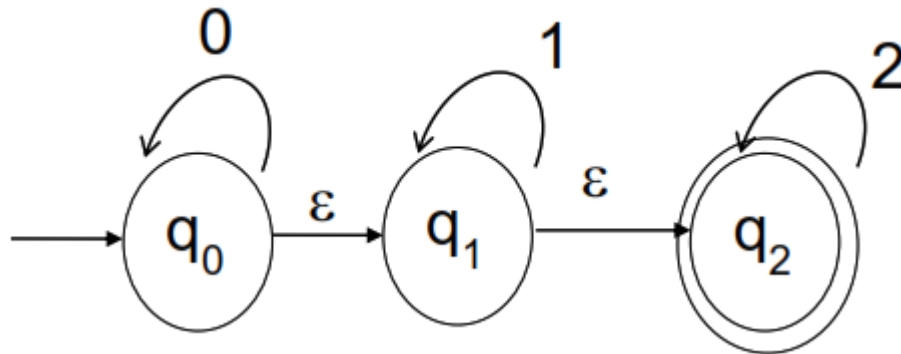


Tugas OPK

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1. Konversi ke DFA dari NDFA e-move



a. Tabel Transisi

δ	0	1	2
q0	q0	{}	{}
q1	{}	q1	{}
q2	{}	{}	q2

b. Closure tiap state

$$\text{e-closure}(q_0) = [q_0, q_1, q_2]$$

$$\text{e-closure}(q_1) = [q_1, q_2]$$

$$\text{e-closure}(q_2) = [q_2]$$

c. Transisi untuk semua pasangan

- $$\begin{aligned} \delta'(q_0, 0) &= \text{e_closure}(\delta(\text{e_closure}(q_0, 0))) \\ &= \text{e_closure}(\delta(\{q_0, q_1, q_2\}, 0)) = \text{e_closure}((q_0, 0) \cup (q_1, 0) \cup (q_2, 0)) \\ &= \text{e_closure}(q_0 \cup \{\} \cup \{\}) = q_0 \end{aligned}$$

$$\text{sehingga } \text{e_closure}(q_0) = \{ \mathbf{q_0, q_1, q_2} \}$$

- $$\begin{aligned} \delta'(q_0, 1) &= \text{e_closure}(\delta(\text{e_closure}(q_0, 1))) \\ &= \text{e_closure}(\delta(\{q_0, q_1, q_2\}, 1)) = \text{e_closure}((q_0, 1) \cup (q_1, 1) \cup (q_2, 1)) \\ &= \text{e_closure}(\{\} \cup q_1 \cup \{\}) = q_1 \end{aligned}$$

$$\text{sehingga } \text{e_closure}(q_1) = \{ \mathbf{q_1, q_2} \}$$

- $$\begin{aligned} \delta'(q_0, 2) &= \text{e_closure}(\delta(\text{e_closure}(q_0, 2))) \\ &= \text{e_closure}(\delta(\{q_0, q_1, q_2\}, 2)) = \text{e_closure}((q_0, 2) \cup (q_1, 2) \cup (q_2, 2)) \\ &= \text{e_closure}(\{\} \cup \{\} \cup q_2) = q_2 \end{aligned}$$

sehingga $\epsilon_closure(q2) = \{ \mathbf{q2} \}$

- $\delta'(q1,0) = \epsilon_closure(\delta(\epsilon_closure(q1,0)))$
 $= \epsilon_closure(\delta(\{q1,q2\},0)) = \epsilon_closure((q1,0) \cup (q2,0))$
 $= \epsilon_closure(\{\} \cup \{\}) = \{\}$

sehingga $\epsilon_closure(\{\}) = \{\}$

- $\delta'(q1,1) = \epsilon_closure(\delta(\epsilon_closure(q1,1)))$
 $= \epsilon_closure(\delta(\{q1,q2\},1)) = \epsilon_closure((q1,1) \cup (q2,1))$
 $= \epsilon_closure(q1 \cup \{\}) = q1$

sehingga $\epsilon_closure(q1) = \{ \mathbf{q1,q2} \}$

- $\delta'(q1,2) = \epsilon_closure(\delta(\epsilon_closure(q1,2)))$
 $= \epsilon_closure(\delta(\{q1,q2\},2)) = \epsilon_closure((q1,2) \cup (q2,2))$
 $= \epsilon_closure(\{\} \cup q2) = q2$

sehingga $\epsilon_closure(q2) = \{ \mathbf{q2} \}$

- $\delta'(q2,0) = \epsilon_closure(\delta(\epsilon_closure(q2,0)))$
 $= \epsilon_closure(\delta(\{q2\},0)) = \epsilon_closure((q2,0))$
 $= \epsilon_closure(\{\}) = \{\}$

sehingga $\epsilon_closure(\{\}) = \{\}$

- $\delta'(q2,1) = \epsilon_closure(\delta(\epsilon_closure(q2,1)))$
 $= \epsilon_closure(\delta(\{q2\},1)) = \epsilon_closure((q2,1))$
 $= \epsilon_closure(\{\}) = \{\}$

sehingga $\epsilon_closure(\{\}) = \{\}$

- $\delta'(q2,2) = \epsilon_closure(\delta(\epsilon_closure(q2,2)))$
 $= \epsilon_closure(\delta(\{q2\},2)) = \epsilon_closure((q2,2))$
 $= \epsilon_closure(q2) = q2$

sehingga $\epsilon_closure(q2) = \{ \mathbf{q2} \}$

d. Tabel Transisi baru

δ	0	1	2
q0	q0,q1,q2	q1,q2	q2
q1	{}	q1,q2	q2
q2	{}	{}	q2

e. Final State baru

Final state awal = q2

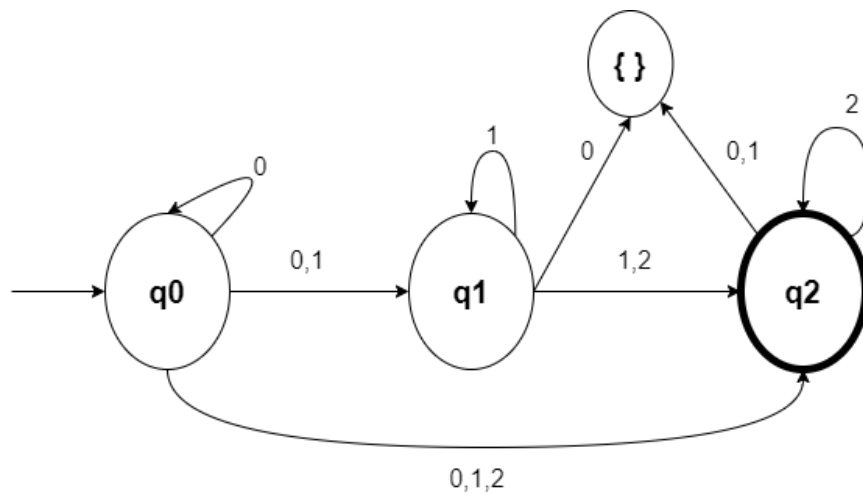
$\epsilon_{\text{closure}}(q2) = \{ \mathbf{q2} \}$ 0 dan $\{ \mathbf{q2} \}$ 1 dan $\{ \mathbf{q2} \}$ 2

(q2,0) dan (q2,1) dan (q2,2)

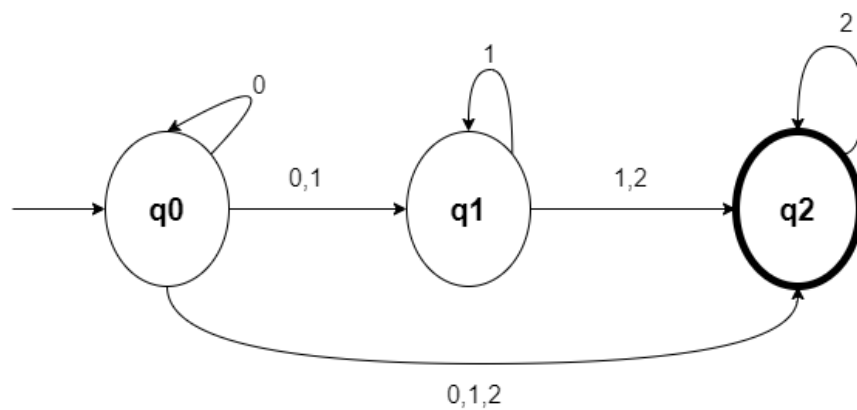
{ } dan { } dan q2 = q2

F nya berarti q2 dan q2 = q2

f. Gambar ndfa tanpa e-move nya



Tanpa himp kosong



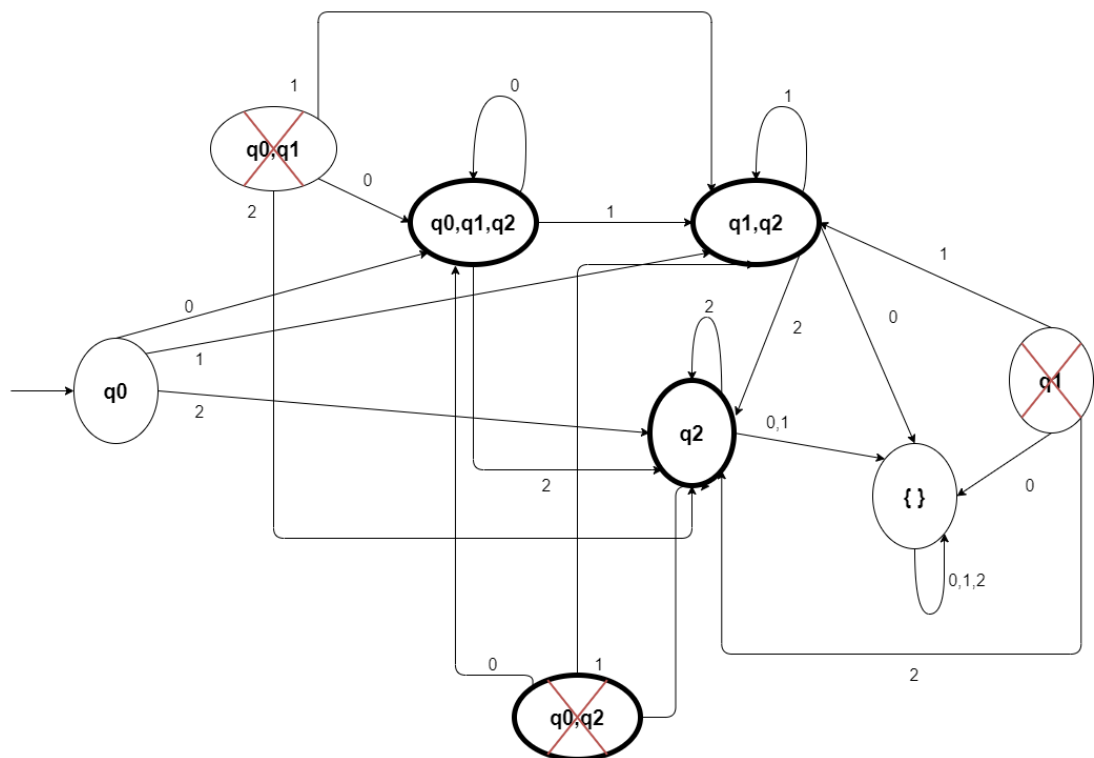
g. Tabel transisi untuk DFA

δ	0	1	2
{}	{}	{}	{}
q0	q0,q1,q2	q1,q2	q2
q1	{}	q1,q2	q2
q2	{}	{}	q2
q0,q1	q0,q1,q2	q1,q2	q2
q0,q2	q0,q1,q2	q1,q2	q2
q1,q2	{}	q1,q2	q2
q0,q1,q2	q0,q1,q2	q1,q2	q2

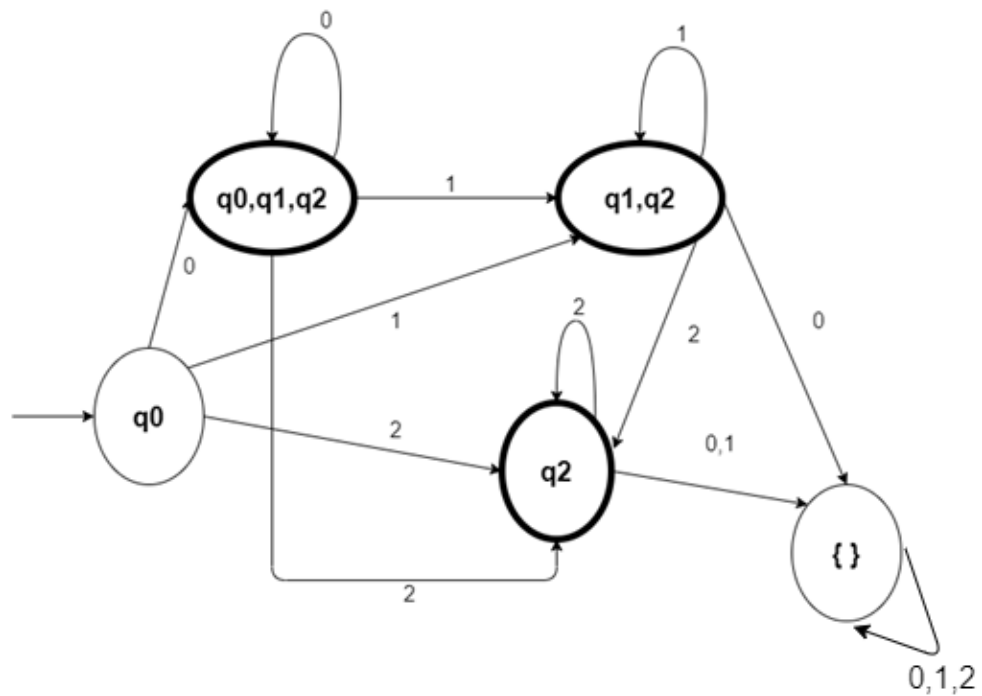
Start state = q0

State Akhir = q2 yaitu {q2},{q0,q1,q2},{ q1,q2}

h. Gambar DFA nya



Dibuang yang tidak perlu menjadi



2. Penyederhanaan CFG

$S \rightarrow ABCd$

$A \rightarrow B \mid CD \mid D \mid \varepsilon$

$B \rightarrow abc \mid \varepsilon$

$C \rightarrow cd \mid \varepsilon$

$D \rightarrow e \mid \varepsilon$

a. $S \rightarrow ABCd$ A nya direplace dengan B jadi **BBCd**

b. **BBCd** (B dan C direplace ε) nya jadi **d**

c. $S \rightarrow ABCd$ A nya direplace dengan ε jadi **BCd**

d. **BCd** (B direplace dengan ε) jadi **Cd**

e. $S \rightarrow ABCd$ B nya direplace dengan ε jadi **ACd**

f. **ACd** (C direplace dengan ε) jadi **Ad**

g. $S \rightarrow ABCd$ C nya direplace dengan ε jadi **ABd**

Hasil sementara

$S \rightarrow ABCd \mid BCd \mid ACd \mid ABd \mid Cd \mid Ad \mid d$

$A \rightarrow B \mid CD \mid D$

$B \rightarrow abc$

$C \rightarrow cd$

$D \rightarrow e$

h. Yang satu symbol langsung diganti

$S \rightarrow ABCd \mid BCd \mid ACd \mid ABd \mid Cd \mid Ad \mid d$

$A \rightarrow abc \mid CD \mid e$

$B \rightarrow abc$

$C \rightarrow cd$

$D \rightarrow e$

i. Selesai dengan hasil akhir

$S \rightarrow ABCd \mid BCd \mid ACd \mid ABd \mid Cd \mid Ad \mid d$

$A \rightarrow abc \mid CD \mid e$

$B \rightarrow abc$

$C \rightarrow cd$

$D \rightarrow e$