

Assignment 1

AI1110: Probability and Random Variables - ICSE 2019 Grade10

Sathvika marri - ai21btech11020

April 30, 2022

Question: 6 (a)

In the given figure, $\angle PQR = \angle PST = 90^\circ$, $PQ = 5$ cm and $PS = 2$ cm.

(i) Prove that $\triangle PQR \sim \triangle PST$.

(ii) Find ratio of Area of $\triangle PQR$ and Area of quadrilateral $SRQT$.

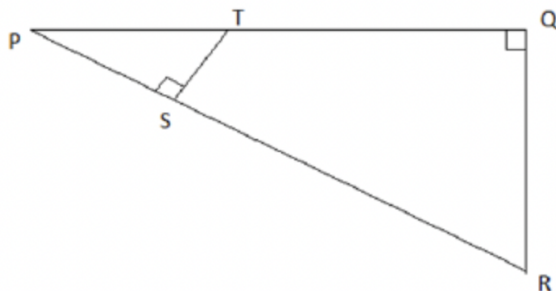


Figure 1: triangle PQR

Solution:-

(i) To prove $\triangle PQR \sim \triangle PST$

consider $\triangle PQR$ and $\triangle PST$

$\angle PQR = \angle PST = 90^\circ$ (given)

$\angle P$ is common.

$\therefore \triangle PQR \sim \triangle PST$ (By AAA criterion)

(ii) Now, Area of $\triangle PQR$ is,

From the given diagram we can say

$$= \frac{PQ}{PS} = \frac{QR}{ST} \quad (1)$$

$PQ = 5$ cm (given), $QR = 5$ cm (stated above)

$$= \frac{1}{2} \times 5 \times 5 = \frac{25}{2} \quad (2)$$

Area of triangle PST

$$= \frac{1}{2} \times PS \times ST \quad (3)$$

$PS = 2$ cm (given), $ST = 2$ cm (stated above)

$$= \frac{1}{2} \times 2 \times 2 = \frac{4}{2} \quad (4)$$

Area of Quadrilateral $SQRT$ = Area of triangle PQR - Area of triangle PST

$$= \frac{25}{2} - \frac{4}{2} = \frac{21}{2} \quad (5)$$

$$\Rightarrow \frac{25/2}{21/2} = \frac{25}{21} \quad (6)$$

$$\therefore \text{ratio} = \frac{25}{21}$$

METHOD-2: steps for construction;

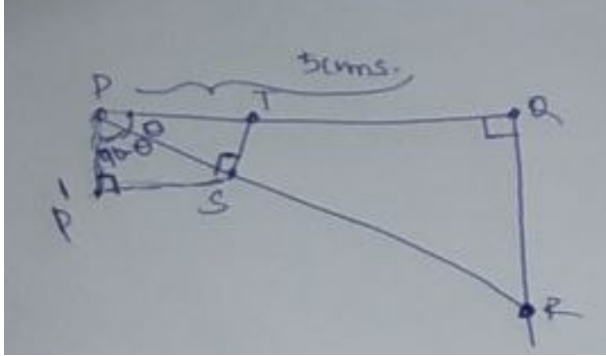


Figure 2: triangle-2

From the above figure;

$$\frac{PQ}{PR} = \cos \theta$$

$$PR = \frac{PQ}{\cos \theta} \quad (7)$$

$$\frac{QR}{PR} = \tan \theta$$

$$QR = \tan \theta PQ \quad (8)$$

Given, PS=2cm PQ=5cm take an angle;

$$\angle RPQ = 60^\circ$$

$$PT \text{ will be; } \Rightarrow \frac{PS}{PT} = \cos \theta$$

$$T \text{ will be; } \mathbf{T} = \begin{pmatrix} -(5 - \frac{PS}{\cos \theta}) \\ 0 \end{pmatrix} \quad (9)$$

$$(10)$$

$$\frac{P'S}{PS} = \sin(90 - \theta) \quad (11)$$

$$P'S = PS \sin(90 - \theta) \quad (12)$$

$$\frac{P'P}{PS} = \cos(90 - \theta) \quad (13)$$

$$P'P = PS \cos(90 - \theta) \quad (14)$$

$$\mathbf{S} = \begin{pmatrix} -(5 - PS \cos \theta) \\ -P \sin \theta \end{pmatrix} \quad (15)$$

$$(16)$$

Using the above coordinates,
Generating the figure using python:

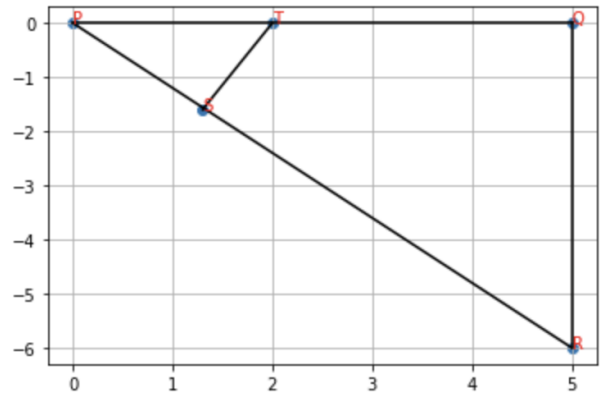


Figure 3: constructed triangle

The input and output parameters required for drawing the figure are available in the below table.

| input parameters | output paramters |
|--|--|
| PQ,PS | P,S,R,T-coordinates |
| $\angle PQR, \angle PST, \angle SPT.$ | $P = \begin{pmatrix} -PQ \\ 0 \end{pmatrix}$ |
| $Q = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$ | $R = \begin{pmatrix} 0 \\ -\tan \theta \cdot PQ \end{pmatrix}$ |
| | $T = \begin{pmatrix} -(S - PS / \cos \theta) \\ -PS \sin \theta \end{pmatrix}$ |
| | $S = \begin{pmatrix} -(S - PS \cos \theta) \\ -PS \sin \theta \end{pmatrix}$ |