

# Comparison of Mixed phase and frequency coded SSVEP and c-VEP BCI

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# Review of last seminar

- Mixed phase and frequency coded SSVEP was proposed in 2014
- It improves the performance of SSVEP BCI
- I did the further experiment,  
frequency detection was succeed, phase detection was failed
  - 32 Targets accuracy : about 20 % (chance level : 3.1 %)
  - Only frequency : about 60 % (chance level : 12.5 % )
  - Only Phase : about 30 % (chance level : 25 %)
- I considered the reasons
  1. The number of training samples were not enough
  2. The channel positions were not optimized for visual stimuli
    - The paper : F3, FZ, F4, CZ, P1, PZ, P2, PO3, POZ, PO4, PO3, O1, OZ, O2, PO8, CPZ
    - My old study : P1, PZ, P2, PO3, POZ, PO4, PO7, O1, OZ, O2, PO8, PO9, O9, IZ, O10, PO10
  3. The images were not checker-board images
  4. The measurement time was too short (single trial : 4 sec)

# Mixed frequency and phase coded SSVEP

- SSVEP problems
  - restricted the number of targets by display refresh rate
  - It has been reported lower ITR compared to c-VEP [1]
- Mixed frequency and phase coded SSVEP [2]
  - 32 targets (8 frequency x 4 phase)
  - Classification method was ensemble of CCA spatial filter
    - It needs training data for phase detection
  - exhibited 166 bits/min
    - It broke the previous record (c-VEP) 144 bits/min
- The paper [2] was not compared ITR with mixed SSVEP and c-VEP in same experimental condition.  
It just compared with the results of papers

[1] G. Bin, X. Gao, Y. Wang, B. Hong, and S. Gao. VEP-based brain- computer interfaces: time, frequency, and code modulations [research frontier]. *Computational Intelligence Magazine, IEEE*, 4(4):22–26, 2009.

[2] A high-speed brain speller using steady-state visual evoked potentials,

M. Nakanishi, *International journal of neural systems*, Vol. 24 Issue 06, 2014

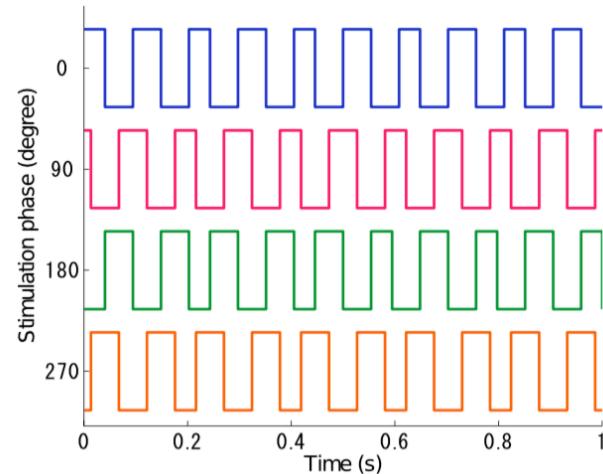
# Mixed Coded SSVEP : Visual Stimuli

- To generate any frequency of visual stimuli, approximate approach [3] was proposed
- Visual stimuli of mixed coded SSVEP is given by

$$S(f, \phi, i) = \text{square} \left[ 2\pi f \left( \frac{i}{\text{RefreshRate}} \right) + \phi \right]$$

- $f$  : Frequency of visual stimuli
- $i$  : frame index
- $\phi$  : initial phase
- `square[]` : generates square wave ([0, 1])

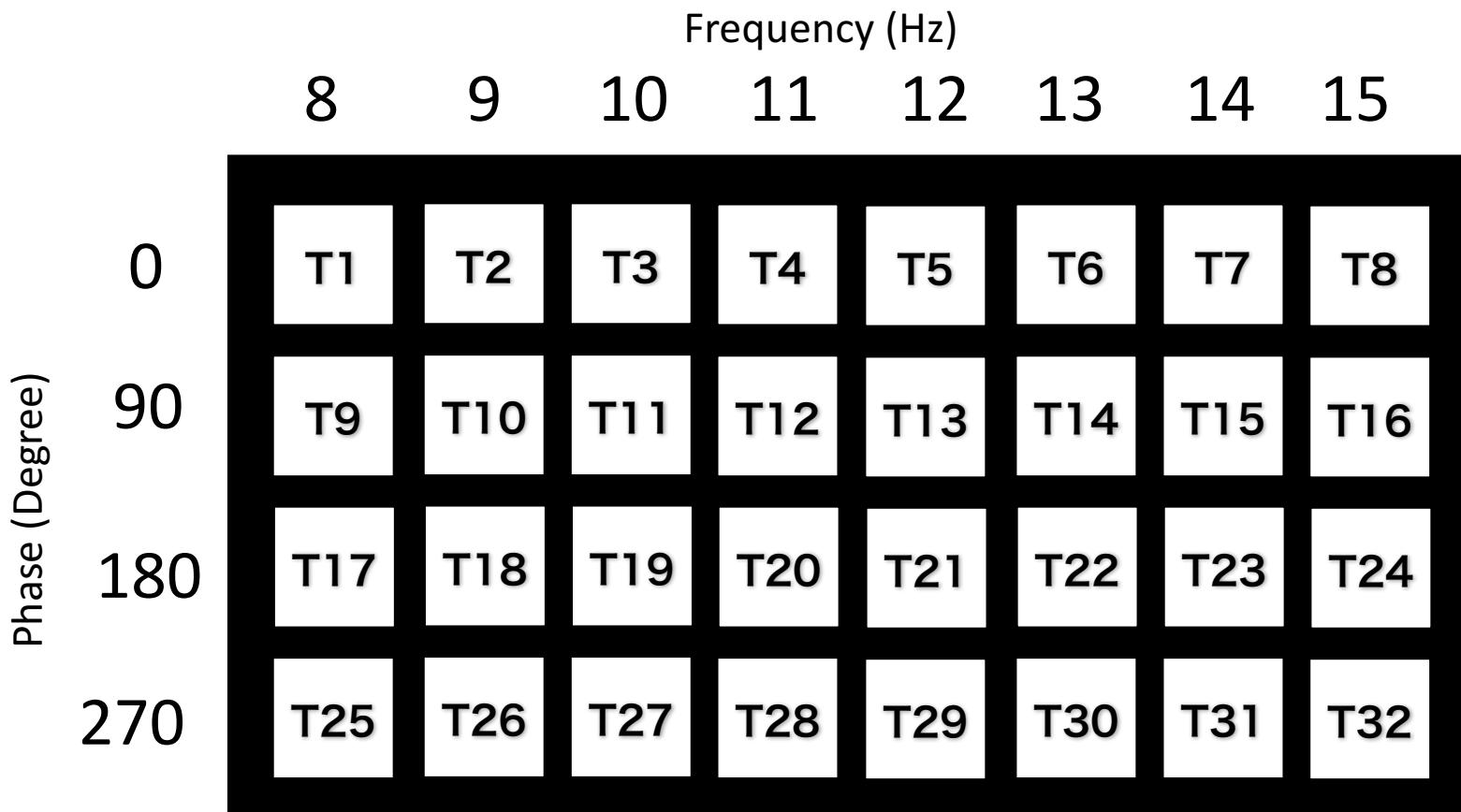
- In the paper, initial phases 0, 90, 180, 270 were used



[3] Y. Wang, Y. T. Wang and T. P. Jung, Visual stimulus design for high-rate SSVEP BCI, Electron. Lett. 46(15) (2010) 1057-1058.

# Mixed Coded SSVEP : Targets alignment

- 32 targets were aligned like below figure



# Normal SSVEP Classification

## Canonical Correlation Analysis (CCA) for SSVEP

- $\mathbf{X}$  : EEG matrix (row : electrodes, columns : times)
- $\mathbf{Y}$  : reference signals

$$\mathbf{Y}_f = \begin{bmatrix} \sin(2\pi f n) \\ \cos(2\pi f n) \\ \vdots \\ \sin(2\pi N_h f n) \\ \cos(2\pi N_h f n) \end{bmatrix}, \quad n = \frac{1}{f_s}, \frac{2}{f_s}, \dots, \frac{N}{f_s}$$

- $f$  : target frequency
- $f_s$  : sampling frequency
- $N_h$  : number of harmonics frequencies
- The weight of spatial filter is given by

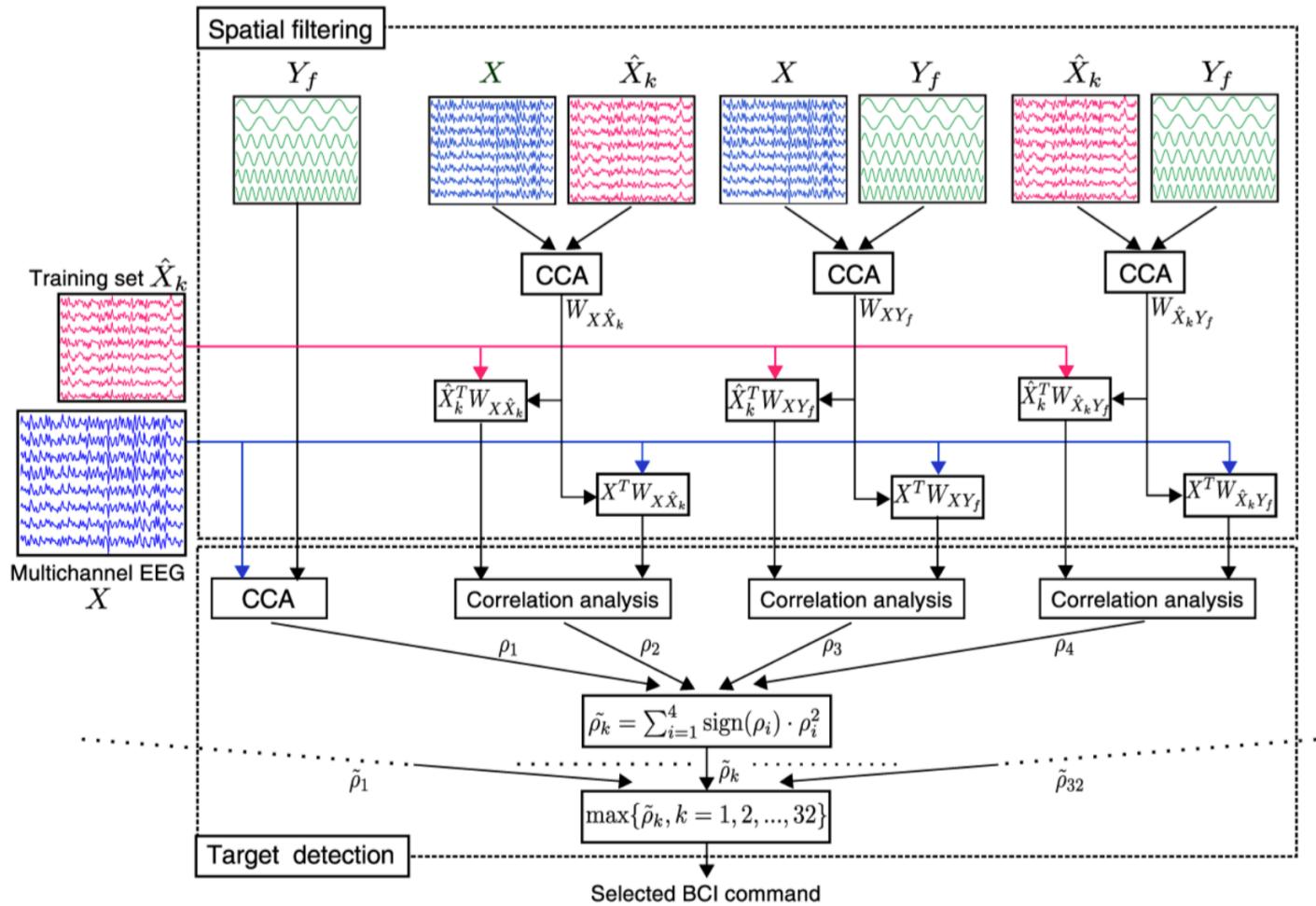
$$\max_{\mathbf{w}_X^T, \mathbf{w}_Y^T} \rho_f = \frac{\mathbf{w}_X^T \mathbf{X} \mathbf{Y}_f^T \mathbf{w}_Y}{\sqrt{\mathbf{w}_X^T \mathbf{X} \mathbf{X}^T \mathbf{w}_X} \sqrt{\mathbf{w}_Y^T \mathbf{Y}_f \mathbf{Y}_f^T \mathbf{w}_Y}}$$

- Correlation coefficient  $\rho$  is used for detecting a command

$$f^* = \operatorname{argmax}_f \rho_f$$

# Mixed Coded SSVEP : Classification (1)

- To detect the phase, averaging EEG  $\hat{X}_k$  ( $k = 1, \dots, 32$ , target number) are used



# Mixed Coded SSVEP : Classification (2)

$$\boldsymbol{\rho} = \begin{bmatrix} \rho_1 \\ \rho_2 \\ \rho_3 \\ \rho_4 \end{bmatrix} = \begin{bmatrix} \rho(X^T \mathbf{w}_{XY} \mathbf{Y}_f^T \mathbf{w}_{XY}) \\ \rho(X^T \mathbf{w}_{X\hat{X}}, \hat{X}^T \mathbf{w}_{X\hat{X}}) \\ \rho(X^T \mathbf{w}_{XY}, \hat{X}^T \mathbf{w}_{XY}) \\ \rho(X^T \mathbf{w}_{\hat{X}Y}, \hat{X}^T \mathbf{w}_{\hat{X}Y}) \end{bmatrix}$$

- M1 :  $\rho_1$ , Normal SSVEP Classification
- M2 :  $\rho_2$ , Spatial filter between test and training
- M3 :  $\rho_3$ , Spatial filter between test and sin-cos reference
- M4 :  $\rho_4$ , Spatial filter between training and sin-cos reference
- M5 :  $\tilde{\rho}$ , combined decision,

$$\tilde{\rho} = \sum_{i=1}^4 \text{sign}(\rho_i) \cdot \rho_i^2$$

Reduction of calculation cost

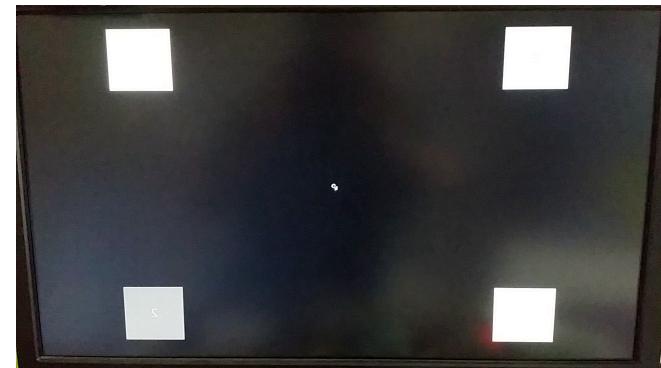
- In M1 and M4, same spatial filter was used
- $\mathbf{Y}_f = \mathbf{Y}_{\text{mod}(k-1, 8)+8}$  ( $k = 1, \dots, 32$ )

# Preliminary experiments

- I did five experiments to investigate why phase detection was failed
  - The electrodes were positioned at
    - P1, PZ, P2, PO3, POZ, PO4, PO7, O1, OZ, O2, PO8, PO9, O9, IZ, O10, PO10
1. 4 commands SSVEP (32 targets remain)
    - Increasing the training samples (40 samples)
  2. 4 command SSVEP (Displayed 4 targets, same frequency)
    - Increasing the training samples (40 samples)
    - Eliminate the effect of other targets



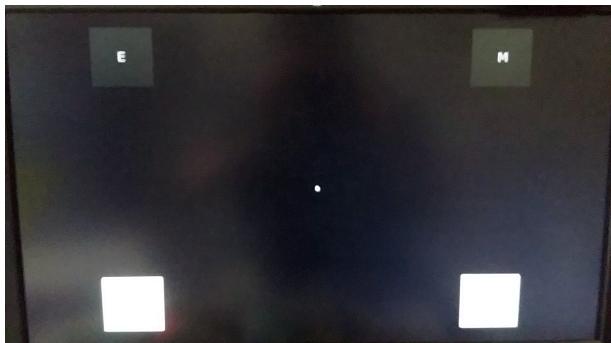
ex. 1



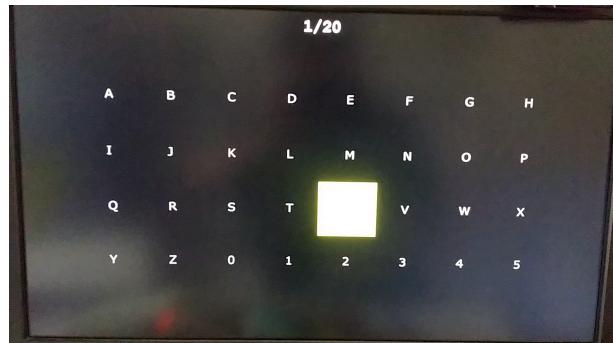
ex. 2

# Preliminary experiments

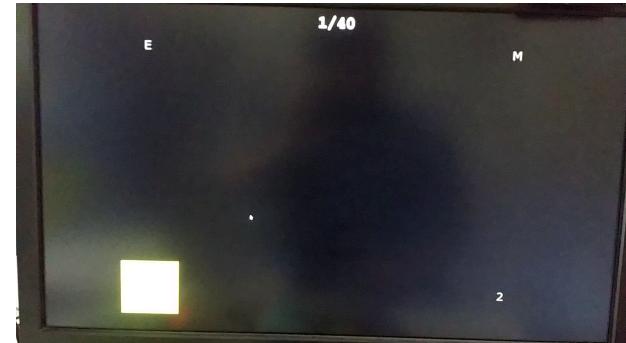
3. 4 commands c-VEP
  - almost same as ex. 2, stimuli was replaced m-sequences
4. 32 commands c-VEP
  - my old experiment
5. 4 commands SSVEP (Displayed 4 targets, same frequency), each measurement is divided



ex. 3



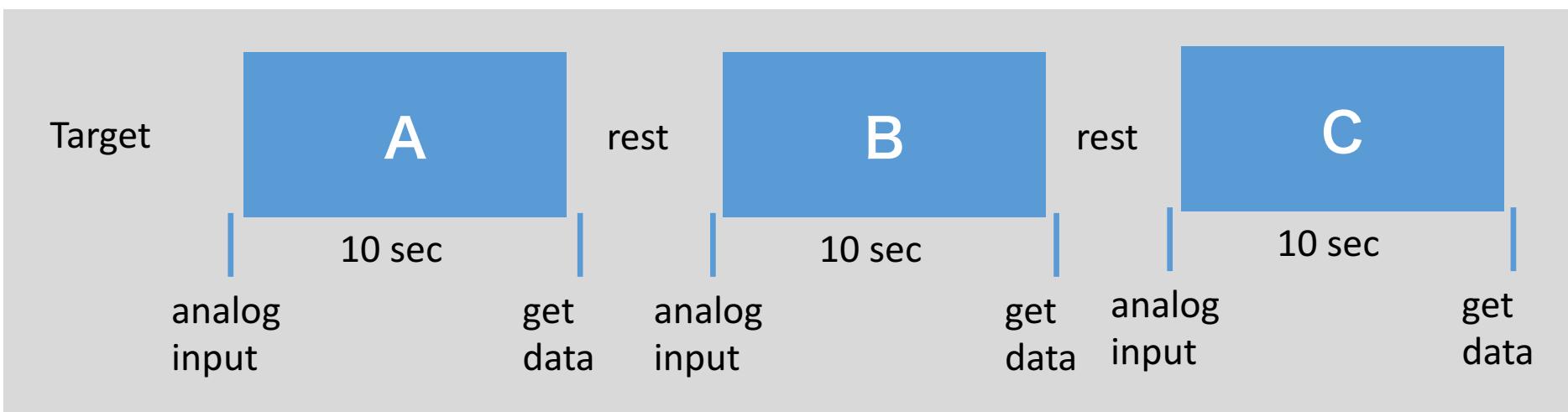
ex. 4



ex. 5

# Measurement

Measurement is divided



Measurement is not divided



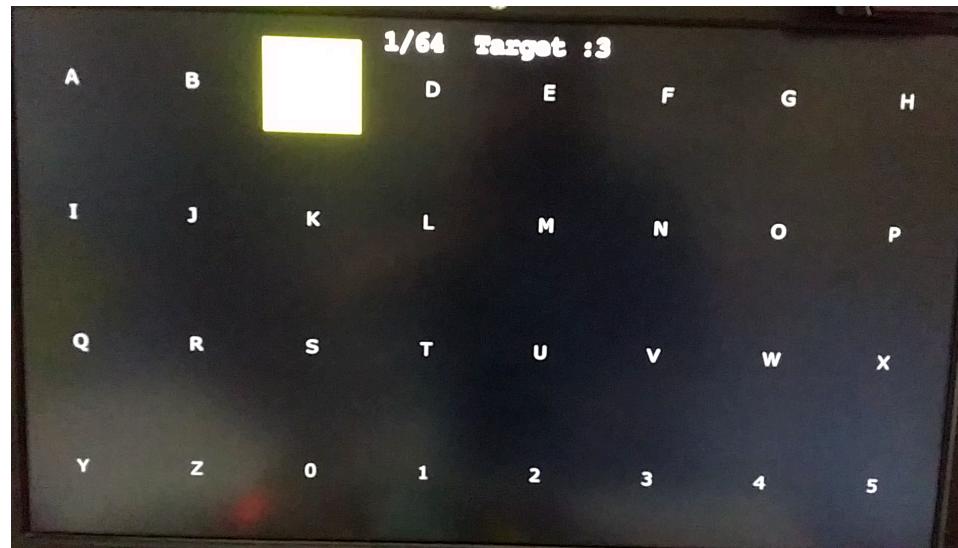
# Preliminary experiments : Results and Discussions

- ex. 1 and ex. 2 was failed  
→ the number of trainings is the reasons
- The classification of four command c-VEP (ex. 3) was failed
- However, old c-VEP experiment (ex. 4) was succeeded
- **whether measurement is divided or not is the factor**
- When measurement time is long, it may become unstable

|       | <b>type</b> | <b>commands</b> | <b>measurement was divided</b> | <b>Accuracy</b> |
|-------|-------------|-----------------|--------------------------------|-----------------|
| ex. 1 | SSVEP       | 4               | false                          | 0.35            |
| ex. 2 | SSVEP       | 4               | false                          | 0.30            |
| ex. 3 | c-VEP       | 4               | false                          | 0.26            |
| ex. 4 | c-VEP       | 32              | true                           | 0.94            |
| ex. 5 | SSVEP       | 4               | true                           | 0.95            |

# Experiment : mixed-coded SSVEP VS c-VEP

- I compared mixed-coded SSVEP with c-VEP at same experimental condition
- SSVEP or c-VEP stimuli is randomly displayed
- One run : 64 targets (SSVEP:32, c-VEP:32)
- Six runs were carried out ( $6 \times 32 = 192$  targets)
- Single target was recorded for 4 seconds
  - It recorded 5 seconds,  
first 0.5 sec and last 0.5 sec were removed after filtered
- Beginning of each trial, yellow rectangle appeared



# c-VEP : classification

## CCA spatial filter

- $X_k$  :  $k$  trial training EEG matrix
- $R = \frac{1}{K} \sum_{k=1}^K X_k$

$$\max_{\mathbf{w}_X, \mathbf{w}_R} \frac{\mathbf{w}_X^T \mathbf{X} \mathbf{R}^T \mathbf{w}_R}{\sqrt{\mathbf{w}_X^T \mathbf{X} \mathbf{X}^T \mathbf{w}_X} \sqrt{\mathbf{w}_R^T \mathbf{R} \mathbf{R}^T \mathbf{w}_R}}$$

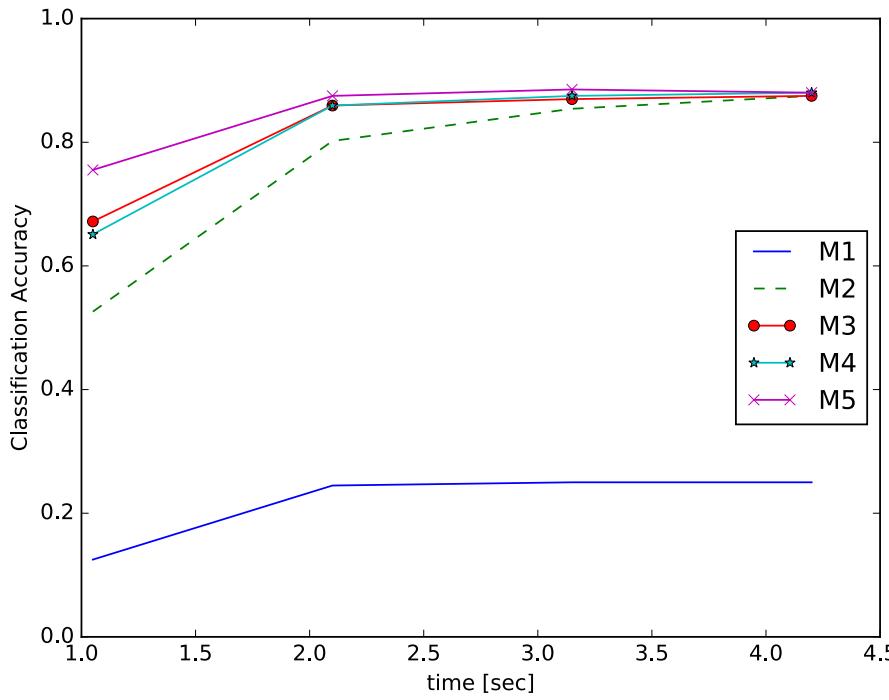
## Template matching

- In conventional c-VEP research, templates were generated by circular shifting of averaged signal
- In this experiment, training and testing was not separated. Template  $T_k[t]$  is generated by averaged signal of target  $k$  **without circular shifting**
- The target is estimated by

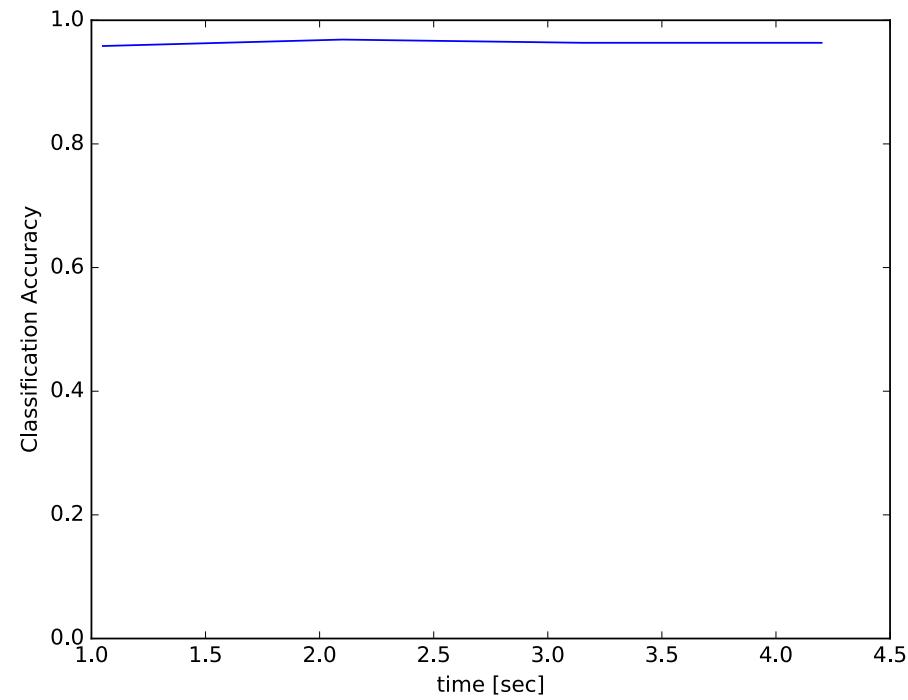
$$\operatorname{argmax}_k \frac{\sum_{t=0}^{T-1} T_k[t] x[t]}{\sqrt{\sum_{t=0}^{T-1} T_k^2[t]} \sqrt{\sum_{t=0}^{T-1} x^2[t]}}$$

# mixed coded SSVEP vs c-VEP : Accuracy

- Leave one out : (the number of samples was 192)
- mixed coded SSVEP : 0.8802
- c-VEP : **0.9635**
- c-VEP was obviously better than mixed coded SSVEP



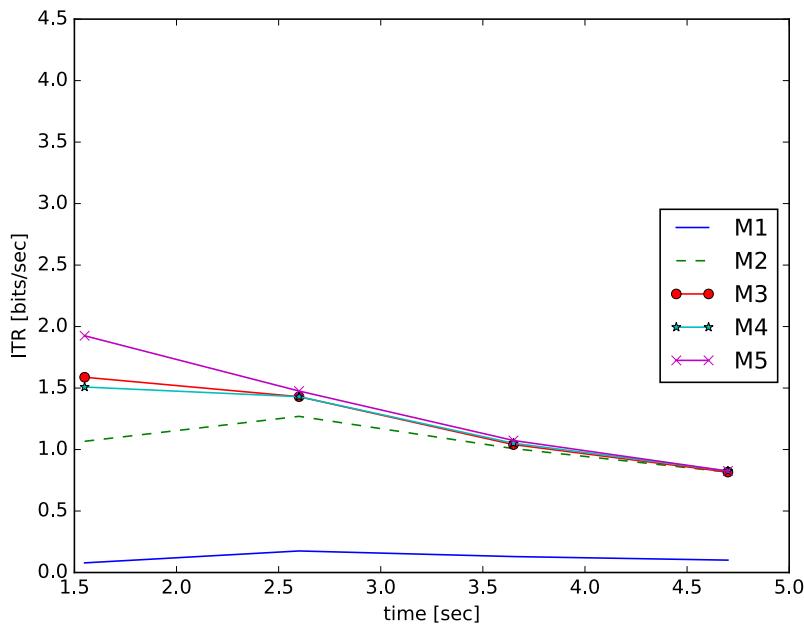
mixed coded SSVEP



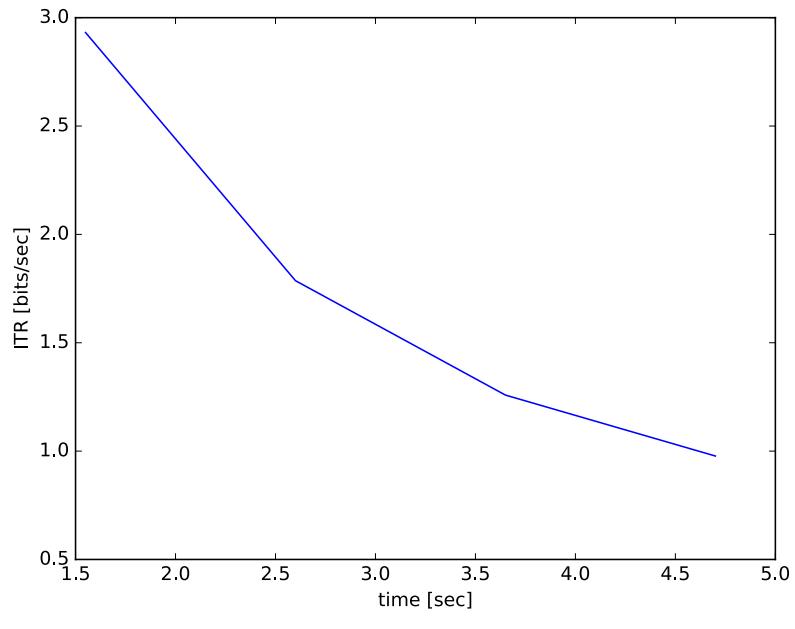
c-VEP

# mixed coded SSVEP vs c-VEP : ITR

- To compare [2], The time contains the gaze shifting time (0.5 sec)
- mixed coded SSVEP : 1.92 [bit/sec] (at 1.05 sec + 0.5 sec, M5)
- c-VEP : **2.93 [bit/sec]** (at 1.05 + 0.5 sec sec)



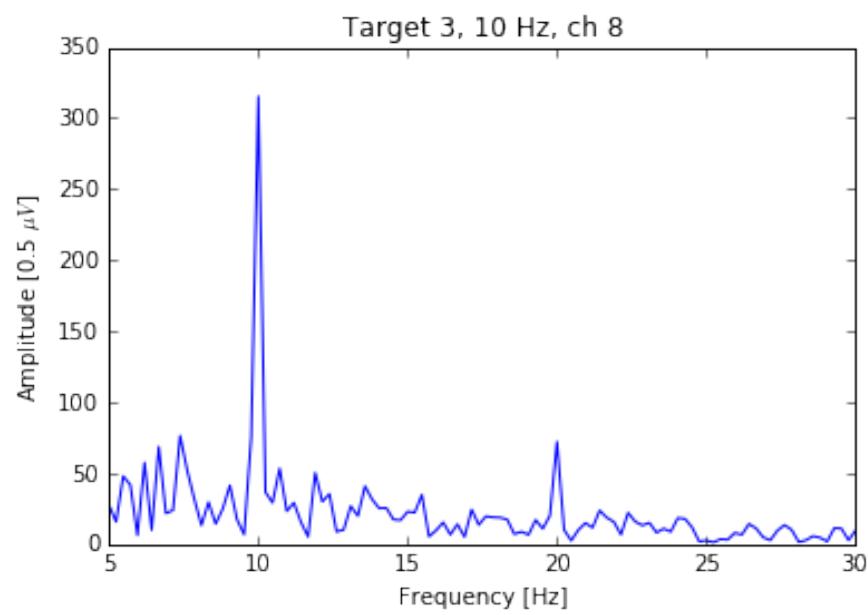
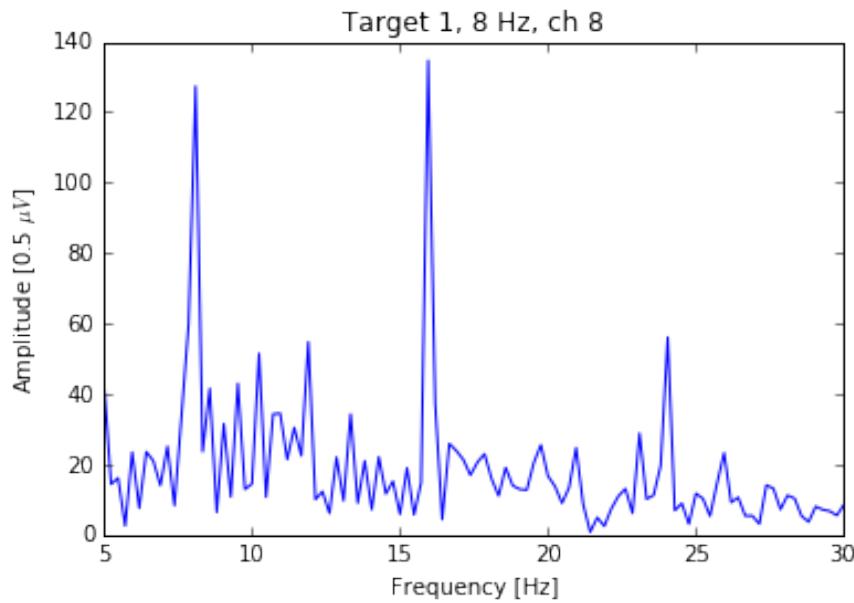
mixed coded SSVEP



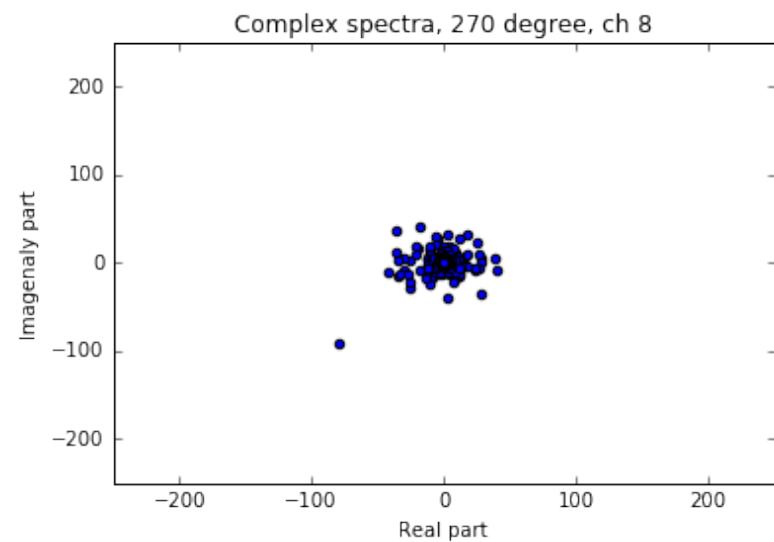
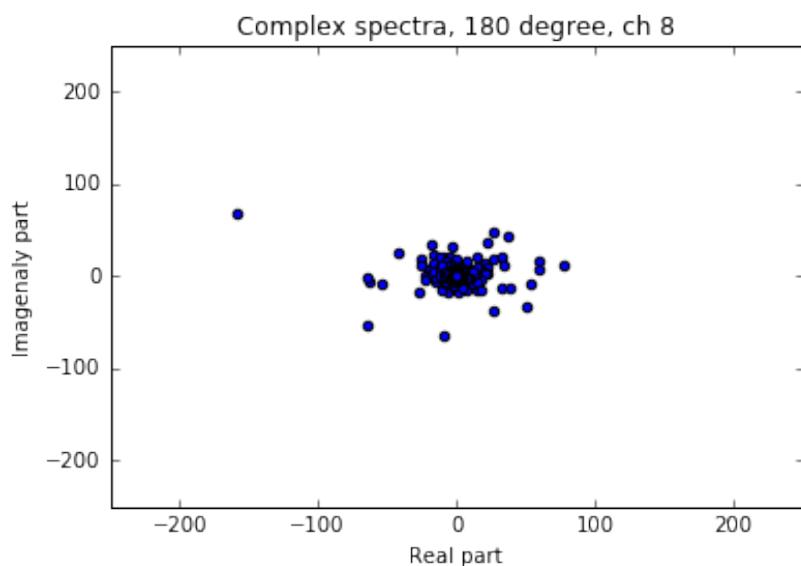
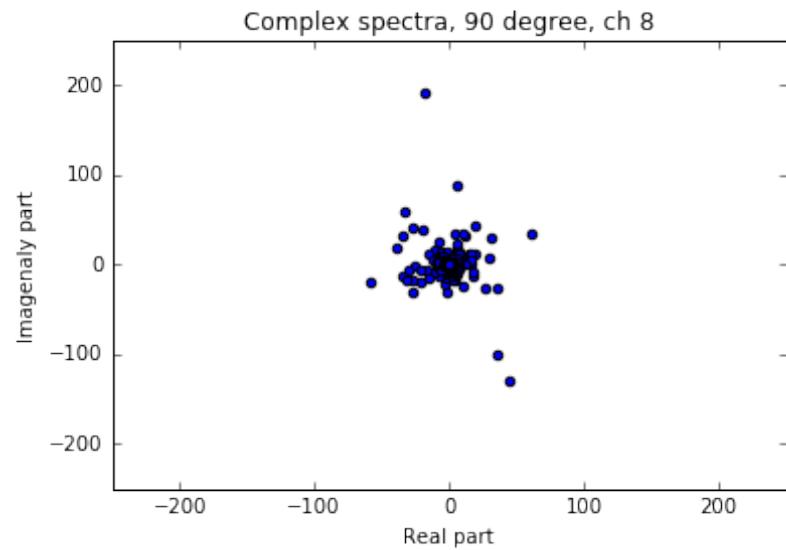
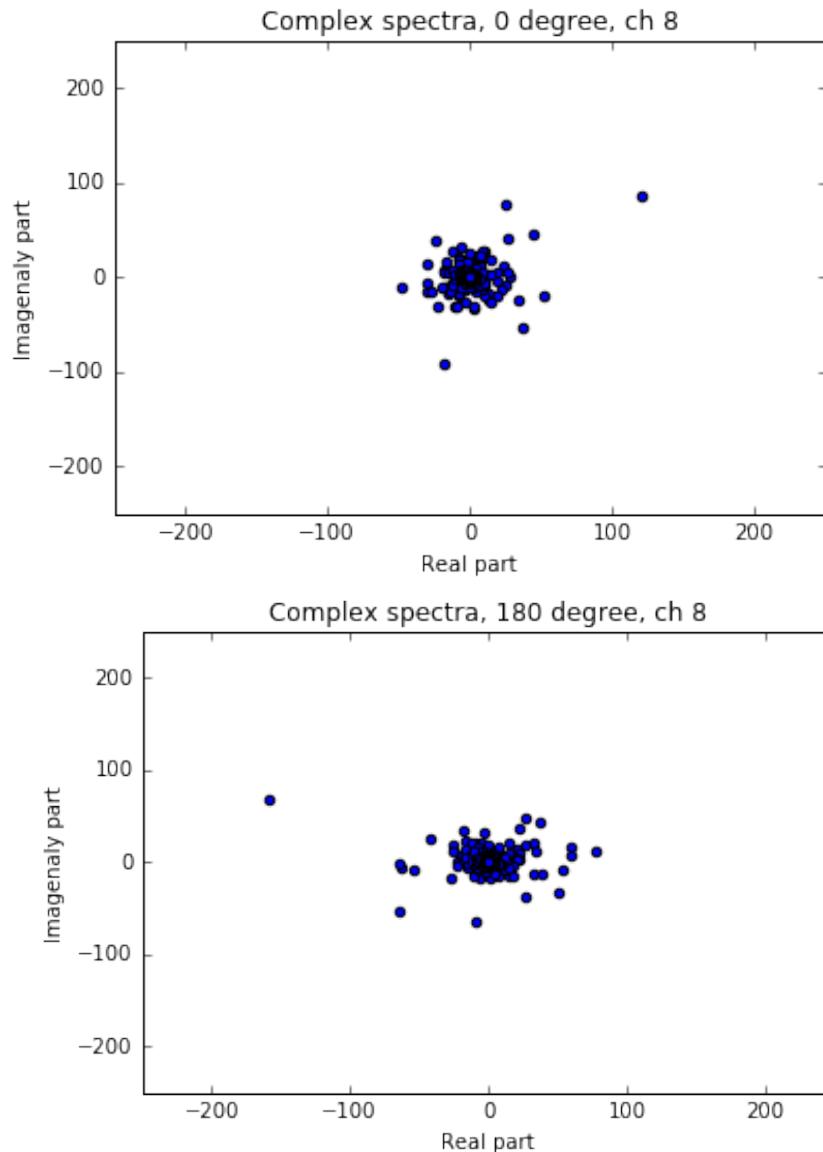
c-VEP

# Spectrum Analysis

- The target frequency components was observed clearly



# Mixed coded SSVEP : Complex spectra



# Optimized combined decision : Logistic Regression

- Optimized weight  $w_i$  is given by logistic regression

$$\tilde{\rho}_k = \sum_{i=0}^4 w_i \cdot \rho_i^{(k)}$$

- $\rho_0 = 1$  : bias
  - $k : k = 1, \dots, 32$ , target index
  - label  $t_n$ :
    - when  $k$  is the gazed target  $t_n = 1$
    - when  $k$  is not the gazed target  $t_n = 0$
- The probability is given by

$$p_k = \frac{1}{1 + \exp(-\tilde{\rho}_k)}$$

- Predicted label is,

$$\operatorname{argmax}_k p_k$$

# Optimized combined decision : Logistic Regression (2)

- Experiment
  - training and test were divided into two (hold out, not cross validation)
- M5 (conventional)
  - 89.58 %
- Logistic Regression (Proposed)
  - 85.50 %
- Proposed method is lower than M5,  
We need to do cross validation

# Discussion

- In the paper [2], the average of offline classification accuracy was 88.8 % (at 1 sec), ITR was 161 [bits/min] (2.68 [bits/sec])
- My result of SSVEP is lower than the paper [2],  
This is caused by
  - Electrodes condition (8~16 ch were not good)
  - The number of trainings is few (paper [2] : 7 runs, my experiment : 6 runs)
  - Individual differences
- In the paper [2], online experiment was also compared,  
I should do online experiment
- In c-VEP experiment, I used conventional CCA spatial filter,  
I can use my old research filters (CCF, Neural decoding) to improve the performance

# Conclusion and future works

## Conclusion

- I did experiments of Mixed frequency and phase coded SSVEP and c-VEP
- In the experiment, c-VEP exhibits higher accuracy and ITR than mixed coded SSVEP

## Future works

- More subjects
- Online experiment