## Parallel Lines

## $11^{th}$ Maths - Chapter 10

This is Problem-6 from Exercise 10.3

- 1. Find the distance between parallel lines
  - (i) 15x+8y-34=0 and 15x+8y+31=0
  - (ii) l(x+y)+p=0 and l(x+y)-r=0
- 2. solution for problem 1 Given line is

$$15x + 8y - 34 = 0 \text{ and } 15x + 8y + 31 = 0 \tag{1}$$

this equation can be expressed as

$$\mathbf{n}^{\top}\mathbf{x} = c_1 \tag{2}$$

$$\mathbf{n}^{\top}\mathbf{x} = c_2 \tag{3}$$

where 
$$\mathbf{n} = \begin{pmatrix} 15 \\ 8 \end{pmatrix}, c_1 = -34, c_2 = 31$$
 (4)

$$\begin{pmatrix} 15 & 8 \end{pmatrix} \mathbf{x} = -34 \tag{5}$$

$$\begin{pmatrix} 15 & 8 \end{pmatrix} \mathbf{x} = 31 \tag{6}$$

(7)

distance between parallel lines

$$d = \frac{|c_1 - c_2|}{\|\mathbf{n}\|} \tag{8}$$

$$=\frac{|-34-31|}{\sqrt{289}}\tag{9}$$

$$=\frac{65}{17}\tag{10}$$

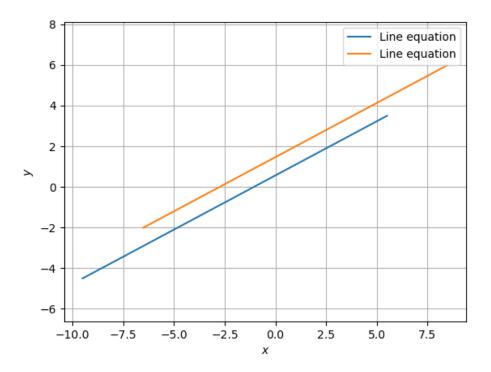


Figure 1

3. solution for problem 2 Given line is

$$l(x+y) + p = 0$$
 and  $l(x+y) - r = 0$  (11)

this equation can be expressed as

$$\mathbf{n}^{\top}\mathbf{x} = c_1 \tag{12}$$

$$\mathbf{n}^{\top}\mathbf{x} = c_2 \tag{13}$$

where 
$$\mathbf{n} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}, c_1 = 1, c_2 = -1$$
 (14)

$$= (1 1) \mathbf{x} = 1 (15)$$

$$= (1 1) \mathbf{x} = -1 (16)$$

$$= \begin{pmatrix} 1 & 1 \end{pmatrix} \mathbf{x} = -1 \tag{16}$$

distance between parallel lines

$$d = \frac{|c_1 - c_2|}{\|\mathbf{n}\|}$$

$$= \frac{|2|}{\sqrt{2}}$$

$$= \sqrt{2}$$
(18)
$$= (19)$$

$$=\frac{|2|}{\sqrt{2}}\tag{18}$$

$$=\sqrt{2}\tag{19}$$

The distance between parallel lines is shown in figure 2 with normal vector as

$$\mathbf{n} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$
 and  $c_1 = 1, c_2 = -1$ 

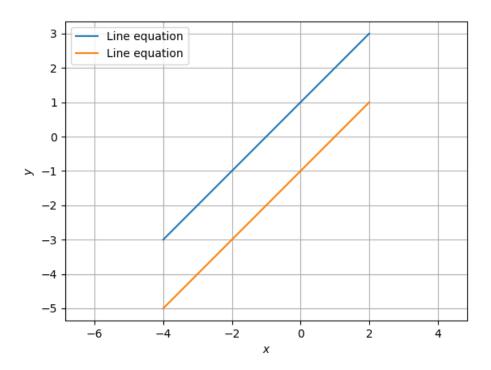


Figure 2