Vector Algebra

1 12^{th} Maths - Exercise 10.3.13

1. If \overrightarrow{a} , \overrightarrow{b} , \overrightarrow{c} are unit vectors such that $\overrightarrow{a} + \overrightarrow{b} + \overrightarrow{c} = 0$, find the value of \overrightarrow{a} , \overrightarrow{b} , \overrightarrow{c} are unit vectors such that \overrightarrow{a} + \overrightarrow{b} + \overrightarrow{c} = 0, find the value

2 Solution

The given vectors \mathbf{a}, \mathbf{b} and \mathbf{c} are unit vectors

The magnitude of vectors $\mathbf{a}, \mathbf{b}, \mathbf{c}$ are

$$\|\mathbf{a}\| = \sqrt{1^2} = 1 \tag{1}$$

$$\|\mathbf{b}\| = \sqrt{1^2} = 1 \tag{2}$$

$$\|\mathbf{c}\| = \sqrt{1^2} = 1\tag{3}$$

The Given equation is

$$\mathbf{a} + \mathbf{b} + \mathbf{c} = 0 \tag{4}$$

$$\|\mathbf{a} + \mathbf{b} + \mathbf{c}\|^2 = 0^2 \tag{5}$$

$$\|\mathbf{a}\|^2 + \|\mathbf{b}\|^2 + \|\mathbf{c}\|^2 + 2(\mathbf{a}\mathbf{b} + \mathbf{b}\mathbf{c} + \mathbf{c}\mathbf{a}) \implies 0$$
 (6)

$$||1||^2 + ||1||^2 + ||1||^2 + 2(\mathbf{ab} + \mathbf{bc} + \mathbf{ca}) \implies 0$$
 (7)

$$3 + 2(\mathbf{ab} + \mathbf{bc} + \mathbf{ca}) \implies 0 \tag{8}$$

$$ab + bc + ca \implies \frac{-3}{2}$$
 (9)