

SATISH KUMAR & THOMI FLAVIO

ASSIGNMENT - 1

1/4

Exercise - 1

Yes, the student can pass by performing good in Homework assignment.

The student got in Mid-term

$$= 50\% \text{ of } 30\% \Rightarrow 15\%$$

And he got in final exam.

$$40\% \text{ of } 40\% \Rightarrow 16\%$$

Then he has total $\Rightarrow 15 + 16 = 31\%$

And total passing point is 60%.

He require $= 60\% - 31\% = 29\%$.

And homework assignment has 30%. Then the student got 29% of his homework point. He is passed.

Exercise-2

$$\sum_{k=1}^n k^2 = \frac{n(n+1)(2n+1)}{6}$$

Base case : $n = 1$

$$\sum_{k=1}^1 (1)^2 = \frac{1(1+1)(2(1)+1)}{6} = \frac{(2)(3)}{6} = \frac{6}{6} = 1$$

Induction hypothesis -

Suppose $\sum_{k=1}^n k^2 = \frac{n(n+1)(2n+1)}{6}$ is true.

Induction step : $\sum_{k=1}^{n+1} k^2 = \frac{(n+1)(n+1+1)(2(n+1)+1)}{6}$

$$= \sum_{k=1}^n k^2 + (n+1)^2 = \frac{(n+1)(n+2)(2n+3)}{6}$$

I. H

$$\Rightarrow \frac{n(n+1)(2n+1)}{6} + n^2 + 1 + 2n = \frac{(n^2 + 2n + n + 2)(2n + 3)}{6}$$

$$\Rightarrow \frac{(n^2 + n)(2n + 1) + 6(n^2 + 1 + 2n)}{6} = \frac{2n^3 + 3n^2 + 4n^2 + 6n + 2n^2 + 3n + 4n + 6}{6}$$

$$\Rightarrow \frac{2n^3 + n^2 + 2n^2 + n + 6n^2 + 6 + 4n}{6} = \frac{2n^3 + 9n^2 + 13n + 6}{6}$$

JATISH KUMAR & THOMI FLAVIO

3/4

$$\Rightarrow \frac{2n^3 + 9n^2 + 13n + 6}{6} = \frac{2n^3 + 9n^2 + 13n + 6}{6}$$

Exercise 3

$$(x+y)(x-y) = (x \cdot x) - (y \cdot y)$$

$$(x+y)(x+(-y))$$

$$(-y = +(-y))$$

(F5) Distributivity

$$((x+y) \cdot x) + ((x+y) \cdot (-y))$$

(F5) Distributivity

$$((x \cdot x) + (y \cdot x)) + ((x \cdot (-y)) + (y \cdot (-y)))$$

$$((x \cdot x) + (y \cdot x)) + (x \cdot (-y)) + (y \cdot (-y))$$

$$((x \cdot x) + ((y \cdot x) + (x \cdot (-y)))) + (y \cdot (-y)) \quad (F1) \text{ Associative}$$

$$((x \cdot x) + ((y \cdot x) + (x \cdot (-y)))) + (y \cdot (-y)) \quad (F1) \text{ Associative}$$

$$((x \cdot x) + ((y \cdot x) - (y \cdot x))) + (y \cdot (-y)) \quad (F2) \text{ Commutativity}$$

$$((x \cdot x) + 0) + (y \cdot (-y)) \quad (F4) \text{ Inverse elements}$$

$$(x \cdot x) + (y \cdot (-y)) \quad (F3) \text{ Identity elements}$$

$$(x \cdot x) - (y \cdot y) = (x \cdot x) - (y \cdot y)$$

Proved

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4/4

Bonus Question

In equation $a(a+b-c)$
 $= b(b+a-c)$ is equal to 0. because
 $1+2-3=0$ than both sides is zero
than it is not arrived $a=b$
it comes $0=0$.