Assignments:

- Add another feature called Preferential Attachment with followers and followees data of vertex. you can check about Preferential Attachment in below link http://be.amazd.com/link-prediction/
- Add feature called svd_dot. you can calculate svd_dot as Dot product between sourse node svd and destination node svd features. you can read about this in below pdf https://storage.googleapis.com/kaggle-forum-message-attachments/2594/supervised_link_prediction.pdf
- 3. Tune hyperparameters for XG boost with all these features and check the error metric.

In [10]:

```
#Importing Libraries
# please do go through this python notebook:
import warnings
warnings.filterwarnings("ignore")
import csv
import pandas as pd#pandas to create small dataframes
import datetime #Convert to unix time
import time #Convert to unix time
# if numpy is not installed already : pip3 install numpy
import numpy as np#Do aritmetic operations on arrays
# matplotlib: used to plot graphs
import matplotlib
import matplotlib.pylab as plt
import seaborn as sns#Plots
from matplotlib import rcParams#Size of plots
from sklearn.cluster import MiniBatchKMeans, KMeans#Clustering
import math
import pickle
import os
# to install xgboost: pip3 install xgboost
import xgboost as xgb
import warnings
import networkx as nx
import pdb
import pickle
from pandas import HDFStore, DataFrame
from pandas import read hdf
from scipy.sparse.linalg import svds, eigs
import gc
from tqdm import tqdm
from sklearn.ensemble import RandomForestClassifier
from sklearn.metrics import f1 score
from sklearn.model_selection import RandomizedSearchCV
from scipy.stats import randint as sp_randint
from scipy.stats import uniform
from sklearn.metrics import confusion matrix
```

In [27]:

```
from google.colab import drive
drive.mount('/content/gdrive')
```

Drive already mounted at /content/gdrive; to attempt to forcibly remount, call drive.mount("/content/gdrive", force remount=True).

1. Reading Data

```
In [28]:
```

```
if os.path.isfile('/content/gdrive/MyDrive/Facebook/data/after_eda/train_after_eda.csv'):
    train_graph=nv_read_edgelist('/content/gdrive/MyDrive/Facebook/data/after_eda/train_after_eda.csv')
```

```
delimiter=',',create_using=nx.DiGraph(),nodetype=int)
    print(nx.info(train_graph))
else:
    print("please run the FB_EDA.ipynb or download the files from drive")

Name:
Type: DiGraph
```

Number of nodes: 1862196 Number of edges: 15100030 Average in degree: 8.1087 Average out degree: 8.1087

2. Similarity measures

2.1 Jaccard Distance:

http://www.statisticshowto.com/jaccard-index/

```
In [29]:
```

In [30]:

```
#one test case
print(jaccard_for_followees(273084,1505602))
```

0.0

In [31]:

```
#node 1635354 not in graph
print(jaccard_for_followees(273084,1505602))
```

0.0

In [32]:

```
In [33]:
print(jaccard for followers(273084,470294))
0
In [34]:
#node 1635354 not in graph
print (jaccard for followees (669354, 1635354))
0.0
2.2 Cosine distance
\begin{equation} CosineDistance = \frac{|X\cap Y|}{|X|\cdot|Y|} \end{equation}
In [35]:
#for followees
def cosine for followees(a,b):
    try:
        if len(set(train graph.successors(a))) == 0 | len(set(train graph.successors(b))) == 0:
        sim = (len(set(train graph.successors(a)).intersection(set(train graph.successors(b)))))/\
                                     (math.sqrt(len(set(train graph.successors(a)))*len((set(train graph
.successors(b)))))
        return sim
    except:
        return 0
In [36]:
print(cosine for followees(273084,1505602))
0.0
In [37]:
  print (cosine for followees (273084, 1635354))
0.0
In [38]:
def cosine for followers(a,b):
    try:
        if len(set(train_graph.predecessors(a))) == 0 | len(set(train_graph.predecessors(b))) == 0:
        sim = (len(set(train graph.predecessors(a)).intersection(set(train graph.predecessors(b)))))/\
                                      (math.sqrt(len(set(train graph.predecessors(a))))*(len(set(train g
raph.predecessors(b)))))
        return sim
    except:
        return 0
In [39]:
print(cosine for followers(2,470294))
```

0 020412414523193152

O.OCOTTCTTTOCOTYOT

```
In [40]:
```

```
print(cosine_for_followers(669354,1635354))
```

0.0

3. Ranking Measures

https://networkx.github.io/documentation/networkx-

1.10/reference/generated/networkx.algorithms.link analysis.pagerank alg.pagerank.html

PageRank computes a ranking of the nodes in the graph G based on the structure of the incoming links.

Mathematical PageRanks for a simple network, expressed as percentages. (Google uses a logarithmic scale.) Page C has a higher PageRank than Page E, even though there are fewer links to C; the one link to C comes from an important page and hence is of high value. If web surfers who start on a random page have an 85% likelihood of choosing a random link from the page they are currently visiting, and a 15% likelihood of jumping to a page chosen at random from the entire web, they will reach Page E 8.1% of the time. (The 15% likelihood of jumping to an arbitrary page corresponds to a damping factor of 85%) Without damping, all web surfers would eventually end up on Pages A, B, or C, and all other pages would have PageRank zero. In the presence of damping, Page A effectively links to all pages in the web, even though it has no outgoing links of its own.

3.1 Page Ranking

https://en.wikipedia.org/wiki/PageRank

In [41]:

```
if not os.path.isfile('/content/gdrive/MyDrive/case_study_2/data/page_rank.p'):
    pr = nx.pagerank(train_graph, alpha=0.85)
    pickle.dump(pr,open('/content/gdrive/MyDrive/case_study_2/data/page_rank.p','wb'))
else:
    pr = pickle.load(open('/content/gdrive/MyDrive/case_study_2/data/page_rank.p','rb'))
```

In [42]:

```
print('min',pr[min(pr, key=pr.get)])
print('max',pr[max(pr, key=pr.get)])
print('mean',float(sum(pr.values())) / len(pr))
```

min 8.216658719151825e-08 max 1.2201861685116973e-05 mean 5.370004016764232e-07

In [43]:

```
#for imputing to nodes which are not there in Train data
mean_pr = float(sum(pr.values())) / len(pr)
print(mean_pr)
```

5.370004016764232e-07

4. Other Graph Features

Getting Shortest path between twoo nodes, if nodes have direct path i.e directly connected then we are removing that edge and calculating path.

```
In [44]:
#if has direct edge then deleting that edge and calculating shortest path
def compute shortest path length(a,b):
    p=-1
    try:
        if train graph.has edge(a,b):
            train graph.remove edge(a,b)
            p= nx.shortest_path_length(train_graph,source=a,target=b)
            train_graph.add_edge(a,b)
            p= nx.shortest_path_length(train_graph,source=a,target=b)
        return p
    except:
        return -1
In [45]:
#testing
compute_shortest_path_length(77697, 826021)
Out[45]:
```

In [46]:

7

```
#testing
compute_shortest_path_length(669354,1635354)
```

Out[46]:

8

4.2 Checking for same community

In [47]:

```
#getting weekly connected edges from graph
wcc=list(nx.weakly connected components(train graph))
def belongs_to_same_wcc(a,b):
    index = []
    if train graph.has edge(b,a):
        return 1
    if train_graph.has_edge(a,b):
            for i in wcc:
                if a in i:
                    index= i
                    break
            if (b in index):
                train graph.remove edge(a,b)
                if compute_shortest_path_length(a,b) ==-1:
                    train graph.add edge(a,b)
                    return 0
                else:
                    train_graph.add_edge(a,b)
                    {\tt return} \ 1
            else:
                return 0
    else:
            for i in wcc:
                if a in i:
                    index= i
                    break
            if(b in index):
                return 1
            else:
                return 0
```

```
In [48]:
belongs_to_same_wcc(861, 1659750)
Out[48]:
1
In [49]:
belongs_to_same_wcc(669354,1635354)
Out[49]:
1
```

4.3 Adamic/Adar Index:

Adamic/Adar measures is defined as inverted sum of degrees of common neighbours for given two vertices. $A(x,y)=\sum_{u \in N(y)}\frac{1}{\log(|N(u)|)}$

```
In [50]:
```

```
#adar index
def calc_adar_in(a,b):
    sum=0
    try:
        n=list(set(train_graph.successors(a)).intersection(set(train_graph.successors(b))))
    if len(n)!=0:
        for i in n:
            sum=sum+(1/np.log10(len(list(train_graph.predecessors(i)))))
        return sum
    else:
        return 0
    except:
        return 0
```

```
In [51]:
```

```
calc_adar_in(1,189226)
Out[51]:
0
```

```
In [52]:
```

0

```
calc_adar_in(669354,1635354)
Out[52]:
```

4.4 Is persion was following back:

```
In [53]:
```

```
def follows_back(a,b):
    if train_graph.has_edge(b,a):
        return 1
    else:
        return 0
```

```
In [54]:
follows back (1, 189226)
Out[54]:
1
In [55]:
follows back (669354, 1635354)
Out[55]:
Ω
4.5 Katz Centrality:
https://en.wikipedia.org/wiki/Katz_centrality
https://www.geeksforgeeks.org/katz-centrality-measure/ Katz centrality computes the centrality for a node based on the
centrality of its neighbors. It is a generalization of the eigenvector centrality. The Katz centrality for node i is
$$x_i = \alpha \sum_{j} A_{ij} x_j + \beta,$$
where A is the adjacency matrix of the graph G with eigenvalues $$\lambda$$.
The parameter $$\beta$$ controls the initial centrality and
\ \lambda_{\max}}.$$
In [56]:
```

```
if not os.path.isfile('/content/gdrive/MyDrive/case_study_2/data/katz.p'):
    katz = nx.katz.katz_centrality(train_graph,alpha=0.005,beta=1)
    pickle.dump(katz,open('/content/gdrive/MyDrive/case_study_2/data/katz.p','wb'))
else:
    katz = pickle.load(open('/content/gdrive/MyDrive/case_study_2/data/katz.p','rb'))
```

In [57]:

```
print('min', katz[min(katz, key=katz.get)])
print('max', katz[max(katz, key=katz.get)])
print('mean', float(sum(katz.values())) / len(katz))

min 0.0007010497950790909
max 0.0033211318137773504
```

In [58]:

```
mean_katz = float(sum(katz.values())) / len(katz)
print(mean_katz)
```

0.0007318221196993401

mean 0.0007318221196993401

4.6 Hits Score

The HITS algorithm computes two numbers for a node. Authorities estimates the node value based on the incoming links. Hubs estimates the node value based on outgoing links.

https://en.wikipedia.org/wiki/HITS_algorithm

```
if not os.path.isfile('/content/gdrive/MyDrive/case_study_2/data/hits.p'):
    hits = nx.hits(train graph, max iter=100, tol=1e-08, nstart=None, normalized=True)
    pickle.dump(hits,open('/content/gdrive/MyDrive/case study 2/data/hits.p','wb'))
else:
   hits = pickle.load(open('/content/gdrive/MyDrive/case study 2/data/hits.p','rb'))
In [60]:
print('min', hits[0][min(hits[0], key=hits[0].get)])
print('max',hits[0][max(hits[0], key=hits[0].get)])
print('mean', float(sum(hits[0].values())) / len(hits[0]))
min 0.0
max 0.004727078856184644
mean 5.370004016762928e-07
5. Featurization
5. 1 Reading a sample of Data from both train and test
In [61]:
import random
if os.path.isfile('/content/gdrive/MyDrive/Facebook/data/after eda/train after eda.csv'):
    filename = "/content/gdrive/MyDrive/Facebook/data/after eda/train after eda.csv"
    # you uncomment this line, if you don't know the lentgh of the file name
    # here we have hardcoded the number of lines as 15100030
    n train = sum(1 for line in open(filename)) #number of records in file (excludes header)
    s = 100000 #desired sample size
    skip_train = sorted(random.sample(range(1,n_train+1),n_train-s))
    #https://stackoverflow.com/a/22259008/4084039
In [62]:
if os.path.isfile('/content/gdrive/MyDrive/Facebook/data/after eda/test after eda.csv'):
   filename = "/content/qdrive/MyDrive/Facebook/data/after eda/test after eda.csv"
    # you uncomment this line, if you dont know the lentgh of the file name
    # here we have hardcoded the number of lines as 3775008
    n test = sum(1 for line in open(filename)) #number of records in file (excludes header)
    s = 50000 #desired sample size
    skip test = sorted(random.sample(range(1, n test+1), n test-s))
    #https://stackoverflow.com/a/22259008/4084039
In [63]:
print("Number of rows in the train data file:", n_train)
print("Number of rows we are going to elimiate in train data are", len(skip train))
print("Number of rows in the test data file:", n test)
print("Number of rows we are going to elimiate in test data are", len(skip test))
Number of rows in the train data file: 15100030
Number of rows we are going to elimiate in train data are 15000030
Number of rows in the test data file: 3775008
Number of rows we are going to elimiate in test data are 3725008
In [64]:
df final train = pd.read csv('/content/gdrive/MyDrive/Facebook/data/after eda/train after eda.csv', ski
prows=skip train, names=['source node', 'destination node'])
df final train['indicator link'] = pd.read csv('/content/gdrive/MyDrive/Facebook/data/train y.csv', ski
prows=skip train, names=['indicator link'])
print("Our train matrix size ", df final train.shape)
df final train.head(2)
```

ın [59]:

```
Our train matrix size (100001, 3)
```

Out[64]:

	source_node	destination_node	indicator_link
0	273084	1505602	1
1	1548737	1664354	1

In [65]:

```
df_final_test = pd.read_csv('/content/gdrive/MyDrive/Facebook/data/after_eda/test_after_eda.csv', skipr
ows=skip_test, names=['source_node', 'destination_node'])
df_final_test['indicator_link'] = pd.read_csv('/content/gdrive/MyDrive/Facebook/data/test_y.csv', skipr
ows=skip_test, names=['indicator_link'])
print("Our test matrix size ",df_final_test.shape)
df_final_test.head(2)
```

Our test matrix size (50001, 3)

Out[65]:

	source_node	destination_node	indicator_link
0	848424	784690	1
1	354852	1311092	1

5.2 Adding a set of features

we will create these each of these features for both train and test data points

- 1. jaccard followers
- 2. jaccard_followees
- 3. cosine_followers
- 4. cosine followees
- 5. num_followers_s
- 6. num_followees_s
- 7. num_followers_d
- 8. num_followees_d
- 9. inter_followers
- 10. inter_followees

In [66]:

```
if not os.path.isfile('/content/gdrive/MyDrive/case study 2/data/storage sample stage1.h5'):
    #mapping jaccrd followers to train and test data
   df final train['jaccard followers'] = df final train.apply(lambda row:
                                            jaccard for followers(row['source node'], row['destination n
ode']),axis=1)
   df final_test['jaccard_followers'] = df_final_test.apply(lambda row:
                                            jaccard for followers(row['source node'],row['destination n
ode']),axis=1)
    #mapping jaccrd followees to train and test data
   df_final_train['jaccard_followees'] = df_final_train.apply(lambda row:
                                            jaccard_for_followees(row['source_node'],row['destination_n
ode'l),axis=1)
   df final test['jaccard followees'] = df final test.apply(lambda row:
                                            jaccard_for_followees(row['source_node'],row['destination_n
ode']),axis=1)
        #mapping jaccrd followers to train and test data
   df final train['cosine followers'] = df final train.apply(lambda row:
```

Tn [67]:

```
def compute_features_stage1(df_final):
    #calculating no of followers followees for source and destination
   #calculating intersection of followers and followees for source and destination
   num followers s=[]
   num_followees_s=[]
   num followers d=[]
   num followees d=[]
   inter followers=[]
   inter followees=[]
   for i, row in df final.iterrows():
            s1=set(train graph.predecessors(row['source node']))
            s2=set(train graph.successors(row['source node']))
       except:
           s1 = set()
           s2 = set()
            d1=set(train_graph.predecessors(row['destination node']))
           d2=set(train graph.successors(row['destination node']))
       except:
           d1 = set()
           d2 = set()
       num followers s.append(len(s1))
       num_followees_s.append(len(s2))
       num followers d.append(len(d1))
       num_followees_d.append(len(d2))
       inter followers.append(len(s1.intersection(d1)))
       inter followees.append(len(s2.intersection(d2)))
   return num followers s, num followers d, num followees s, num followees d, inter followers, inter f
ollowees
```

In [68]:

```
if not os.path.isfile('/content/gdrive/MyDrive/case_study_2/data/storage_sample_stage1.h5'):
    df final train['num followers s'], df final train['num followers d'], \
    df_final_train['num_followees_s'], df_final_train['num_followees_d'], \
df_final_train['inter_followers'], df_final_train['inter_followees'] = compute_features_stage1(df_fi
nal train)
    df_final_test['num_followers_s'], df_final_test['num_followers_d'], \
    df_final_test['num_followees_s'], df_final_test['num_followees_d'], \
    df final test['inter followers'], df final test['inter followees'] = compute features stage1(df fina
1 test)
    hdf = HDFStore('/content/gdrive/MyDrive/case_study_2/data/storage_sample_stage1.h5')
    hdf.put('train df', df final train, format='table', data columns=True)
    hdf.put('test_df',df_final_test, format='table', data_columns=True)
    hdf.close()
else:
    df final train = read hdf('/content/gdrive/MyDrive/case study 2/data/storage sample stage1.h5', 'tr
ain_df', mode='r')
    df final test = read hdf('/content/gdrive/MyDrive/case study 2/data/storage sample stage1.h5', 'tes
t_df', mode='r')
```

5.3 Adding new set of features

we will create these each of these features for both train and test data points

- 1 adar index
- 2. is following back
- 3. belongs to same weakly connect components
- 4. shortest path between source and destination

In [69]:

```
if not os.path.isfile('/content/gdrive/MyDrive/case study 2/data/storage sample stage2.h5'):
    #mapping adar index on train
   df final train['adar index'] = df final train.apply(lambda row: calc adar in(row['source node'], row
['destination node']),axis=1)
   #mapping adar index on test
   df final test['adar index'] = df final test.apply(lambda row: calc adar in(row['source node'],row['
destination node']),axis=1)
    #mapping followback or not on train
   df final train['follows back'] = df final train.apply(lambda row: follows back(row['source node'],r
ow['destination node']),axis=1)
    #mapping followback or not on test
   df final test['follows back'] = df final test.apply(lambda row: follows back(row['source node'], row
['destination node']),axis=1)
   #---
    #mapping same component of wcc or not on train
   df final train['same comp'] = df final train.apply(lambda row: belongs to same wcc(row['source node
'],row['destination_node']),axis=1)
    ##mapping same component of wcc or not on train
   df final test['same comp'] = df final test.apply(lambda row: belongs to same wcc(row['source node']
,row['destination_node']),axis=1)
   #mapping shortest path on train
   df final train['shortest path'] = df final train.apply(lambda row: compute shortest path length(row
['source node'], row['destination node']), axis=1)
    #mapping shortest path on test
   df final test['shortest path'] = df final test.apply(lambda row: compute shortest path length(row['
source node'],row['destination node']),axis=1)
   hdf = HDFStore('/content/gdrive/MyDrive/case_study_2/data/storage_sample_stage2.h5')
   hdf.put('train_df',df_final_train, format='table', data_columns=True)
   hdf.put('test_df',df_final_test, format='table', data_columns=True)
   hdf.close()
else:
   df final train = read hdf('/content/gdrive/MyDrive/case study 2/data/storage sample stage2.h5', 'tr
ain_df', mode='r')
   df final test = read hdf('/content/gdrive/MyDrive/case study 2/data/storage sample stage2.h5', 'tes
t df', mode='r')
```

5.4 Adding new set of features

we will create these each of these features for both train and test data points

- 1. Weight Features
 - · weight of incoming edges
 - · weight of outgoing edges
 - weight of incoming edges + weight of outgoing edges
 - · weight of incoming edges * weight of outgoing edges
 - 2*weight of incoming edges + weight of outgoing edges
 - weight of incoming edges + 2*weight of outgoing edges

- 2. Page Ranking of source
- 3. Page Ranking of dest
- 4. katz of source
- 5. katz of dest
- 6. hubs of source
- 7. hubs of dest
- 8. authorities_s of source
- 9. authorities s of dest

Weight Features

In order to determine the similarity of nodes, an edge weight value was calculated between nodes. Edge weight decreases as the neighbor count goes up. Intuitively, consider one million people following a celebrity on a social network then chances are most of them never met each other or the celebrity. On the other hand, if a user has 30 contacts in his/her social network, the chances are higher that many of them know each other.

| Credit - Graph-based Features for Supervised Link Prediction William Cukierski, Benjamin Hamner, Bo Yang

\begin{equation} W = \frac{1}{\sqrt{1+|X|}} \end{equation}

it is directed graph so calculated Weighted in and Weighted out differently

In [70]:

```
#weight for source and destination of each link
Weight_in = {}
Weight_out = {}
for i in tqdm(train_graph.nodes()):
    s1=set(train_graph.predecessors(i))
    w_in = 1.0/(np.sqrt(1+len(s1)))
    Weight_in[i]=w_in

    s2=set(train_graph.successors(i))
    w_out = 1.0/(np.sqrt(1+len(s2)))
    Weight_out[i]=w_out

#for imputing with mean
mean_weight_in = np.mean(list(Weight_in.values()))
mean_weight_out = np.mean(list(Weight_out.values()))
100%| | 1862196/1862196 [00:22<00:00, 84555.42it/s]
```

In [71]:

```
if not os.path.isfile('/content/gdrive/MyDrive/case study 2/data/storage sample stage3.h5'):
    #mapping to pandas train
    df final train['weight in'] = df final train.destination node.apply(lambda x: Weight in.get(x, mean
weight_in))
    df final train['weight out'] = df final train.source node.apply(lambda x: Weight out.get(x, mean wei
ght out))
    #mapping to pandas test
    df final test['weight in'] = df final test.destination node.apply(lambda x: Weight in.get(x,mean we
ight in))
   df final test['weight out'] = df final test.source node.apply(lambda x: Weight out.get(x, mean weigh
t out))
    #some features engineerings on the in and out weights
    df_final_train['weight_f1'] = df_final_train.weight_in + df_final_train.weight_out
    df_final_train['weight_f2'] = df_final_train.weight_in * df_final_train.weight_out
       final train['weight f3'] = (2*df final train.weight in + 1*df final train.weight out)
    df final train['weight f4'] = (1*df final train.weight in + 2*df final train.weight out)
    #some features engineerings on the in and out weights
    df_final_test['weight_f1'] = df_final_test.weight_in + df_final_test.weight_out
    df_final_test['weight_f2'] = df_final_test.weight_in * df_final_test.weight_out
df_final_test['weight_f3'] = (2*df_final_test.weight_in + 1*df_final_test.weight_out)
    df_final_test['weight_f4'] = (1*df_final_test.weight_in + 2*df_final_test.weight_out)
```

```
In [72]:
```

```
if not os.path.isfile('/content/gdrive/MyDrive/case study 2/data/storage sample stage3.h5'):
       #page rank for source and destination in Train and Test
       #if anything not there in train graph then adding mean page rank
      df final train['page rank s'] = df final train.source node.apply(lambda x:pr.get(x,mean pr))
      df final train['page rank d'] = df final train.destination node.apply(lambda x:pr.get(x,mean pr))
      df final test['page rank s'] = df final test.source node.apply(lambda x:pr.get(x,mean pr))
      df final test['page rank d'] = df final test.destination node.apply(lambda x:pr.get(x,mean pr))
       #Katz centrality score for source and destination in Train and test
       #if anything not there in train graph then adding mean katz score
      df final train['katz s'] = df final train.source node.apply(lambda x: katz.get(x,mean katz))
      df final train['katz d'] = df final train.destination node.apply(lambda x: katz.get(x, mean katz))
      df_final_test['katz_s'] = df_final_test.source_node.apply(lambda x: katz.get(x,mean_katz))
      df final test['katz d'] = df final test.destination node.apply(lambda x: katz.get(x,mean katz))
       #Hits algorithm score for source and destination in Train and test
       #if anything not there in train graph then adding 0
      \label{eq:df_final_train} $$ df_{final_train.source_node.apply(lambda x: hits[0].get(x,0)) $$ $$ df_{final_train}(x,0) = (x,0) $$ for the context of the c
      df final train['hubs d'] = df final train.destination node.apply(lambda x: hits[0].get(x,0))
      df final test['hubs s'] = df final test.source node.apply(lambda x: hits[0].get(x,0))
      df final test['hubs d'] = df final test.destination node.apply(lambda x: hits[0].get(x,0))
       #Hits algorithm score for source and destination in Train and Test
       #if anything not there in train graph then adding 0
      df_final_train['authorities_s'] = df_final_train.source_node.apply(lambda x: hits[1].get(x,0))
      df final train['authorities d'] = df final train.destination node.apply(lambda x: hits[1].get(x,0))
      df final test['authorities s'] = df final test.source node.apply(lambda x: hits[1].get(x,0))
      df final test['authorities d'] = df final test.destination node.apply(lambda x: hits[1].get(x,0))
      hdf = HDFStore('/content/gdrive/MyDrive/case_study_2/data/storage_sample_stage3.h5')
      hdf.put('train_df',df_final_train, format='table', data_columns=True)
      hdf.put('test df', df final test, format='table', data columns=True)
      hdf.close()
else:
      df final train = read hdf('/content/gdrive/MyDrive/case_study_2/data/storage_sample_stage3.h5', 'tr
ain df', mode='r')
      df final test = read hdf('/content/gdrive/MyDrive/case study 2/data/storage sample stage3.h5', 'tes
t df', mode='r')
```

5.5 Adding new set of features

we will create these each of these features for both train and test data points

1. SVD features for both source and destination

```
In [73]:
```

```
#for svd features to get feature vector creating a dict node val and inedx in svd vector
sadj_col = sorted(train_graph.nodes())
sadj_dict = { val:idx for idx, val in enumerate(sadj_col)}
```

In [74]:

```
def svd(x, S):
    try:
        z = sadj_dict[x]
        return S[z]
    except:
```

```
return [0,0,0,0,0,0]
```

In [75]:

```
Adj = nx.adjacency_matrix(train_graph,nodelist=sorted(train_graph.nodes())).asfptype()
```

In [76]:

```
U, s, V = svds(Adj, k = 6)
print('Adjacency matrix Shape', Adj.shape)
print('U Shape', U.shape)
print('V Shape', V.shape)
print('S Shape', s.shape)
Adjacency matrix Shape (1862196, 1862196)
```

Adjacency matrix Shape (1862196, 1862196) U Shape (1862196, 6) V Shape (6, 1862196) s Shape (6,)

In [77]:

```
if not os.path.isfile('/content/gdrive/MyDrive/case study 2/data/storage sample stage4.h5'):
   df final train[['svd u s 1', 'svd u s 2', 'svd u s 3', 'svd u s 4', 'svd u s 5', 'svd u s 6']] = \
   df final train.source node.apply(lambda x: svd(x, U)).apply(pd.Series)
   df final train[['svd u d 1', 'svd u d 2', 'svd u d 3', 'svd u d 4', 'svd u d 5', 'svd u d 6']] = \
   df final train.destination node.apply(lambda x: svd(x, U)).apply(pd.Series)
   df final train[['svd v s 1','svd v s 2', 'svd v s 3', 'svd v s 4', 'svd v s 5', 'svd v s 6',]] = \
   df final train.source node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
   df final train[['svd_v_d_1', 'svd_v_d_2', 'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5','svd_v_d_6']] = \
   df final train.destination node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
   df final test[['svd u s 1', 'svd u s 2', 'svd u s 3', 'svd u s 4', 'svd u s 5', 'svd u s 6']] = \
   df final test.source node.apply(lambda x: svd(x, U)).apply(pd.Series)
   df_final_test[['svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4', 'svd_u_d_5','svd_u_d_6']] = \
   df final test.destination node.apply(lambda x: svd(x, U)).apply(pd.Series)
   df_final_test[['svd_v_s_1','svd_v_s_2', 'svd_v_s_3', 'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6',]] = \
   df final test.source node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
   df final test[['svd v d 1', 'svd v d 2', 'svd v d 3', 'svd v d 4', 'svd v d 5','svd v d 6']] = \
   df final test.destination node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
    #=
   hdf = HDFStore('/content/gdrive/MyDrive/case study 2/data/storage sample stage4.h5')
   hdf.put('train_df',df_final_train, format='table', data_columns=True)
   hdf.put('test_df',df_final_test, format='table', data_columns=True)
   hdf.close()
else:
   df_final_train = read_hdf('/content/gdrive/MyDrive/case_study_2/data/storage_sample_stage4.h5', 'tr
ain_df',mode='r')
   df final test = read hdf('/content/gdrive/MyDrive/case_study_2/data/storage_sample_stage4.h5', 'tes
t df', mode='r')
```

ргетегниат апаститетт.

Preferential Attachment with followers and followees data of vertex. you can check about Preferential Attachment in below link http://be.amazd.com/link-prediction/

```
In [78]:
```

In [79]:

```
def compute features stage5(df final):
    #calculating the product of followers for source and destination
    #calculating the product of followees for source and destination
   num followers s=[]
   num followees s=[]
   num followers d=[]
   num followees d=[]
   for i, row in df final.iterrows():
        try:
            s1=set(train_graph.predecessors(row['source_node']))
           s2=set(train graph.successors(row['source node']))
       except:
           s1 = set()
           s2 = set()
       try:
           dl=set(train graph.predecessors(row['destination node']))
           d2=set(train graph.successors(row['destination node']))
       except:
           d1 = set()
           d2 = set()
       num_followers_s.append(len(s1))
       num followees s.append(len(s2))
       num followers d.append(len(d1))
       num followees d.append(len(d2))
       followers_attachment = np.array(num_followers_s)*np.array(num_followers_d)
        followees attachment = np.array(num followees s)*np.array(num followees d)
   return followers_attachment, followees_attachment
```

In [80]:

```
if not os.path.isfile('/content/gdrive/MyDrive/case_study_2/data/storage_sample_stage5.h5'):
    df_final_train['prefer_followers'], df_final_train['prefer_followees'] = compute_features_stage5(df_final_train)
    df_final_test['prefer_followers'], df_final_test['prefer_followees'] = compute_features_stage5(df_final_test)

    hdf = HDFStore('/content/gdrive/MyDrive/case_study_2/data/storage_sample_stage5.h5')
    hdf.put('train_df',df_final_train, format='table', data_columns=True)
    hdf.put('test_df',df_final_test, format='table', data_columns=True)
```

```
hdf.close()
else:
    df_final_train = read_hdf('/content/gdrive/MyDrive/case_study_2/data/storage_sample_stage5.h5', 'tr
ain_df',mode='r')
    df_final_test = read_hdf('/content/gdrive/MyDrive/case_study_2/data/storage_sample_stage5.h5', 'tes
t_df',mode='r')
```

In [81]:

```
df_final_train.columns
```

Out[81]:

svd dot

Add feature called svd_dot. you can calculate svd_dot as Dot product between sourse node svd and destination node svd features. you can read about this in below pdf https://storage.googleapis.com/kaggle-forum-message-attachments/2594/supervised_link_prediction.pdf

In [82]:

```
# function to calculate svd_dot product of source and destination features for matrix 'U' and 'V.T' sep
erately :
def compute_features_stage6(df_final,U):
    source_features = df_final.source_node.apply(lambda x: svd(x, U)).apply(pd.Series)
    destination_features = df_final.destination_node.apply(lambda x: svd(x, U)).apply(pd.Series)

# convert to numpy arrays to do dot product of source and destination features:
    source_features = [row.to_numpy() for i,row in source_features.iterrows()]
    destination_features = [row.to_numpy() for i,row in destination_features.iterrows()]

L = len(source_features)

result_dot = []

for i in range(L):
    result_dot.append(np.dot(source_features[i],destination_features[i]))

result_dot = np.array(result_dot).reshape(-1,1)
return_result_dot
```

Tn [831:

```
if not os.path.isfile('/content/gdrive/MyDrive/case_study_2/data/storage_sample_stage6.h5'):

# svd_dot of source and destination in matrix 'U' in train

df_final_train['svdot_u_sd'] = compute_features_stage6(df_final_train,U)

# svd_dot of source and destination in matrix 'V.T' in train

df_final_train['svdot_v_sd'] = compute_features_stage6(df_final_train,V.T)

# svd_dot of source and destination in matrix 'U' in test

df_final_test['svdot_u_sd'] = compute_features_stage6(df_final_test,U)

# svd_dot of source and destination in matrix 'V.T' in test

df_final_test['svdot_v_sd'] = compute_features_stage6(df_final_test,V.T)
```

```
hdf = HDFStore('/content/gdrive/MyDrive/case_study_2/data/storage_sample_stage6.hb')
hdf.put('train_df',df_final_train, format='table', data_columns=True)
hdf.put('test_df',df_final_test, format='table', data_columns=True)
hdf.close()
else:
    df_final_train = read_hdf('/content/gdrive/MyDrive/case_study_2/data/storage_sample_stage6.h5', 'tr
ain_df',mode='r')
    df_final_test = read_hdf('/content/gdrive/MyDrive/case_study_2/data/storage_sample_stage6.h5', 'tes
t_df',mode='r')
```

Training Model: xgboost

```
In [1]:
```

```
#reading
from pandas import read_hdf

df_final_train = read_hdf('/content/gdrive/MyDrive/case_study_2/data/storage_sample_stage6.h5', 'train_
    df', mode='r')

df_final_test = read_hdf('/content/gdrive/MyDrive/case_study_2/data/storage_sample_stage6.h5', 'test_df
',mode='r')
```

```
In [37]:
```

```
df_final_train[['prefer_followers','prefer_followees','svdot_u_sd','svdot_v_sd']].head(2)
```

Out[37]:

	prefer_followers	prefer_followees	svdot_u_sd	svdot_v_sd
0	130	187	1.123026e-11	2.334976e-12
1	306	169	5.797253e-17	4.876798e-17

In [3]:

```
df_final_train.columns
```

Out[3]:

```
Index(['source_node', 'destination_node', 'indicator_link',
    'jaccard_followers', 'jaccard_followees', 'cosine_followers',
    'cosine_followees', 'num_followers_s', 'num_followers_d',
    'num_followees_s', 'num_followees_d', 'inter_followers',
    'inter_followees', 'adar_index', 'follows_back', 'same_comp',
    'shortest_path', 'weight_in', 'weight_out', 'weight_f1', 'weight_f2',
    'weight_f3', 'weight_f4', 'page_rank_s', 'page_rank_d', 'katz_s',
    'katz_d', 'hubs_s', 'hubs_d', 'authorities_s', 'authorities_d',
    'svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5',
    'svd_u_s_6', 'svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4',
    'svd_u_d_5', 'svd_u_d_6', 'svd_v_s_1', 'svd_v_s_2', 'svd_v_s_3',
    'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6', 'svd_v_d_1', 'svd_v_d_2',
    'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5', 'svd_v_d_6', 'prefer_followers',
    'prefer_followees', 'svdot_u_sd', 'svdot_v_sd'],
    dtype='object')
```

In [4]:

```
y_train = df_final_train.indicator_link
y_test = df_final_test.indicator_link
```

In [5]:

```
df_final_train.drop(['source_node', 'destination_node','indicator_link'],axis=1,inplace=True)
df_final_test.drop(['source_node', 'destination_node','indicator_link'],axis=1,inplace=True)
```

```
In [6]:
```

```
y_train.value_counts()
```

Out[6]:

1 50012 0 49989

Name: indicator_link, dtype: int64

In [7]:

```
y_test.value_counts()
```

Out[7]:

0 25021 1 24980

Name: indicator link, dtype: int64

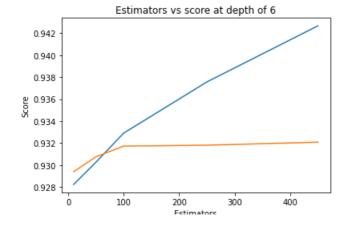
In [12]:

```
# to find best estimator
estimators = [10, 50, 100, 250, 450]
train scores = []
test scores = []
for i in estimators:
   clf = xgb.XGBClassifier(n_estimators=i, max_depth=6, learning_rate=0.1, verbosity=0, objective='binary:
logistic',booster='gbtree',n_jobs=-1,
                            min child weight=15, colsample bytree=0.8, colsample bylevel=0.8, random state
=39)
    clf.fit(df_final_train,y_train)
    train_sc = f1_score(y_train,clf.predict(df_final_train))
    test_sc = f1_score(y_test,clf.predict(df_final_test))
    test scores.append(test sc)
    train_scores.append(train_sc)
   print('Estimators = ',i,'Train Score',train_sc,'test Score',test sc)
plt.plot(estimators, train scores, label='Train Score')
plt.plot(estimators,test_scores,label='Test Score')
plt.xlabel('Estimators')
plt.ylabel('Score')
plt.title('Estimators vs score at depth of 6')
```

Estimators = 10 Train Score 0.9282376749557644 test Score 0.9294025390500816
Estimators = 50 Train Score 0.9302547365744077 test Score 0.9307539093952621
Estimators = 100 Train Score 0.9329078209043546 test Score 0.9317263981393383
Estimators = 250 Train Score 0.937567855298247 test Score 0.9318105049822664
Estimators = 450 Train Score 0.9426742217970417 test Score 0.93208144319021

Out[12]:

Text(0.5, 1.0, 'Estimators vs score at depth of 6')

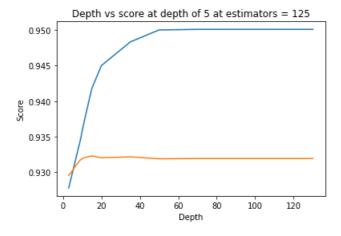


Laumatora

In [13]:

```
# to find best depth
depths = [3,9,11,15,20,35,50,70,130]
train scores = []
test scores = []
for i in depths:
   clf = xgb.XGBClassifier(n estimators=125, max depth=i, learning rate=0.05, verbosity=0, objective='bina
ry:logistic',booster='gbtree',n_jobs=-1,
                            min_child_weight=15,colsample_bytree=0.8,colsample_bylevel=0.8,random_state
   clf.fit(df_final_train,y_train)
   train_sc = f1_score(y_train,clf.predict(df_final_train))
   test_sc = f1_score(y_test,clf.predict(df_final_test))
    test scores.append(test sc)
   train scores.append(train sc)
   print('depth = ',i,'Train Score',train sc,'test Score',test sc)
plt.plot(depths,train scores,label='Train Score')
plt.plot(depths, test scores, label='Test Score')
plt.xlabel('Depth')
plt.ylabel('Score')
plt.title('Depth vs score at depth of 5 at estimators = 125')
plt.show()
```

```
depth = 3 Train Score 0.9278002125398513 test Score 0.9295451649891707
depth = 9 Train Score 0.9344705857484094 test Score 0.9317450914014895
depth = 11 Train Score 0.9370970294940115 test Score 0.932041709850039
depth = 15 Train Score 0.9417582995738413 test Score 0.9323158873763422
depth = 20 Train Score 0.9449949613705072 test Score 0.9320310352846664
depth = 35 Train Score 0.9483195476913412 test Score 0.932172590119596
depth = 50 Train Score 0.95000731804211 test Score 0.9318964606444796
depth = 70 Train Score 0.9500878220140516 test Score 0.9319415978194265
depth = 130 Train Score 0.9500878220140516 test Score 0.9319415978194265
```



In [14]:

MEGII CLAIM SCOLES [0.737/0037 0.733070/7 0.733710203 0.73007037 0.73000733]

silent=None, subsample=1, verbosity=1)

```
In [23]:
print(xgb random.best estimator)
XGBClassifier(base score=0.5, booster='gbtree', colsample bylevel=1,
              colsample_bynode=1, colsample_bytree=1, gamma=0,
              learning rate=0.1, max delta step=0, max depth=10,
              min child weight=19, missing=None, n estimators=100, n jobs=-1,
              nthread=None, objective='binary:logistic', random_state=39,
              reg_alpha=0, reg_lambda=1, scale_pos weight=1, seed=None,
              silent=None, subsample=1, verbosity=1)
In [24]:
# best model
clf = xgb.XGBClassifier(base score=0.5, booster='gbtree', colsample bylevel=1,
              colsample bynode=1, colsample bytree=1, gamma=0,
              learning_rate=0.1, max_delta_step=0, max_depth=10,
              min_child_weight=19, missing=None, n_estimators=100, n_jobs=-1,
              nthread=None, objective='binary:logistic', random_state=39,
              reg alpha=0, reg lambda=1, scale pos weight=1, seed=None,
```

In [25]:

```
# fit and predict
clf.fit(df_final_train,y_train)
y_train_pred = clf.predict(df_final_train)
y_test_pred = clf.predict(df_final_test)
```

In [26]:

```
print('Train f1 score',f1_score(y_train,y_train_pred))
print('Test f1 score',f1_score(y_test,y_test_pred))
```

Train f1 score 0.937916934523496 Test f1 score 0.932071245959137

In [27]:

```
# function taken from assignment reference:
def plot confusion matrix(test y, predict y):
   C = confusion matrix(test y, predict y)
   A = (((C.T) / (C.sum(axis=1))).T)
   B = (C/C.sum(axis=0))
   plt.figure(figsize=(20,4))
   labels = [0,1]
    # representing A in heatmap format
   cmap=sns.light palette("blue")
   plt.subplot(1, 3, 1)
   sns.heatmap(C, annot=True, cmap=cmap, fmt=".3f", xticklabels=labels, yticklabels=labels)
   plt.xlabel('Predicted Class')
   plt.ylabel('Original Class')
   plt.title("Confusion matrix")
   plt.subplot(1, 3, 2)
   sns.heatmap(B, annot=True, cmap=cmap, fmt=".3f", xticklabels=labels, yticklabels=labels)
   plt.xlabel('Predicted Class')
   plt.ylabel('Original Class')
   plt.title("Precision matrix")
   plt.subplot(1, 3, 3)
    # representing B in heatmap format
```

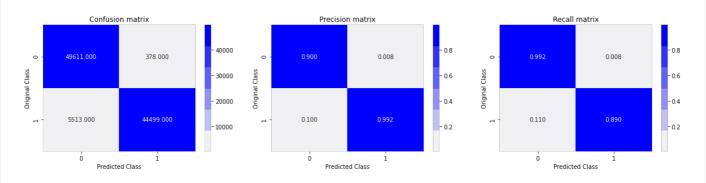
```
sns.heatmap(A, annot=True, cmap=cmap, fmt=".3f", xticklabels=labels, yticklabels=labels)
plt.xlabel('Predicted Class')
plt.ylabel('Original Class')
plt.title("Recall matrix")

plt.show()
```

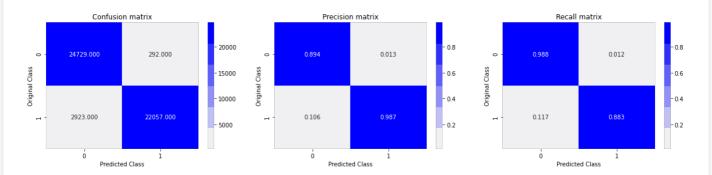
In [28]:

```
print('Train confusion_matrix')
plot_confusion_matrix(y_train,y_train_pred)
print('Test confusion_matrix')
plot_confusion_matrix(y_test,y_test_pred)
```

Train confusion_matrix



Test confusion_matrix



Observations:

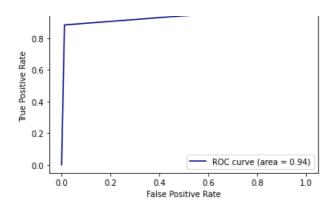
1. for both Train and Test data:

True positive is slightly high than true negative in precision true negative is slightly high than true positive in recall

1. similary in confusion matrix True negative is slightly higher than True positive in both Train and Test data

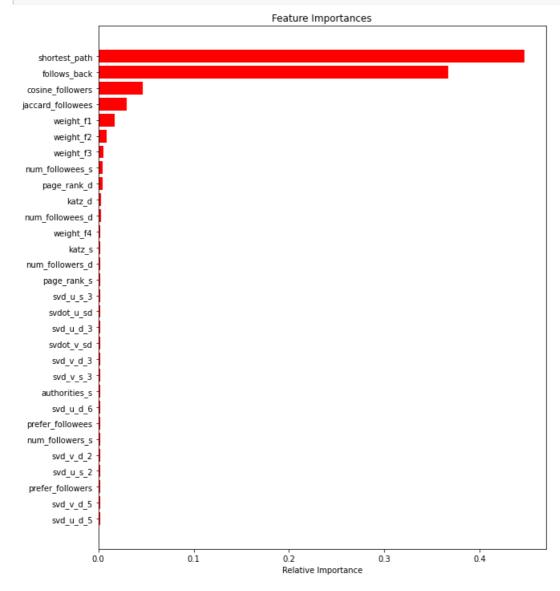
In [29]:

```
from sklearn.metrics import roc_curve, auc
fpr,tpr,ths = roc_curve(y_test,y_test_pred)
auc_sc = auc(fpr, tpr)
plt.plot(fpr, tpr, color='navy',label='ROC curve (area = %0.2f)' % auc_sc)
plt.xlabel('False Positive Rate')
plt.ylabel('True Positive Rate')
plt.title('Receiver operating characteristic with test data')
plt.legend()
plt.show()
```



In [38]:

```
# top 30 features
features = df_final_train.columns
importances = clf.feature_importances_
indices = (np.argsort(importances))[-30:]
plt.figure(figsize=(10,12))
plt.title('Feature Importances')
plt.barh(range(len(indices)), importances[indices], color='r', align='center')
plt.yticks(range(len(indices)), [features[i] for i in indices])
plt.xlabel('Relative Importance')
plt.show()
```



Observations:

- 1. on adding two new features (preferential attachment,svd_dot), there is a some improvement in both test f1_scores and test Auc score.
- 2. and F1 scores for both Train and Test and AUC score

```
Train fl score = 93%
Test fl score = 93%
AUC score = 94%
```

very close and overall best score without overfitting

3. we can see from the best features, in which our newly added features are also got some amount of feature importance (prefer_followees,prefer_followers,svd_dot_u_sd,svd_dot_v_sd)

In []: