

# Mechanical Specification and Verification for Mitigating Timing-based Side Channel Leaks

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# Outline

- 1 Fall-Through Semantics for Mitigating Timing-based Side Channel Leaks
- 2 Interactive Theorem Proving - What's the Fuss About?
- 3 Mechanical Specification and Verification for Mitigating Timing-based Side Channel Leaks
- 4 Interactive Theorem Proving - An Undergraduate Perspective

## An Illustrative Example

Let us consider a C program that checks some input against a given password by comparing it by character by character.

```
bool matchpwd ( int * input , size_t n ) {  
    if ( n != pwd_length ) return false;  
    for ( int i = 0; i < n ; i ++ ) {  
        if ( input [ i ] != pwd [ i ] ) return false ;  
    }  
    return true ;  
}
```

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## Example (An Attack Trace)

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<b>101</b> 100	.....	Rejected in 4 <sup>th</sup> iteration



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<b>1</b> 01000	.....	Rejected in 5 <sup>th</sup> iteration
<b>1</b> 01100	.....	Rejected in 4 <sup>th</sup> iteration
<b>1</b> 01010	.....	Password accepted!

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## Timing Security

The adversary has exact knowledge of when and where each memory access takes place during a program's execution.

# Expression Semantics

CONST

$$\frac{}{n \mid \mu \Downarrow_{pc} \langle \text{CONST} \rangle, n^{pc}}$$

VAR

$$\frac{\mu(x) = n^k}{x \mid \mu \Downarrow_{pc} \langle \text{VAR}_x \rangle, n^{pc \sqcup k}}$$

OPER

$$\frac{e_1 \mid \mu \Downarrow_{pc} T_1, n_1^{k_1} \quad e_2 \mid \mu \Downarrow_{pc} T_2, n_2^{k_2} \quad n = n_1 \oplus n_2}{e_1 \oplus e_2 \mid \mu \Downarrow_{pc} \langle T_1, T_2, \text{OPER}_{\oplus} \rangle, n^{k_1 \sqcup k_2}}$$

# Command Semantics

## The Basics

SKIP

$$\frac{}{\text{skip} \mid \mu \Downarrow_{pc} \langle \text{SKIP} \rangle \mid \mu}$$

ASSN

$$\frac{e \mid \mu \Downarrow_{pc} T, n^k}{x := e \mid \mu \Downarrow_{pc} \langle T, \text{ASSN}_x \rangle \mid \mu, x \mapsto n^k}$$

SEQ

$$\frac{c_1 \mid \mu \Downarrow_{pc} T_1 \mid \mu' \quad c_2 \mid \mu' \Downarrow_{pc} T_2 \mid \mu''}{c_1; c_2 \mid \mu \Downarrow_{pc} \langle T_1, T_2, \text{SEQ} \rangle \mid \mu''}$$



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## IF-HIGH

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$$\frac{\text{debranch}(c_1, n, pc) \mid \mu \Downarrow_k T_1 \mid \mu' \quad \text{debranch}(c_2, !n, pc) \mid \mu' \Downarrow_k T_2 \mid \mu'' \quad k \not\sqsubseteq pc}{\text{if } e \text{ then } c_1 \text{ else } c_2 \mid \mu \Downarrow_{pc} \langle T, T_1, T_2, \text{IF-HIGH} \rangle \mid \mu''}$$

# Debranch Semantics: The Basics

DEB-ASSN-TRUE

$$\frac{e \mid \mu \Downarrow_{pc} T_1, n^k \quad x \mid \mu \Downarrow_{pc} T_2, n_1^{k_1}}{\text{debranch}(x := e, (true), \ell) \mid \mu \Downarrow_{pc} \langle T_1, T_2, \text{DEB} - \text{ASSN}_x \rangle \mid \mu, x \mapsto n^k}$$

DEB-ASSN-FALSE

$$\frac{e \mid \mu \Downarrow_{pc} T_1, n^k \quad x \mid \mu \Downarrow_{pc} T_2, n_1^{k_1}}{\text{debranch}(x := e, (false), \ell) \mid \mu \Downarrow_{pc} \langle T_1, T_2, \text{DEB} - \text{ASSN}_x \rangle \mid \mu, x \mapsto n_1^k}$$

# Debranch Semantics: IFs

DEB-IF-HIGH

$$\frac{e_1 \mid \mu \Downarrow_{\ell} T_3, n_1^{k_{\ell}} \quad e_1 \mid \mu \Downarrow_{pc} T_4, n_1^{k_{pc}} \quad k_{\ell} \not\sqsubseteq \ell \quad n_1 \&\& n = n' \quad !n_1 \&\& n = n''}{\text{debranch}(c_1, n', \ell) \mid \mu \Downarrow_{k_{pc}} T_1 \mid \mu' \quad \text{debranch}(c_2, n'', \ell) \mid \mu' \Downarrow_{k_{pc}} T_2 \mid \mu''} \\ \text{debranch}(\text{if } e_1 \text{ then } c_1 \text{ else } c_2, n, \ell) \mid \mu \Downarrow_{pc} \langle T_1, T_2, T_3, T_4, \text{DEB-IF-HIGH} \rangle \mid \mu''$$

DEB-IF-LOW

$$\frac{e_1 \mid \mu \Downarrow_{\ell} T_1, n_1^k \quad c = \begin{cases} \text{debranch}(c_1, n, \ell) & \text{if } n_1 = \text{true} \\ \text{debranch}(c_2, n, \ell) & \text{otherwise} \end{cases} \quad c \mid \mu \Downarrow_{pc} T_2 \mid \mu' \quad k \sqsubseteq \ell}{\text{debranch}(\text{if } e_1 \text{ then } c_1 \text{ else } c_2, n, \ell) \mid \mu \Downarrow_{pc} \langle T_1, T_2, \text{DEB-IF-LOW} \rangle \mid \mu'}$$

# ITPs

**Interactive Theorem Provers** have been around for quite a while. However, they have been facing a lot of very *recent* adoption.

- LEAN4 (2013)
- FStar (2011)
- Agda (1999)
- **Coq/Rocq (1989/2025)**
- Isabelle (1986)
- Automath (1967)

# Expressing Mathematical Structures

```

Inductive NAT :=
| NAT_zero
| NAT_succ (n: NAT).

Inductive EQ {A: Type} : A → A → Type :=
| EQ_refl (x: A) : EQ x x.

Inductive EXISTS {A: Type} (P: A → Type) :=
| EXISTS_intro (witness: A) (proof: P witness) : EXISTS P.

Definition All_numbers_are_reflexively_equal
: ∀ (n: NAT), EQ n n := λ n ⇒ EQ_refl n.

Theorem All_numbers_are_reflexively_equal' : ∀ (n: NAT), EQ n n.
Proof.
  (** Assuming some n. *)
  intros n.
  (** The theorem holds by definition of EQ. *)
  constructor.
Qed.

```

# Why Bother?

The most important thing that we get from these systems is **trust**.

- **Manual verification** can be error-prone and time-consuming.
- With a theorem prover, the implementation of the core system is comparatively very **small**.
- With this base, it is much easier to **trust results** (although there are caveats we will discuss later).

# Expressing Grammars

```
(** An expression is either a primitive, a variable, or a binary operation. *)
Inductive Expression :=
| PrimitiveExpression (prim: Primitive)
| VarExpression (x: Var)
| BinOpExpression (binop: BinOp) (e1 e2: Expression).

(** The commands in our language are:
    + Skip, corresponding to a NO-OP
    + Assignments
    + Sequences (ie. perform c1 then c2)
    + Conditionals
    + While Loops
    *)
Inductive Command : Type :=
| SkipCommand
| AssnCommand (x: Var) (e: Expression)
| SeqCommand (c1 c2: Command)
| IfCommand (e: Expression) (c1 c2: Command)
| WhileCommand (e: Expression) (c: Command)
```

# Expressing Semantics

```
(** * Language: Semantics *)

(** Described here is the expression semantics. There is not much of interest to talk about here. *)
Inductive ExpressionBigStep
  {binop_eval: BinOp → Primitive → Primitive}
  {rel: Level → Level → Type}
  {latticeProof: JoinSemiLattice rel} : Expression → MemStore → Level → TimingList → Primitive → Level → Type :=
| ConstBigStep (prim: Primitive) {pc: Level} {mu: MemStore}
  : ExpressionBigStep (PrimitiveExpression prim) mu pc (SingleTiming CONST) prim pc

| VarBigStep(x: Var) {mu: MemStore} {pc j: Level} {joinProof: Join rel pc (snd (mu x)) j}
  : ExpressionBigStep (VarExpression x) mu pc (SingleTiming (VAR x)) (fst (mu x)) j

| OperBigStep (oper: BinOp) {mu: MemStore} {e1 e2: Expression} {pc k1 k2 join1k2: Level} {T1 T2: TimingList} {n1 n2: Primitive}
  (p1: ExpressionBigStep e1 mu pc T1 n1 k1)
  (p2: ExpressionBigStep e2 mu pc T2 n2 k2)
  (joinProof: Join rel k1 k2 join1k2)
  : ExpressionBigStep (BinOpExpression oper e1 e2) mu pc (T1 , T2 , (SingleTiming (OPER oper))) (binop_eval oper n1 n2) join1k2.
```



# Expressing Invariants

```

Lemma ExpressionTimSec {binop_eval: BinOp → Primitive → Primitive → Primitive}
  {rel: Level → Level → Type}
  {latticeProof: JoinSemilattice rel}:
  ∀ {e: Expression} {pc1 pc2 k1 k2: Level} {mu1 mu2: MemStore} {n1 n2: Primitive} {T1 T2: TimingList},
    @ExpressionBigStep binop_eval rel latticeProof e mu1 pc1 T1 n1 k1 →
    @ExpressionBigStep binop_eval rel latticeProof e mu2 pc2 T2 n2 k2 →
    (T1 = T2).

Proof.
  intros. dependent induction e; dependent destruction X0; dependent destruction X.
  = reflexivity.
  = reflexivity.
  = specialize (IHe1 _ _ _ _ _ X1 X0_1).
    specialize (IHe2 _ _ _ _ _ X2 X0_2).
    rewrite → IHe1.
    rewrite → IHe2.
    reflexivity.
Qed.

```

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- During December, I spent some time in IIT Delhi with Prof. Vaishnavi Sundararajan and started properly working with theorem provers.
- After this, I got extremely anxious about my **proofs and theorems being incorrect.**

# Learning to write Rocq vs Learning to write Proofs

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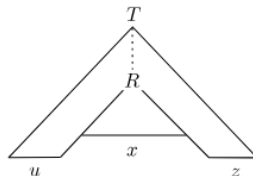
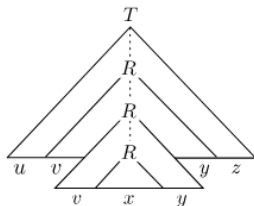
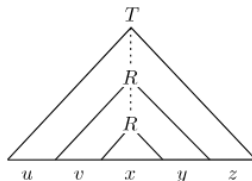
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- This is bad. Spending time on things obvious by intuition, may hamper the **non-obvious** things.
- This is good. It allows for stronger guarantees. **As a student, by default, your intuition is non-existent or bad.**

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- **Bugs** in prover-software. Possibility of **breaking updates**.
- Benefits from **abstractions**.
- Strictness can cause difficulty in **iteration**.

# Concluding

That's all! Thank you for attending my talk. I am part of a student club called , \ **AMBDA**. at IIT Gandhinagar where we like to work on interesting things in PLT along with organising talks to cultivate interest in PLT. Let me know if you are interested in knowing more! You can also contact me at `mailto:aniket.mishra@iitgn.ac.in`.