## Parallel Lines

## $11^{th}$ Maths - Chapter 10

This is Problem-6 from Exercise 10.3

- 1. Find the distance between parallel lines
  - (i) 15x+8y-34=0 and 15x+8y+31=0
  - (ii) l(x+y)+p=0 and l(x+y)-r=0
- 2. solution for problem 1 Given line is

$$15x + 8y - 34 = 0 \text{ and } 15x + 8y + 31 = 0 \tag{1}$$

this equation can be expressed as

$$\mathbf{n}^{\top}\mathbf{x} = c_1 \tag{2}$$

$$\mathbf{n}^{\top}\mathbf{x} = c_2 \tag{3}$$

where 
$$\mathbf{n} = \begin{pmatrix} 15 \\ 8 \end{pmatrix}, c_1 = -34, c_2 = 31$$
 (4)

$$\begin{pmatrix} 15 & 8 \end{pmatrix} \mathbf{x} = -34 \tag{5}$$

$$\begin{pmatrix} 15 & 8 \end{pmatrix} \mathbf{x} = 31 \tag{6}$$

(7)

distance between parallel lines

$$d = \frac{|c_1 - c_2|}{\mathbf{n}} \tag{8}$$

$$= \frac{|-34 - 31|}{\sqrt{289}} \tag{9}$$

$$=\frac{65}{17}\tag{10}$$

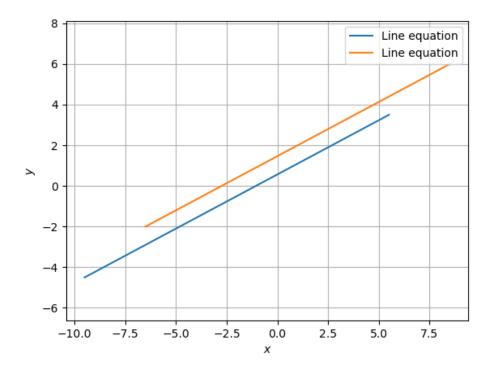


Figure 1

3. solution for problem 2 Given line is

$$l(x+y) + p = 0$$
 and  $l(x+y) - r = 0$  (11)

this equation can be expressed as

$$\mathbf{n}^{\top}\mathbf{x} = c_1 \tag{12}$$

$$\mathbf{n}^{\top}\mathbf{x} = c_2 \tag{13}$$

where 
$$\mathbf{n} = \begin{pmatrix} l \\ l \end{pmatrix}, c_1 = p, c_2 = -r$$
 (14)

$$= (l \quad l) \mathbf{x} = p$$

$$= (l \quad l) \mathbf{x} = -r$$
(15)
$$= (16)$$

$$= \begin{pmatrix} l & l \end{pmatrix} \mathbf{x} = -r \tag{16}$$

distance between parallel lines

$$d = \frac{|c_1 - c_2|}{\mathbf{n}}$$

$$= \frac{|p+r|}{l\sqrt{2}}$$
(17)

$$=\frac{|p+r|}{l\sqrt{2}}\tag{18}$$

The distance between parallel lines is shown in figure 2 with normal vector as

$$\mathbf{n} = \begin{pmatrix} 8 \\ 8 \end{pmatrix}$$
 and  $c_1 = 16, c_2 = -16$ 

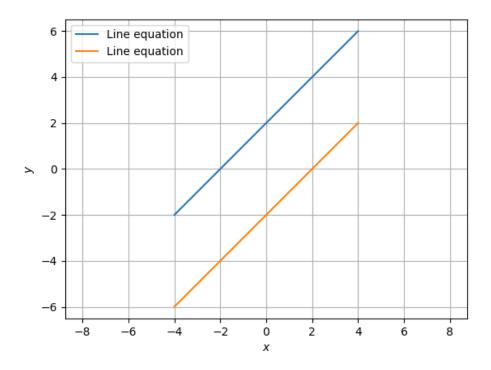


Figure 2