

Activity - 8

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* Suppose a normal distribution has a mean $\mu = 50$ and a standard deviation $\sigma = 10$

- a) what percentage of value lie below 60 (i.e., $P(X \leq 60)$)?
- b) what value corresponds to the 90th percentile (i.e., $q_{norm}(0.90)$)?

Z	0	0.01	0.02	0.03	0.04
I	0.8413	0.8438	0.8461	0.8485	0.8508

a) $z = \frac{60 - 50}{10} = 1$

$= 0.8413 = 84\%$

b) $z = \frac{x - \mu}{\sigma} = 1.29 = \frac{x - 50}{10}$
 $10(1.29) = x - 50$
 $12.9 = x - 50$
 $x = 62.9$

a) The test scores of a group of students are normally distributed with a mean (μ) of 75 and a standard deviation of (σ) 10. what is the probability that a randomly selected student scored below 80?

b) In a factory, the weight of a product follows a normal distribution with a mean weight (μ) of 50kg and a standard deviation (σ) of 5kg. what weight corresponds to the 85th percentile of the distribution?

a) $z = \frac{80 - 75}{10} = \frac{5}{10} = 0.5$
 $z = 0.695$
 69%

b) $85\% = \frac{x - 50}{5}$
 $5(0.85) = x - 50$
 $5.2 = x - 50$
 $x = 55.2$