

Assignment I (ICSE-2019 CLASS 10)

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ICSE-2019 CLASS 10

Question: 6 (a)

(a) In the given figure, $\angle PQR = \angle PST = 90^\circ$, $PQ = 5$ cm and $PS = 2$ cm.

(i) Prove that $\triangle PQR \sim \triangle PST$.

(ii) Find ratio of Area of $\triangle PQR$ and Area of quadrilateral $SQRT$.

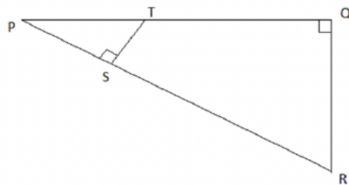


Figure 1: fig PQR

Solution:-

(i) To prove $\triangle PQR \sim \triangle PST$

consider $\triangle PQR$ and $\triangle PST$

$\angle PQR = \angle PST = 90^\circ$ (given)

$\angle P$ is common.

$\therefore \triangle PQR \sim \triangle PST$ (By AAA criterion)

(ii) To find the ratio of area of $\triangle PQR$ and area of quadrilateral $SQRT$.

Now, Area of $\triangle PQR$ is,

$$\Rightarrow \frac{1}{2} \times PQ \times QR$$

from the given diagram we can say $\frac{PQ}{PS} = \frac{QR}{ST}$

$PQ = 5$ cm (given), $QR = 5$ cm (stated above)

$$\Rightarrow \frac{1}{2} \times 5 \times 5 = \frac{25}{2}$$

Area of $\triangle PST$,

$$\Rightarrow \frac{1}{2} \times PS \times ST$$

$PS = 2$ cm (given), $ST = 2$ cm (stated above)

$$\Rightarrow \frac{1}{2} \times 2 \times 2 = \frac{4}{2}$$

Area of Quadrilateral $SQRT$ =
Area of $\triangle PQR$ - Area of $\triangle PST$,

$$\Rightarrow \frac{25}{2} - \frac{4}{2} = \frac{21}{2}$$

Ratio, $\frac{25/2}{21/2} = \frac{25}{21}$

$$\therefore \text{ratio} = \frac{25}{21}$$