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AES-GCM-SIV: Nonce Misuse-Resistant Authenticated Encryption

Abstract

This memo specifies two authenticated encryption algorithms that are nonce misuse resistant — that is, they do not fail catastrophically if a nonce is repeated.

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Table of Contents

1.	Introduction	2
2.	Requirements Language	3
3.	POLYVAL	3
4.	Encryption	4
5.	Decryption	7
6.	AEADs	10
7.	Field Operation Examples	10
8.	Worked Example	10
9.	Security Considerations	11
10.		14
11.	References	14
11	1.1. Normative References	14
11	1.2. Informative References	15
Appe	endix A. The Relationship between POLYVAL and GHASH	17
Appe	endix B. Additional Comparisons with AES-GCM	19
Appe	endix C. Test Vectors	20
	.1. AEAD_AES_128_GCM_SIV	20
	.2. AEAD_AES_256_GCM_SIV	30
С.	.3. Counter Wrap Tests	41
	nowledgements	42
		42

1. Introduction

The concept of Authenticated Encryption with Additional Data (AEAD) [RFC5116] couples confidentiality and integrity in a single operation, avoiding the risks of the previously common practice of using ad hoc constructions of block-cipher and hash primitives. The most popular AEAD, AES-GCM [GCM], is seeing widespread use due to its attractive performance.

However, some AEADs (including AES-GCM) suffer catastrophic failures of confidentiality and/or integrity when two distinct messages are encrypted with the same key and nonce. While the requirements for AEADs specify that the pair of (key, nonce) shall only ever be used once, and thus prohibit this, this is a worry in practice.

Nonce misuse-resistant AEADs do not suffer from this problem. For this class of AEADs, encrypting two messages with the same nonce only discloses whether the messages were equal or not. This is the minimum amount of information that a deterministic algorithm can leak in this situation.

This memo specifies two nonce misuse-resistant AEADs: AEAD_AES_128_GCM_SIV and AEAD_AES_256_GCM_SIV. These AEADs are designed to be able to take advantage of existing hardware support for AES-GCM and can decrypt within 5% of the speed of AES-GCM (for multikilobyte messages). Encryption is, perforce, slower than AES-GCM, because two passes are required in order to achieve that nonce misuse-resistance property. However, measurements suggest that it can still run at two-thirds of the speed of AES-GCM.

We suggest that these AEADs be considered in any situation where nonce uniqueness cannot be guaranteed. This includes situations where there is no stateful counter or where such state cannot be guaranteed, as when multiple encryptors use the same key. As discussed in Section 9, it is RECOMMENDED to use this scheme with randomly chosen nonces.

This document represents the consensus of the Crypto Forum Research Group (CFRG).

2. Requirements Language

The key words "MUST", "MUST NOT", "REQUIRED", "SHALL", "SHALL NOT", "SHOULD", "SHOULD NOT", "RECOMMENDED", "NOT RECOMMENDED", "MAY", and "OPTIONAL" in this document are to be interpreted as described in BCP 14 [RFC2119] [RFC8174] when, and only when, they appear in all capitals, as shown here.

3. POLYVAL

The GCM-SIV construction is similar to GCM: the block cipher is used in counter mode to encrypt the plaintext, and a polynomial authenticator is used to provide integrity. The authenticator in GCM-SIV is called POLYVAL.

POLYVAL, like GHASH (the authenticator in AES-GCM; see [GCM], Section 6.4), operates in a binary field of size 2^128 . The field is defined by the irreducible polynomial $x^128 + x^127 + x^126 + x^121 + 1$. The sum of any two elements in the field is the result of XORing them. The product of any two elements is calculated using standard (binary) polynomial multiplication followed by reduction modulo the irreducible polynomial.

We define another binary operation on elements of the field: dot(a, b), where $dot(a, b) = a * b * x^{-128}$. The value of the field element x^{-128} is equal to $x^{127} + x^{124} + x^{121} + x^{114} + 1$. The result of this multiplication, dot(a, b), is another field element.

Polynomials in this field are converted to and from 128-bit strings by taking the least significant bit of the first byte to be the coefficient of x^0 , the most significant bit of the first byte to be the coefficient of x^7 , and so on, until the most significant bit of the last byte is the coefficient of x^127 .

POLYVAL takes a field element, H, and a series of field elements X_1 , ..., X_s . Its result is S_s , where S_s is defined by the iteration $S_s = 0$; $S_j = dot(S_{j-1} + X_j, H)$, for j = 1..s.

We note that POLYVAL(H, X_1 , X_2 , ...) is equal to ByteReverse(GHASH(ByteReverse(H) * x, ByteReverse(X_1), ByteReverse(X_2), ...)), where ByteReverse is a function that reverses the order of 16 bytes. See Appendix A for a more detailed explanation.

4. Encryption

AES-GCM-SIV encryption takes a 16- or 32-byte key-generating key, a 96-bit nonce, and plaintext and additional data byte strings of variable length. It outputs an authenticated ciphertext that will be 16 bytes longer than the plaintext. Both encryption and decryption are only defined on inputs that are a whole number of bytes.

If the key-generating key is 16 bytes long, then AES-128 is used throughout. Otherwise, AES-256 is used throughout.

The first step of encryption is to generate per-nonce, message-authentication and message-encryption keys. The message-authentication key is 128 bit, and the message-encryption key is either 128 (for AES-128) or 256 bit (for AES-256).

These keys are generated by encrypting a series of plaintext blocks that contain a 32-bit, little-endian counter followed by the nonce, and then discarding the second half of the resulting ciphertext. In the AES-128 case, 128 + 128 = 256 bits of key material need to be generated, and, since encrypting each block yields 64 bits after discarding half, four blocks need to be encrypted. The counter values for these blocks are 0, 1, 2, and 3. For AES-256, six blocks are needed in total, with counter values 0 through 5 (inclusive).

indicates taking only the first eight bytes from x: func derive_keys(key_generating_key, nonce) { message_authentication_key = AES(key = key_generating_key,

In pseudocode form, where "++" indicates concatenation and x[:8]"

block = little_endian_uint32(0) ++ nonce)[:8] ++ AES(key = key_generating_key, block = little_endian_uint32(1) ++ nonce)[:8] message_encryption_key = AES(key = key_generating_key, block = little_endian_uint32(2) ++ nonce)[:8] ++ AES(key = key_generating_key, block = little_endian_uint32(3) ++ nonce)[:8]

if bytelen(key_generating_key) == 32 { message_encryption_key ++= AES(key = key_generating_key, block = little_endian_uint32(4) ++ nonce)[:8] ++ AES(key = key_generating_key, block = little_endian_uint32(5) ++ nonce)[:8]

return message_authentication_key, message_encryption_key

Define the "length block" as a 16-byte value that is the concatenation of the 64-bit, little-endian encodings of bytelen(additional_data) * 8 and bytelen(plaintext) * 8. Pad the plaintext and additional data with zeros until they are each a multiple of 16 bytes, the AES block size. Then X_1, X_2, ... (the series of field elements that are inputs to POLYVAL) are the concatenation of the padded additional data, the padded plaintext, and the length block.

Calculate S_s = POLYVAL (message-authentication-key, X_1, X_2, ...). XOR the first twelve bytes of S_s with the nonce and clear the most significant bit of the last byte. Encrypt the result with AES using the message-encryption key to produce the tag.

(It's worth highlighting a contrast with AES-GCM here: AES-GCM authenticates the encoded additional data and ciphertext, while AES-GCM-SIV authenticates the encoded additional data and plaintext.)

The encrypted plaintext is produced by using AES, with the messageencryption key, in counter mode (see [SP800-38A], Section 6.5) on the unpadded plaintext. The initial counter block is the tag with the most significant bit of the last byte set to one. The counter

}

advances by incrementing the first 32 bits interpreted as an

```
unsigned, little-endian integer, wrapping at 2^32. The result of the
encryption is the encrypted plaintext (truncated to the length of the
plaintext), followed by the tag.
In pseudocode form, the encryption process can be expressed as:
func right_pad_to_multiple_of_16_bytes(input) {
  while (bytelen(input) % 16 != 0) {
   input = input ++ "\x00"
  return input
func AES_CTR(key, initial_counter_block, in) {
 block = initial_counter_block
  output = ""
  while bytelen(in) > 0 {
    keystream_block = AES(key = key, block = block)
    block[0:4] = little_endian_uint32(
        read_little_endian_uint32(block[0:4]) + 1)
   todo = min(bytelen(in), bytelen(keystream_block)
    for j = 0; j < todo; j++ {
     output = output ++ (keystream_block[j] ^ in[j])
   in = in[todo:]
  return output
func encrypt (key_generating_key,
             nonce,
             plaintext,
             additional_data) {
  if bytelen(plaintext) > 2^36 {
   fail()
  if bytelen(additional_data) > 2^36 {
   fail()
  }
  message_encryption_key, message_authentication_key =
      derive_keys(key_generating_key, nonce)
```

```
length_block =
     little_endian_uint64(bytelen(additional_data) * 8) ++
      little_endian_uint64(bytelen(plaintext) * 8)
  padded_plaintext = right_pad_to_multiple_of_16_bytes(plaintext)
  padded_ad = right_pad_to_multiple_of_16_bytes(additional_data)
  S_s = POLYVAL(key = message_authentication_key,
                input = padded_ad ++ padded_plaintext ++
                        length_block)
  for i = 0; i < 12; i++ {
   S_s[i] ^= nonce[i]
  S_s[15] &= 0x7f
  tag = AES(key = message_encryption_key, block = S_s)
  counter_block = tag
  counter\_block[15] = 0x80
  return AES_CTR(key = message_encryption_key,
                initial_counter_block = counter_block,
                in = plaintext) ++
         tag
}
```

5. Decryption

Decryption takes a 16- or 32-byte key-generating key, a 96-bit nonce, and ciphertext and additional data byte strings of variable length. It either fails or outputs a plaintext that is 16 bytes shorter than the ciphertext.

To decrypt an AES-GCM-SIV ciphertext, first derive the messageencryption and message-authentication keys in the same manner as when encrypting.

If the ciphertext is less than 16 bytes or more than 2^36 + 16 bytes, then fail. Otherwise, split the input into the encrypted plaintext and a 16-byte tag. Decrypt the encrypted plaintext with the messageencryption key in counter mode, where the initial counter block is the tag with the most significant bit of the last byte set to one. Advance the counter for each block in the same way as when encrypting. At this point, the plaintext is unauthenticated and MUST NOT be output until the following tag confirmation is complete:

Pad the additional data and plaintext with zeros until they are each a multiple of 16 bytes, the AES block size. Calculate the length block and X_1 , X_2 , ... as above and compute S_s = POLYVAL (message-authentication-key, X_1, X_2, ...)

Compute the expected tag by XORing S_s and the nonce, clearing the most significant bit of the last byte and encrypting with the message-encryption key. Compare the provided and expected tag values in constant time. Fail the decryption if they do not match (and do not release the plaintext); otherwise, return the plaintext.

In pseudocode form, the decryption process can be expressed as:

Gueron, et al. Informational [Page 8]

```
func decrypt (key_generating_key,
             nonce,
             ciphertext,
             additional_data) {
  if bytelen(ciphertext) < 16 | bytelen(ciphertext) > 2^36 + 16 {
   fail()
  if bytelen(additional_data) > 2^36 {
   fail()
 message_encryption_key, message_authentication_key =
      derive_keys(key_generating_key, nonce)
  tag = ciphertext[bytelen(ciphertext)-16:]
  counter_block = tag
  counter_block[15] = 0x80
 plaintext = AES_CTR(key = message_encryption_key,
                      initial_counter_block = counter_block,
                      in = ciphertext[:bytelen(ciphertext)-16])
  length_block =
      little_endian_uint64(bytelen(additional_data) * 8) ++
      little_endian_uint64(bytelen(plaintext) * 8)
  padded_plaintext = right_pad_to_multiple_of_16_bytes(plaintext)
  padded_ad = right_pad_to_multiple_of_16_bytes(additional_data)
  S_s = POLYVAL(key = message_authentication_key,
                input = padded_ad ++ padded_plaintext ++
                        length_block)
  for i = 0; i < 12; i++ {
   S_s[i] \sim nonce[i]
  S_s[15] &= 0x7f
 expected_tag = AES(key = message_encryption_key, block = S_s)
 xor_sum = 0
  for i := 0; i < bytelen(expected_tag); i++ {</pre>
   xor_sum |= expected_tag[i] ^ tag[i]
 if xor_sum != 0 {
   fail()
  }
 return plaintext
```

6. AEADs

We define two AEADs, in the format of RFC 5116, that use AES-GCM-SIV: AEAD_AES_128_GCM_SIV and AEAD_AES_256_GCM_SIV. They differ only in the size of the AES key used.

The key input to these AEADs becomes the key-generating key. Thus, AEAD_AES_128_GCM_SIV takes a 16-byte key and AEAD_AES_256_GCM_SIV takes a 32-byte key.

The parameters for AEAD_AES_128_GCM_SIV are then as follows: K_LEN is 16, P_MAX is 2^36, A_MAX is 2^36, N_MIN and N_MAX are 12, and C_MAX is 2^36 + 16.

The parameters for AEAD_AES_256_GCM_SIV differ only in the key size: K_LEN is 32, P_MAX is 2^36 , A_MAX is 2^36 , N_MIN and N_MAX are 12, and C_MAX is $2^36 + 16$.

7. Field Operation Examples

8. Worked Example

Consider the encryption of the plaintext "Hello world" with the additional data "example" under key ee8eled9ff2540ae8f2ba9f50bc2f27c using AEAD_AES_128_GCM_SIV. The random nonce that we'll use for this example is 752abad3e0afb5f434dc4310.

In order to generate the message-authentication and messageencryption keys, a counter is combined with the nonce to form four blocks. These blocks are encrypted with the key given above:

```
Counter | Nonce Ciphertext 00000000752abad3e0afb5f434dc4310 -> 310728d9911f1f38c40e952ca83d093e 01000000752abad3e0afb5f434dc4310 -> 37b24316c3fab9a046ae90952daa0450 02000000752abad3e0afb5f434dc4310 -> a4c5ae624996327947920b2d2412474b 03000000752abad3e0afb5f434dc4310 -> c100be4d7e2c6edd1efef004305ab1e7
```

The latter halves of the ciphertext blocks are discarded and the remaining bytes are concatenated to form the per-message keys. Thus, the message-authentication key is 310728d9911f1f3837b24316c3fab9a0, and the message-encryption key is a4c5ae6249963279c100be4d7e2c6edd.

Calling POLYVAL with the message-authentication key and the input above results in $S_s = ad7fcf0b5169851662672f3c5f95138f$.

Before encrypting, the nonce is XORed in and the most significant bit of the last byte is cleared. This gives d85575d8b1c630e256bb6c2c5f95130f, because that bit happened to be one previously. Encrypting with the message-encryption key (using AES-128) gives the tag, which is 4fbcdeb7e4793f4a1d7e4faa70100af1.

In order to form the initial counter block, the most significant bit of the last byte of the tag is set to one. That doesn't result in a change in this example. Encrypting this with the message key (using AES-128) gives the first block of the keystream: 1551f2c1787e81deac9a99f139540ab5.

The final ciphertext is the result of XORing the plaintext with the keystream and appending the tag. That gives 5d349ead175ef6bldef6fd4fbcdeb7e4793f4a1d7e4faa70100af1.

9. Security Considerations

AES-GCM-SIV decryption involves first producing an unauthenticated plaintext. This plaintext is vulnerable to manipulation by an attacker; thus, if an implementation released some or all of the plaintext before authenticating it, other parts of a system may process malicious data as if it were authentic. AES-GCM might be less likely to lead implementations to do this because there the ciphertext is generally authenticated before, or concurrently with, the plaintext calculation. Therefore, this text requires that implementations MUST NOT release unauthenticated plaintext. Thus, system designers should consider memory limitations when picking the

size of AES-GCM-SIV plaintexts: large plaintexts may not fit in the available memory of some machines, tempting implementations to release unverified plaintext.

A detailed cryptographic analysis of AES-GCM-SIV appears in [AES-GCM-SIV], and the remainder of this section is a summary of that paper.

The AEADs defined in this document calculate fresh AES keys for each nonce. This allows a larger number of plaintexts to be encrypted under a given key. Without this step, AES-GCM-SIV encryption would be limited by the birthday bound like other standard modes (e.g., AES-GCM, AES-CCM [RFC3610], and AES-SIV [RFC5297]). This means that when 2^64 blocks have been encrypted overall, a distinguishing adversary who is trying to break the confidentiality of the scheme has an advantage of 1/2. Thus, in order to limit the adversary's advantage to 2^-32, at most 2^48 blocks can be encrypted overall. In contrast, by deriving fresh keys from each nonce, it is possible to encrypt a far larger number of messages and blocks with AES-GCM-SIV.

We stress that nonce misuse-resistant schemes guarantee that if a nonce repeats, then the only security loss is that identical plaintexts will produce identical ciphertexts. Since this can also be a concern (as the fact that the same plaintext has been encrypted twice is revealed), we do not recommend using a fixed nonce as a policy. In addition, as we show below, better-than-birthday bounds are achieved by AES-GCM-SIV when the nonce repetition rate is low. Finally, as shown in [BHT18], there is a great security benefit in the multiuser/multikey setting when each particular nonce is reused by a small number of users only. We stress that the nonce misuse-resistance property is not intended to be coupled with intentional nonce reuse; rather, such schemes provide the best possible security in the event of nonce reuse. Due to all of the above, it is RECOMMENDED that AES-GCM-SIV nonces be randomly generated.

Some example usage bounds for AES-GCM-SIV are given below. The adversary's advantage is the "AdvEnc" from [key-derive] and is colloquially the ability of an attacker to distinguish ciphertexts from random bit strings. The bounds below limit this advantage to 2^-32. For up to 256 uses of the same nonce and key (i.e., where one can assume that nonce misuse is no more than this bound), the following message limits should be respected (this assumes a short additional authenticated data (AAD), i.e., less than 64 bytes):

2^29 messages, where each plaintext is at most 1 GiB

2^35 messages, where each plaintext is at most 128 MiB

- 2^49 messages, where each plaintext is at most 1 MiB
- 2^61 messages, where each plaintext is at most 16 KiB

Suzuki et al. [multi-birthday] show that even if nonces are selected uniformly at random, the probability that one or more values would be repeated 256 or more times is negligible until the number of nonces reaches 2^102 . (Specifically, the probability is $1/((2^96)^(255))$ * Binomial(q, 256), where q is the number of nonces.) Since 2^102 is vastly greater than the limit on the number of plaintexts per key given above, we don't feel that this limit on the number of repeated nonces will be a problem. This also means that selecting nonces at random is a safe practice with AES-GCM-SIV. The bounds obtained for random nonces are as follows (as above, for these bounds, the adversary's advantage is at most 2^-32 :

- 2^32 messages, where each plaintext is at most 8 GiB
- 2^48 messages, where each plaintext is at most 32 MiB
- 2^64 messages, where each plaintext is at most 128 KiB

For situations where, for some reason, an even higher number of nonce repeats is possible (e.g., in devices with very poor randomness), the message limits need to be reconsidered. Theorem 7 in [AES-GCM-SIV] contains more details, but for up to 1,024 repeats of each nonce, the limits would be (again assuming a short AAD, i.e., less than 64 bytes):

- 2^25 messages, where each plaintext is at most 1 GiB
- 2^31 messages, where each plaintext is at most 128 MiB
- 2^45 messages, where each plaintext is at most 1 MiB
- 2^57 messages, where each plaintext is at most 16 KiB

In addition to calculating fresh AES keys for each nonce, these AEADs also calculate fresh POLYVAL keys. Previous versions of GCM-SIV did not do this and instead used part of the AEAD's key as the POLYVAL key. Bleichenbacher pointed out [Bleichenbacher16] that this allowed an attacker who controlled the AEAD key to force the POLYVAL key to be zero. If a user of this AEAD authenticated messages with a secret additional-data value, then this would be insecure as the attacker could calculate a valid authenticator without knowing the input. This does not violate the standard properties of an AEAD as the

additional data is not assumed to be confidential. However, we want these AEADs to be robust against plausible misuse and also to be drop-in replacements for AES-GCM and so derive nonce-specific POLYVAL keys to avoid this issue.

We also wish to note that the probability of successful forgery increases with the number of attempts that an attacker is permitted. The advantage defined in [key-derive] and used above is specified in terms of the ability of an attacker to distinguish ciphertexts from random bit strings. It thus covers both confidentiality and integrity, and Theorem 6.2 in [key-derive] shows that the advantage increases with the number of decryption attempts, although much more slowly than with the number of encryptions; the dependence on the number of decryption queries for forgery is actually only linear, not quadratic. The latter is an artifact of the bound in the paper not being tight. If an attacker is permitted extremely large numbers of attempts, then the tiny probability that any given attempt succeeds may sum to a non-trivial chance.

A security analysis of a similar scheme without nonce-based key derivation appears in [GCM-SIV], and a full analysis of the bounds when applying nonce-based key derivation appears in [key-derive]. A larger table of bounds and other information appears at [aes-gcm-siv-homepage].

The multiuser/multikey security of AES-GCM-SIV was studied by [BHT18], which showed that security is almost the same as in the single-user setting, as long as nonces do not repeat many times across many users. This is the case when nonces are chosen randomly.

10. IANA Considerations

IANA has added two entries to the "AEAD Algorithms" registry: AEAD_AES_128_GCM_SIV (Numeric ID 30) and AEAD_AES_256_GCM_SIV (Numeric ID 31), both referencing this document as their specification.

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Gueron, et al. Informational [Page 16]

Appendix A. The Relationship between POLYVAL and GHASH

GHASH and POLYVAL both operate in GF(2^128), although with different irreducible polynomials: POLYVAL works modulo $x^128 + x^127 + x^126 + x^121 + 1$ and GHASH works modulo $x^128 + x^7 + x^2 + x + 1$. Note that these irreducible polynomials are the "reverse" of each other.

GHASH also has a different mapping between 128-bit strings and field elements. Whereas POLYVAL takes the least significant to most significant bits of the first byte to be the coefficients of x^0 to x^7 , GHASH takes them to be the coefficients of x^7 to x^0 . This continues until, for the last byte, POLYVAL takes the least significant to most significant bits to be the coefficients of x^120 to x^127 , while GHASH takes them to be the coefficients of x^127 to x^120 .

The combination of these facts means that it's possible to "convert" values between the two by reversing the order of the bytes in a 16-byte string. The differing interpretations of bit order takes care of reversing the bits within each byte, and then reversing the bytes does the rest. This may have a practical benefit for implementations that wish to implement both GHASH and POLYVAL.

In order to be clear which field a given operation is performed in, let mulX_GHASH be a function that takes a 16-byte string, converts it to an element of GHASH's field using GHASH's convention, multiplies it by x, and converts it back to a string. Likewise, let mulX_POLYVAL be a function that converts a 16-byte string to an element of POLYVAL's field using POLYVAL's convention, multiplies it by x, and converts it back.

Lastly, let ByteReverse be the function that takes a 16-byte string and returns a copy where the order of the bytes has been reversed.

```
Now GHASH and POLYVAL can be defined in terms of one another:
 POLYVAL(H, X_1, ..., X_n) =
 ByteReverse(GHASH(mulX_GHASH(ByteReverse(H)), ByteReverse(X_1), ...,
ByteReverse(X_n)))
 GHASH (H, X_1, ..., X_n) =
ByteReverse (POLYVAL (mulX_POLYVAL (ByteReverse (H)), ByteReverse (X_1),
 ..., ByteReverse(X_n)))
As a worked example:
    let H = 25629347589242761d31f826ba4b757b,
        X_1 = 4f4f95668c83dfb6401762bb2d01a262, and
        X_2 = d1a24ddd2721d006bbe45f20d3c9f362.
   POLYVAL(H, X_1, X_2) = f7a3b47b846119fae5b7866cf5e5b77e.
 If we wished to calculate this given only an implementation of GHASH,
 then the key for GHASH would be
mulX_GHASH(ByteReverse(H)) = dcbaa5dd137c188ebb21492c23c9b112.
 Then ByteReverse(GHASH(dcba..., ByteReverse(X_1), ByteReverse(X_2)))
     = f7a3b47b846119fae5b7866cf5e5b77e, as required.
 In the other direction, GHASH(H, X_1, X_2) =
bd9b3997046731fb96251b91f9c99d7a. If we wished to calculate this
 given only an implementation of POLYVAL, then we would first
calculate the key for POLYVAL:
mulx_POLYVAL(ByteReverse(H)) = f6ea96744df0633aec8424b18e26c54a.
Then ByteReverse (POLYVAL (f6ea..., ByteReverse (X_1), ByteReverse (X_2)))
    = bd9b3997046731fb96251b91f9c99d7a.
```

Gueron, et al. Informational [Page 18]

Appendix B. Additional Comparisons with AES-GCM

Some functional properties that differ between AES-GCM and AES-GCM-SIV that are also worth noting:

AES-GCM allows plaintexts to be encrypted in a streaming fashion -- i.e., the beginning of the plaintext can be encrypted and transmitted before the entire message has been processed. AES-GCM-SIV requires two passes for encryption and so cannot do this.

AES-GCM allows a constant additional-data input to be precomputed in order to save per-message computation. AES-GCM-SIV varies the authenticator key based on the nonce and so does not permit this.

The performance for AES-GCM versus AES-GCM-SIV on small machines can be roughly characterized by the number of AES operations and the number of GF(2^128) multiplications needed to process a message.

```
Let a = (bytelen(additional-data) + 15) / 16 and p = (bytelen(plaintext) + 15) / 16.
```

Then AES-GCM requires p + 1 AES operations and p + a + 1 field multiplications.

Defined similarly, AES-GCM-SIV with AES-128 requires p + 5 AES operations and p + a + 1 field multiplications. With AES-256, that becomes p + 7 AES operations.

With large machines, the available parallelism becomes far more important, and such simple performance analysis is no longer representative. For such machines, we find that decryption of AES-GCM-SIV is only about 5% slower than AES-GCM, as long as the message is at least a couple of kilobytes. Encryption tends to run about two-thirds the speed because of the additional pass required.

Appendix C. Test Vectors

C.1. AEAD_AES_128_GCM_SIV

Tag =

Plaintext (0 bytes) =AAD (0 bytes) =Key = 03000000000000000000000 Nonce = Record authentication key = d9b360279694941ac5dbc6987ada7377 Plaintext (8 bytes) = 01000000000000000 AAD (0 bytes) = Key =Nonce = 03000000000000000000000 Record authentication key = d9b360279694941ac5dbc6987ada7377 Record encryption key = 4004a0dcd862f2a57360219d2d44ef6c POLYVAL input = POLYVAL result = POLYVAL result "" eb93b7740962c5e49d2a90a7dc5cec74 POLYVAL result XOR nonce = e893b7740962c5e49d2a90a7dc5cec74 \dots and masked = e893b7740962c5e49d2a90a7dc5cec74 578782fff6013b815b287c22493a364c Tag = Initial counter = 578782fff6013b815b287c22493a36cc b5d839330ac7b786578782fff6013b81 Result (24 bytes) = 5b287c22493a364c Plaintext (12 bytes) = 0100000000000000000000000 AAD (0 bytes) = Key = 030000000000000000000000 Nonce = Record authentication key = d9b360279694941ac5dbc6987ada7377 POLYVAL result XOR nonce = 4beb6c6c5a2dbe4a1dde508fee06361b ... and masked = 4beb6c6c5a2dbe4a1dde508fee06361b

a4978db357391a0bc4fdec8b0d106639

AAD (0 bytes) = Key =030000000000000000000000 Nonce = Record authentication key = d9b360279694941ac5dbc6987ada7377 POLYVAL result = 23806c26e3c1de019e111255708031d6
... and masked = 23806c26e3c1de019e11125570803156
Tag = 303aaf90f6fe21199c6068577437a0c4
Result (32 bytes) = 743f7c8077ab25f8624e2e948579cf77
303aaf90f6fe21199c6068577437a0c4 AAD (0 bytes) = Key =03000000000000000000000 Nonce = Record authentication key = d9b360279694941ac5dbc6987ada7377 POLYVAL result XOR nonce = cd6edc9a50b36d9a98986bbf6a261c3b 1a8e45dcd4578c667cd86847bf6155ff AAD (0 bytes) = Key = Nonce =

```
Record authentication key = d9b360279694941ac5dbc6987ada7377
Record encryption key = 4004a0dcd862f2a57360219d2d44ef6c
POLYVAL input =
                    POLYVAL result =
                    81388746bc22d26b2abc3dcb15754222
POLYVAL result XOR nonce = 82388746bc22d26b2abc3dcb15754222
... and masked =
                  82388746bc22d26b2abc3dcb15754222
                   5e6e311dbf395d35b0fe39c2714388f8
Tag =
                 5e6e311dbf395d35b0fe39c2714388f8
Initial counter =
Result (64 bytes) =
                  3fd24ce1f5a67b75bf2351f181a475c7
                   b800a5b4d3dcf70106b1eea82fa1d64d
                    f42bf7226122fa92e17a40eeaac1201b
                    5e6e311dbf395d35b0fe39c2714388f8
                    Plaintext (64 bytes) =
                    AAD (0 bytes) =
                    Key =
                    03000000000000000000000
Nonce =
Record authentication key = d9b360279694941ac5dbc6987ada7377
Record encryption key =
                    4004a0dcd862f2a57360219d2d44ef6c
                    POLYVAL input =
                    POLYVAL result =
                    1e39b6d3344d348f6044f89935d1cf78
POLYVAL result XOR nonce = 1d39b6d3344d348f6044f89935d1cf78
                  1d39b6d3344d348f6044f89935d1cf78
... and masked =
Tag =
                   8a263dd317aa88d56bdf3936dba75bb8
Initial counter =
                   8a263dd317aa88d56bdf3936dba75bb8
Result (80 bytes) =
                   2433668f1058190f6d43e360f4f35cd8
                    e475127cfca7028ea8ab5c20f7ab2af0
                    2516a2bdcbc08d521be37ff28c152bba
                    36697f25b4cd169c6590d1dd39566d3f
                    8a263dd317aa88d56bdf3936dba75bb8
Plaintext (8 bytes) =
                   02000000000000000
AAD (1 bytes) =
Key =
                    030000000000000000000000
Nonce =
Record authentication key = d9b360279694941ac5dbc6987ada7377
```

Record encryption key = 4004a0dcd862f2a57360219d2d44ef6c Record encryption _ POLYVAL input = 080000000000000400000000000000 POLYVAL result = b26781e7e2c1376f96bec195f3709b2a POLYVAL result XOR nonce = b16781e7e2c1376f96bec195f3709b2a District Festit AoR Honce - Biordie Pestit Festit For Honce - Biordie Pestit Festit For Honce - Biordie Pestit For Honce - Biordi AAD (1 bytes) = Key = 030000000000000000000000 Nonce = Record authentication key = d9b360279694941ac5dbc6987ada7377 0800000000000006000000000000000 POLYVAL result = 111f5affb18e4cc1164a01bdc12a4145 POLYVAL result XOR nonce = 121f5affb18e4cc1164a01bdc12a4145
... and masked = 121f5affb18e4cc1164a01bdc12a4145
Tag = 08299c5102745aaa3a0c469fad9e075a
Initial counter = 08299c5102745aaa3a0c469fad9e07da
Result (28 bytes) = 296c7889fd99f41917f4462008299c51
02745aaa3a0c469fad9e075a AAD (1 bytes) = Key = 030000000000000000000000 Nonce = Record authentication key = d9b360279694941ac5dbc6987ada7377

Plaintext (32 bytes) =	020000000000000000000000000000000000000
AAD (1 bytes) =	01
Key =	010000000000000000000000000000000000000
Nonce =	0300000000000000000000
Record authentication key =	
Record encryption key =	4004a0dcd862f2a57360219d2d44ef6c
POLYVAL input =	010000000000000000000000000000000000000
	020000000000000000000000000000000000000
	030000000000000000000000000000000000000
	08000000000000000100000000000
POLYVAL result =	2ce7daaf7c89490822051255b12eca6b
POLYVAL result XOR nonce =	2fe7daaf7c89490822051255b12eca6b
and masked =	2fe7daaf7c89490822051255b12eca6b
Tag =	e6af6a7f87287da059a71684ed3498e1
Initial counter =	e6af6a7f87287da059a71684ed3498e1
Result (48 bytes) =	620048ef3c1e73e57e02bb8562c416a3
	19e73e4caac8e96a1ecb2933145a1d71
	e6af6a7f87287da059a71684ed3498e1
Plaintext (48 bytes) =	020000000000000000000000000000000000000
	030000000000000000000000000000000000000
	040000000000000000000000000000000000000
AAD (1 bytes) =	01
Key =	010000000000000000000000000000000000000
Nonce =	0300000000000000000000
Record authentication key =	
Record encryption key =	4004a0dcd862f2a57360219d2d44ef6c
POLYVAL input =	010000000000000000000000000000000000000
	020000000000000000000000000000000000000
	030000000000000000000000000000000000000
	040000000000000000000000000000000000000
DOI 3/1/1/1 1 +-	0800000000000000800100000000000
POLYVAL result =	9ca987715d69c1786711dfcd22f830fc
POLYVAL result XOR nonce = and masked =	9fa987715d69c1786711dfcd22f830fc
	9fa987715d69c1786711dfcd22f8307c 6a8cc3865f76897c2e4b245cf31c51f2
Tag = Initial counter =	6a8cc3865f76897c2e4b245cf31c51f2
Result (64 bytes) =	50c8303ea93925d64090d07bd109dfd9
Meaure (04 Dyces) -	515a5a33431019c17d93465999a8b005
	3201d723120a8562b838cdff25bf9d1e
	6a8cc3865f76897c2e4b245cf31c51f2
Plaintext (64 bytes) =	020000000000000000000000000000000000000
	030000000000000000000000000000000000000
	040000000000000000000000000000000000000

```
AAD (1 bytes) =
                    Key =
                    030000000000000000000000
Nonce =
Record authentication key = d9b360279694941ac5dbc6987ada7377
Record encryption key =
                    4004a0dcd862f2a57360219d2d44ef6c
                    POLYVAL input =
                    08000000000000000002000000000000
POLYVAL result =
                    ffcd05d5770f34ad9267f0a59994b15a
POLYVAL result XOR nonce = fccd05d5770f34ad9267f0a59994b15a
                    fccd05d5770f34ad9267f0a59994b15a
... and masked =
                   cdc46ae475563de037001ef84ae21744
Tag =
                   cdc46ae475563de037001ef84ae217c4
Initial counter =
                   2f5c64059db55ee0fb847ed513003746
Result (80 bytes) =
                    aca4e61c711b5de2e7a77ffd02da42fe
                    ec601910d3467bb8b36ebbaebce5fba3
                    0d36c95f48a3e7980f0e7ac299332a80
                    cdc46ae475563de037001ef84ae21744
Plaintext (4 bytes) = 02000000
AAD (12 bytes) =
                    010000000000000000000000
Key =
                    03000000000000000000000
Nonce =
Record authentication key = d9b360279694941ac5dbc6987ada7377
Record encryption key =
                    4004a0dcd862f2a57360219d2d44ef6c
                    POLYVAL input =
                    POLYVAL result =
                    f6ce9d3dcd68a2fd603c7ecc18fb9918
POLYVAL result XOR nonce = f5ce9d3dcd68a2fd603c7ecc18fb9918
                  f5ce9d3dcd68a2fd603c7ecc18fb9918
... and masked =
                   07eb1f84fb28f8cb73de8e99e2f48a14
Tag =
Initial counter =
                   07eb1f84fb28f8cb73de8e99e2f48a94
Result (20 bytes) =
                   a8fe3e8707eb1f84fb28f8cb73de8e99
                    e2f48a14
                    Plaintext (20 bytes) =
                    04000000
AAD (18 bytes) =
                    Key =
                    03000000000000000000000
Nonce =
```

```
Record authentication key = d9b360279694941ac5dbc6987ada7377
Record encryption key = 4004a0dcd862f2a57360219d2d44ef6c
                       POLYVAL input =
                       POLYVAL result =
                       4781d492cb8f926c504caa36f61008fe
POLYVAL result XOR nonce = 4481d492cb8f926c504caa36f61008fe
Tag = 4481d492cb8f926c504caa36f610087e
Tag = 24afc9805e976f451e6d87f6fe106514
Initial counter = 24afc9805e976f451e6d87f6fe106594
Result (36 bytes) = 6bb0fecf5ded9b77f902c7d5da236a43
91dd029724afc9805e976f451e6d87f6
                       fe106514
                       Plaintext (18 bytes) =
                       0400
                       AAD (20 bytes) =
                       02000000
                       Key =
                       03000000000000000000000
Nonce =
Record authentication key = d9b360279694941ac5dbc6987ada7377
Record encryption key = 4004a0dcd862f2a57360219d2d44ef6c
                       POLYVAL input =
                       POLYVAL result =
                       75cbc23a1a10e348aeb8e384b5cc79fd
POLYVAL result XOR nonce = 76cbc23a1a10e348aeb8e384b5cc79fd
                    76cbc23a1a10e348aeb8e384bbce797a
bff9b2ef00fb47920cc72a0c0f13b9fd
bff9b2ef00fb47920cc72a0c0f13b9fd
44d0aaf6fb2f1f34add5e8064e83e12a
2adabff9b2ef00fb47920cc72a0c0f13
... and masked =
Tag =
Initial counter =
Result (34 bytes) =
                       b9fd
Plaintext (0 bytes) =
AAD (0 bytes) =
                       e66021d5eb8e4f4066d4adb9c33560e4
Key =
                       f46e44bb3da0015c94f70887
Nonce =
Record authentication key = 036ee1fe2d7926af68898095e54e7b3c
POLYVAL result XOR nonce = f46e44bb3da0015c94f7088700000000
```

[Page 26]

... and masked = f46e44bb3da0015c94f7088700000000
Tag = a4194b79071b01a87d65f706e3949578
Initial counter = a4194b79071b01a87d65f706e39495f8
Result (16 bytes) = a4194b79071b01a87d65f706e3949578 Plaintext (3 bytes) = 7a806c

AAD (5 bytes) = 46bb91c3c5

Key = 36864200e0eaf5284d884a0e77d31646

Nonce = bae8e37fc83441b16034566b Record authentication key = 3e28de1120b2981a0155795ca2812af6POLYVAL result XOR nonce = f931443a99298e137ba28b0b6f1d5720 a428a8 Plaintext (6 bytes) = bdc66f146545

AAD (10 bytes) = fc880c94a95198874296

Key = aedb64a6c590bc84d1a5e269e4b47801

Nonce = afc0577e34699b9e671fdd4f afc0577e34699b9e671fdd4f Nonce = Record authentication key = 43b8de9cea62330d15cccfc84a33e8c8 500000000000000300000000000000 POLYVAL result = 26498e0d2b1ef004e808c458e8f2f515 POLYVAL result XOR nonce = 8989d9731f776b9a8f171917e8f2f515
... and masked = 8989d9731f776b9a8f171917e8f2f515
Tag = d6a9c45545cfc11f03ad743dba20f966
Initial counter = d6a9c45545cfc11f03ad743dba20f9e6
Result (22 bytes) = bb93a3e34d3cd6a9c45545cfc11f03ad743dba20f966 743dba20f966 Plaintext (9 bytes) = 1177441f195495860f

AAD (15 bytes) = 046787f3ea22c127aaf195d1894728

Key = d5cc1fd161320b6920ce07787f86743b

Nonce = 275d1ab32f6d1f0434d8848c Record authentication key = 8a51df64d93eaf667c2c09bd454ce5c5 Record encryption key = 43ab276c2b4a473918ca73f2dd85109c

... and masked = 44fe5faf244e2b5ee4f33ed59565174f
Tag = 1d02fd0cd174c84fc5dae2f60f52fd2b
Initial counter = 1d02fd0cd174c84fc5dae2f60f52fdab
Result (25 bytes) = 4f37281f7ad12949d01d02fd0cd174c8
4fc5dae2f60f52fd2b Plaintext (12 bytes) = 9f572c614b4745914474e7c7 AAD (20 bytes) = c9882e5386fd9f92ec489c8fde2be2cf 97e74e93 Key = b3fed1473c528b8426a582995929a149 9e9ad8780c8d63d0ab4149c0 Nonce = Record authentication key = 22f50707a95dd416df069d670cb775e89f572c614b4745914474e7c700000000 POLYVAL result = 0cca0423fba9d77fe7e2e6963b08cdd0 POLYVAL result XOR nonce = 9250dc5bf724b4af4ca3af563b08cdd0 FORWAL result XOR Holice - 9250dc5bf724b4af4ca3af563b08cdd0

... and masked = 9250dc5bf724b4af4ca3af563b08cd50

Tag = c1dc2f871fb7561da1286e655e24b7b0

Result (28 bytes) = f54673c5ddf710c745641c8bc1dc2f87

1fb7561da1286e655e24b7b0 Plaintext (15 bytes) = 0d8c8451178082355c9e940fea2f58
AAD (25 bytes) = 2950a70d5a1db2316fd568378da107b5
2b0da55210cc1c1b0a
Key = 2d4ed87da44102952ef94b02b805249b
Nonce = ac80e6f61455bfac8308a2d4 Record authentication key = 0b00a29a83e7e95b92e3a0783b29f1402b0da55210cc1c1b0a00000000000000 0d8c8451178082355c9e940fea2f5800 c800000000000000780000000000000 POLYVAL result = 1086ef25247aa41009bbc40871d9b350 POLYVAL result XOR nonce = bc0609d3302f1bbc8ab366dc71d9b350 ... and masked = bc0609d3302f1bbc8ab366dc71d9b350
Tag = 83b3449b9f39552de99dc214a1190b0b Initial counter = 83b3449b9f39552de99dc214a1190b8b

Result (31 bytes) = c9ff545e07b88a015f05b274540aa183 b3449b9f39552de99dc214a1190b0b Plaintext (18 bytes) = 6b3db4da3d57aa94842b9803a96e07fb 6de7 1860f762ebfbd08284e421702de0de18 baa9c9596291b08466f37de21c7f bde3b2f204d1e9f8b06bc47f9745b3d1 AAD (30 bytes) = Key = ae06556fb6aa7890bebc18fe Nonce = Record authentication key = 21c874a8bad3603d1c3e8784df5b3f9fRecord encryption key = d1c16d72651c3df504eae27129d818e8
POLYVAL input = 1860f762ebfbd08284e421702de0de18
baa9c9596291b08466637do21c7f0000 baa9c9596291b08466f37de21c7f0000 6b3db4da3d57aa94842b9803a96e07fb POLYVAL result = 55462a5afa0da8d646481e049ef9c764 POLYVAL result XOR nonce = fb407f354ca7d046f8f406fa9ef9c764 Tag = 3e377094f04709f64d7b985310a4db84
Result (34 bytes) = 5b1071351cd7dd11612110111d2c136767

151071351cd7dd11612110111d2c136767

151071351cd7dd11612110111d2c136767

3e377094f04709f64d7b985310a4db84

6298b296e24e8cc35dce0bed484b7f30
d5803e377094f04709f64d7b985310a4 db84 Plaintext (21 bytes) = e42a3c02c25b64869e146d7b233987bd dfc240871d AAD (35 bytes) = 7576f7028ec6eb5ea7e298342a94d4b2 02b370ef9768ec6561c4fe6b7e7296fa 859c21 Key = f901cfe8a69615a93fdf7a98cad48179 6245709fb18853f68d833640 Record authentication key = 3724f55f1d22ac0ab830da0b6a995d74Record encryption key = 75ac87b70c05db287de779006105a344 POLYVAL input = 7576f7028ec6eb5ea7e298342a94d4b2 POLYVAL input = 02b370ef9768ec6561c4fe6b7e7296fa e42a3c02c25b64869e146d7b233987bd 1801000000000000a800000000000000 POLYVAL result = 4cbba090f03f7d1188ea55749fa6c7bd POLYVAL result XOR nonce = 2efed00f41b72ee7056963349fa6c7bd c.. and masked = 2efed00f41b72ee7056963349fa6c73d
Tag = 2d15506c84a9edd65e13e9d24a2a6e70
Initial counter = 2d15506c84a9edd65e13e9d24a2a6ef0
Result (37 bytes) = 391cc328d484a4f46406181bcd62efd9 b3ee197d052d15506c84a9edd65e13e9 d24a2a6e70

C.2. AEAD_AES_256_GCM_SIV

Plaintext (0 bytes) = AAD (0 bytes) =Key =03000000000000000000000 Nonce = Record authentication key = b5d3c529dfafac43136d2d11be284d7f Record encryption key = b914f4742be9e1d7a2f84addbf96dec3 456e3c6c05ecc157cdbf0700fedad222 POLYVAL input = POLYVAL result = 01000000000000000 Plaintext (8 bytes) = AAD (0 bytes) =Key = 03000000000000000000000 Nonce = Record authentication key = b5d3c529dfafac43136d2d11be284d7f Record encryption key = b914f4742be9e1d7a2f84addbf96dec3 456e3c6c05ecc157cdbf0700fedad222 POLYVAL input = 000000000000000040000000000000000POLYVAL result = 05230f62f0eac8aa14fe4d646b59cd41 POLYVAL result XOR nonce = 06230f62f0eac8aa14fe4d646b59cd41POLYVAL result Ack

... and masked = 06230f62f0eac8aa14Ie4uu4ubbccc.

Tag = 843122130f7364b761e0b97427e3df28

843122130f7364b761e0b97427e3dfa8 Result (24 bytes) = c2ef328e5c71c83b843122130f7364b7 61e0b97427e3df28 010000000000000000000000 Plaintext (12 bytes) = AAD (0 bytes) =Key =03000000000000000000000 Record authentication key = b5d3c529dfafac43136d2d11be284d7f Record encryption key = b914f4742be9e1d7a2f84addbf96dec3

```
456e3c6c05ecc157cdbf0700fedad222
                         POLYVAL input =
                        POLYVAL result =
                        6d81a24732fd6d03ae5af544720a1c13
POLYVAL result XOR nonce = 6e81a24732fd6d03ae5af544720a1c13
\cdot \cdot \cdot and masked = 6e81a24732fd6d03ae5af544720a1c13
                    8ca50da9ae6559e48fd10f6e5c9ca17e
8ca50da9ae6559e48fd10f6e5c9ca1fe
9aab2aeb3faa0a34aea8e2b18ca50da9
ae6559e48fd10f6e5c9ca17e
Tag =
Initial counter =
Result (28 bytes) =
                       Plaintext (16 bytes) =
AAD (0 bytes) =
                         Key =
                         030000000000000000000000
Nonce =
Record authentication key = b5d3c529dfafac43136d2d11be284d7f
Record encryption key = b914f4742be9e1d7a2f84addbf96dec3
                         456e3c6c05ecc157cdbf0700fedad222
                         POLYVAL input =
                         POLYVAL result =
                         74eee2bf7c9a165f8b25dea73db32a6d
POLYVAL result XOR nonce = 77eee2bf7c9a165f8b25dea73db32a6d
Tolly All Tesure Not Notice 77662251763410510525464734352464  
... and masked = 776ee2bf7c9a165f8b25dea73db32a6d  
Tag = c9eac6fa700942702e90862383c6c366  
Result (32 bytes) = 85a01b63025ba19b7fd3ddfc033b3e76  
C9eac6fa700942702e90862383c6c366
                        c9eac6fa700942702e90862383c6c366
AAD (0 bytes) =
                         Key =
                         030000000000000000000000
Nonce =
Record authentication key = b5d3c529dfafac43136d2d11be284d7f
Record encryption key =
                        b914f4742be9e1d7a2f84addbf96dec3
                         456e3c6c05ecc157cdbf0700fedad222
                         POLYVAL input =
                         000000000000000000100000000000
                         899b6381b3d46f0def7aa0517ba188f5
POLYVAL result =
POLYVAL result XOR nonce = 8a9b6381b3d46f0def7aa0517ba188f5
... and masked = 8a9b6381b3d46f0def7aa0517ba18875
Tag = 819e63abcd020b006a976397632eb5d
Tag =
Initial counter = e819e63abcd020b006a976397632ebdd
```

Result (48 bytes) =	4a6a9db4c8c6549201b9edb53006cba8 21ec9cf850948a7c86c68ac7539d027f e819e63abcd020b006a976397632eb5d
Plaintext (48 bytes) =	01000000000000000000000000000000000000
AAD (0 bytes) = Key =	01000000000000000000000000000000000000
Nonce = Record authentication key = Record encryption key =	03000000000000000000000000000000000000
POLYVAL input =	456e3c6c05ecc157cdbf0700fedad222 01000000000000000000000000000000000
<pre>POLYVAL result = POLYVAL result XOR nonce = and masked = Tag =</pre>	c1f8593d8fc29b0c290cae1992f71f51 c2f8593d8fc29b0c290cae1992f71f51 c2f8593d8fc29b0c290cae1992f71f51 790bc96880a99ba804bd12c0e6a22cc4
<pre>Initial counter = Result (64 bytes) =</pre>	790bc96880a99ba804bd12c0e6a22cc4 c00d121893a9fa603f48ccc1ca3c57ce 7499245ea0046db16c53c7c66fe717e3 9cf6c748837b61f6ee3adcee17534ed5 790bc96880a99ba804bd12c0e6a22cc4
Plaintext (64 bytes) =	01000000000000000000000000000000000000
AAD (0 bytes) = Key =	010000000000000000000000000000000000000
Nonce = Record authentication key = Record encryption key =	00000000000000000000000000000000000000
POLYVAL input =	01000000000000000000000000000000000000
POLYVAL result = POLYVAL result XOR nonce =	6ef38b06046c7c0e225efaef8e2ec4c4 6df38b06046c7c0e225efaef8e2ec4c4

```
... and masked = 6df38b06046c7c0e225efaef8e2ec444
Tag = 112864c269fc0d9d88c61fa47e39aa08
Initial counter = 112864c269fc0d9d88c61fa47e39aa88
Result (80 bytes) = c2d5160a1f8683834910acdafc41fbb1
                                632d4a353e8b905ec9a5499ac34f96c7
                                e1049eb080883891a4db8caaa1f99dd0
                                04d80487540735234e3744512c6f90ce
                                112864c269fc0d9d88c61fa47e39aa08
                              02000000000000000
Plaintext (8 bytes) =
AAD (1 bytes) =
                                0.1
                                Key =
                                030000000000000000000000
Nonce =
Record authentication key = b5d3c529dfafac43136d2d11be284d7f
Record encryption key = b914f4742be9e1d7a2f84addbf96dec3 456e3c6c05ecc157cdbf0700fedad222
POLYVAL result XOR nonce = 37e57bafe011b9b36fc6821b7ffb3354
Tolly All Tesult Xok Honce - 37637bale011b3b361c0821b711b3334

... and masked = 37657bafe011b9b36fc6821b7ffb3354

Tag = 91213f267e3b452f02d01ae33e4ec854

Initial counter = 91213f267e3b452f02d01ae33e4ec8d4

Result (24 bytes) = 1de22967237a813291213f267e3b452f

02d01ae33e4ec854
                               02d01ae33e4ec854
AAD (1 bytes) =
                          Key =
                                Nonce =
                                03000000000000000000000
Record authentication key = b5d3c529dfafac43136d2d11be284d7f
Record encryption key = b914f4742be9e1d7a2f84addbf96dec3 456e3c6c05ecc157cdbf0700fedad222
                                POLYVAL input =
                                0800000000000006000000000000000
POLYVAL result = 5c47d68a22061c1ad5623a3b66a8e206
POLYVAL result XOR nonce = 5f47d68a22061c1ad5623a3b66a8e206
... and masked = 5f47d68a22061c1ad5623a3b66a8e206
Tag = c1a4a19ae800941ccdc57cc8413c277f
Initial counter = c1a4a19ae800941ccdc57cc8413c27ff
Result (28 bytes) = 163d6f9cc1b346cd453a2e4cc1a4a19a
                               e800941ccdc57cc8413c277f
```

AAD (1 by Key = Nonce = Record at Record er POLYVAL if POLYVAL if and if Tag = Initial c	<pre>inthentication key = incryption key = input = input = incryption key = input = in</pre>	02000000000000000000000000000000000000
AAD (1 by Key = Nonce = Record at Record er POLYVAL if POLYVAL if and if Tag = Initial c	thentication key = ncryption key = Input = result = result XOR nonce = masked =	02000000000000000000000000000000000000
Plaintext AAD (1 by Key =	(48 bytes) = vtes) =	02000000000000000000000000000000000000

Nonce = 030000000000000000000000 Record authentication key = b5d3c529dfafac43136d2d11be284d7fRecord encryption key = b914f4742be9e1d7a2f84addbf96dec3 456e3c6c05ecc157cdbf0700fedad222 POLYVAL input = 0800000000000000800100000000000 POLYVAL result = 2566a4aff9a525df9772c16d4eaf8d2a POLYVAL result XOR nonce = 2666a4aff9a525df9772c16d4eaf8d2a ... and masked = 2666a4aff9a525df9772c16d4eaf8d2a03332742b228c647173616cfd44c54eb Tag = 03332742b228c647173616cfd44c54eb c67a1f0f567a5198aa1fcc8e3f213143 Initial counter = Result (64 bytes) = 36f7f51ca8b1af61feac35a86416fa47 fbca3b5f749cdf564527f2314f42fe25 03332742b228c647173616cfd44c54eb Plaintext (64 bytes) = AAD (1 bytes) =Key = Nonce = 03000000000000000000000 Record authentication key = b5d3c529dfafac43136d2d11be284d7f Record encryption key = b914f4742be9e1d7a2f84addbf96dec3 456e3c6c05ecc157cdbf0700fedad222 POLYVAL input = 080000000000000000200000000000 da58d2f61b0a9d343b2f37fb0c519733 POLYVAL result = POLYVAL result XOR nonce = d958d2f61b0a9d343b2f37fb0c519733 7d3f0e4d217c1e551f59727870beefc9 8cb933a8fce9de887b1e40799988db1f c3f91880ed405b2dd298318858467c89 5bde0285037c5de81e5b570a049b62a0

Plaintext (4 bytes) = AAD (12 bytes) = Key = Nonce = Record authentication key = Record encryption key = POLYVAL input = POLYVAL result = POLYVAL result XOR nonce = and masked = Tag = Initial counter = Result (20 bytes) =	02000000 010000000000000000000000000000
Plaintext (20 bytes) = AAD (18 bytes) = Key = Nonce = Record authentication key = Record encryption key = POLYVAL input =	03000000000000000000000000000000000000
POLYVAL result XOR nonce = and masked = Tag = Initial counter = Result (36 bytes) =	943ef4fd04bd31d193816ab26f8655ca 943ef4fd04bd31d193816ab26f86554a b879ad976d8242acc188ab59cabfe307 b879ad976d8242acc188ab59cabfe387 43dd0163cdb48f9fe3212bf61b201976 067f342bb879ad976d8242acc188ab59 cabfe307
Plaintext (18 bytes) = AAD (20 bytes) =	03000000000000000000000000000000000000

02000000 Key = 030000000000000000000000 Nonce = Record authentication key = b5d3c529dfafac43136d2d11be284d7f Record encryption key = b914f4742be9e1d7a2f84addbf96dec3 456e3c6c05ecc157cdbf0700fedad222 POLYVAL input = 2cbb6b7ab2dbffefb797f825f826870c POLYVAL result = POLYVAL result XOR nonce = 2fbb6b7ab2dbffefb797f825f826870c
... and masked = 2fbb6b7ab2dbffefb797f825f826870c
Tag = 2fbb6b7ab2dbffefb797f825f826870c
cfcdf5042112aa29685c912fc2056543
Result (34 bytes) = 462401724b5ce6588d5a54aae5375513 a075cfcdf5042112aa29685c912fc205 6543 Plaintext (0 bytes) = AAD (0 bytes) = Key = e66021d5eb8e4f4066d4adb9c33560e4 f46e44bb3da0015c94f7088736864200 e0eaf5284d884a0e77d31646 Nonce = Record authentication key = e40d26f82774aa27f47b047b608b9585POLYVAL result XOR nonce = e0eaf5284d884a0e77d3164600000000 Plaintext (3 bytes) = 671fdd AAD (5 bytes) = 4fbdc66 AAD (5 bytes) = 4fbdc66f14 Key = bae8e37fc83441b16034566b7a806c46 bb91c3c5aedb64a6c590bc84d1a5e269 e4b47801afc0577e34699b9e Nonce = Record authentication key = b546f5a850d0a90adfe39e95c2510fc6 Record encryption key = b9d1e239d62cbb5c49273ddac8838bdc c53bca478a770f07087caa4e0a924a55 POLYVAL input =

280000000000000180000000000000 POLYVAL result = b91f91f96b159a7c611c05035b839e92 Plaintext (6 bytes) = 195495860f04 AAD (10 bytes) = 6787f3ea22c127aaf195 Key = 6545fc880c94a95198874 6545fc880c94a95198874296d5cc1fd1 Key = 61320b6920ce07787f86743b275d1ab3 2f6d1f0434d8848c1177441f Nonce = Record authentication key = e156e1f9b0b07b780cbe30f259e3c8daPOLYVAL result XOR nonce = 032511dde6ee355335b1aade09bd40c1
... and masked = 032511dde6ee355335b1aade09bd4041
Tag = 6b62b84dc40c84636a5ec12020ec8c2c
Initial counter = 6b62b84dc40c84636a5ec12020ec8cac
Result (22 bytes) = a254dad4f3f96b62b84dc40c84636a5e
c12020ec8c2c c12020ec8c2c Plaintext (9 bytes) = c9882e5386fd9f92ec

AAD (15 bytes) = 489c8fde2be2cf97e74e932d4ed87d

Key = d1894728b3fed1473c528b8426a58299
5929a1499e9ad8780c8d63d0ab4149c0

Nonce = 9f572c614b4745914474e7c7 Nonce = 9f572c614b4745914474e7c7 Record authentication key = 0533fd71f4119257361a3ff1469dd4e5c9882e5386fd9f92ec00000000000000 POLYVAL result XOR nonce = 204127a8959f83a113a6244dae552fb4 Polival result for honce - 204127a8959f83a113a6244dae552f34

Tag = 204127a8959f83a113a6244dae552f34

cofd3dc6628dfe55ebb0b9fb2295c8c2

Result (25 bytes) = 204127a8959f83a113a6244dae552f34

cofd3dc6628dfe55ebb0b9fb2295c8c2

Odf9e308678244c44bc0fd3dc6628dfe
55ebb0b9fb2295c8c2

Plaintext (12 bytes) = 1db2316fd568378da107b52b

AAD (20 bytes) = 0da55210cc1c1b0abde3b2f204d1e9f8
b06bc47f b06bc47f a44102952ef94b02b805249bac80e6f6 Key = 1455bfac8308a2d40d8c845117808235 5c9e940fea2f582950a70d5a Nonce = Record authentication key = 64779ab10ee8a280272f14cc8851b727Record encryption key = 25f40fc63f49d3b9016a8eeeb75846e0 d72ca36ddbd312b6f5ef38ad14bd2651 POLYVAL input = 0da55210cc1c1b0abde3b2f204d1e9f8 1db2316fd568378da107b52b00000000 POLYVAL result = cc86ee22c861e1fd4/4c846/6b42/39c
POLYVAL result XOR nonce = 90187a2d224eb9d417eb893d6b42739c
... and masked = 90187a2d224eb9d417eb893d6b42731c
Tag = 404099c2587f64979f21826706d497d5
Initial counter = 404099c2587f64979f21826706d497d5
Result (28 bytes) = 8dbeb9f7255bf5769dd56692404099c2
587f64979f21826706d497d5 Plaintext (15 bytes) = 21702de0de18baa9c9596291b08466
AAD (25 bytes) = f37de21c7ff901cfe8a69615a93fdf7a 98cad481796245709f 9745b3d1ae06556fb6aa7890bebc18fe Key = 6b3db4da3d57aa94842b9803a96e07fb 6de71860f762ebfbd08284e4 Nonce = Record authentication key = 27c2959ed4daea3b1f52e849478de376 Record encryption key = 307a38a5a6cf231c0a9af3b527f23a62 e9a6ff09aff8ae669f760153e864fc93 POLYVAL input = f37de21c7ff901cfe8a69615a93fdf7a 98cad481796245709f00000000000000 21702de0de18baa9c9596291b0846600 POLIVAL result = C41a3e3b713833703bC16e64243031a3
POLIVAL result XOR nonce = a91d463b865ab88beb4d0a8024505fa5

... and masked = a91d463b865ab88beb4d0a8024505f25

Tag = b3080d28f6ebb5d3648ce97bd5ba67fd

Result (31 bytes) = 793576dfa5c0f88729a7ed3c2f1bffb3
080d28f6ebb5d3648ce97bd5ba67fd Plaintext (18 bytes) = b202b370ef9768ec6561c4fe6b7e7296 fa85 AAD (30 bytes) = 9c2159058b1f0fe91433a5bdc20e214e ab7fecef4454a10ef0657df21ac7

Key = b18853f68d833640e42a3c02c25b6486 9e146d7b233987bddfc240871d7576f7 Nonce = 028ec6eb5ea7e298342a94d4 Record authentication key = 670b98154076ddb59b7a9137d0dcc0f0 Record encryption key = 78116d78507fbe69d4a820c350f55c7c b36c3c9287df0e9614b142b76a587c3f 9c2159058b1f0fe91433a5bdc20e214e POLYVAL input = ab7fecef4454a10ef0657df21ac70000 b202b370ef9768ec6561c4fe6b7e7296 POLYVAL result = 4e4108f09f41d797dc9256f8da8d58c7 POLYVAL result XOR nonce = 4ccfce1bc1e6350fe8b8c22cda8d58c7 Tag = 454fc2a154fea91f8363a39fec7d0a49
Initial counter = 454fc2a154fea91f8363a39fec7d0ac9
Result (34 bytes) = 857e16a64915a787637687db4a951963 Initial counter =
Result (34 bytes) = 5cdd454fc2a154fea91f8363a39fec7d 0a49 Plaintext (21 bytes) = ced532ce4159b035277d4dfbb7db6296 8b13cd4eec 734320ccc9d9bbbb19cb81b2af4ecbc3 AAD (35 bytes) =e72834321f7aa0f70b7282b4f33df23f 167541 Key = 3c535de192eaed3822a2fbbe2ca9dfc8 8255e14a661b8aa82cc54236093bbc23 Nonce = 688089e55540db1872504e1c Record authentication key = cb8c3aa3f8dbaeb4b28a3e86ff6625f8 Record encryption key = 02426ce1aa3ab31313b0848469a1b5fc6c9af9602600b195b04ad407026bc06d POLYVAL input = 734320ccc9d9bbbb19cb81b2af4ecbc3 e72834321f7aa0f70b7282b4f33df23f ced532ce4159b035277d4dfbb7db6296 1801000000000000a800000000000000 POLYVAL result = ffd503c7dd712eb3791b7114b17bb0cf ${\tt POLYVAL\ result\ XOR\ nonce\ =\ 97558a228831f5ab0b4b3f08b17bb0cf}$... and masked = 97558a228831f5ab0b4b3f08b17bb04f Tag = 9d6c7029675b89eaf4ba1ded1a286594Tag = Initial counter = 9d6c7029675b89eaf4balded1a286594
Result (37 bytes) = 626660c26ea6612fb17ad91e8e767639 edd6c9faee9d6c7029675b89eaf4ba1d ed1a286594

C.3. Counter Wrap Tests

The tests in this section use AEAD_AES_256_GCM_SIV and are crafted to test correct wrapping of the block counter.

Plaintext (32 bytes) = 4db923dc793ee6497c76dcc03a98e108 AAD (0 bytes) =Key =Nonce = Record authencication Record encryption key = Record authentication key = dc95c078a24089895275f3d86b4fb868779b38d15bffb63d39d6e9ae76a9b2f3 75d11b0e3a68c422845c7d4690fa594f POLYVAL input = 4db923dc793ee6497c76dcc03a98e108 7367cdb411b730128dd56e8edc0eff56 POLYVAL result = POLYVAL result XOR nonce = 7367cdb411b730128dd56e8edc0eff56 Plaintext (24 bytes) = eb3640277c7ffd1303c7a542d02d3e4c 0000000000000000 AAD (0 bytes) =Key = Nonce = Record authencication
Record encryption key = Record authentication key = dc95c078a24089895275f3d86b4fb868779b38d15bffb63d39d6e9ae76a9b2f3 75d11b0e3a68c422845c7d4690fa594f eb3640277c7ffd1303c7a542d02d3e4c POLYVAL input = POLYVAL result = 7367cdb411b730128dd56e8edc0eff56 POLYVAL result XOR nonce = 7367cdb411b730128dd56e8edc0eff56 ... and masked = 7367cdb411b730128dd56e8edc0eff56 Tag = Initial counter = Result (40 bytes) = 888e53e72299e56dfffffff00000000 0000000000000000

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