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Assignment 1

AI1110: Probability and Random Variables Indian Institute of Techonology Hyderabad

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Exemplar, 10.13.3.39:

Question.

A die has its six faces marked 0, 1, 1, 1, 6, 6. Two such dice are thrown together and the total score is recorded.

- (i) How many different scores are possible?
- (ii) What is the probability of getting a total of 7? **Answer:**
 - i) 6
 - ii) $\frac{1}{3}$

Solution:

- i) The possible sums are
 - 0 (If both the times outcome is zero)
 - 1 (If the outcome was 0 and 1 or viceversa)
 - 2 (If both times the outcome was 1)
 - 6 (If the outcome was 0 and 6 or viceversa
 - 7 (If the outcome was 1 and 6 or viceversa
 - 12 (If both times the outcome was 6)

ii)The sum 7 can be obtained only if $1 \mid 6$ or $6 \mid 1$

The total possible scores are 6 from equation (1)

∴ Required probability =
$$\frac{2}{6}$$

= $\frac{1}{3}$

PMF of the distribution

X				_
Outcome	0	1	6	
P(X=x)	$\frac{1}{6}$	$\frac{1}{2}$	$\frac{1}{3}$	

PMF of sum of numbers on the dice

Let X be the random variable representing the total score when two dice with markings 0, 1, 1, 1, 6, 6 are thrown together. Then the PMF of X can be expressed as:

$$P(X = x) = \begin{cases} \frac{1}{36} & x = 0\\ \frac{1}{6} & x = 1\\ \frac{1}{4} & x = 2\\ \frac{1}{3} & x = 7\\ \frac{1}{9} & x \in \{6, 12\}\\ 0 & \text{otherwise} \end{cases}$$

where x is the possible score, and the values of the PMF are given in the corresponding cases.

X						
Score	0	1	2	6	7	12
P(X=x)	$\frac{1}{36}$	$\frac{1}{6}$	$\frac{1}{4}$	$\frac{1}{9}$	$\frac{1}{3}$	$\frac{1}{9}$

Let x[n] be the discrete-time signal representing the probability mass function (PMF) for the total score when two dice with markings 0, 1, 1, 1, 6, 6 are thrown together. Then the Z transform of x[n] is given by:

$$X(z) = \sum_{n = -\infty}^{\infty} x[n] \cdot z^{-n}$$

where z is a complex variable and n is a discretetime index. The Z transform is a powerful tool in digital signal processing, as it allows us to analyze and manipulate signals in the frequency domain. The inverse Z transform can also be used to recover the original signal x[n] from its Z transform X(z).