# **Electrical Quantity Division Principles**

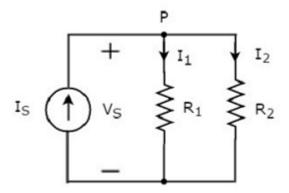
In this chapter, let us discuss about the following two division principles of electrical quantities.

- Current Division Principle
- Voltage Division Principle

### **Current Division Principle**

When two or more passive elements are connected in parallel, the amount of current that flows through each element gets **divided** (shared) among themselves from the current that is entering the node.

Consider the following circuit diagram.



The above circuit diagram consists of an input current source  $I_S$  in parallel with two resistors  $R_1$  and  $R_2$ . The voltage across each element is  $V_S$ . The currents flowing through the resistors  $R_1$  and  $R_2$  are  $I_1$  and  $I_2$  respectively.

The KCL equation at node P will be

$$I_S = I_1 + I_2$$

• Substitute  $I_1=rac{V_S}{R_1}$  and  $I_2=rac{V_S}{R_2}$  in the above equation.

$$I_S = rac{V_S}{R_1} + rac{V_S}{R_2} = V_S(rac{R_2 + R_1}{R_1 R_2})$$

$$\Rightarrow V_S = I_S \left( rac{R_1 R_2}{R_1 + R_2} 
ight)$$

• Substitute the value of  $V_{\mathbb{S}}$  in  $I_1 = rac{V_S}{R_1}$  .

$$I_1 = \frac{I_S}{R_1} \left( \frac{R_1 R_2}{R_1 + R_2} \right)$$

$$A\Rightarrow I_1=I_S(rac{R_2}{R_1+R_2})$$

• Substitute the value of  $V_{\mathbb{S}}$  in  $\ I_2 = rac{V_S}{R_2}$  .

$$I_2 = rac{I_S}{R_2} (rac{R_1 R_2}{R_1 + R_2})$$

$$r \Rightarrow I_2 = I_S(rac{R_1}{R_1+R_2})$$

From equations of  $I_1$  and  $I_2$ , we can generalize that the current flowing through any passive element can be found by using the following formula.

$$I_N = I_S(rac{Z_1 \|Z_2\| \ldots \|Z_{N-1}}{Z_1 + Z_2 + \ldots + Z_N})$$

This is known as **current division principle** and it is applicable, when two or more passive elements are connected in parallel and only one current enters the node.

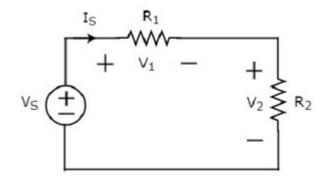
#### Where,

- $I_N$  is the current flowing through the passive element of N<sup>th</sup> branch.
- $I_S$  is the input current, which enters the node.
- $Z_1, Z_2, ..., Z_N$  are the impedances of 1<sup>st</sup> branch, 2<sup>nd</sup> branch, ..., N<sup>th</sup> branch respectively.

# Voltage Division Principle

When two or more passive elements are connected in series, the amount of voltage present across each element gets **divided** (shared) among themselves from the voltage that is available across that entire combination.

Consider the following circuit diagram.



The above circuit diagram consists of a voltage source,  $V_S$  in series with two resistors  $R_1$  and  $R_2$ . The current flowing through these elements is  $I_S$ . The voltage drops across the resistors  $R_1$  and  $R_2$  are  $V_1$  and  $V_2$  respectively.

The KVL equation around the loop will be

$$V_S = V_1 + V_2$$

• Substitute  $V_1 = I_S R_1$  and  $V_2 = I_S R_2$  in the above equation

$$V_S = I_S R_1 + I_S R_2 = I_S (R_1 + R_2)$$

$$I_S = rac{V_S}{R_1 + R_2}$$

• Substitute the value of  $I_S$  in  $V_1 = I_S R_1$ .

$$V_1 = (rac{V_S}{R_1 + R_2})R_1$$

$$\Rightarrow V_1 = V_S(rac{R_1}{R_1+R_2})$$

• Substitute the value of  $I_S$  in  $V_2 = I_S R_2$ .

$$V_2 = (rac{V_S}{R_1 + R_2})R_2$$

$$\Rightarrow V_2 = V_S(rac{R_2}{R_1+R_2})$$

From equations of  $V_1$  and  $V_2$ , we can generalize that the voltage across any passive element can be found by using the following formula.

$$V_N = V_S(rac{Z_N}{Z_1 + Z_2 + \ldots + Z_N})$$

This is known as **voltage division principle** and it is applicable, when two or more passive elements are connected in series and only one voltage available across the entire combination.

### Where,

- V<sub>N</sub> is the voltage across N<sup>th</sup> passive element.
- $V_S$  is the input voltage, which is present across the entire combination of series passive elements.
- $Z_1, Z_2, ..., Z_3$  are the impedances of 1<sup>st</sup> passive element, 2<sup>nd</sup> passive element, ..., N<sup>th</sup> passive element respectively.