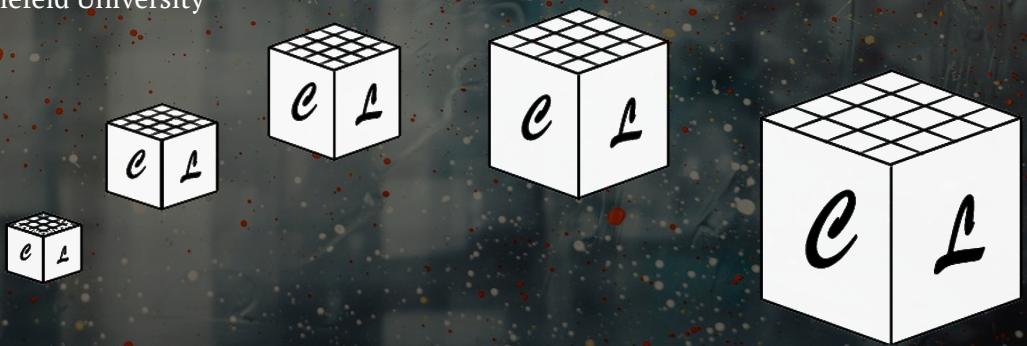


Parallelization in C_osmoLattice

September 2025, Daejeon

Franz R. Sattler

Bielefeld University



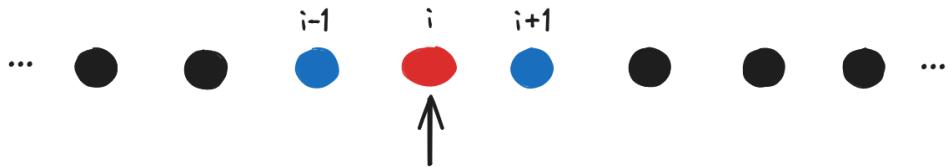
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And why would we want to?

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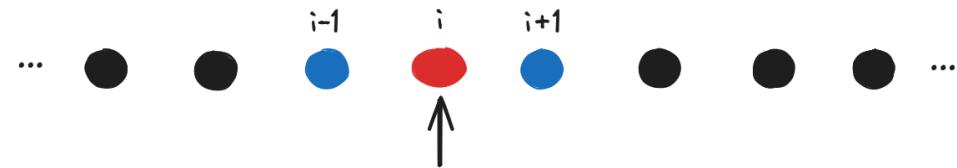
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(*Leapfrog scheme.*)

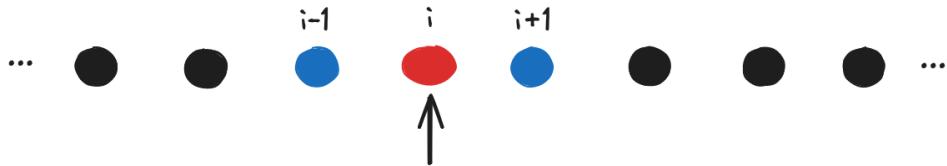
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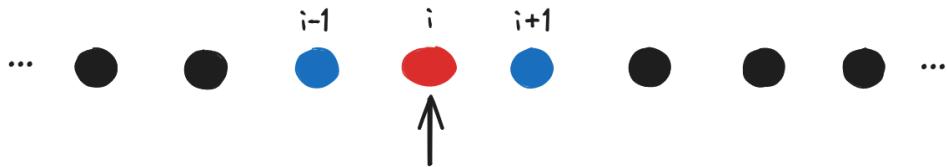
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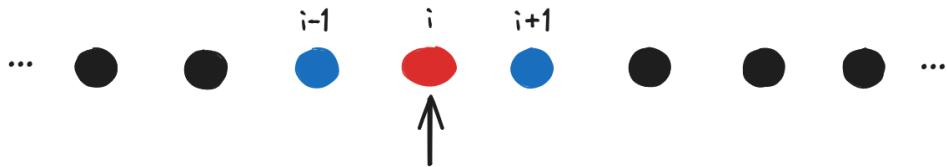
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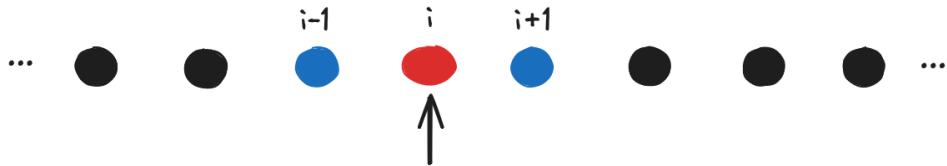
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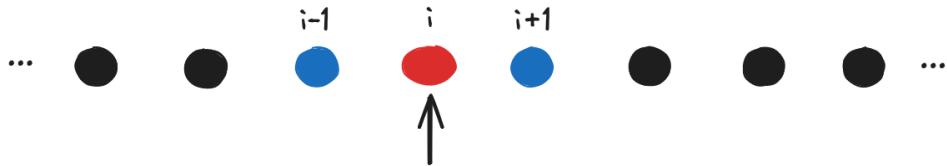
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Less granular: split **sub-regions** of lattice across many computers (**nodes**)

Type **distributed** **shared**

Data split between **nodes** shared by all **threads**

Computation split between **nodes** split between **threads**

Type	distributed	shared
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Cores: **Nodes** (distributed) and **Threads** (shared).

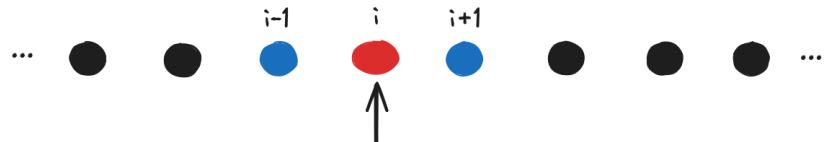
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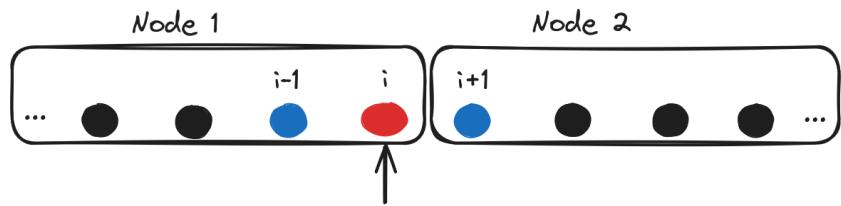
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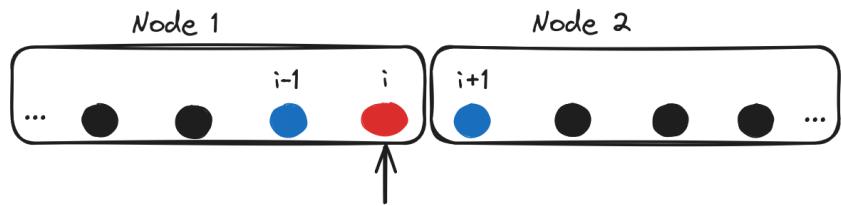
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Problem: Data is missing on node 1

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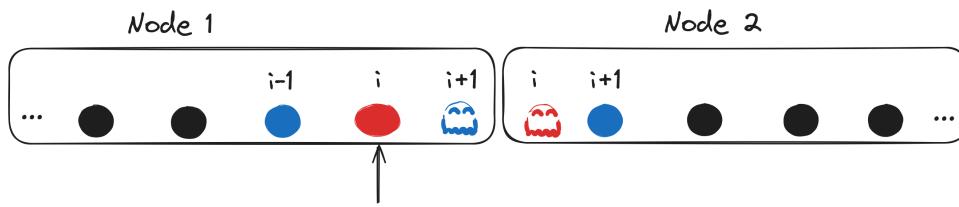
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Ghosts are local copies of data on other nodes.

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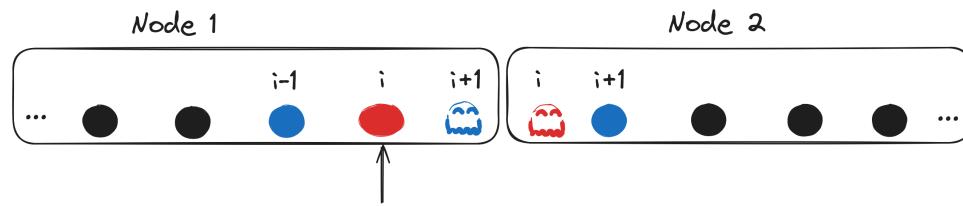
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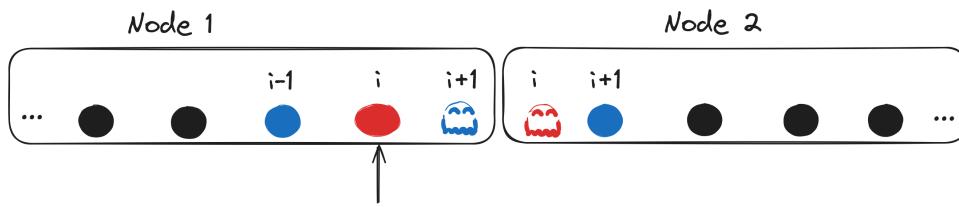
Need to update ghosts after every time-step.

Data communication

The standard for communication in distributed-memory applications:

Message Passing Interface (MPI)

Exchange ghost data between **nodes** over the **network** automatically if anything changes.

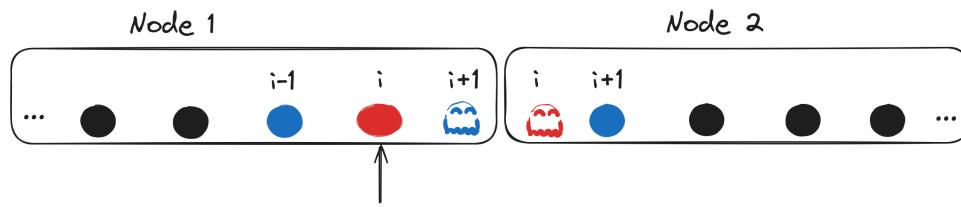


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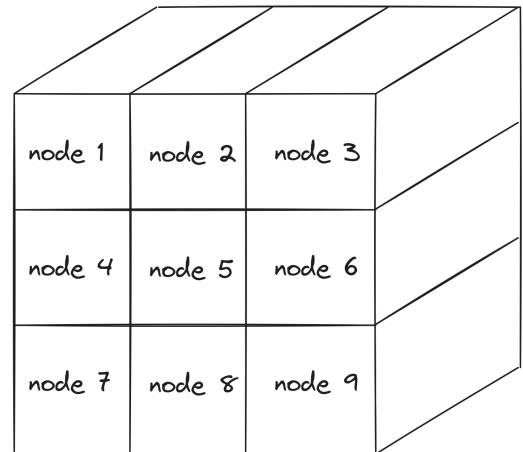
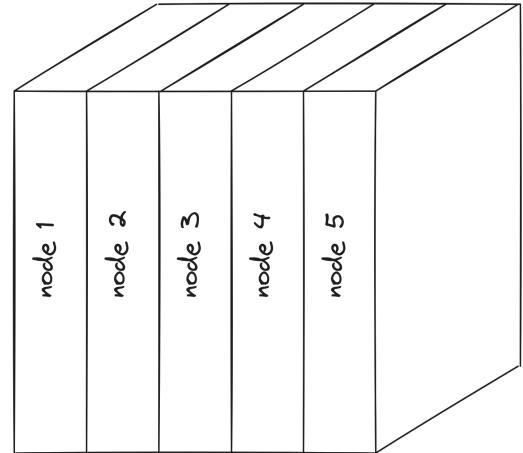
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CosmoLattice does this automatically under the hood!

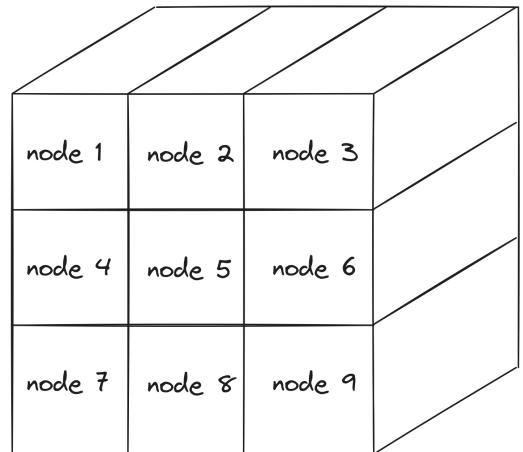
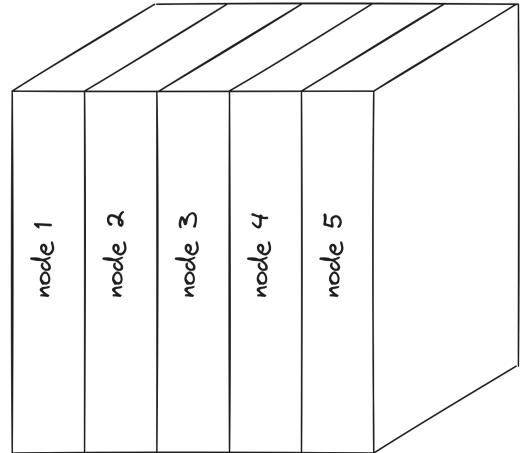
FFT parallelization

- FFTW supports parallelization along 1 direction.



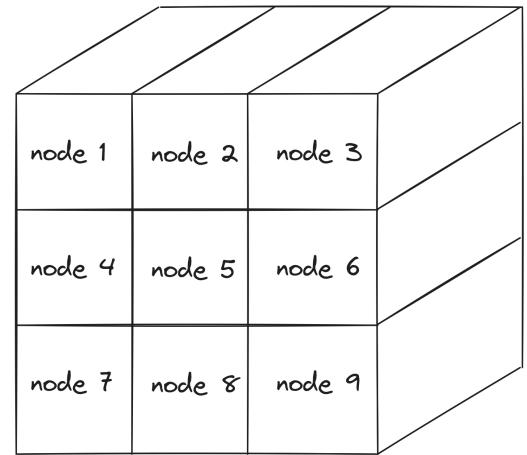
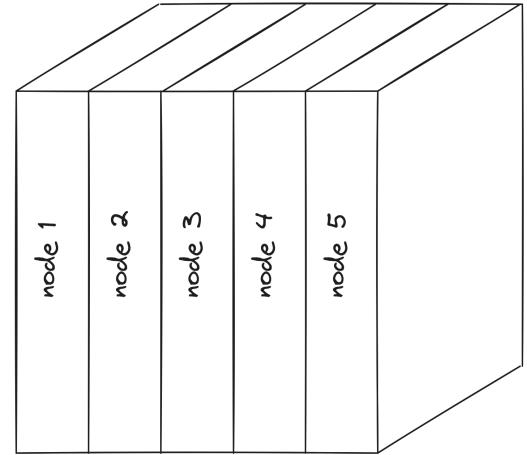
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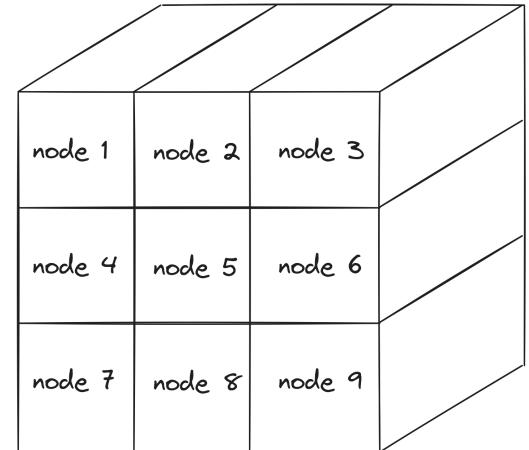
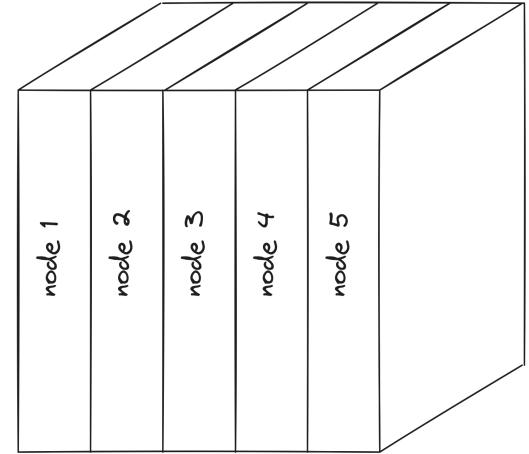
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$$N = n_p * m$$

$$N = 50$$

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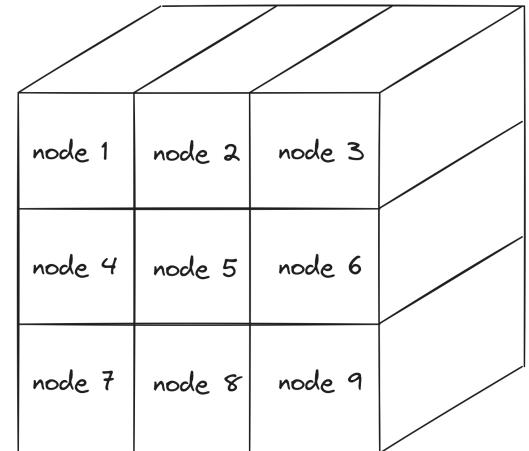
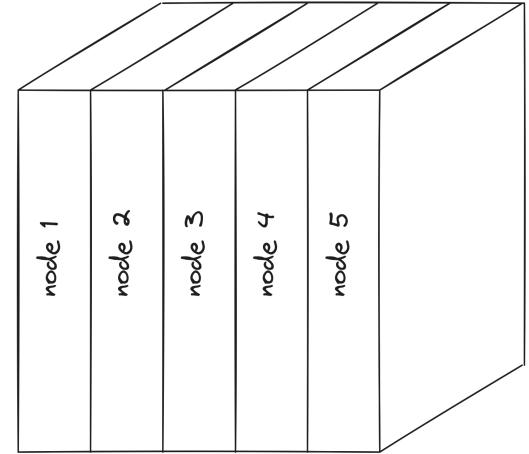
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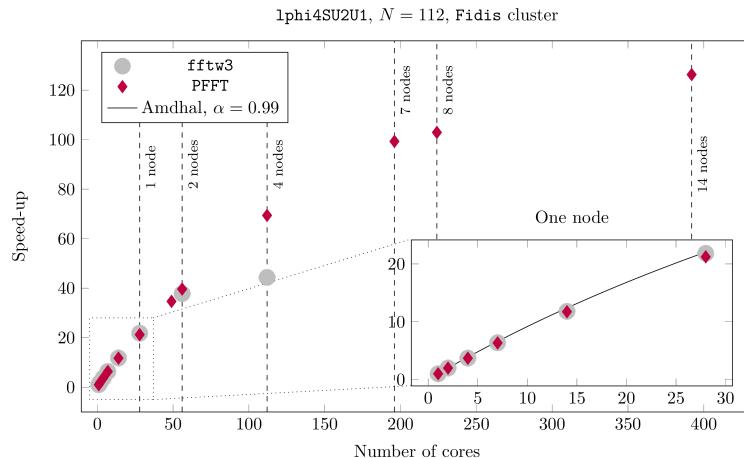
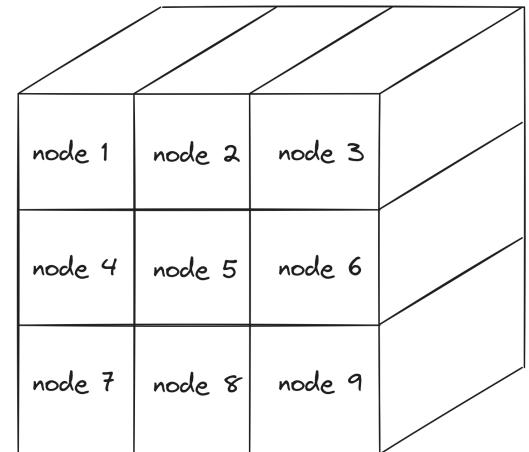
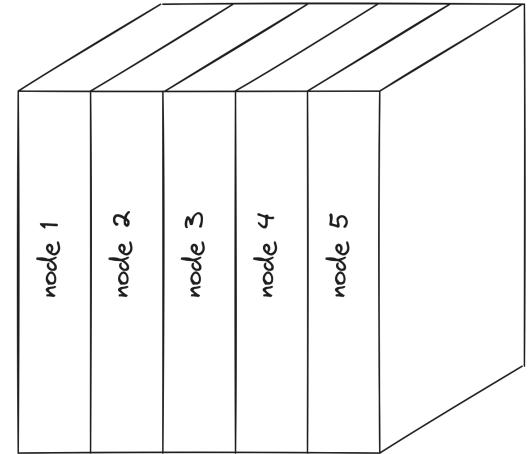


Figure 3: Speed up factor in parallelized simulations as a number of cores (tested on the Gacrux cluster from the EPFL HPC center SCITAS, Switzerland).



Questions?

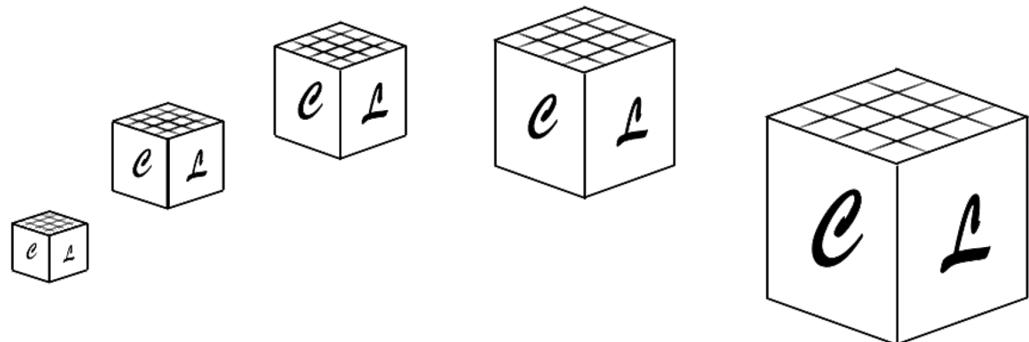
Tomorrow: Shared-memory parallelization with GPUs.

CosmoLattice on GPUs

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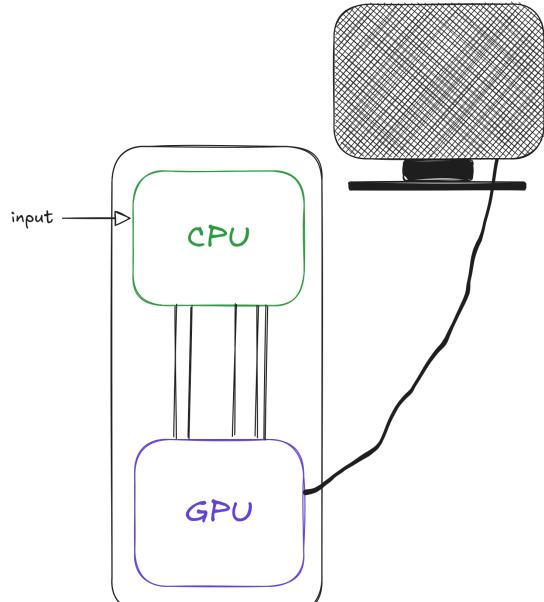
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GPUs: dedicated just for **video and graphics** applications.



A consumer machine

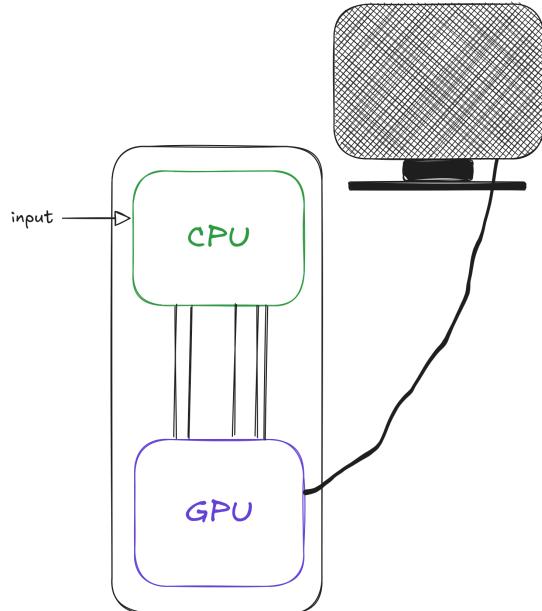
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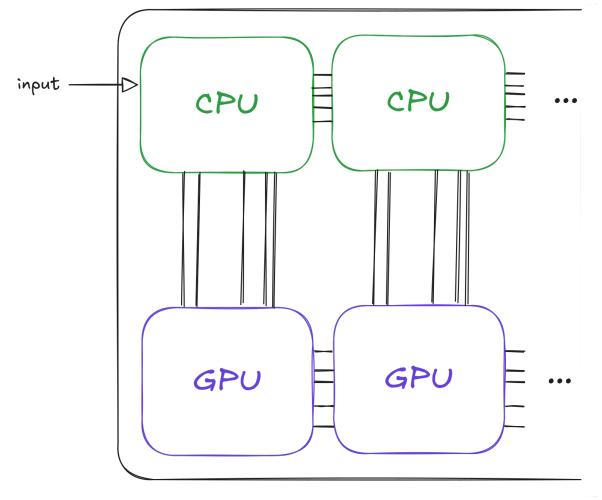
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Current (heterogeneous) clusters have both **CPU**s and **GPU**s for **computations**.



A consumer machine



A typical heterogeneous computing cluster

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Lattice points independently computed & updated → Limit of threads is number of lattice sites!

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■ Intel Xeon 6148 (Skylake): 20	Clock speed	~ 3 GHz	~ 1.5 GHz

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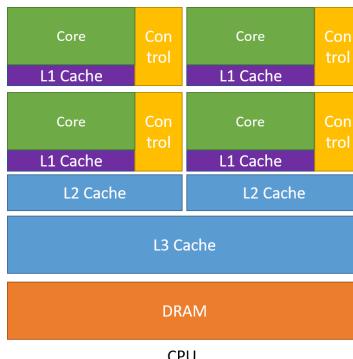
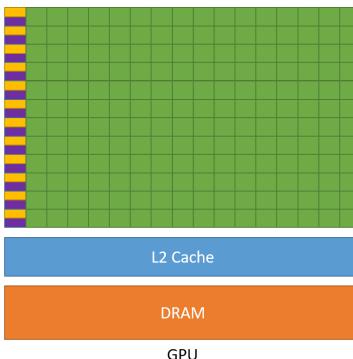
CPU: Low parallelization, high clock speed

GPU: High parallelization, moderate clock speed

→ CosmoLattice on GPUs has the potential for *massive parallelism* with $\gg 10^5$ simultaneous operations.

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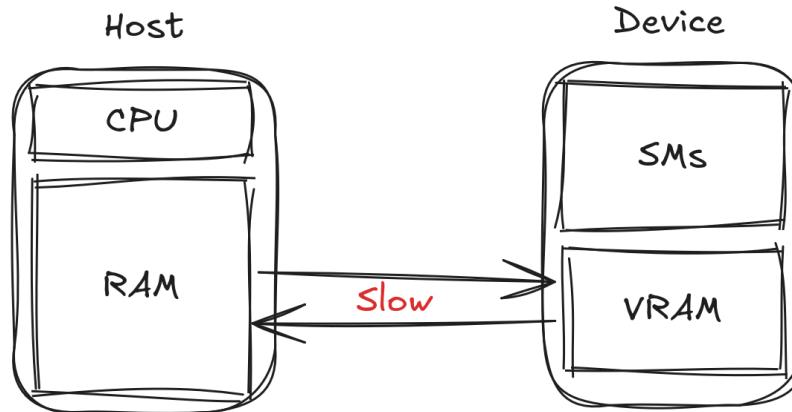
	CPU	GPU
Cache/Thread	64KB / 16MB	1KB
Local Cache	64MB	256KB / 50MB
		

CPU: Thread-constrained

GPU: Memory-constrained

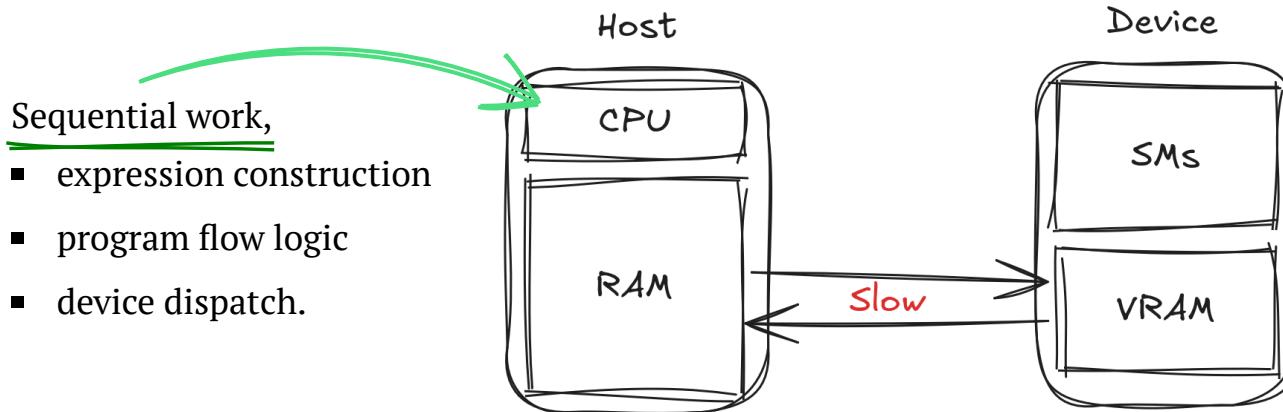
Redesigning TempLat for GPUs

Device-centric programming.



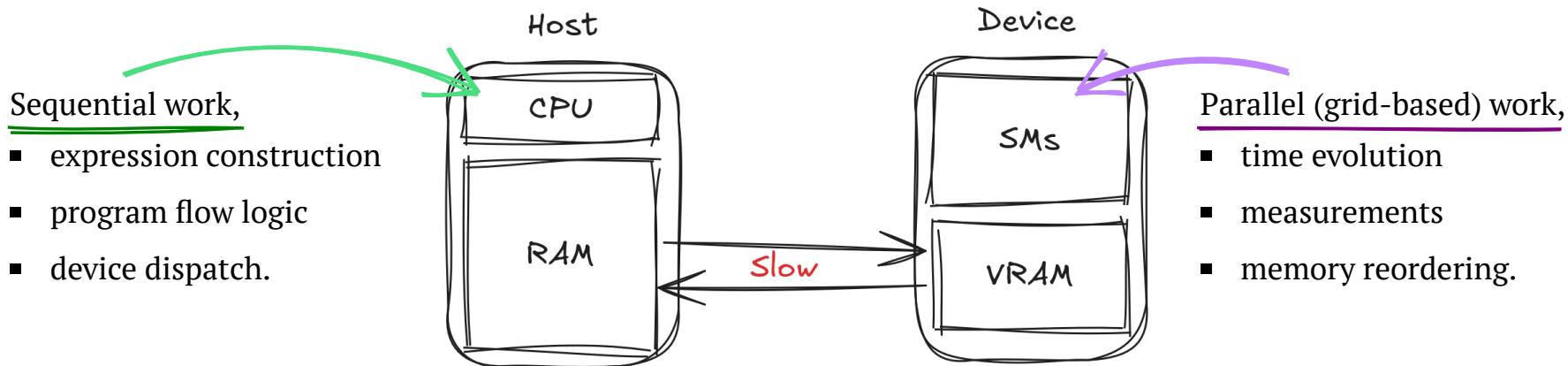
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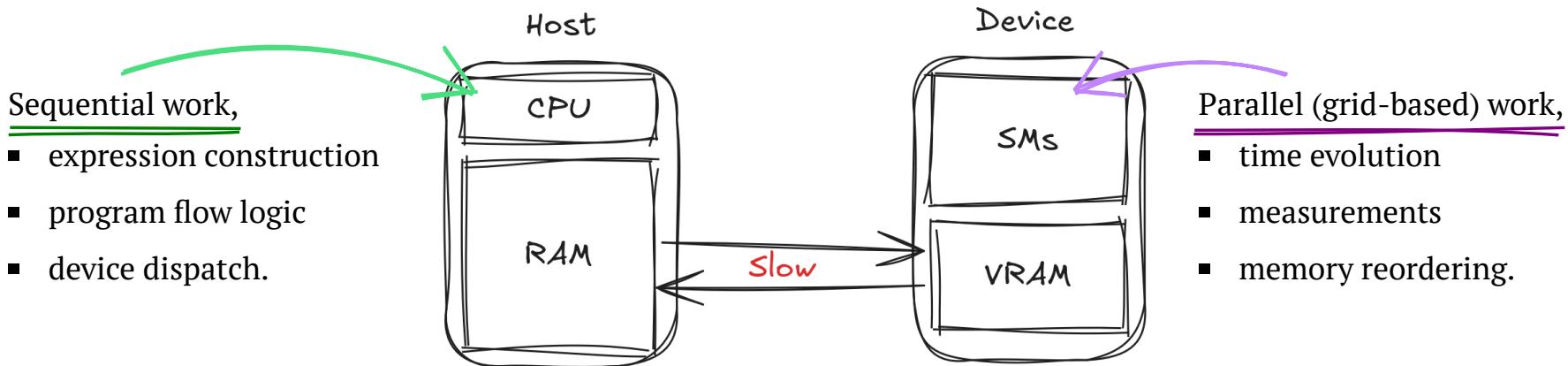
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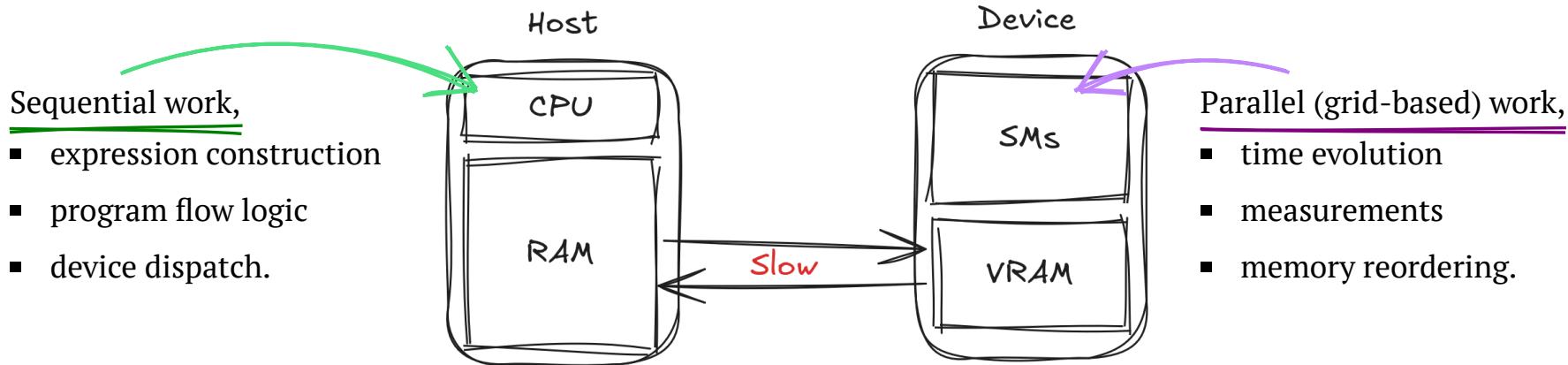
Standard C++ on CPU

Hardware-dependent

- NVIDIA: CUDA
- AMD: ROCM
- Intel: SYCL
- shared-memory CPUs
- FPGPAs

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Standard C++ on CPU

Backends

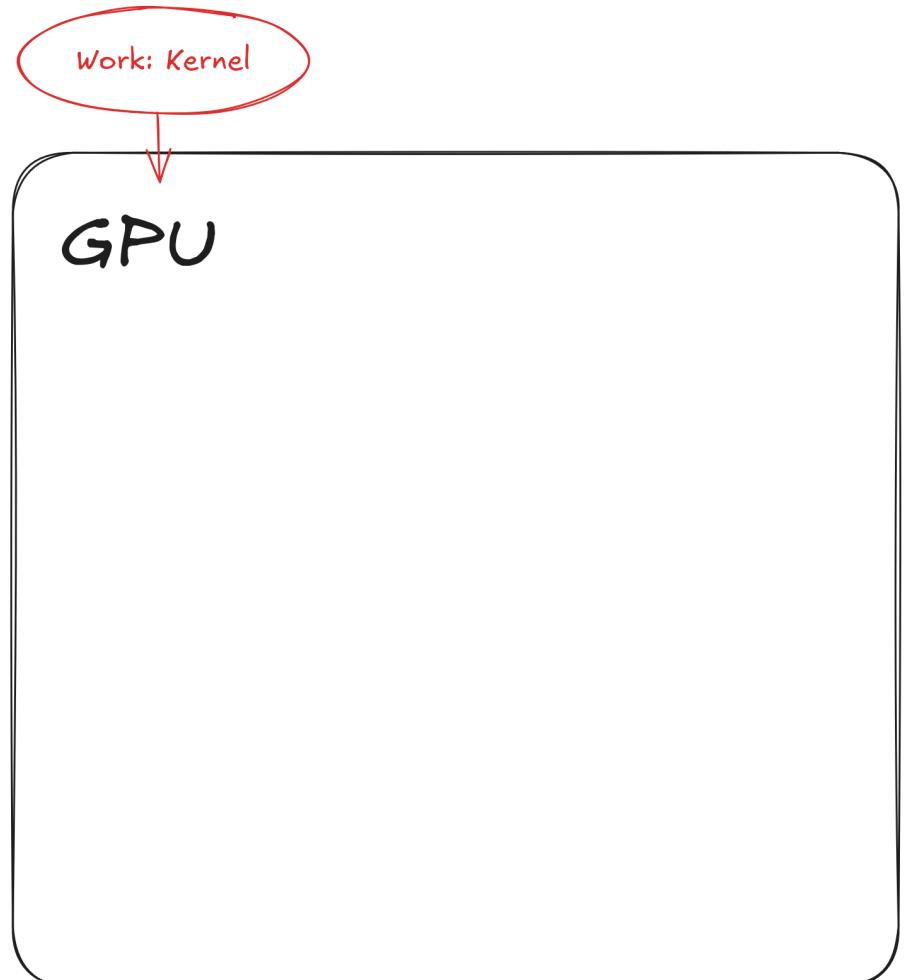
Abstracted away in TempLat

- Kokkos
- Sequential STL (2020/2023)
- ...

- `device::iterate::parallel_for`
- `device::iterate::parallel_reduce`
- `device::memory::copyHostToDevice`
- ...

GPU architecture

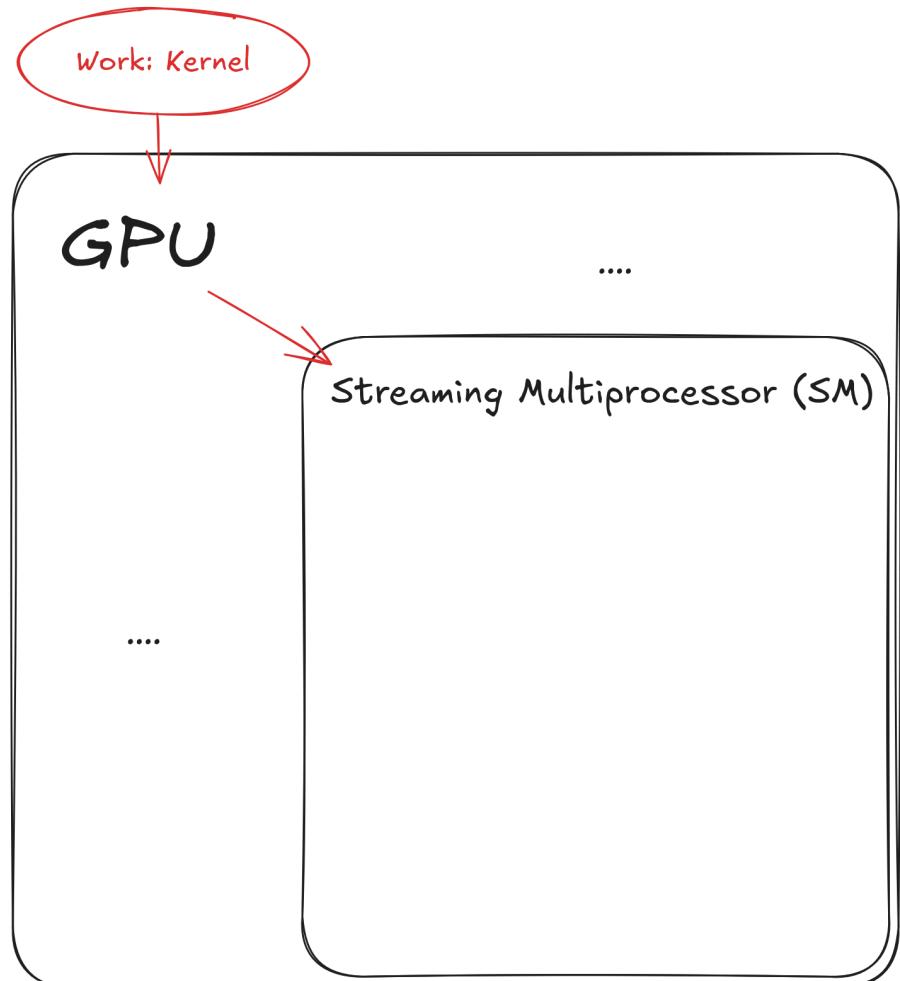
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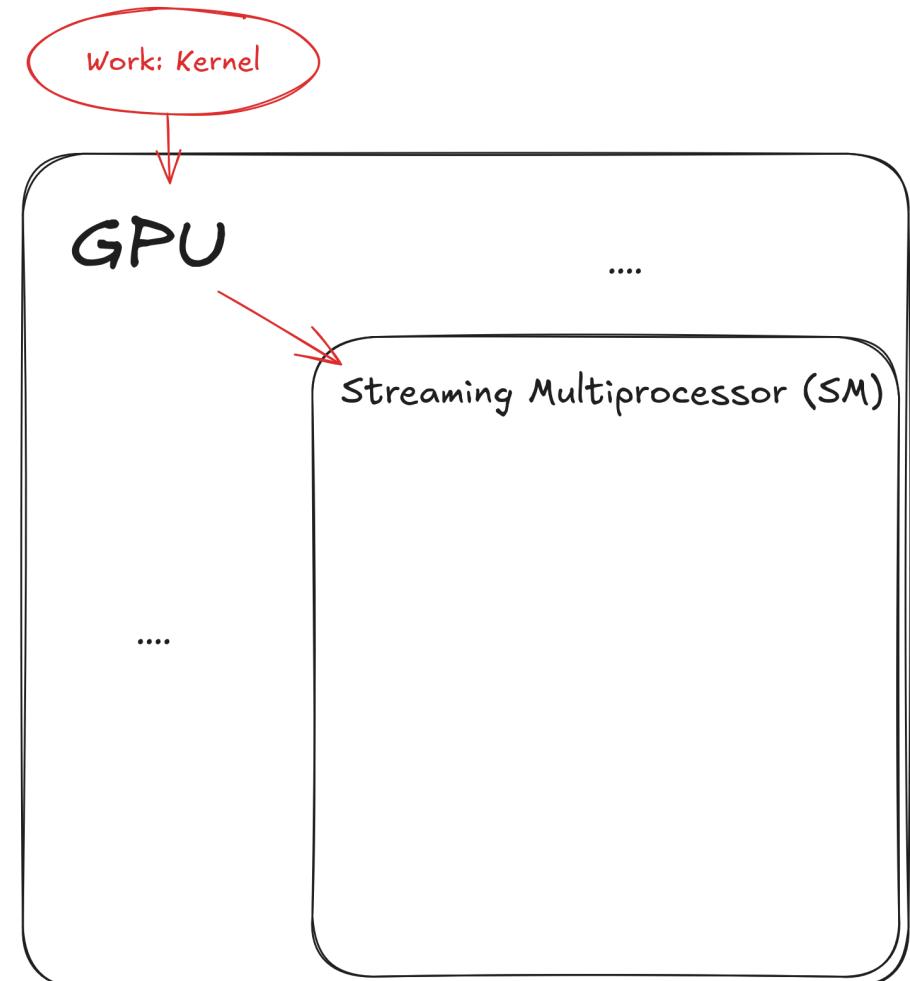
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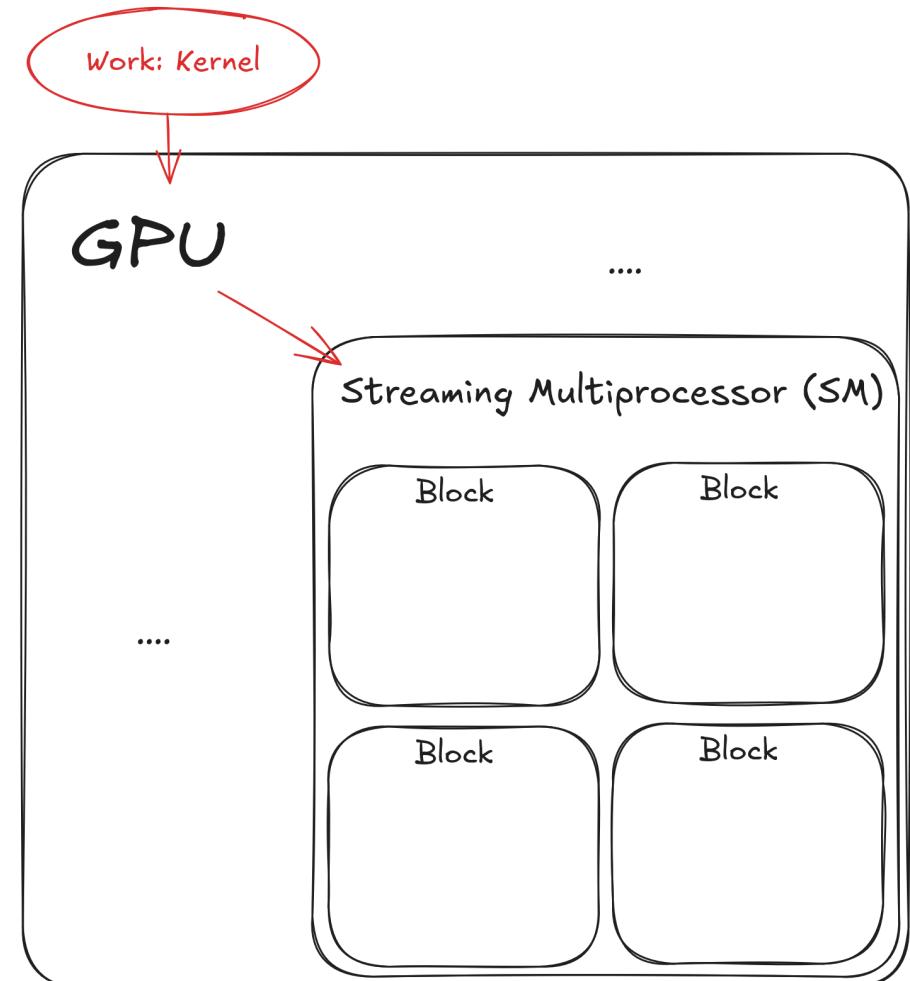
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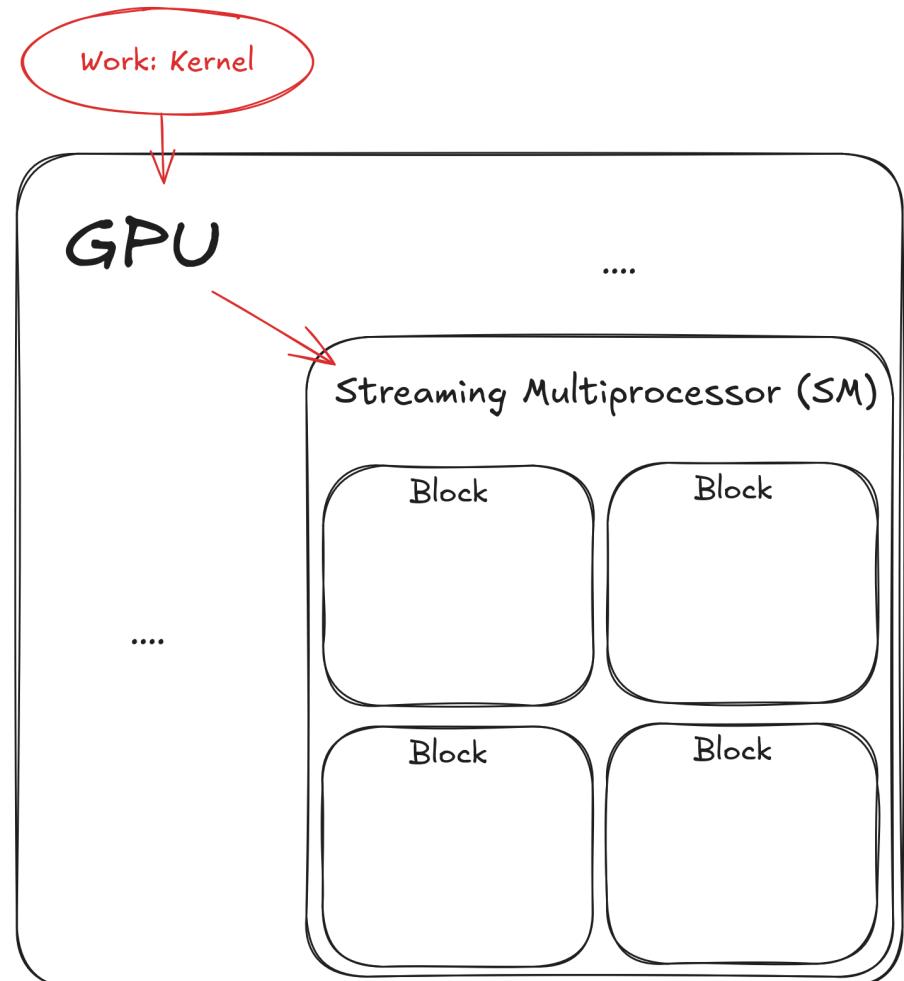
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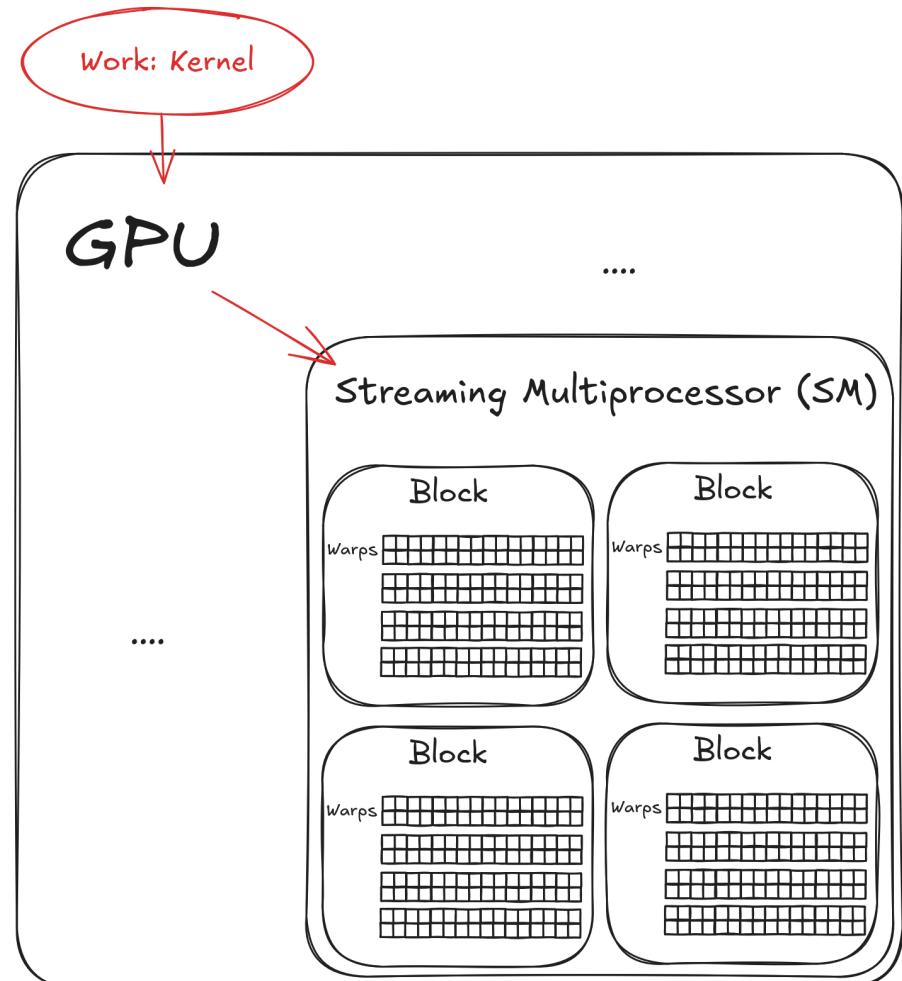
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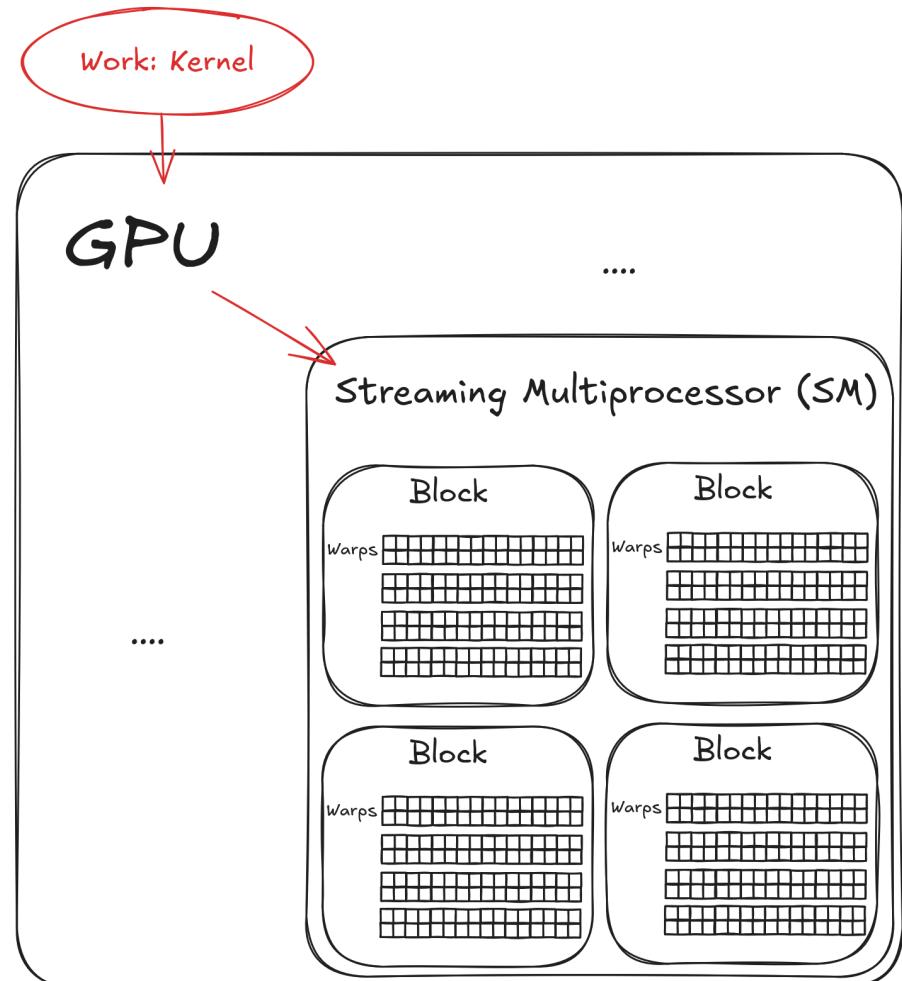
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- Internally, blocks are subdivided into *warps*.
 - Each warp runs a single instruction in a *kernel* in parallel.
 - Warp size is always 32 for Nvidia, 32 or 64 for AMD.



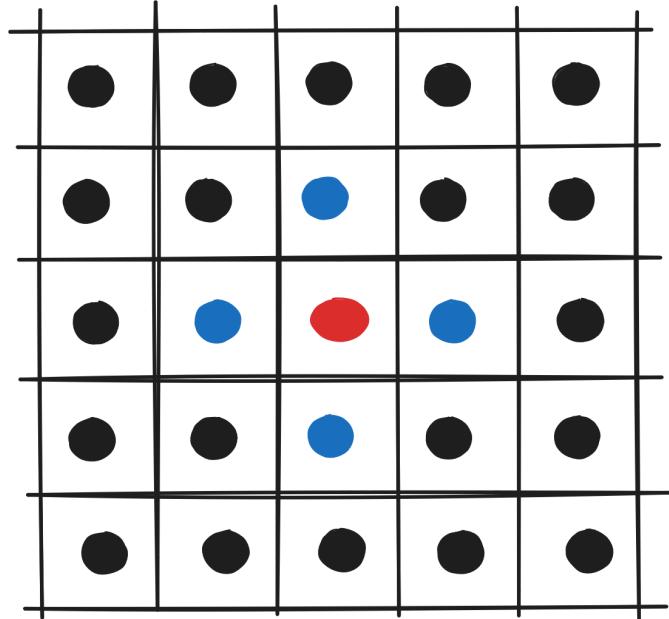
Memory access patterns

Coalescing vs. sequential access

Example: Solving massless Klein-Gordon equation in $d = 3$,

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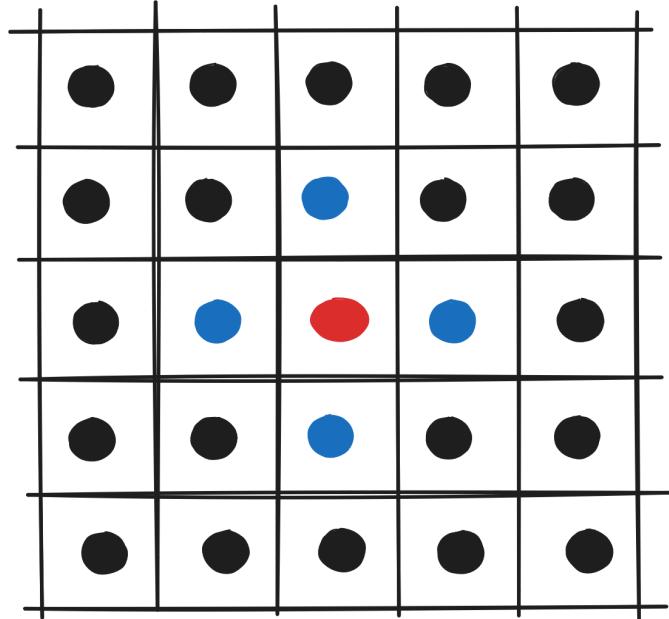
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What is the optimal way to iterate over sites?



Memory access patterns

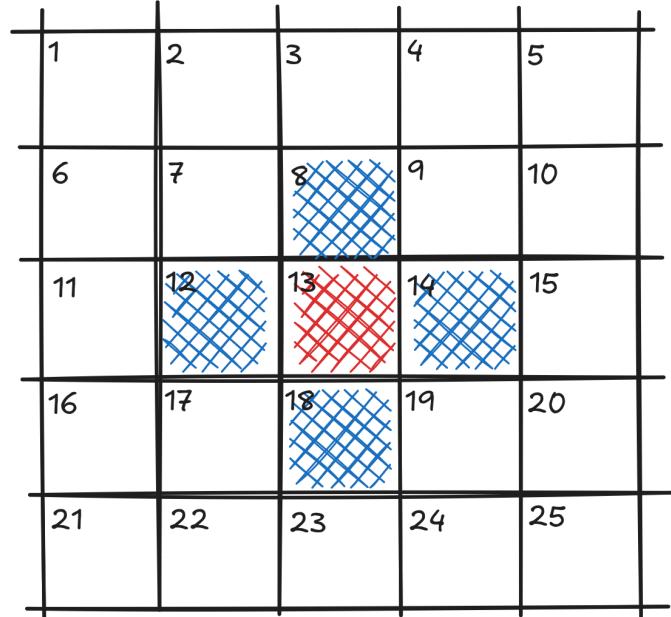
Coalescing vs. sequential access

Example: Solving massless Klein-Gordon equation in $d = 3$,

$$\partial_t^2 \phi(t, x) = \Delta \phi(t, x).$$

- Calculation of 1 thread at **red site**.
- **Blue sites** dependents for lattice Laplacian.
- Memory is ordered row-major.

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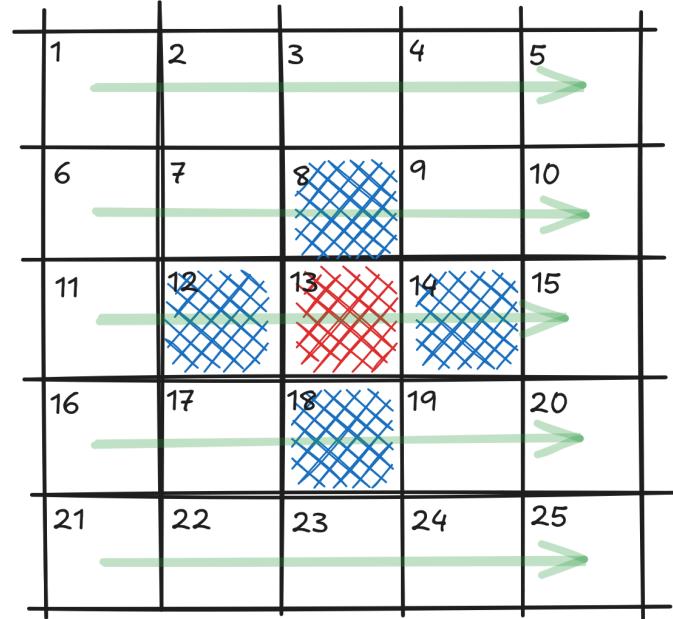
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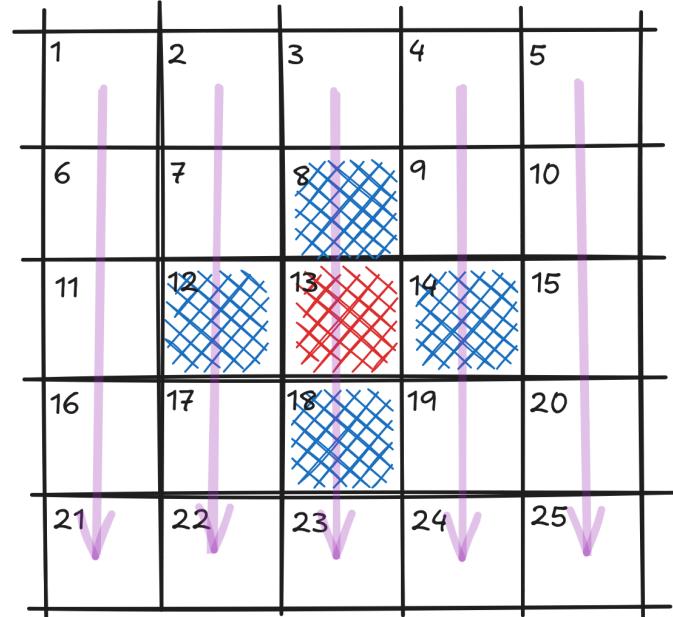
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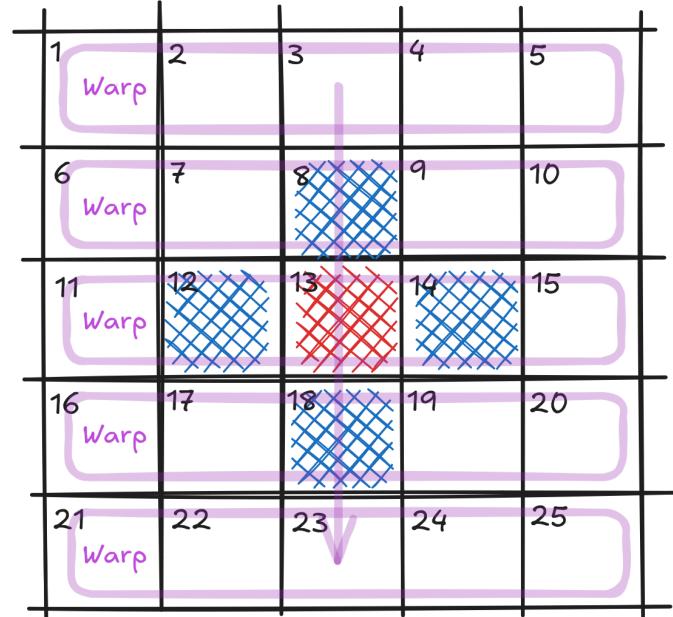
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This is similar to vectorization on a CPU!

SIMD (Single Instruction, Multiple Data) vs **SIMT** (Single Instruction, Multiple Threads)



Memory access patterns

Coalescing vs. sequential access

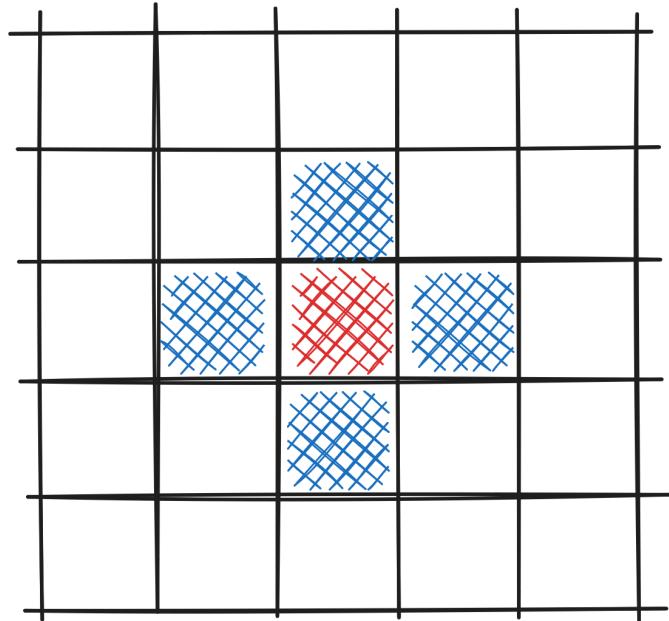
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CPU: Prefer **prefer row-major access pattern**.

GPU: Prefer **column-major access pattern**.



How does this perform *in vivo*?

```
1 #define FORCE_ACCESS_PATTERN 0 // or 1
2 ...
3
4 int main(int argc, char **argv)
5 {
6     constexpr size_t NDim = 3;
7     using T = double;
8     constexpr size_t nGrid = 512;
9     constexpr size_t nGhost = 1;
10    constexpr size_t nSteps = 512;
11    constexpr T dt = 0.01;
12    ...
13    Field<NDim, T> phi("phi", toolBox);
14    Field<NDim, T> pi("pi", toolBox);
15
16    Benchmark bench([&](Benchmark::Measurer &measurer) {
17        phi.inFourierSpace() = RandomGaussianField<NDim, T>("Rand", toolBox);
18        pi.inFourierSpace() = RandomGaussianField<NDim, T>("Rand2", toolBox);
19
20        for (size_t i = 0; i < nSteps; ++i) {
21            pi.updateGhosts();
22            device::iteration::fence();
23            measurer.measure("timestepping", [&]() {
24                pi = LatticeLaplacian<NDim, decltype(phi)>(phi); // kick
25                phi = phi + dt * pi;                                // drift
26                device::iteration::fence();
27            });
28        });
29    });
30}
```

```
1 ...
2     for (size_t i = 0; i < nSteps; ++i) {
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7             phi = phi + dt * pi;                                // drift
8             device::iteration::fence();
9         });
10    }
```

Running this on my PC:

GPU: NVIDIA 4070RTX mobile - 4788 Cores @ 2.175 GHz

CPU: Ryzen 9 7945HX - 16 Cores @ 5.4GHz

Taking a closer look

```
...
Benchmark bench([&](Benchmark::Measurer &measurer) {
    measurer.measure("x->k fourier", [&]() {
        phi.getMemoryManager()->confirmFourierSpace();
        pi.getMemoryManager()->confirmFourierSpace();
    });

    measurer.measure("initialize field", [&]() {
        phi.inFourierSpace() = RandomGaussianField<NDim, T>("Hoi", toolBox);
        pi.inFourierSpace() = RandomGaussianField<NDim, T>("Hai", toolBox);
    });

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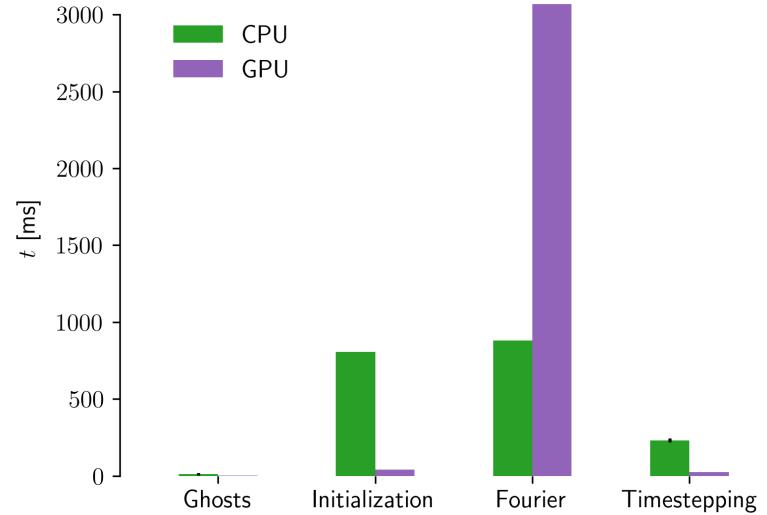
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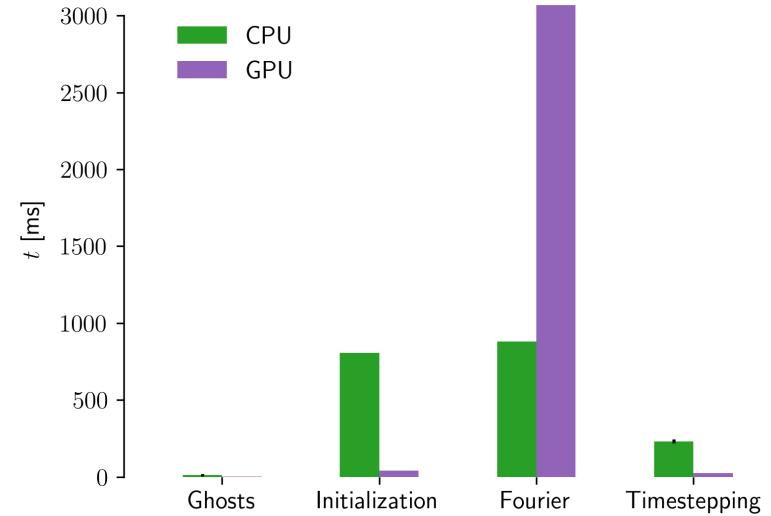
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- Fourier transformation is not yet optimized.
(take later benchmarks with a grain of salt!)

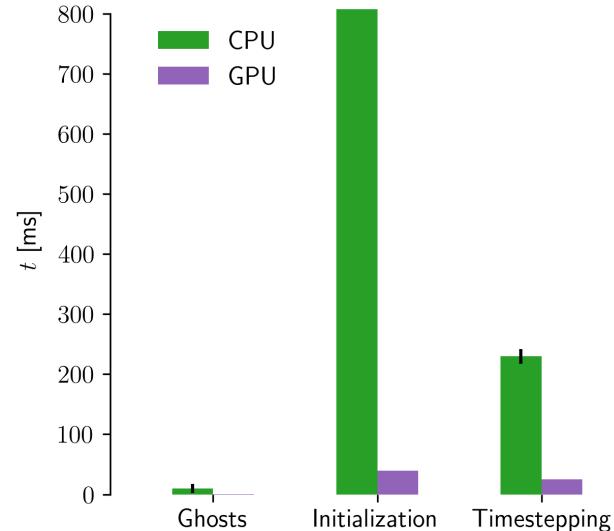
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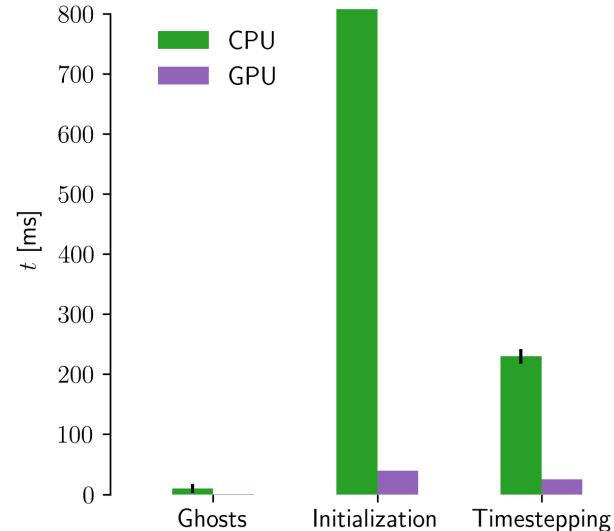
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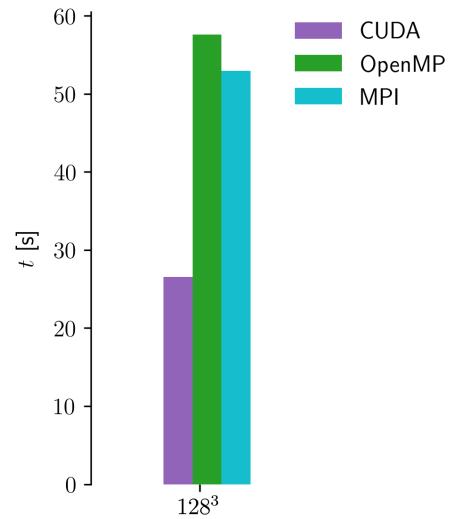
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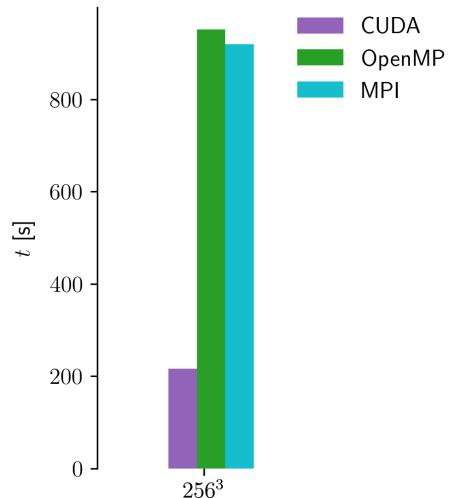
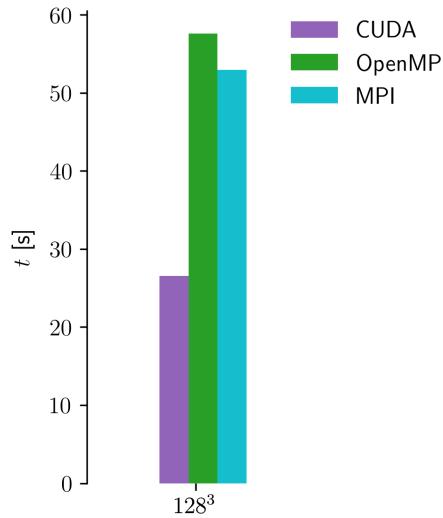
Benchmarking ϕ^4 -theory

with the `lphi4` model in CosmoLattice



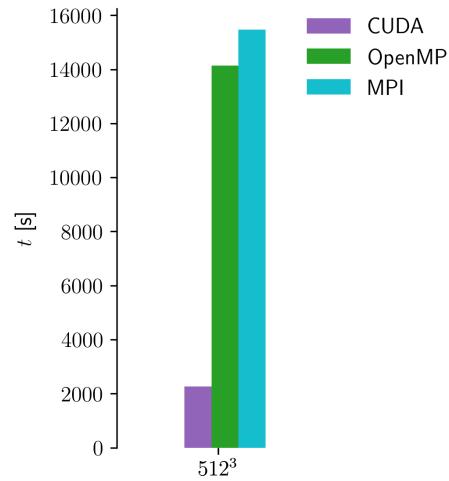
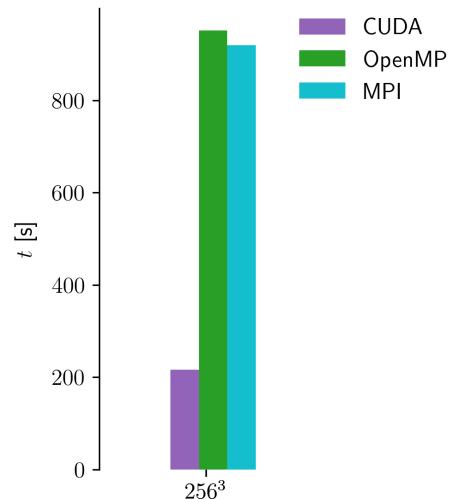
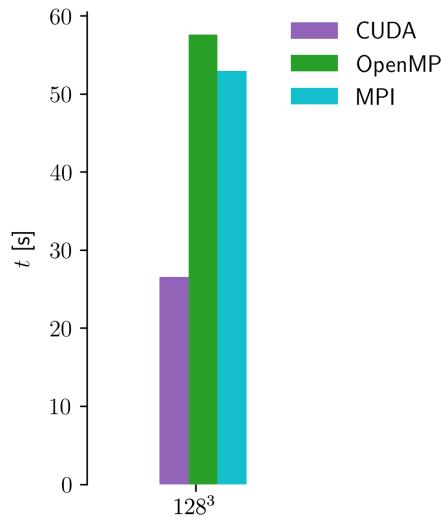
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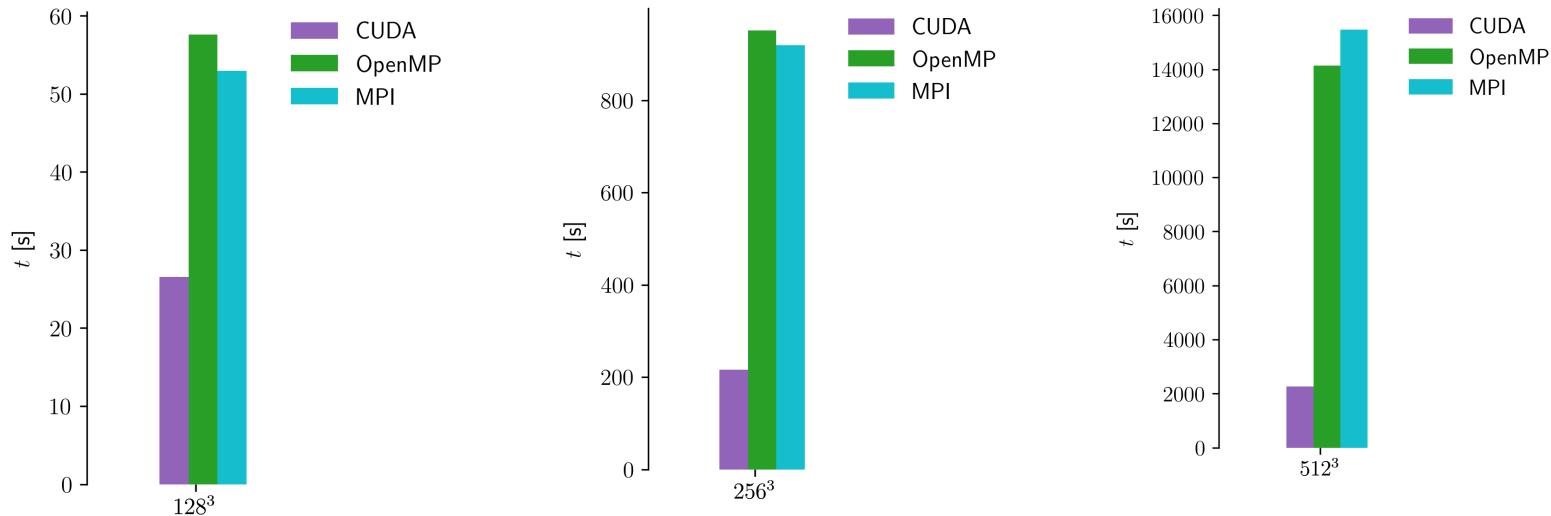
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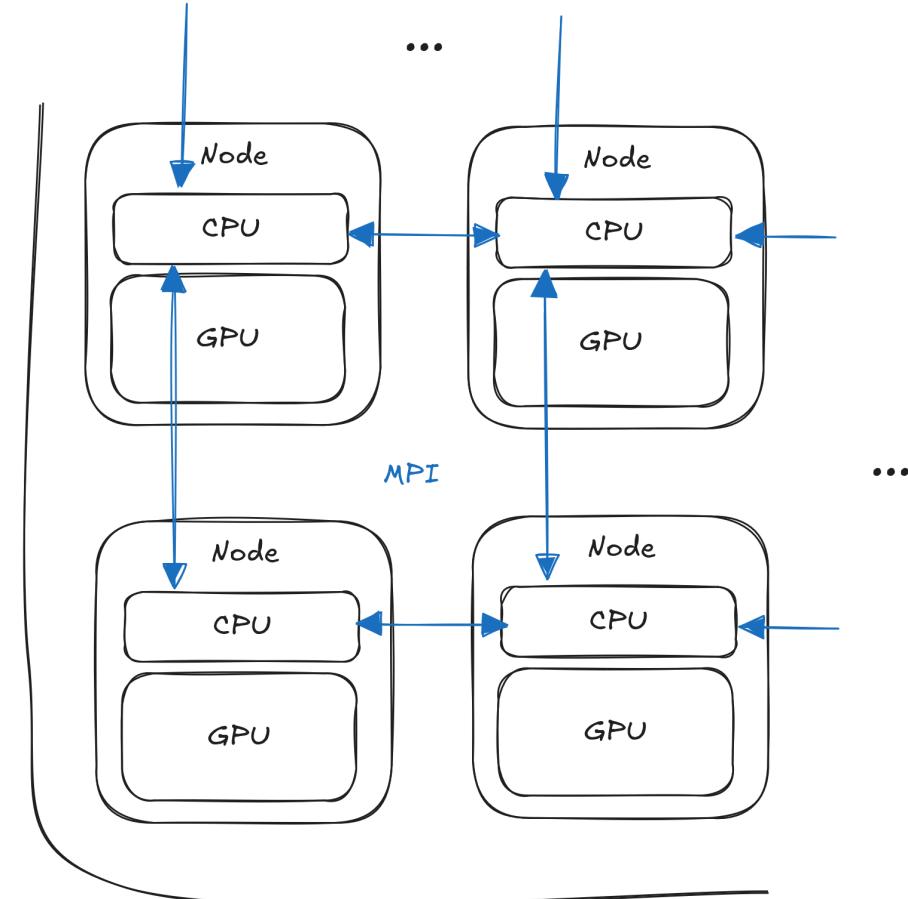


	CUDA runtime [s]	OpenMP runtime [s]	MPI runtime [s]	speedup factor
N=128	27	58	53	2
N=256	216	951	920	4
N=512	2260	14147	15471	7

Scaling it up

Using large GPU clusters

- To use large clusters and link up many nodes, CosmoLattice uses the **Message-Passing Interface (MPI)** (see lecture yesterday).
- Send data in RAM (e.g. ghosts) between neighbouring nodes.

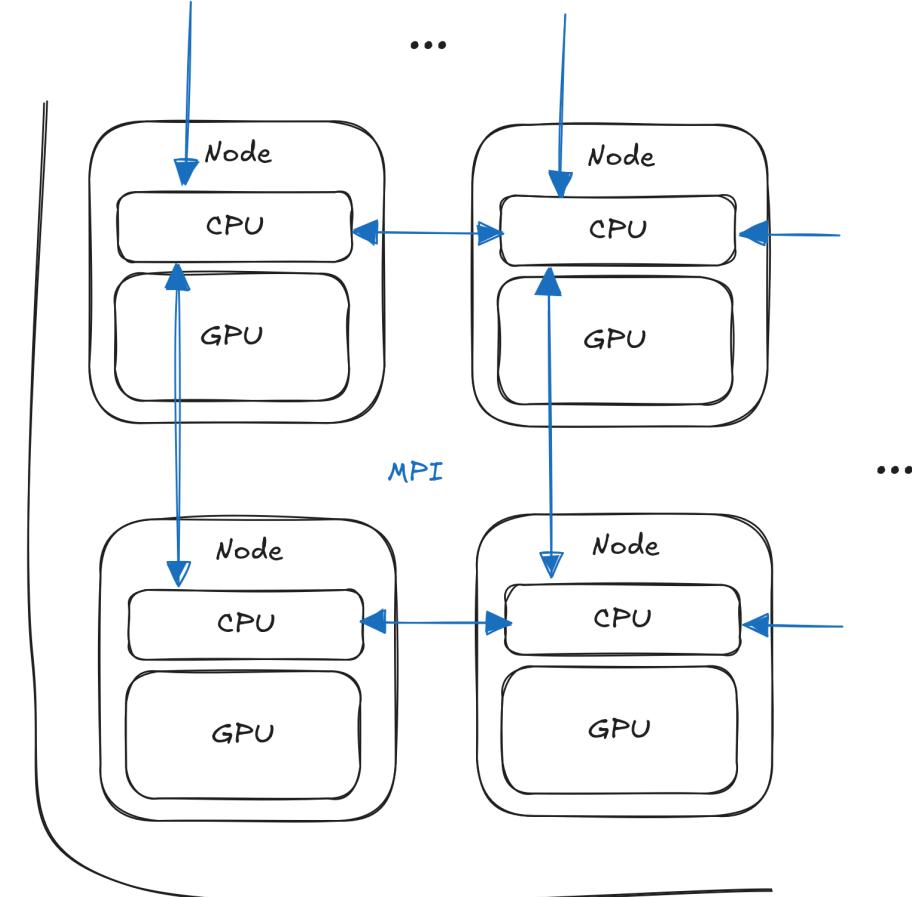


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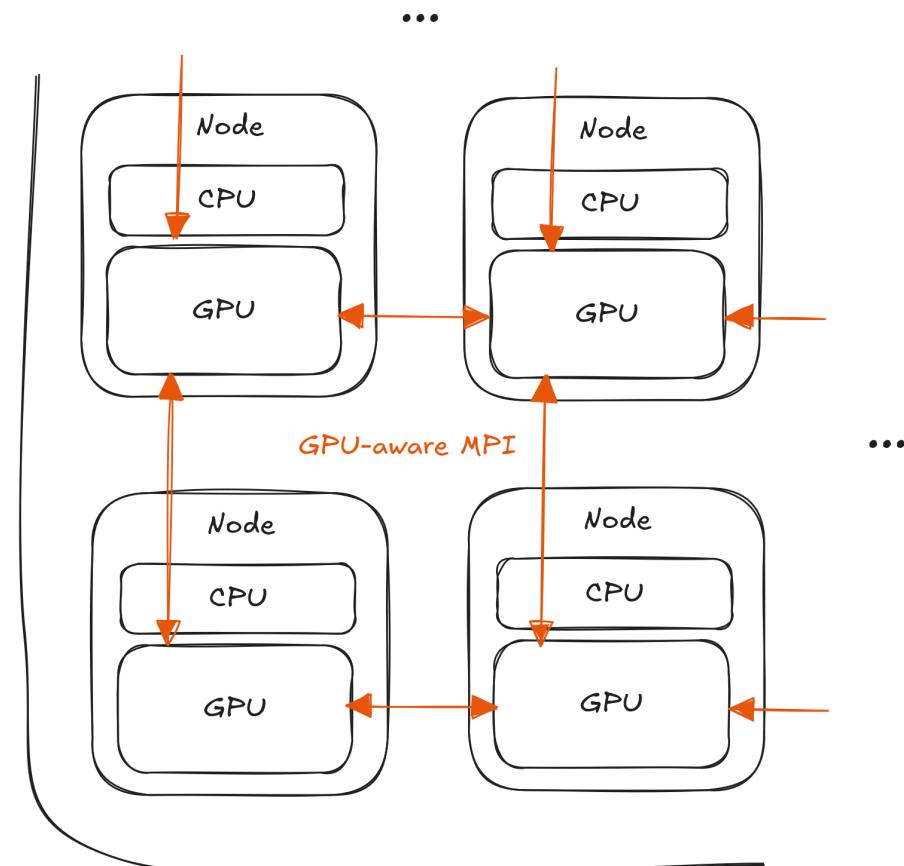
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What about MPI+GPUs?

- GPU-aware MPI** can exchange data directly between device memory.

Support since before 2013:

- OpenMPI
 - MVAPICH2
 - Cray MPI
 - IBM MPI
- No changes in MPI-code!



Questions?

Thanks for your attention!

Release of CosmoLattice with GPUs ~ early 2026