Equation of Line

$1 \quad 11^{th} \text{ Maths}$ - Chapter 10

This is Problem-5 from Exercise 10.2

1. Instersecting the x-axis at a distance of 3 units to the left of origin with slope of -2.

Solution:

where \mathbf{A} and \mathbf{m} is

$$\mathbf{m} = -2 \tag{1}$$

$$\mathbf{A} = \begin{pmatrix} -3\\0 \end{pmatrix} \tag{2}$$

 \implies The normal vector ${\bf n}$ to the line is given as

$$\mathbf{n} = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} 1 \\ m \end{pmatrix} \tag{3}$$

$$\mathbf{n} = \begin{pmatrix} 2\\1 \end{pmatrix} \tag{4}$$

The equation of a line with normal vector \mathbf{n} and passing through a point \mathbf{A} is given by

$$\mathbf{n}^{\top} \left(\mathbf{x} - \mathbf{A} \right) = 0 \tag{5}$$

$$\begin{pmatrix} 2 & 1 \end{pmatrix} \begin{pmatrix} \mathbf{x} - \begin{pmatrix} -3 \\ 0 \end{pmatrix} \end{pmatrix} = 0 \tag{6}$$

$$\begin{pmatrix} 2 & 1 \end{pmatrix} \mathbf{x} + 6 = 0 \tag{7}$$

$$(2 \quad 1) \mathbf{x} = -6 \tag{8}$$

The line segment is as shown in Figure 1.

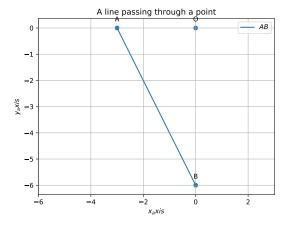


Figure 1