

$$\tan(45^\circ) = 1;$$

same as

$$\tan \frac{\pi}{4} = 1;$$

So that;

$$4 * \tan^{-1} 1 = \pi$$

From the integral tables we can find

$$\tan^{-1} x = \int \frac{1}{1+x^2} dx$$

or

$$\tan^{-1} 1 = \int_0^1 \frac{1}{1+x^2} dx$$

Using the mid-point rule with panels of uniform length  $h = 1/n$ , for various values of  $n$ .

Evaluate the function at the midpoints of each subinterval  $(x_{i-1}, x_i)$   $i * h - h/2$  is the midpoint.

Formula for the integral is

$$x = \sum_{i=1}^n f(h * (i - 1/2))$$

$$\pi = h * x$$

where

$$f(x) = \frac{4}{1+x^2}$$

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```
#include "mpi.h"
#include <math.h>
int main(int argc, char *argv[])
{
    int done = 0, n, myid, numprocs, i, rc;
    double PI25DT = 3.141592653589793238462643;
    double mypi, pi, h, sum, x, a;
    MPI_Init(&argc,&argv);
    MPI_Comm_size(MPI_COMM_WORLD,&numprocs);
    MPI_Comm_rank(MPI_COMM_WORLD,&myid);
    while (!done) {
        if (myid == 0) {
            printf("Enter the number of intervals: (0 quits) ");
            scanf("%d",&n);
        }
        MPI_Bcast(&n, 1, MPI_INT, 0, MPI_COMM_WORLD);
        if (n == 0) break;
```

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```
h    = 1.0 / (double) n;
sum  = 0.0;
for (i = myid + 1; i <= n; i += numprocs) {
    x = h * ((double)i - 0.5);
    sum += 4.0 / (1.0 + x*x);
}
mypi = h * sum;
MPI_Reduce(&mypi, &pi, 1, MPI_DOUBLE, MPI_SUM, 0,
           MPI_COMM_WORLD);
if (myid == 0)
    printf("pi is approximately %.16f, Error is %.16f\n",
           pi, fabs(pi - PI25DT));
}
MPI_Finalize();
return 0;
}
```