$$\stackrel{\downarrow}{U_g} = \stackrel{\downarrow}{U_{g^{-1}}}$$