Texts in Computer Science

Recommendation Engines

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Guide to Intelligent Data Science

How to Intelligently Make Use of Real Data

Second Edition



Summary of this lesson

"We all make choices, but in the end our choices make us"
-Ken Levine

Are there events that always happen together?

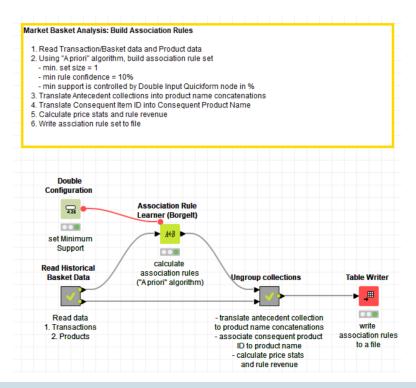
*This lesson refers to chapter 7 of the GIDS book

What you will learn

- Associaition Rules
- Itemset Mining
- Generating Associaition Rules
- Collaborative Filtering

Datasets

- Datasets used : transaction data & products data
- Example Workflow:
 - "Association_Rules_for_MarketBasketAnalysis" https://kni.me/w/fQ9yZLztzEUmAsQ0



Association Rules

Overview

Association Rules: Motivation

- Item Set Mining
 - Breadth First Searching: The Apriori Algorithm
 - Depth First Searches: The Eclat Algorithm
 - (Compact) Representation of Itemsets
- Finding Association Rules

Association Rule Mining

Association rule induction

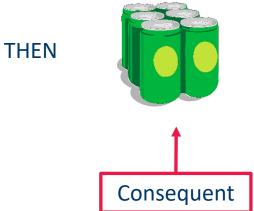
- Originally designed for market basket analysis.
- Aims at finding patterns in the shopping behavior of customers of supermarkets, mail-order companies, on-line shops etc.

More specifically:

- Find sets of products that are frequently bought together.
- Example of an association rule:
- IF a customer buys bread and wine,
- THEN she/he will probably also buy cheese.

Association Rule: Example





Market Basket Analysis

From the analysis of many shopping baskets ...



A-priori algorithm

Recommendation

IF





THEN



Association Rule Mining

Possible applications of found association rules:

- Improve arrangement of products in shelves, on a catalog's pages.
- Support of cross-selling (suggestion of other products), product bundling.
- Fraud detection, technical dependence analysis.
- Finding business rules and detection of data quality problems.

- . . .

Association Rules

- Two step implementation:
- Find the frequent item sets (also called large item sets), i.e., the item sets that have at least a user-defined minimum support.
- Form rules using the frequent item sets found and select those that have at least a user-defined minimum confidence.

Association Rules

Assessing the quality of association rules:

Support of an item set:

 Fraction of transactions (shopping baskets/carts) that contain the item set.

Support of an association rule $X \rightarrow Y$:

- Either: Support of $X \cup Y$ (more common: rule is correct)

Or: Support of X (more plausible: rule is applicable)

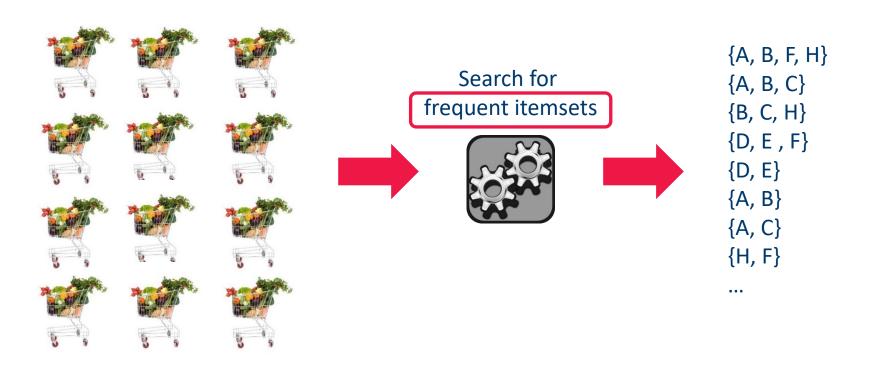
Confidence of an association rule $X \rightarrow Y$:

- Support of $X \cup Y$ divided by support of X (estimate of $P(Y \mid X)$).

Itemset Mining

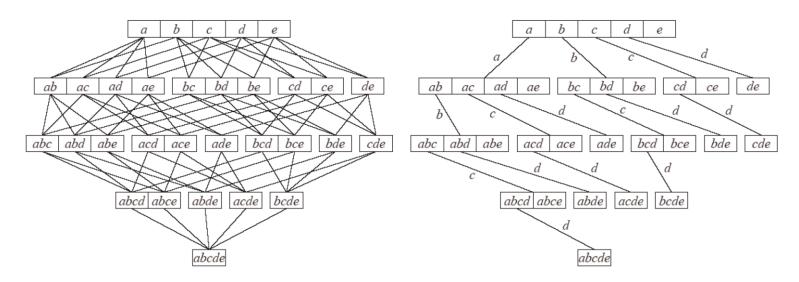
Building the Association Rule

N shopping baskets

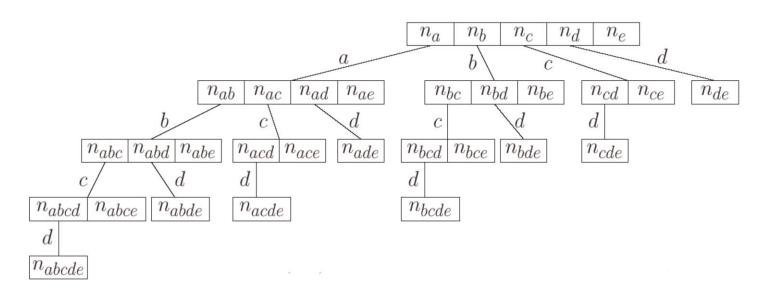


Finding frequent item sets

Subset lattice and a prefix tree for five items:



- It is not possible to determine the support of all possible item sets,
 because their number grows exponentially with the number of items.
- Efficient methods to search the subset lattice are needed.



- A (full) item set tree for the five items a, b, c, d, and e.
- Based on a global order of the items.
- The item sets counted in a node consist of all items labeling the edges to the node (common prefix) and one item following the last edge label.

Item Set Tree Pruning

 In applications item set trees tend to get very large, so pruning is needed.

Structural Pruning:

- Make sure that there is only one counter for each possible item set.
- Explains the unbalanced structure of the full item set tree.

Size Based Pruning:

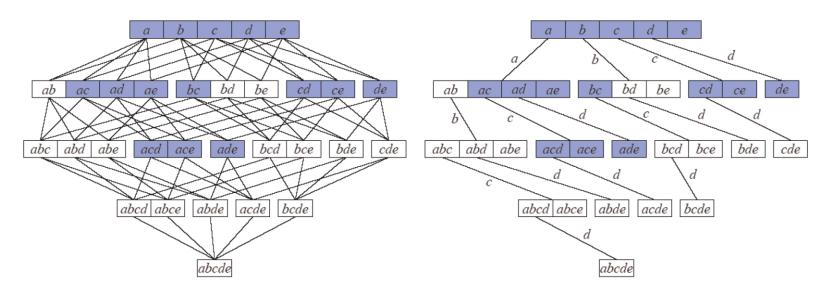
- Prune the tree if a certain depth (a certain size of the item sets) is reached.
- Idea: Rules with too many items are difficult to interpret.

Support Based Pruning:

- No superset of an infrequent item set can be frequent.
- No counters for item sets having an infrequent subset are needed

Searching the Subset Lattice

Boundary between frequent (blue) and infrequent (white) item sets:



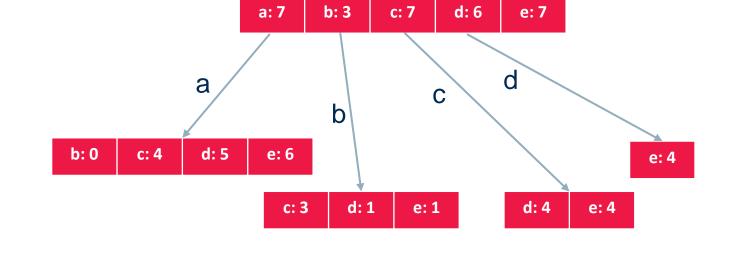
- Apriori: Breadth-first search (item sets of same size).
- Eclat: Depth-first search (item sets with same prefix).

- 1. {a, d, e}
- 2. $\{b, c, d\}$
- 3. {a, c, e}
- 4. {a, c, d, e}
- 5. {a, e}
- 6. $\{a, c, d\}$
- 7. {*b*, *c*}
- 8. {a, c, d, e}
- 9. {*c*, *b*, *e*}
- 10. {a, d, e}

a: 7 b: 3 c: 7 d: 6 e: 7

- Example transaction database with 5 items { a,b,c,d,e } and 10 transactions.
- Minimum support: 30%, i.e., at least 3 transactions must contain the item set.
- All one item sets are frequent -> full second level is needed.

- 1. {a, d, e}
- 2. {b, c, d}
- 3. {a, c, e}
- 4. {a, c, d, e}
- 5. {a, e}
- 6. {a, c, d}
- 7. {*b*, *c*}
- 8. {a, c, d, e}
- 9. {*c*, *b*, *e*}
- 10. {a, d, e}



- Determining the support of item sets: For each item set traverse the database and count the transactions that contain it (highly inefficient).
- Better: Traverse the tree for each transaction and find the item sets it contains (efficient: can be implemented as a simple double recursive procedure).

- 1. {a, d, e}
- 2. {b, c, d}
- 3. {*a*, *c*, *e*}
- {a, c, d, e}
- {a, e}
- {a, c, d}
- 7. {*b*, *c*}
- {a, c, d, e}
- 9. {*c*, *b*, *e*}



a: 7

e: 6

c: 3

a

d: 5

b: 3

b

c: 7

d: 6

e: 7

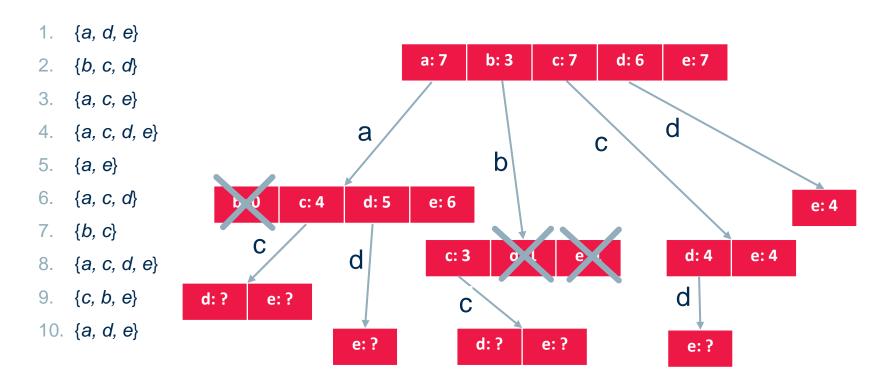
d: 4

e: 4

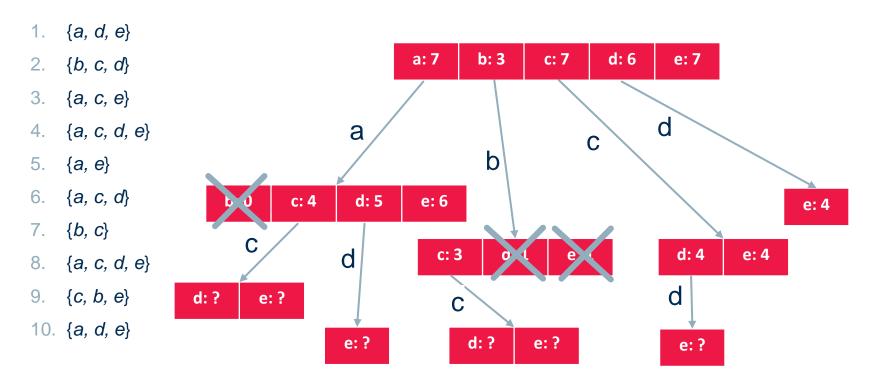
d

- Minimum support: 30%, i.e., at least 3 transactions must contain the item set.
- Infrequent item sets: $\{a, b\}, \{b, d\}, \{b, e\}.$
- The subtrees starting at these item sets can be pruned.

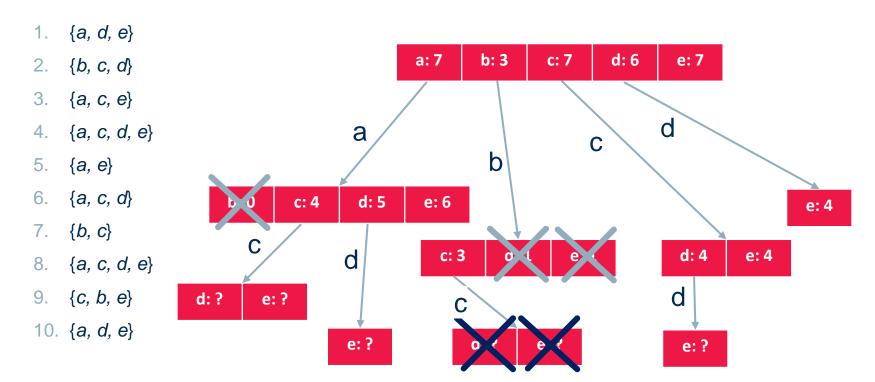
e: 4



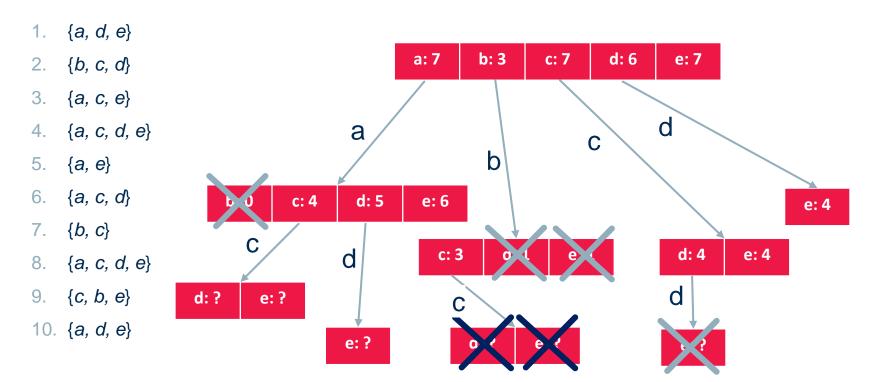
Generate candidate item sets with 3 items (parents must be frequent).



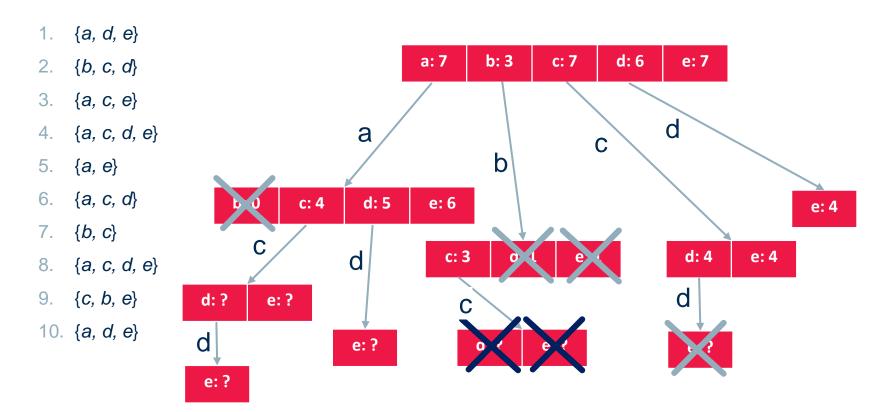
- Before counting, check whether the candidates contain an infrequent item set.
- An item set with k items has k subsets of size k 1.
- The parent is only one of these subsets



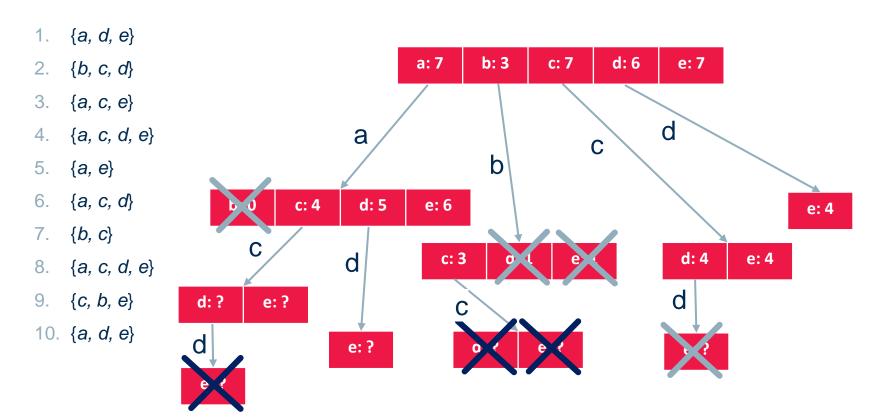
- The item sets {b, c, d} and {b, c, e} can be pruned, because
 - {b, c, d} contains the infrequent item set {b, d} and
 - {b, c, e} contains the infrequent item set {b, e}.
- Only the remaining four item sets of size 3 are evaluated.



- Minimum support: 30%, i.e., at least 3 transactions must contain the item set.
- Infrequent item set: {c, d, e}.



- Generate candidate item sets with 4 items (parents must be frequent).
- Before counting, check whether the candidates contain an infrequent item set.



- The item set {a,c,d,e} can be pruned, because it contains the infrequent item set {c, d, e}.
- Consequence: No candidate item sets with four items. Stop.



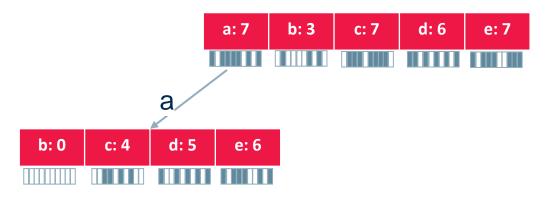


- 3. {a, c, e}
- 4. {a, c, d, e}
- 5. {*a*, *e*}
- 6. $\{a, c, d\}$
- 7. {*b*, *c*}
- 8. {a, c, d, e}
- 9. {*c*, *b*, *e*}
- 10. {a, d, e}

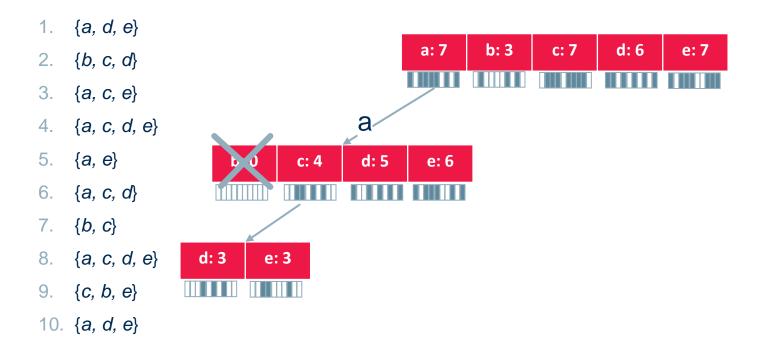


- Form a transaction list for each item. Here: bit vector representation.
 - grey: item is contained in transaction
 - white: item is not contained in transaction
- Transaction database is needed only once (for the single item transaction lists).

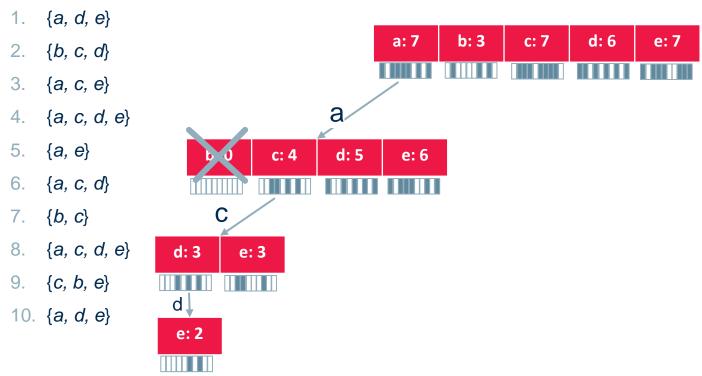
- 1. {a, d, e}
- 2. {b, c, d}
- 3. {a, c, e}
- 4. {a, c, d, e}
- 5. {*a*, *e*}
- 6. {a, c, d}
- 7. {*b*, *c*}
- 8. {a, c, d, e}
- 9. {*c*, *b*, *e*}
- 10. {a, d, e}



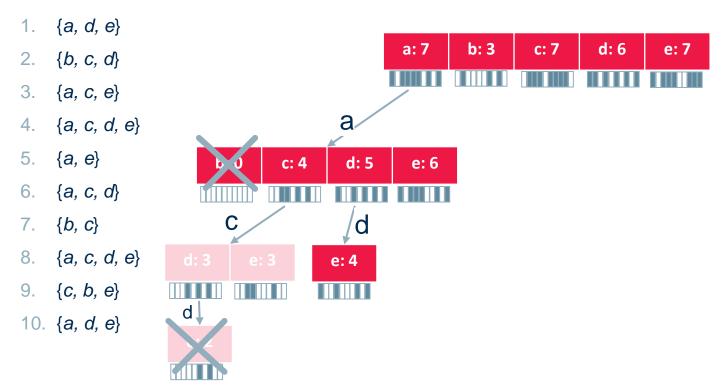
- Intersect the transaction list for item a with the transaction lists of all other items.
- Count the number of set bits (containing transactions).
- The item set {a, b} is infrequent and can be pruned.



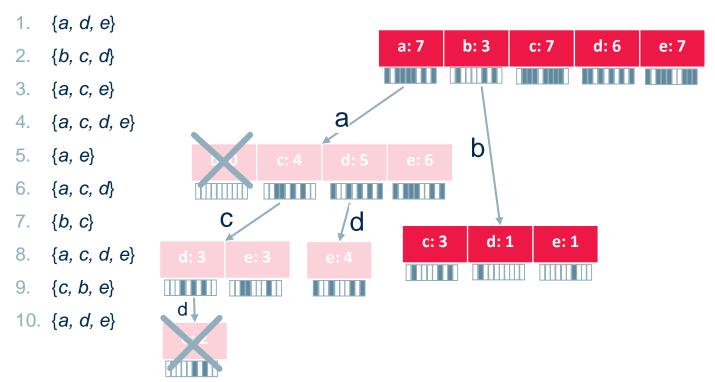
- Intersect the transaction list for {a, c} with the transaction lists of {a, x}, x ∈ {d, e}.
- Result: Transaction lists for the item sets {a, c, d} and {a, c, e}.



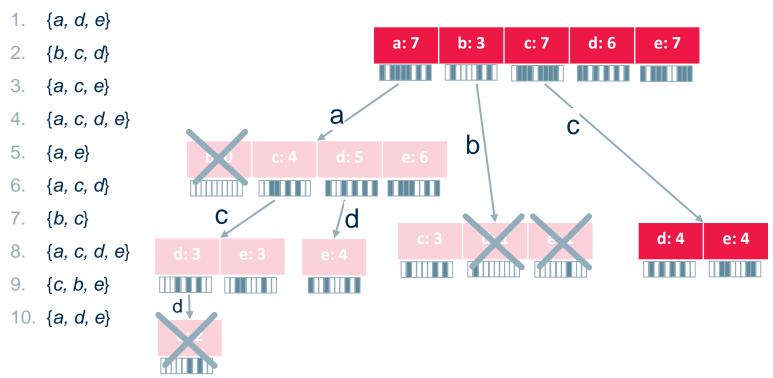
- Intersect the transaction list for {a, c, d} and {a, c, e}.
- Result: Transaction list for the item set {a, c, d, e}.
- With Apriori this item set could be pruned before counting, because it was known that {c, d, e} is infrequent.



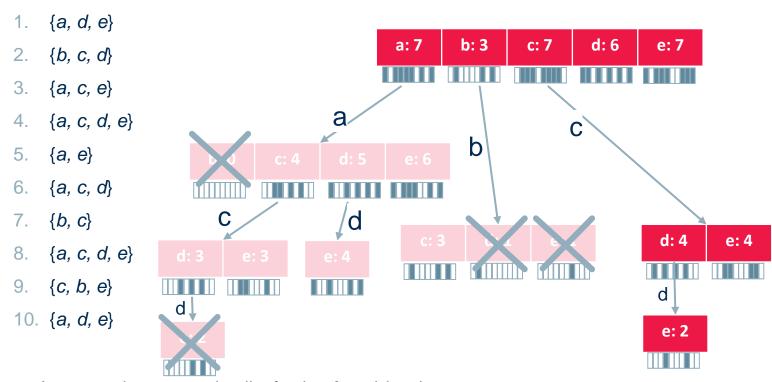
- Backtrack to the second level of the search tree and intersect the transaction list for {a, d} and {a, e}.
- Result: Transaction list for {a, d, e}.



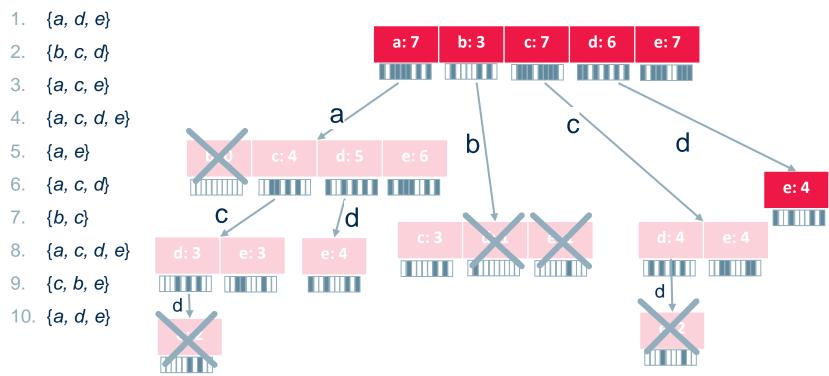
- Backtrack to the first level of the search tree and intersect the transaction list for b with the transaction lists for c, d, and e.
- Result: Transaction lists for the item sets {b, c}, {b, d}, and {b, e}.
- Only one item set with sufficient support -> prune all subtrees.



- Backtrack to the first level of the search tree and intersect the transaction list for c with the transaction lists for d and e.
- Result: Transaction lists for the item sets {c, d} and {c, e}.



- Intersect the transaction list for $\{c, d\}$ and $\{c, e\}$.
- Result: Transaction list for {c, d, e}.
- Infrequent item set: {c, d, e}.



- Backtrack to the first level of the search tree and intersect the transaction list for d with the transaction list for e.
- Result: Transaction list for the item set {d, e}.
- With this step the search is finished.

Frequent Item Sets

| 1 item | 2 items | | 3 items |
|--------------------------------|----------------------|-------------------|-----------------------|
| ${a}^{+}:70\%$ | $\{a,c\}^+$: 40% | $\{c,e\}^+$: 40% | ${a, c, d}^{+*}:30\%$ |
| { <i>b</i> } :30% | ${a,d}^+:50\%$ | ${d,e}^+:40\%$ | ${a, c, e}^{+*}:30\%$ |
| $\{c\}^+$: 70% | $\{a,e\}^+$: 60% | | ${a,d,e}^{+*}:40\%$ |
| { <i>d</i> } ⁺ :60% | $\{b,c\}^{+*}$: 30% | | |
| { <i>e</i> } ⁺ :70% | $\{c,d\}^+$: 40% | | |

- Types of frequent item sets
- Free Item Set: Any frequent item set (support is higher than the minimal support).
- Closed Item Set (marked with +): A frequent item set is called closed if no superset has the same support.
- Maximal Item Set (marked with): A frequent item set is called maximal if no superset is frequent.

Generating Association Rules

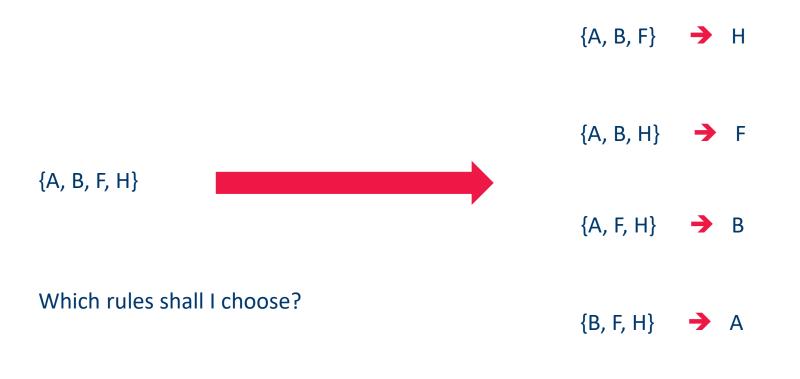
Generating Association Rules

- For each frequent item set S:
- Consider all pairs of sets $X, Y \in S$ with $X \cup Y = S$ and $X \cap Y = \emptyset$. Common restriction: |Y| = 1, i.e. only one item in consequent
- -X =antecedent, Y =consequent
- Form the association rule $X \rightarrow Y$ and compute its confidence.

$$conf(X \to Y) = \frac{supp(X \cup Y)}{supp(X)} = \frac{supp(S)}{supp(X)}$$

Report rules with a confidence higher than the minimum confidence.

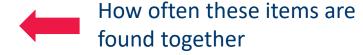
From "Frequent Itemsets" to "Rules"



Support, Confidence, and Lift

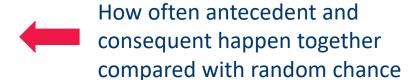
$$\{A, B, F\} \rightarrow H$$

- Item set support
$$s = \frac{freq(A,B,F,H)}{N}$$



- Rule confidence
$$c = \frac{freq(A,B,F,H)}{freq(A,B,F)}$$

- Rule lift =
$$\frac{support(\{A,B,F\}\Rightarrow H)}{support(A,B,F)\times support(H)}$$



The rules with support, confidence and lift above a threshold → most reliable ones

Association Rule Mining (ARM): Two Phases

Discover all <u>frequent</u> and <u>strong</u> association rules

$$X \Rightarrow Y \rightarrow$$
 "if X then Y"

with sufficient support and confidence

Two phases:

1. find all frequent itemsets (FI)

← Most of the complexity

Select itemsets with a minimum support

$$FI = \{ \{X, Y\}, X, Y \subset I | s(X, Y) \geq S_{min} \}$$

- 2. build strong association rules
 - Select rules with a minimum confidence:

Rules:
$$\{X \Rightarrow Y, X, Y \subset FI, | c(X \Rightarrow Y) \in C_{min} \}$$

User parameters

Generating Association Rules: Example

- **Example:** $S = \{a, c, e\}, X = \{c, e\}, Y = \{a\}.$

$$conf(c, e \rightarrow a) = \frac{supp(\{a, c, e\})}{supp(\{c, e\})} = \frac{30\%}{40\%} = 75\%$$

Minimum confidence: 80%

| Association Rule | Support of all items | Support of antecedent | confidence |
|----------------------|----------------------|-----------------------|------------|
| $b \rightarrow c$ | 30% | 30% | 100% |
| $d \rightarrow a$ | 50% | 60% | 83.3% |
| $e \rightarrow a$ | 60% | 70% | 85.7% |
| $a \rightarrow e$ | 60% | 70% | 85.7% |
| $d, e \rightarrow a$ | 40% | 40% | 100% |
| $a, d \rightarrow e$ | 40% | 50% | 80% |

A-Priori Algorithm: Example

- Let's consider milk, diaper, and beer: $\{milk, diaper\} \Rightarrow beer$

How often are they found together across all shopping baskets?

How often are they found together across all shopping baskets containing the

antecedents?

| TID | Transactions | |
|-----|---------------------------|--|
| 1 | Bread, Milk | |
| 2 | Bread, Diaper, Beer, Eggs | |
| 3 | Milk, Diaper, Beer, Coke | |
| 4 | Bread, Milk, Diaper, Beer | |
| 5 | Bread, Milk, Diaper, Coke | |

support
$$s(milk, diaper, beer)$$

$$= \frac{P(milk, diaper, beer)}{|T|} = \frac{2}{5} = 0.4$$

$$c = \frac{P(milk, diaper, beer)}{P(milk, diaper)} = \frac{2}{3} = 0.67$$
confidence

A-priori algorithm: an example

- Let's consider milk, diaper, and beer: $\{milk, diaper\} \Rightarrow beer$
- How often are they found together across all shooping baskets?
- How often are they found together across all shopping baskets containing the antecedents?

| TID | Transactions |
|-----|---------------------------|
| 1 | Bread, Milk |
| 2 | Bread, Diaper, Feer, Eggs |
| 3 | Milk, Diaper, Beer, Coke |
| 4 | Bread, Milk, Diaper, Beer |
| 5 | Bread, Milk, Diaper, Coke |

$$s(milk, diaper) = \frac{P(milk, diaper)}{|T|} = \frac{3}{5} = 0.6$$

$$s(beer) = \frac{P(beer)}{|T|} = \frac{3}{5} = 0.6$$

$$Rule \ lift = \frac{s(milk, diaper, beer)}{s(milk, diaper) \times s(beer)}$$

$$= \frac{0.4}{0.6 \times 0.6} = 1.11$$

Summary Association Rules

Association Rule Induction is a Two Step Process

- Find the frequent item sets (minimum support).
- Form the relevant association rules (minimum confidence).

Finding the Frequent Item Sets

- Top-down search in the subset lattice / item set tree.
- Apriori: Breadth first search;
- Eclat: Depth first search.
 - Other algorithms: FP-growth, H-Mine, LCM, Mafia, Relim etc.
 - Search Tree Pruning: No superset of an infrequent item set can be frequent.

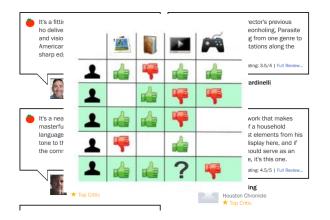
Generating the Association Rules

- Form all possible association rules from the frequent item sets.
- Filter "interesting" association rules.

Collaborative Filtering

Recommendation Engines or Market Basket Analysis

From the analysis of the reactions of many people to the same item ...







Recommendation



Inspired by your purchases

IF A has the same opinion as B on an item,

THEN A is more likely to have B's opinion on another item than that of a randomly chosen person



theory11 Artisan Playing Cards (White) ★★★☆ 152 \$10.75



theory11 Artisan Playing Cards (Black) ★★★☆↑ 71 \$9.60



theory11 High Victorian Playing Cards ★★★☆ 15 \$10.70



theory11 Citizen Playing Cards ★★★☆ 72 \$9.93 vprime



The Poetry and Short
Stories of Dorothy...
Dorothy Parker

ARCOVER
18
Hardcover
\$30,46

Collaborative Filtering (CF)

Collaborative filtering systems have many forms, but many common systems can be reduced to two steps:

- 1. Look for users who share the same rating patterns with the active user (the user whom the recommendation is for)
- Use the ratings from those like-minded users found in step 1 to calculate a prediction for the active user
- 3. Implemented in Spark

Spark Collaborative
Filtering Learner (MLlib)

https://www.knime.com/blog/movie-recommendations-with-spark-collaborative-filtering

Collaborative Filtering: Memory based approach

- User u to give recommendations to
- U = set of top N users most similar to user u
- Rating of user u on item i calculated as average of ratings of all similar users in
 U:

$$r_{u,i} = \frac{1}{N} \sum_{u' \in U} r_{u',i}$$
 or weighted $r_{u,i} = \frac{1}{N} \sum_{u' \in U} \text{simil}(u,u') r_{u',i}$

Pearson correlation

$$simil(u,u') = \frac{\sum_{i \in I_{xy}} (r_{u,i} - \overline{r_u}) (r_{u',i} - \overline{r_{u'}})}{\sqrt{\sum_{i \in I_{xy}} (r_{u,i} - \overline{r_u})^2} \sqrt{\sum_{i \in I_{xy}} (r_{u',i} - \overline{r_{u'}})^2}}$$

Set of items rated by both user x and y

Association Rules in Practice

... In practice

