

Assignment I (ICSE-2019 CLASS 10)

Sathvika marri - AI21B TECH11020

April 1, 2022

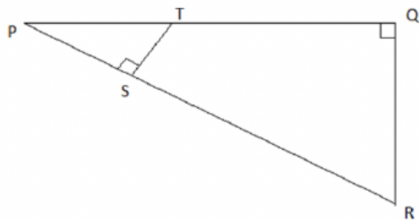
ICSE-2019 CLASS 10

Question: 6 (a)

(a) In the given figure, $\angle PQR = \angle PST = 90^\circ$, $PQ = 5$ cm and $PS = 2$ cm.

(i) Prove that $\triangle PQR \sim \triangle PST$.

(ii) Find ratio of Area of $\triangle PQR$ and Area of quadrilateral $SRQT$.



Solution:-

(i) To prove $\triangle PQR \sim \triangle PST$

consider $\triangle PQR$ and $\triangle PST$

$\angle PQR = \angle PST = 90^\circ$ (given)

$\angle P$ is common

$\therefore \triangle PQR \sim \triangle PST$ (By AA criterion)

(ii) To find the ratio of area of $\triangle PQR$ and area of quadrilateral $SRQT$.

Now,

$$\frac{Ar\triangle PQR}{Ar\triangle PST}$$

$$= \frac{1}{2} \times PQ \times QR / \frac{1}{2} \times PQ \times QR$$

$$= \frac{5}{2} \times \frac{5}{2} = \frac{25}{4} \quad [\because \frac{PQ}{PS} = \frac{QR}{ST}]$$

Taking the reciprocals on both sides

$$\frac{Ar\triangle PST}{Ar\triangle PQR} = \frac{4}{25}$$

Now deducting both sides by 1,

$$1 - \frac{Ar\triangle PST}{Ar\triangle PQR} = 1 - \frac{4}{25}$$

$$\Rightarrow \frac{Ar\triangle PQR - Ar\triangle PST}{Ar\triangle PQR} = \frac{25-4}{25}$$

$$\Rightarrow \frac{Ar\text{ of quadrilateral } SRQT}{Ar\text{ of } \triangle PQR} = \frac{21}{25}$$

THE END