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1 The "carry forward" problem

An example of the "carry forward" problem															
seq_along	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
values	89.7	26.6	37.2	57.3	90.8	20.2	89.8	94.5	66.1	62.9	6.2	20.6	17.7	68.7	38.4
value > 50	Т	F	F	T	T	F	T	Т	Т	Т	F	F	F	Т	F

In the situarion depicted above, we sometimes wish to replace values for which a condition (in the example shown above, "value > 50") is FALSE with the most recent value for which that same condition was TRUE, moving from left to right. This is the "carry forward" problem. For example, we might want to fill **NA** values with the last valid observation in a time-series of measurments. Because this problem occurs frequently, we need a fast formula for this. R loops would be way too slow.

- We can compute the result directly using the rep function with the vector version of the times argument
- We can compute indices into the original vector that produce the desired result using cummax on the "squelched" seq_along vector

1.1 The solution using rep

The rep function with a vector times argument allows us to replicate individual elements by arbitrary counts. If sum of times is equal to the length of the original vector, we will get a result with the same length as the original.

Consider the vector 1:10. We might want to replace even values with their preceding odd values.

```
x<-1:10
```

odd values are:

```
x[x%%2==1]
## [1] 1 3 5 7 9
```

and the number of items between odd values is:

```
diff(c(which(x%%2==1),length(x)+1))
## [1] 2 2 2 2 2
```

replicating each element in the "odd" subset by the corresponding element in the repetition vector, gives the desired result:

```
rep(x[x\%2==1],times=diff(c(which(x\%2==1),length(x)+1)))
## [1] 1 1 3 3 5 5 7 7 9 9
```

1.2 The solution using cummax

cummax naturally carries forward the recent maximum. We can apply a "mask" vector containing 0 or 1 values to the seq_along vector to get the "squelched" seq_along vector. Applying cummax the "squelched" seq_along and obtain a vector of indices

A seq_along vector would look like this:

```
1:10
## [1] 1 2 3 4 5 6 7 8 9 10
```

The "mask" vector looks like this:

```
rep(c(1,0,1),times=c(4,2,4))
## [1] 1 1 1 1 0 0 1 1 1 1
```

The "squelched" seq_along vector will then be:

```
1:10*rep(c(1,0,1),times=c(4,2,4))

## [1] 1 2 3 4 0 0 7 8 9 10
```

Applying cummax to the "squelched" seq_along vector carries forward non-zero values:

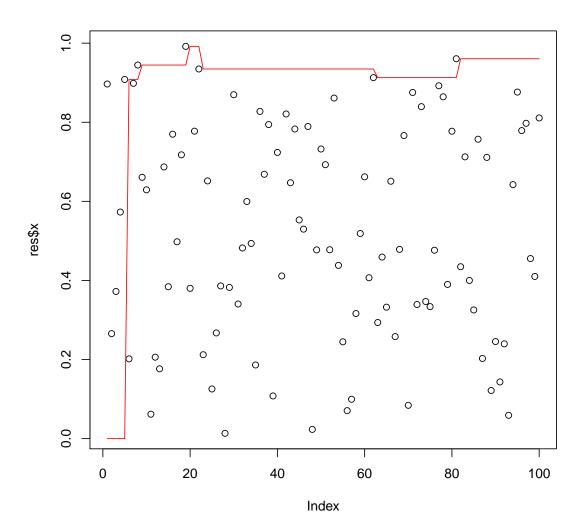
```
cummax(1:10*rep(c(1,0,1),times=c(4,1,5)))
## [1] 1 2 3 4 4 6 7 8 9 10
```

1.3 Carrying forward a value, version 1

We sometimes need to "carry forward" a value at a specific points in a vector. For example, we might want to carry forward non-zero values in a time-series. We can use the times argument of the rep function to assemble the result

```
set.seed(0)
x<-runif(100)
loc<-x>0.9
loc_diff(-diff(c(0,which(loc),length(x)))
x_cf<-rep(c(0,x[loc]),times=loc_diff)

res<-data.table(
    x=x,
    carry_cforward=x_cf
)</pre>
```



1.4 Carrying forward a value, version 2

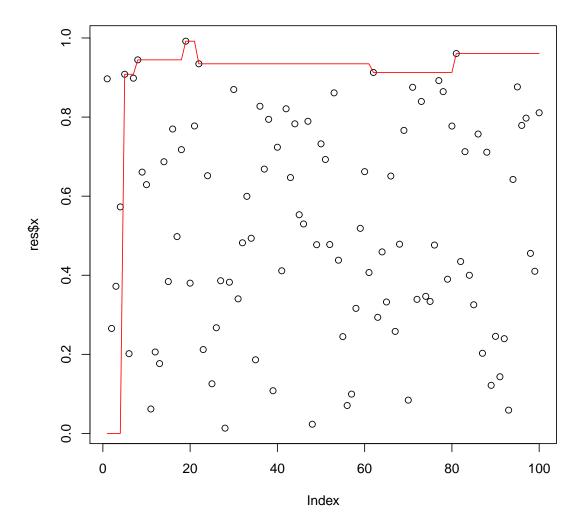
We sometimes need to "carry forward" a value at a specific points in a vector. For example, we might want to carry forward non-zero values in a time-series. We can apply the condition to the seq_along vector to produce a vector that has is non-zero and equal to the index of the "carry-forward" values. Because the seq_along vector is increasing, we can use cummax to do the "carry-forward" operation for us.

```
set.seed(0)
x<-runif(100)
loc<-x>0.9

ndx<-cummax(seq_along(x)*loc)

x_cf<-c(0,x)[ndx+1]

res<-data.table(
    x=x,
    carry_cforward=x_cf
)</pre>
```



2 The re-setting count problem

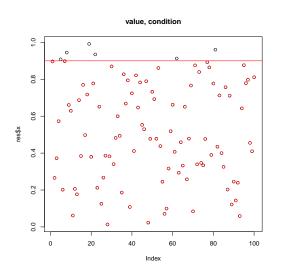
We sometimes need to count the length over which a condition holds. This is called the **re-setting sum**. For example, in the context of some systematic strategies we would like to know how many days ago a signal was triggered. Because of frequent use, a vectorized calculation of the **re-setting sum** is needed.

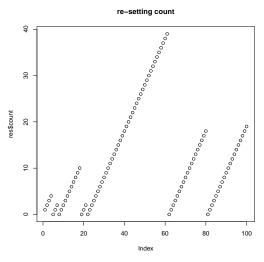
2.1 Re-setting count, solution using cummax

```
set.seed(0)
x<-runif(100)
test<-x<0.9
y<-cumsum(test)
c(0,y-cummax(y*!test))

res<-data.table(
    x=x,
    test=test*1,
    count=cumsum(test)-cummax(cumsum(test)*!test)
)</pre>
```

re-setting sum of elements since condition is met





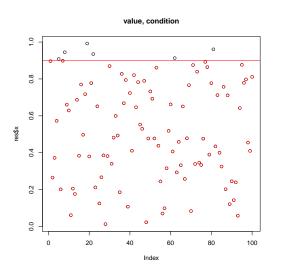
2.2 Resetting count, solution using partial seq_along concatenation

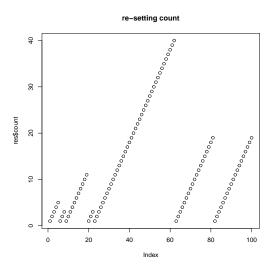
We sometimes need to count the length over which a condition holds. This is called the **re-setting sum**. For example, in the context of some systematic strategies we would like to know how many days ago a signal was triggered. Because of frequent use, a vectorized calculation of the **re-setting sum** is needed. We can compute the re-setting sum by explicitly combining subsets of the seq_along vector as follows:

```
set.seed(0)
x<-runif(100)
test<-x<0.9
condition_length<-diff(c(0,which(!test),length(x)))
vcs<-mapply(function(i,s)s[1:i],i=condition_length,MoreArgs=list(s=seq_along(x)),SIMPLIFY = FALSE)
count<-do.call(c,vcs)

res<-data.table(
    x=x,
    test=test*1,
    count=count
)</pre>
```

re-setting sum of elements since condition is met





3 The outer produce problem

We sometimes need to create all combinations of values in 2 vectors. For example, when creating a grid of strategy performance for all values of two parameters. The expand.grid function can be used for this. Some times we want to do this in-line and avoid the extra function call. The rep function has two parameters, times and each which can be used to achieve this:

```
item1<-paste0("square",1:3)
item2<-paste0("circle",1:3)

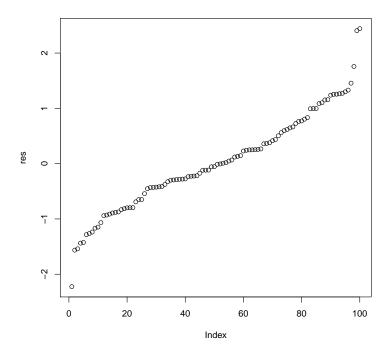
combinations<-data.table(
    x=rep(item1,times=length(item2)),
    y=rep(item2,each=length(item1))
)</pre>
```

combinations table:					
	X	у			
1	square1	circle1			
2	square2	circle1			
3	square3	circle1			
4	square1	circle2			
5	square2	circle2			
6	square3	circle2			
7	square1	circle3			
8	square2	circle3			
9	square3	circle3			

4 The sorting permutation matrix problem

It is sometimes useful to express sorting operations in the form of permutation matrices. The reason for this is that we can chain permutations by multiplying the permutation matrix. Dense element ranks are used as column indices into the diagonal matrix to form the permutation matrix.

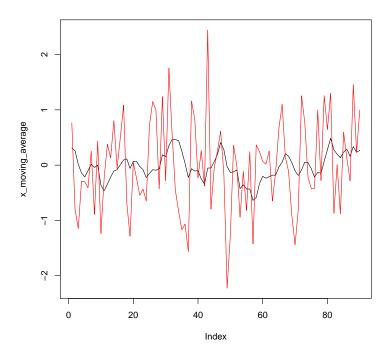
```
set.seed(0)
x<-rnorm(100)
m<-diag(length(x))[,frank(x,ties.method = "dense")]
res<-drop(m%*%cbind(x))</pre>
```



5 The moving average problem

Moving averages are basic ingredients for signal calculations. We need a fast method for computing these.

```
set.seed(0)
x<-rnorm(100,mean=0)
x_sum<-cumsum(x)
x_moving_average<-(tail(x_sum,-10)-head(x_sum,-10))/10</pre>
```





7 The drawdown statistics problem

Drowdown analysis is an importan component of strategy design. A fast calculation of common statistics is therefore needed. Drawdown statistics are computed daily, so each stat is a vector of values corresponding to a vector of dates, starting at inception and ending at the current date. A strategy's history can be seen as being split by high-watermark dates into a series of **drawdown episodes**. Every day will belong to a single drawdown episode and episodes ordered by episode start date will cover the whole history without gaps. A strategy that trends upwards without downdays will be composed of adjacent 1-day episodes each having a drawdown of zero.

The most common statistics are:

	Common drawdown statistics
${\tt drawdown_episode}$	count of high water mark dates since inception
$high_water_mark$	NAV at start of current drawdown episode
drawdown	distance of current NAV relative to most recent high water mark
${\tt maximum_drawdown}$	the maximum drawdown in the current drawdown episode
${\tt drawdown_length}$	the length, in days, of a completed drawdown episode
drawdown_date	the date on which an episode's maximum drawdown occured