## Properties of Collinear

## $1 \quad 10^{th} \text{ Maths}$ - Chapter 7

This is Problem-2 from Exercise 7.3.2

- 1. In each of the following find the value of 'k', for which the points are collinear.
- 1. (7, -2), (5, 1), (3, k)
- 2. (8, 1), (k, -4), (2, -5).
- 1. Solution for problem:1

$$\mathbf{A} = \begin{pmatrix} 7 \\ -2 \end{pmatrix} \mathbf{B} = \begin{pmatrix} 5 \\ 1 \end{pmatrix} \mathbf{C} = \begin{pmatrix} 3 \\ k \end{pmatrix} \tag{1}$$

$$\mathbf{D} = (\mathbf{A} - \mathbf{B}) = \left( \begin{pmatrix} 7 \\ -2 \end{pmatrix} - \begin{pmatrix} 5 \\ 1 \end{pmatrix} \right) = \begin{pmatrix} 2 \\ -3 \end{pmatrix}$$
 (2)

$$\mathbf{E} = (\mathbf{A} - \mathbf{C}) = \left( \begin{pmatrix} 7 \\ -2 \end{pmatrix} - \begin{pmatrix} 3 \\ K \end{pmatrix} \right) = \begin{pmatrix} 4 \\ 12 - K \end{pmatrix}$$
 (3)

If points on a line are collinear, rank of matrix is " 1 "then the vectors are in linearly dependent. For  $2\times 2$  matrix Rank =1 means Determinant is 0.

Through pivoting, we obtain

$$\mathbf{F} = \begin{pmatrix} \mathbf{D} \\ \mathbf{E} \end{pmatrix} \tag{4}$$

$$\begin{pmatrix} 2 & -3 \\ 4 & -2 - k \end{pmatrix} \tag{5}$$

$$\begin{pmatrix} 2 & -3 \\ 4 & -2 - k \end{pmatrix} \stackrel{R_2 = R_2 - 2R_1}{\longleftrightarrow} \begin{pmatrix} -2 - k & -4 \\ 4 & -2 - k \end{pmatrix} \tag{6}$$

if the rank of the matrix is 1 means any one of the row must be zero. So, making the first element in the matrix to 0.

$$(-2 - k - 2(-3)) = 0$$

$$(-2 - k - 6) = 0$$

$$(k = 4)$$
(7)

Hence proved.

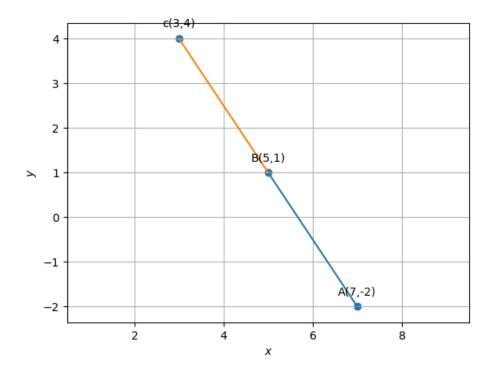


Figure 1

• Solution for problem :2

$$\mathbf{A} = \begin{pmatrix} 8 \\ 1 \end{pmatrix} \mathbf{B} = \begin{pmatrix} k \\ -4 \end{pmatrix} \mathbf{C} = \begin{pmatrix} 2 \\ -5 \end{pmatrix} \tag{8}$$

$$\mathbf{D} = (\mathbf{A} - \mathbf{B}) = \begin{pmatrix} 8 \\ 1 \end{pmatrix} - \begin{pmatrix} k \\ -4 \end{pmatrix} = \begin{pmatrix} 8 - k \\ 5 \end{pmatrix}$$
 (9)

$$\mathbf{E} = (\mathbf{A} - \mathbf{C}) = \begin{pmatrix} 8 \\ 1 \end{pmatrix} - \begin{pmatrix} 2 \\ -5 \end{pmatrix} \end{pmatrix} = \begin{pmatrix} 6 \\ 6 \end{pmatrix} \tag{10}$$

If points on a line are collinear, rank of matrix is " 1 "then the vectors are in linearly dependent. For  $2\times 2$  matrix Rank =1 means Determinant is 0. Through pivoting, we obtain

$$\mathbf{F} = \begin{pmatrix} \mathbf{D} \\ \mathbf{E} \end{pmatrix} \tag{11}$$

$$\begin{pmatrix} 8-k & 5\\ 6 & 6 \end{pmatrix} \tag{12}$$

$$\begin{pmatrix} 8-k & 5 \\ 6 & 6 \end{pmatrix} \stackrel{R_1=3R_1-3R_2}{\longleftrightarrow} \begin{pmatrix} 24-3k & 15 \\ 6 & 6 \end{pmatrix} \tag{13}$$

if the rank of the matrix is 1 means any one of the row must be zero. So, making the first element in the matrix to 0.

$$(3(8-k)-3(5)) = 0$$

$$(24-3k-15) = 0$$

$$(k=3)$$
(14)

Hence proved.

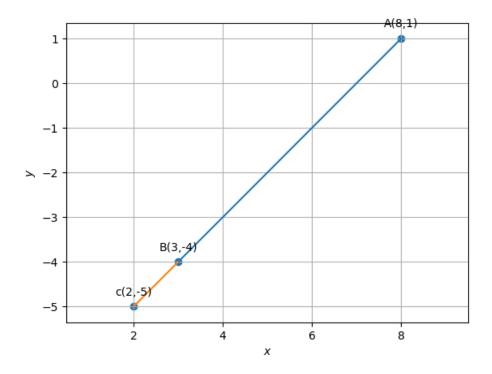


Figure 2