

# Decision Trees and Random Forests

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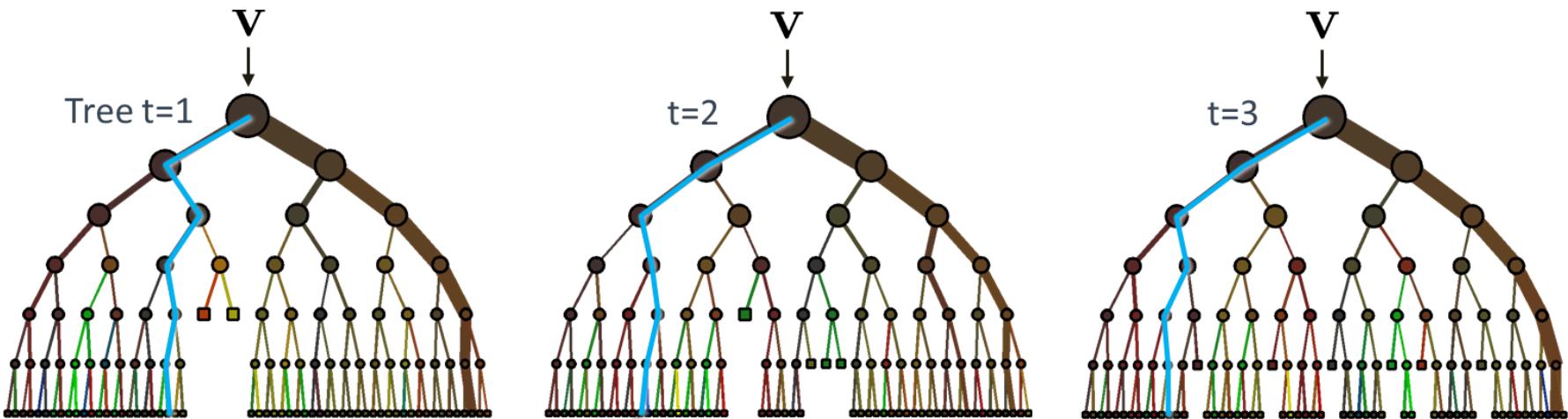


# NOT ABOUT WALKING IN A FOREST





# IS ALL ABOUT





# Overview

- Historical Perspective
- Decision Tree
- Random Forest
- Computational Complexity
- Variable Importance



# Historical Perspective

## Decision Trees

- L. Breiman, J. Friedman, C. J. Stone, and R. A. Olshen, *Classification and Regression Trees*. Chapman and Hall/CRC (SIAM), **1984**.
- J. R. Quinlan, *C4.5: Programs for Machine Learning*. **1993**.

## Random Forests

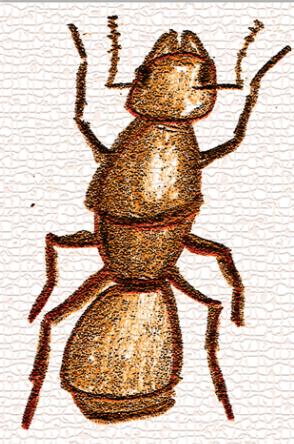
- Y. Amit and D. Geman., "Shape quantization and recognition with randomized trees," *Neural Computation*, vol. 9, pp. 1545–1588, **1997**.
- T. K. Ho, "The random subspace method for constructing decision forests," *IEEE T-PAMI*, vol. 20, no. 8, pp. 832–844, **1998**.
- L. Breiman, "Random forests," *Machine Learning*, vol. 45, no. 1, pp. 5–32, **2001**.



# DECISION TREE



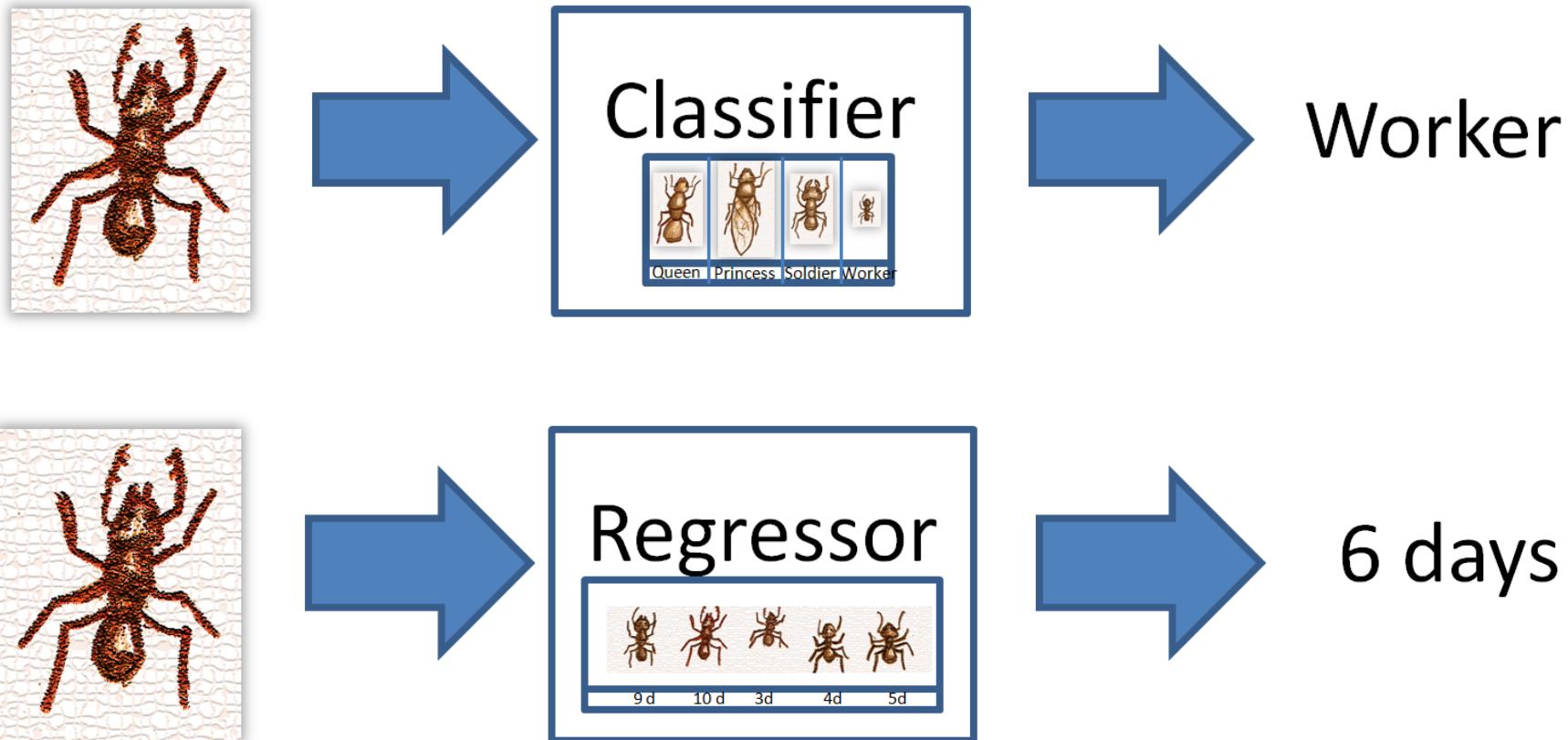
# Problem Statement

			
Queen	Princess	Soldier	Worker

*Formica rufa* (Red wood ant)

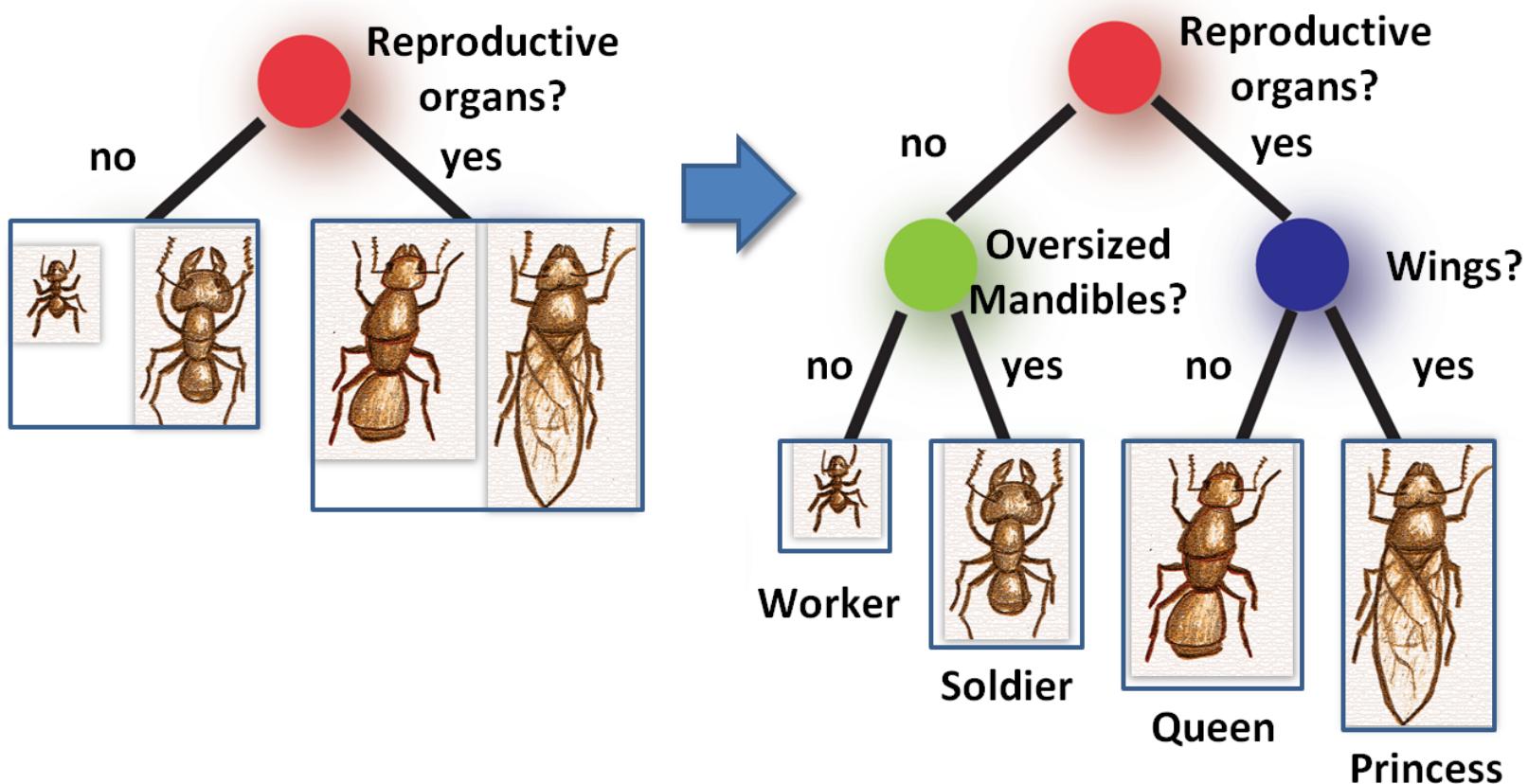


# Classification vs. Regression

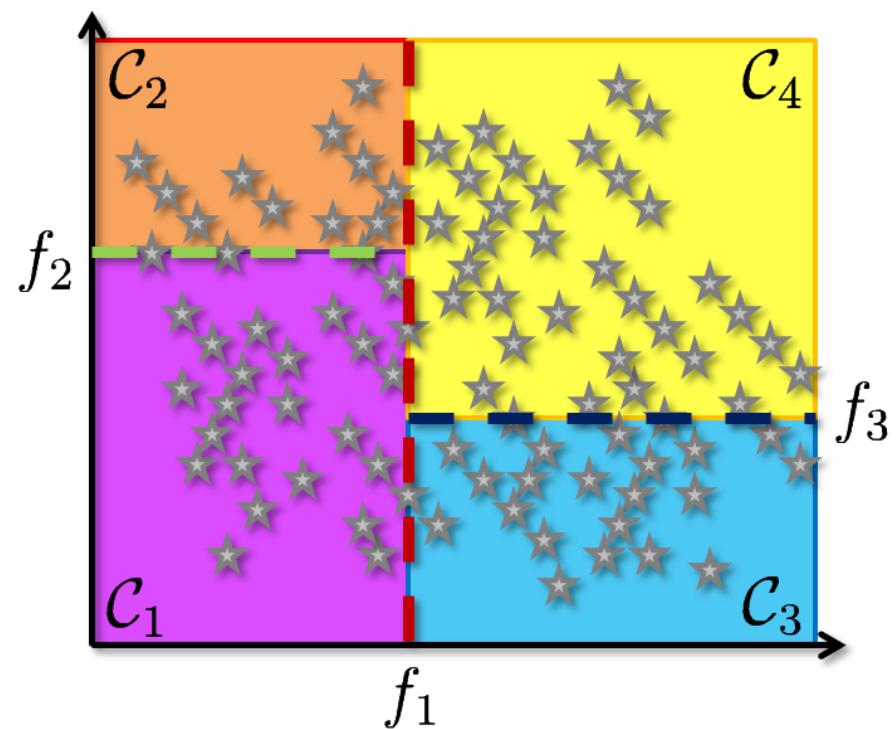
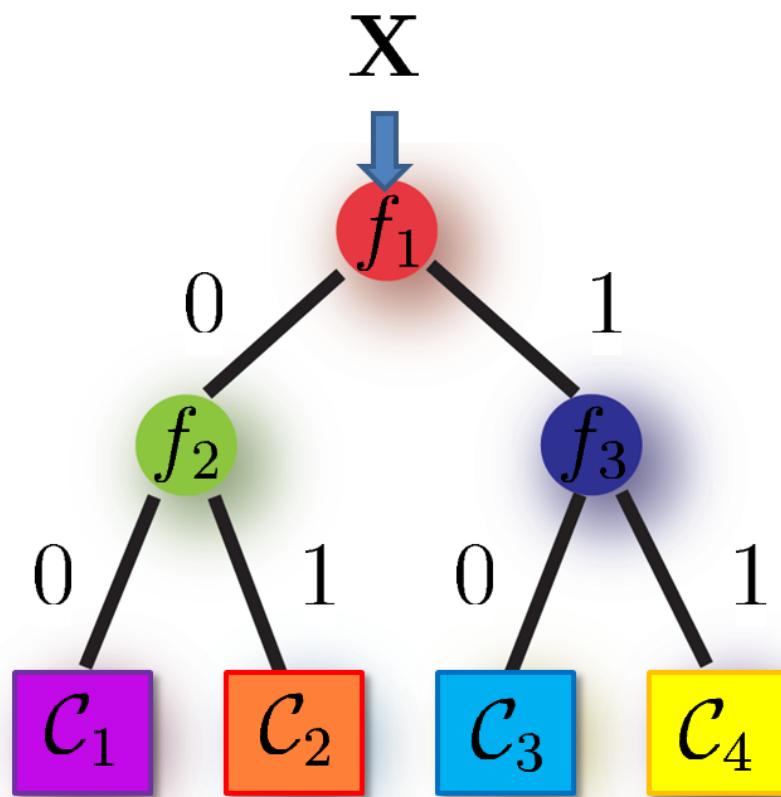




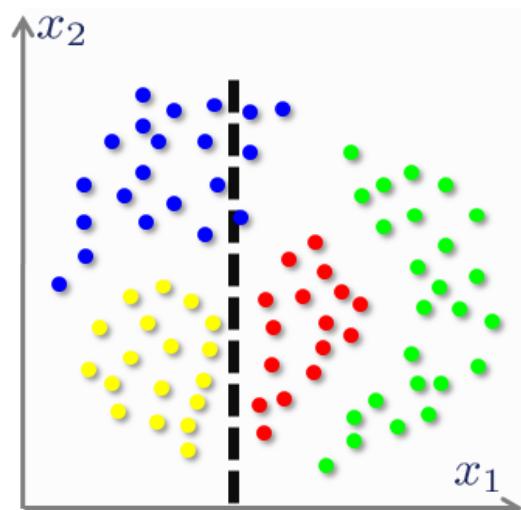
# Decision Tree



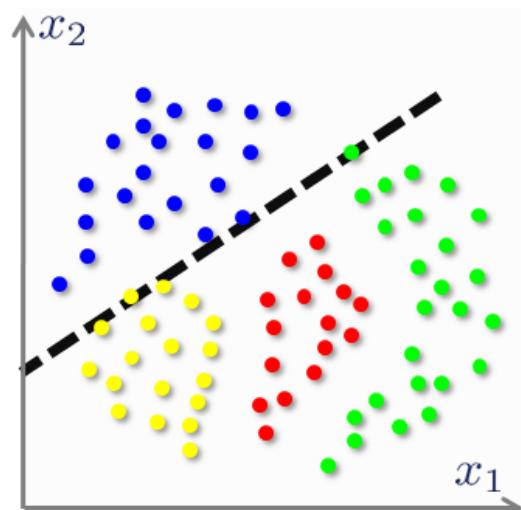
# Forming a Decision Tree



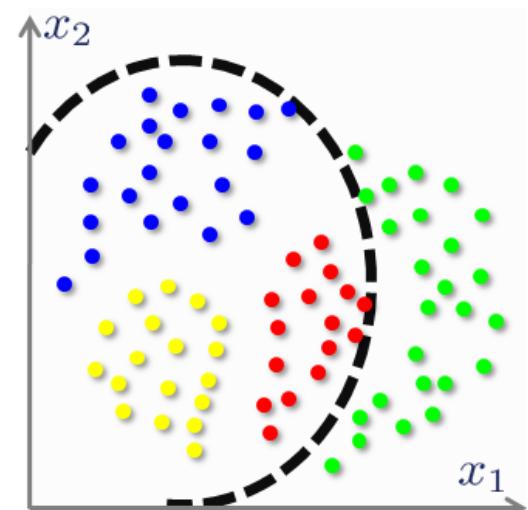
# Step 1: Split Function at Node



(a)  
Axis aligned split

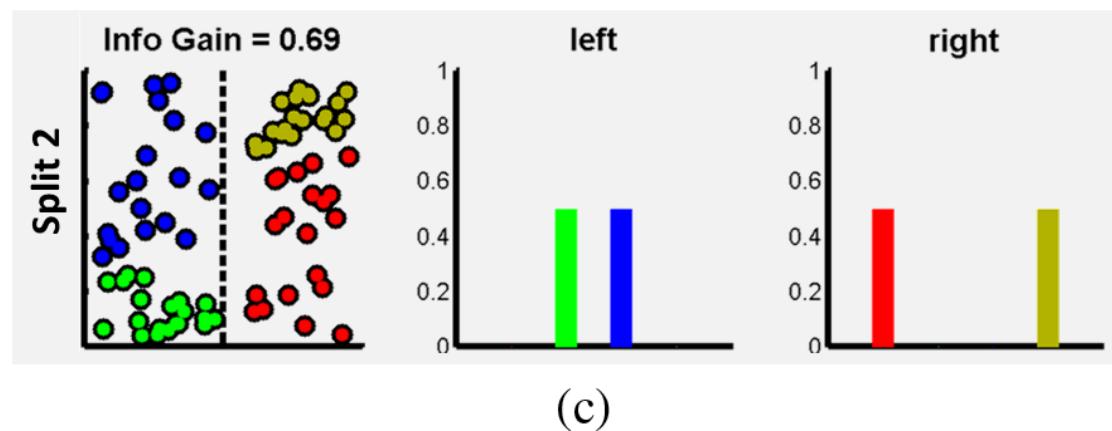
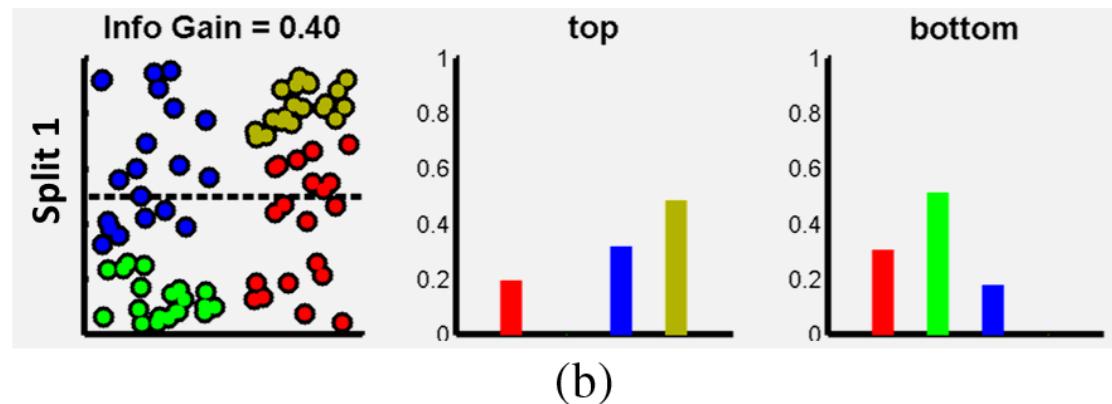
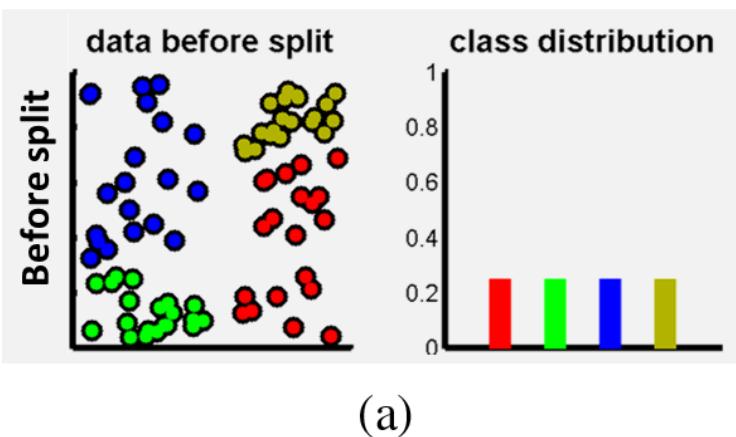


(b)  
Oblique split

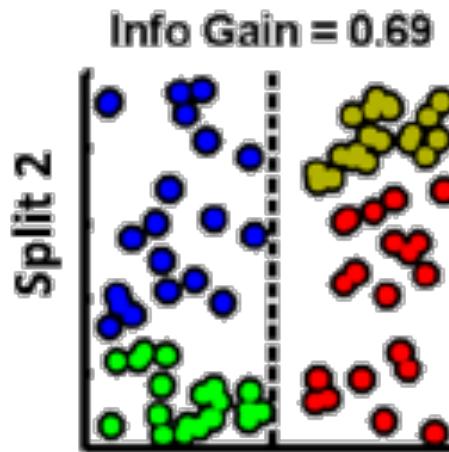


(c)  
Polynomial split

# Step 2: Assessing Purity of Split

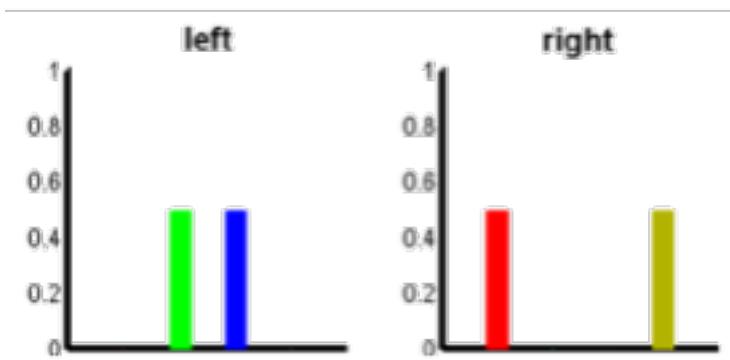


# Cost function for Split Purity



Entropy of class distribution

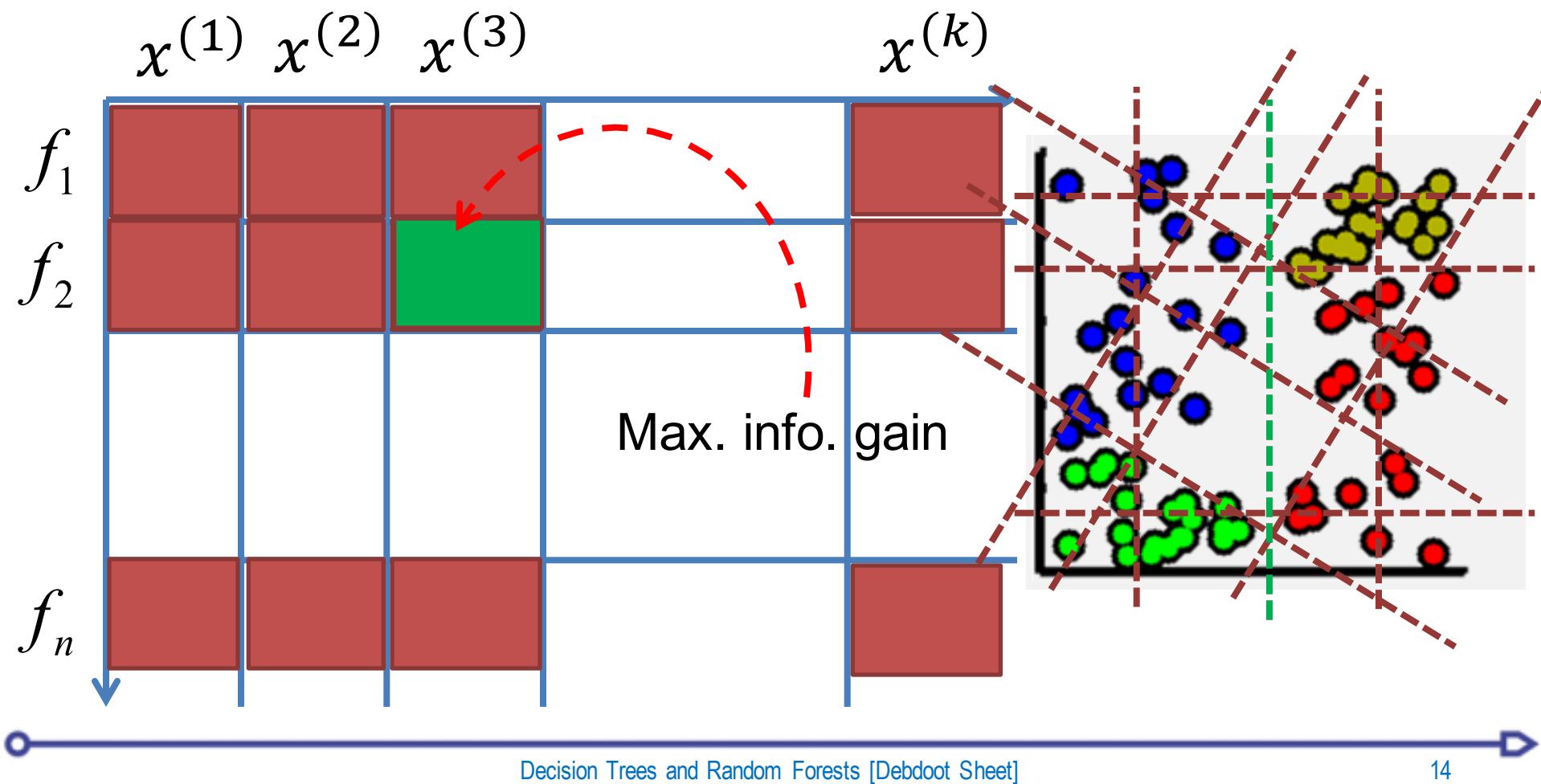
$$H(S) = - \sum_{c \in \mathcal{C}} p(c) \log(p(c)),$$



Information Gain

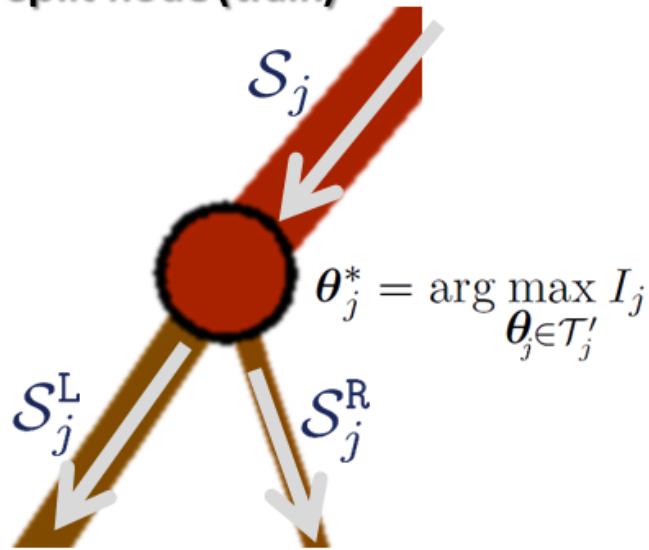
$$I = H(S) - \sum_{i \in \{L,R\}} \frac{|S^i|}{|S|} H(S^i).$$

# Step 3: Selecting Optimum Split

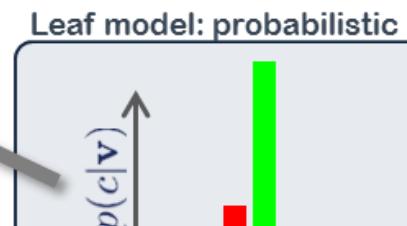
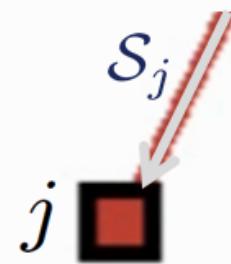
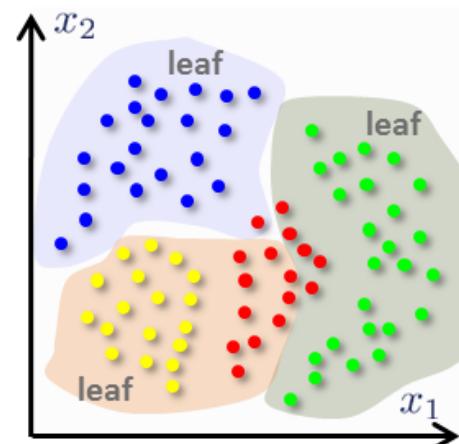


# Step 4: Stopping Criteria

## Split node (train)

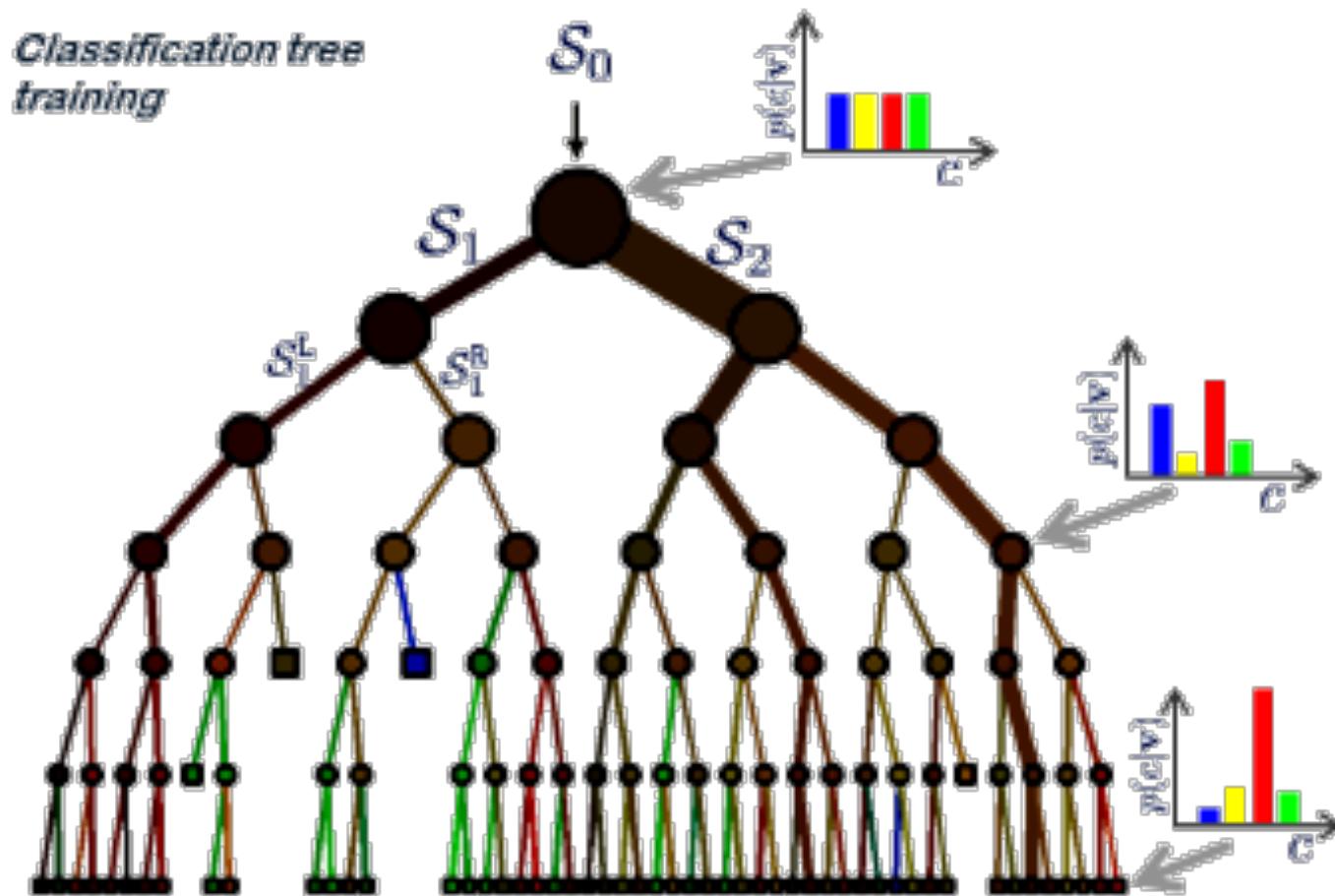


## Leaf node



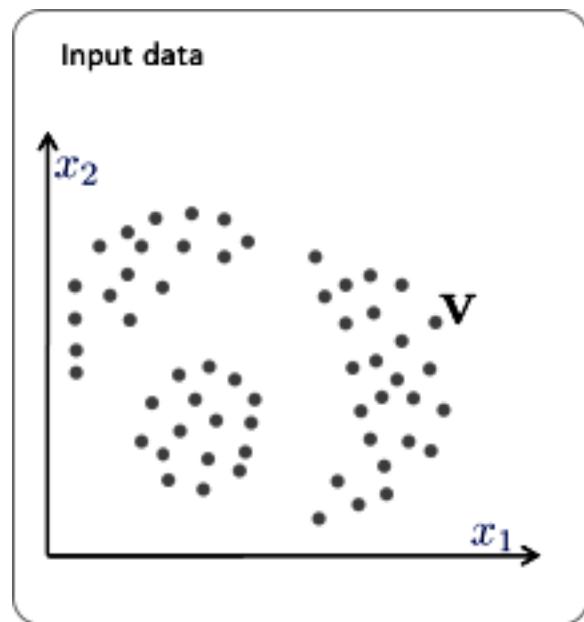


# Step 5: Leaf Prediction Model

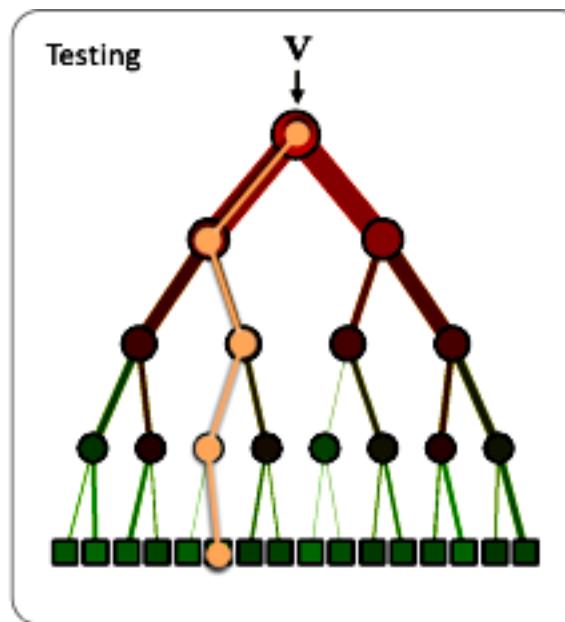




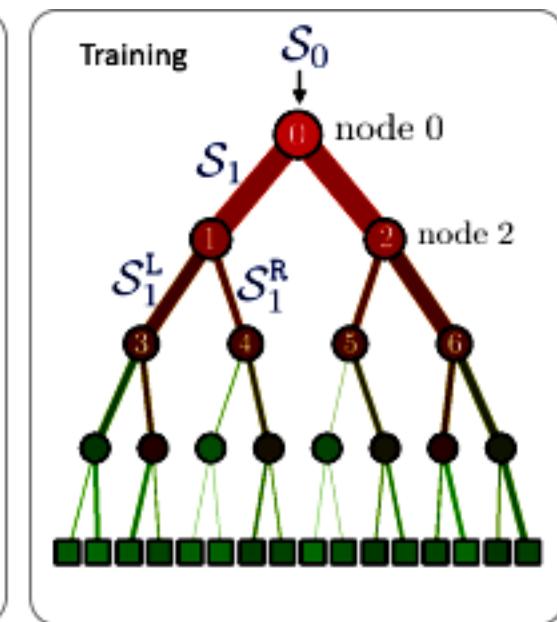
# Deploying a Decision Tree



(a)



(b)



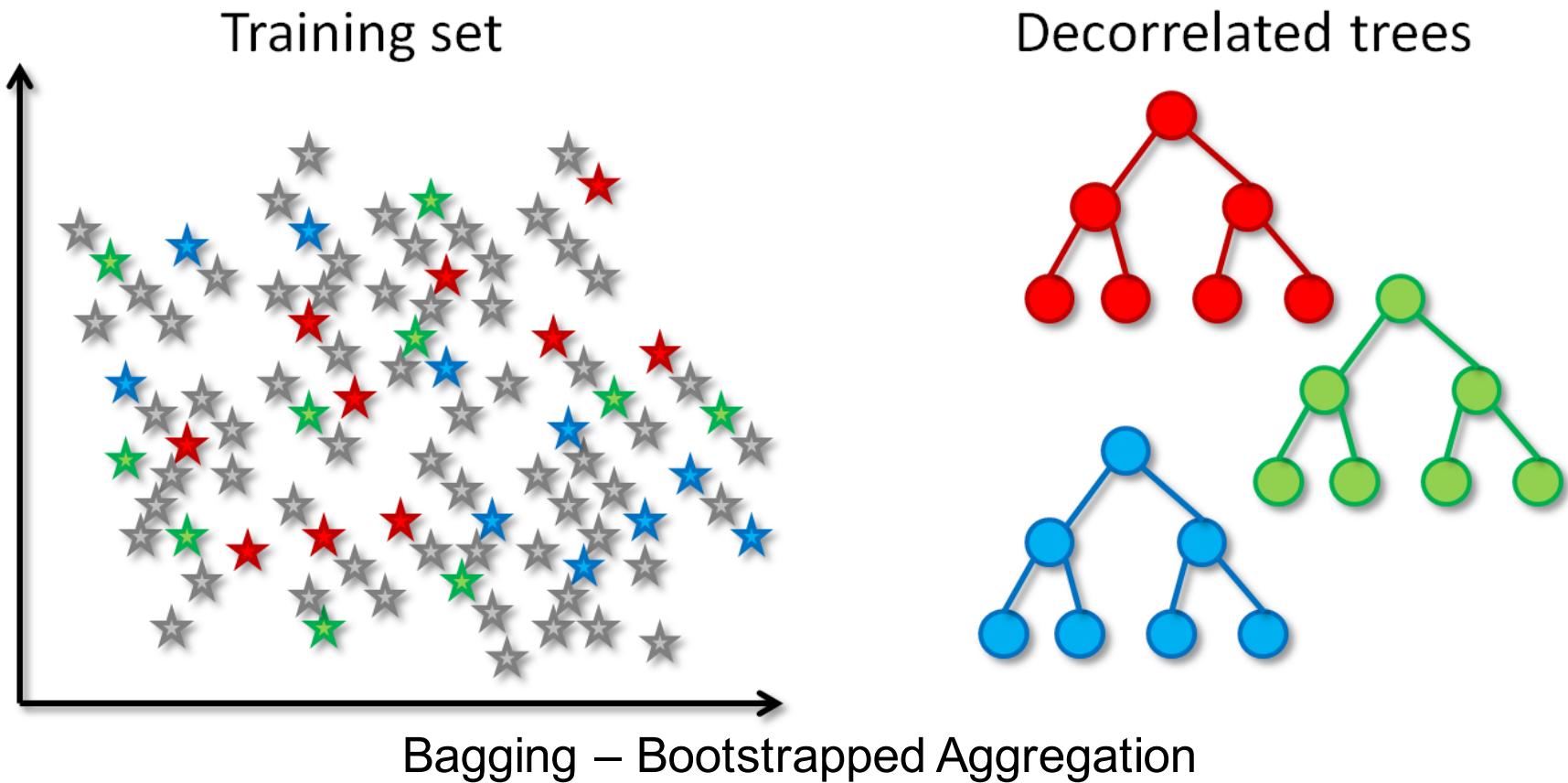
(c)



# RANDOM FOREST

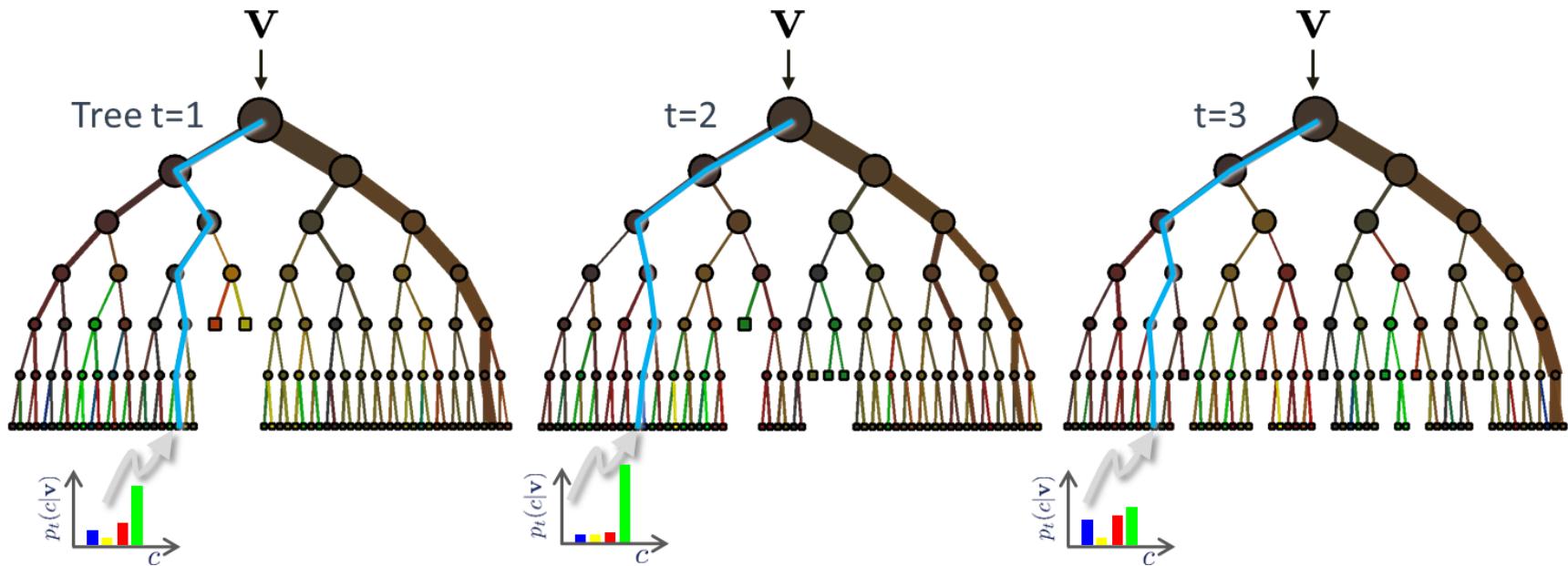


# Growing Multiple Trees in a Forest





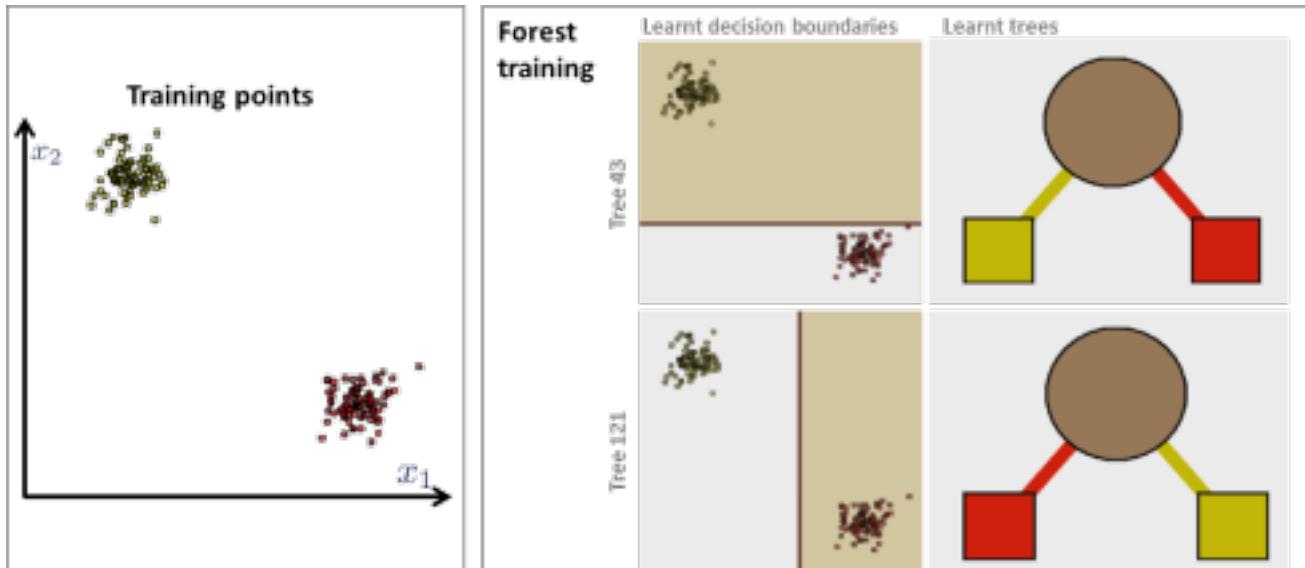
# Ensemble Prediction Model



$$p(c|v) = \frac{1}{T} \sum_t p_t(c|v)$$

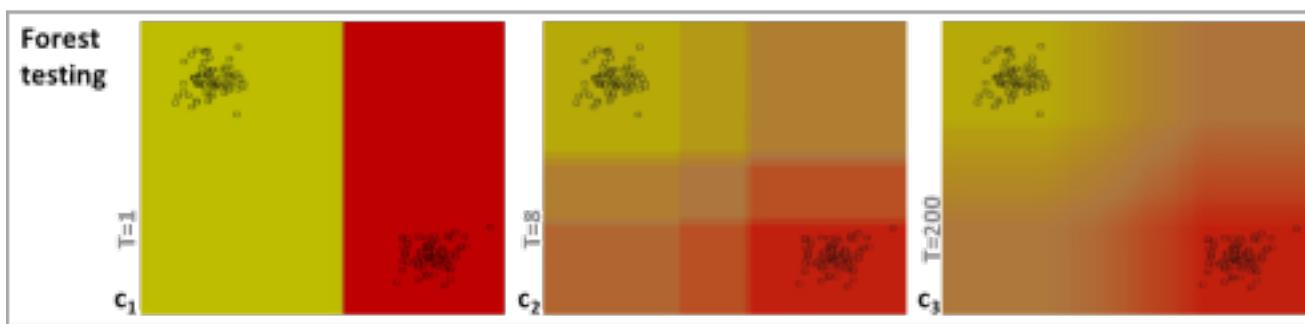


# What do we gain by using a Forest?



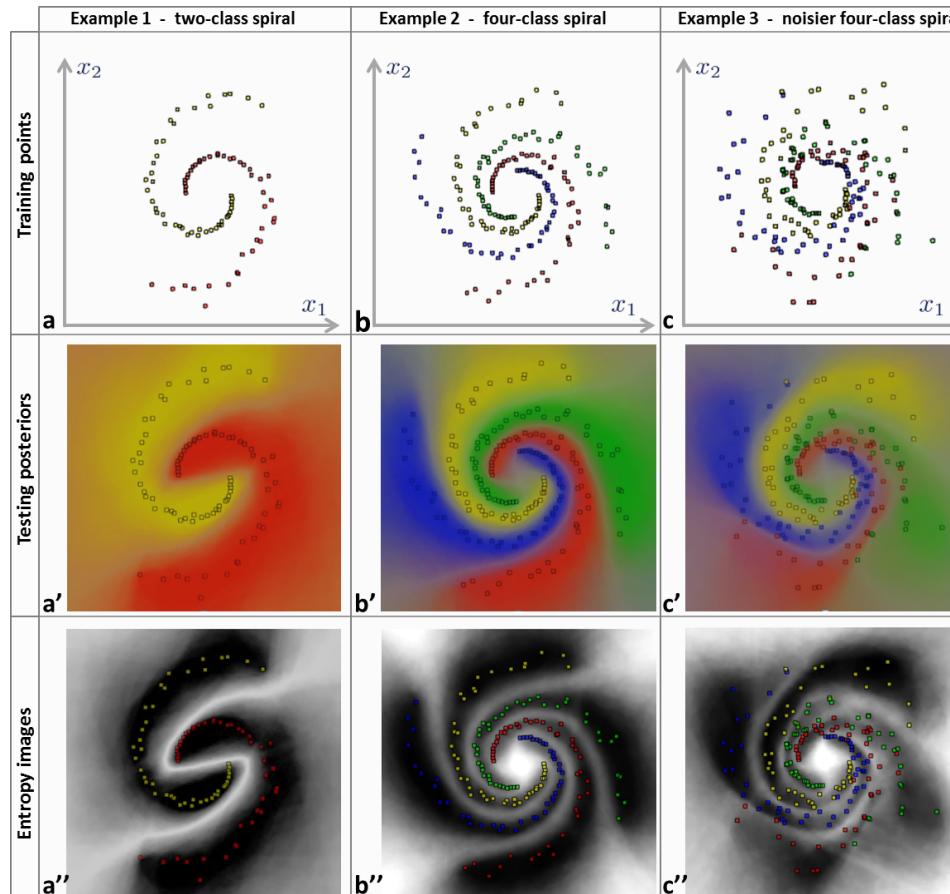
(a)

(b)

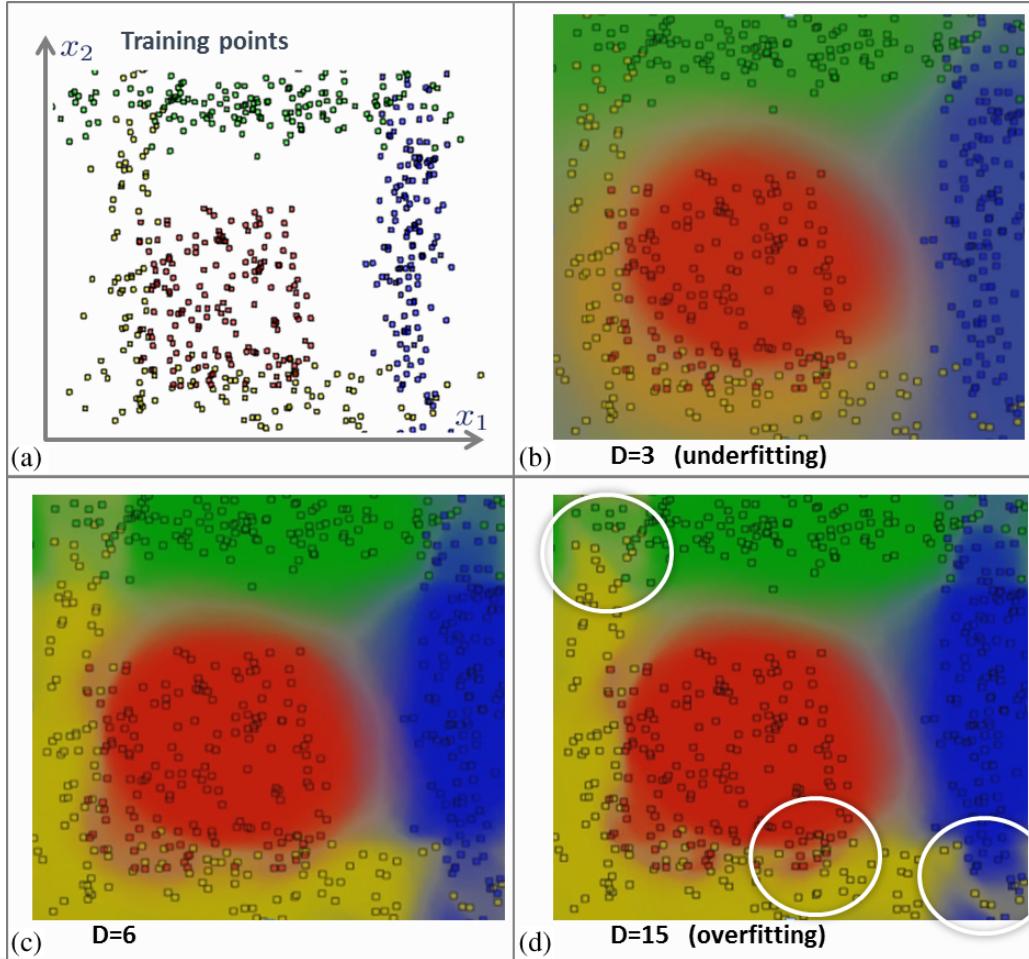




# Noise Resilience and Topology Independence

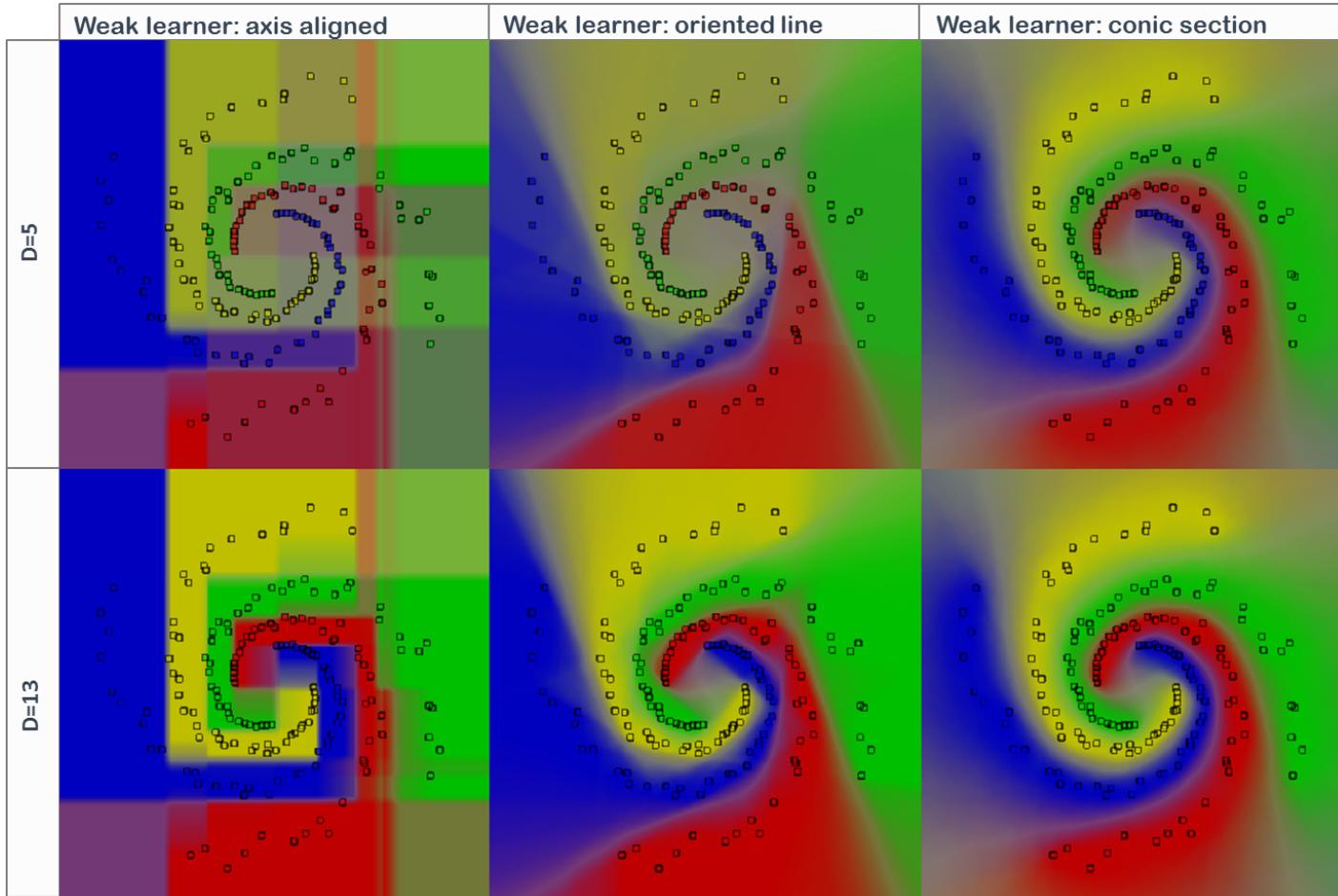


# Effect of Tree Depth

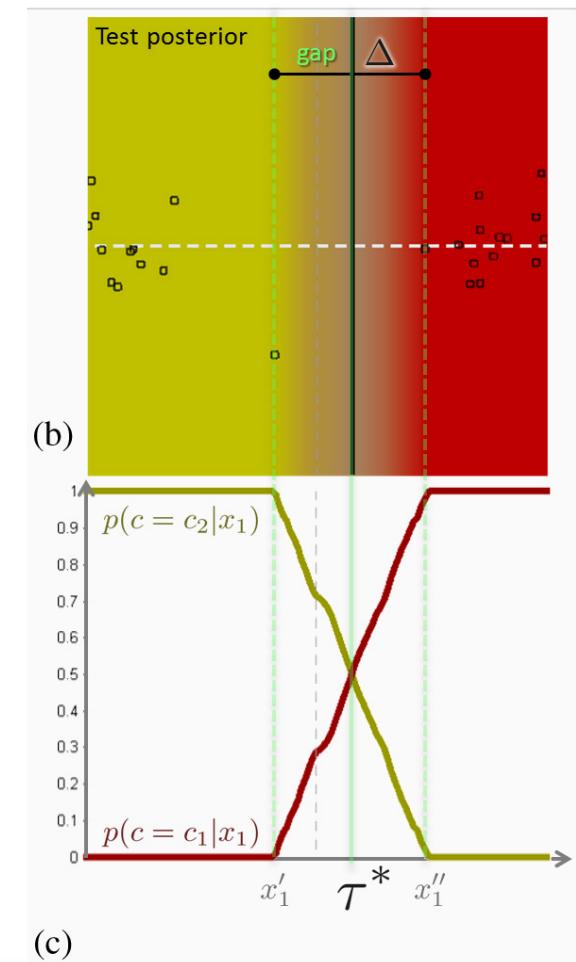
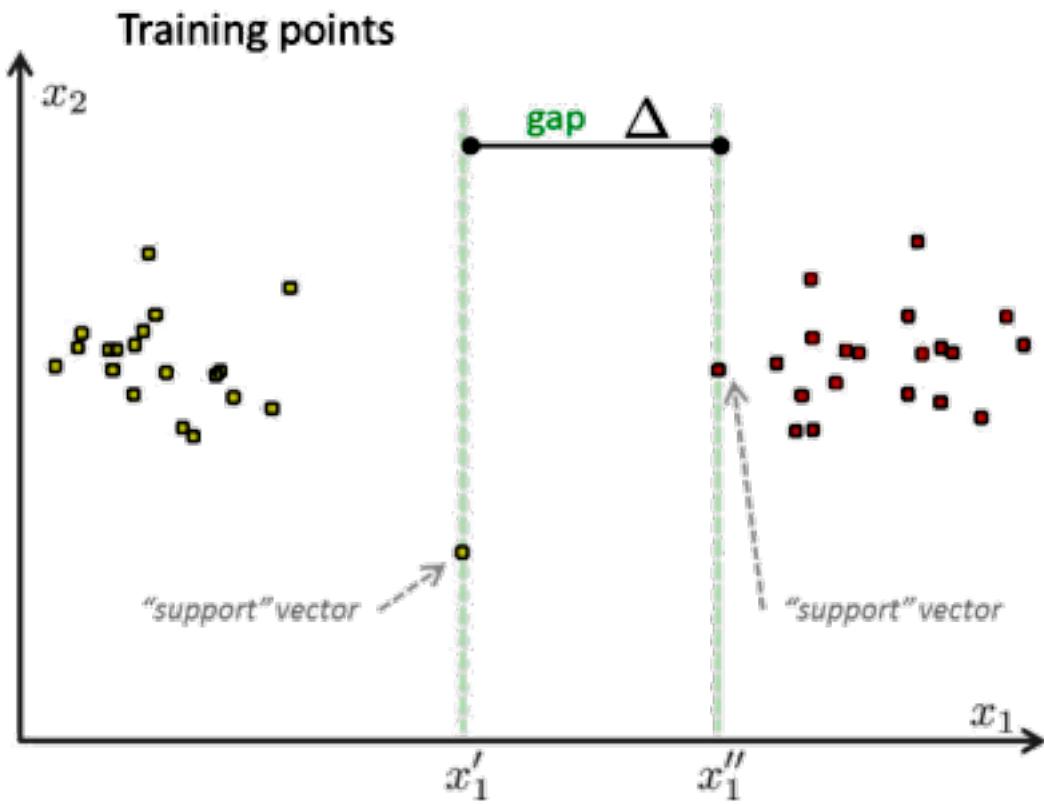




# Effect of Split Function

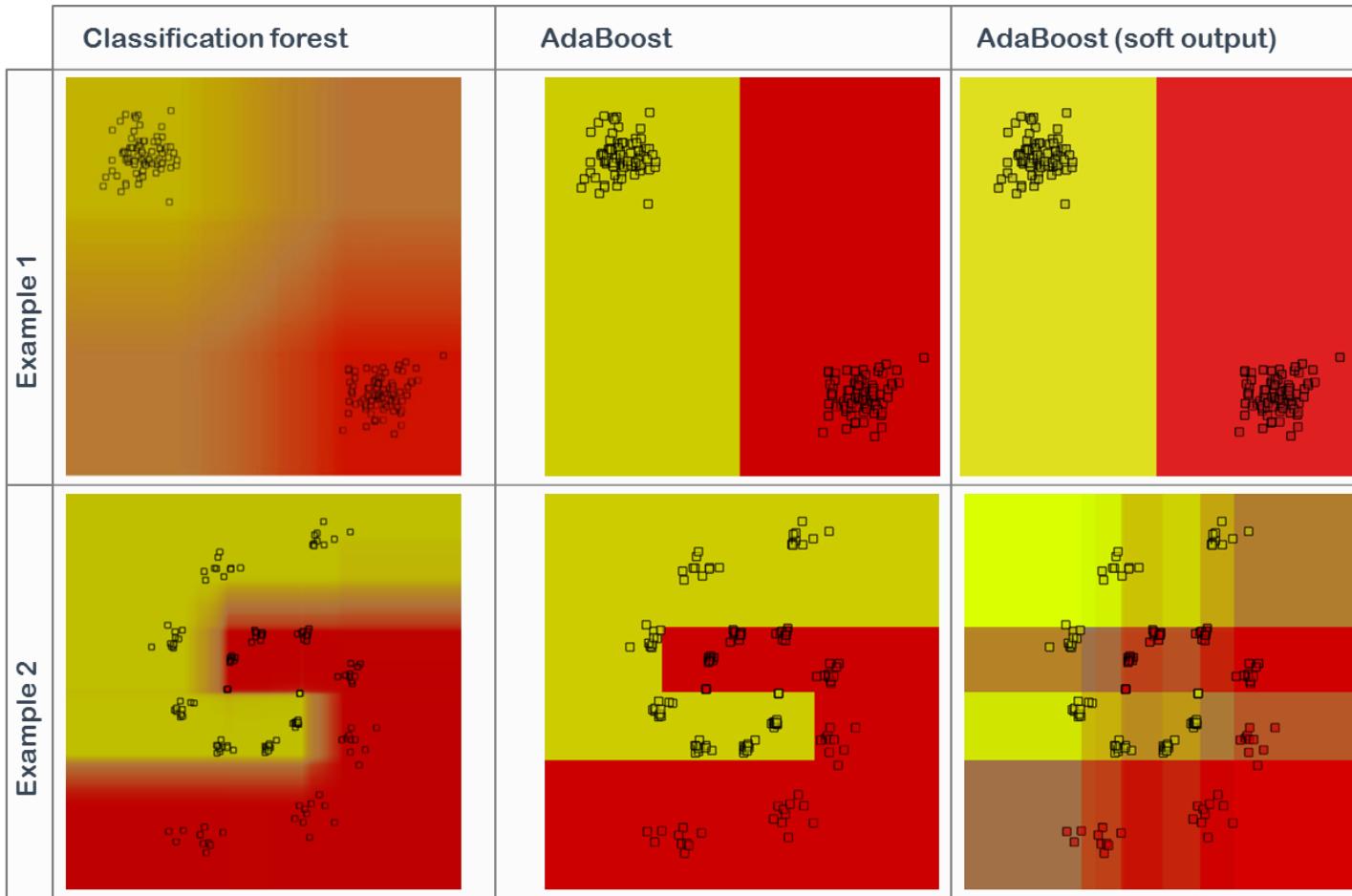


# Classification Margin



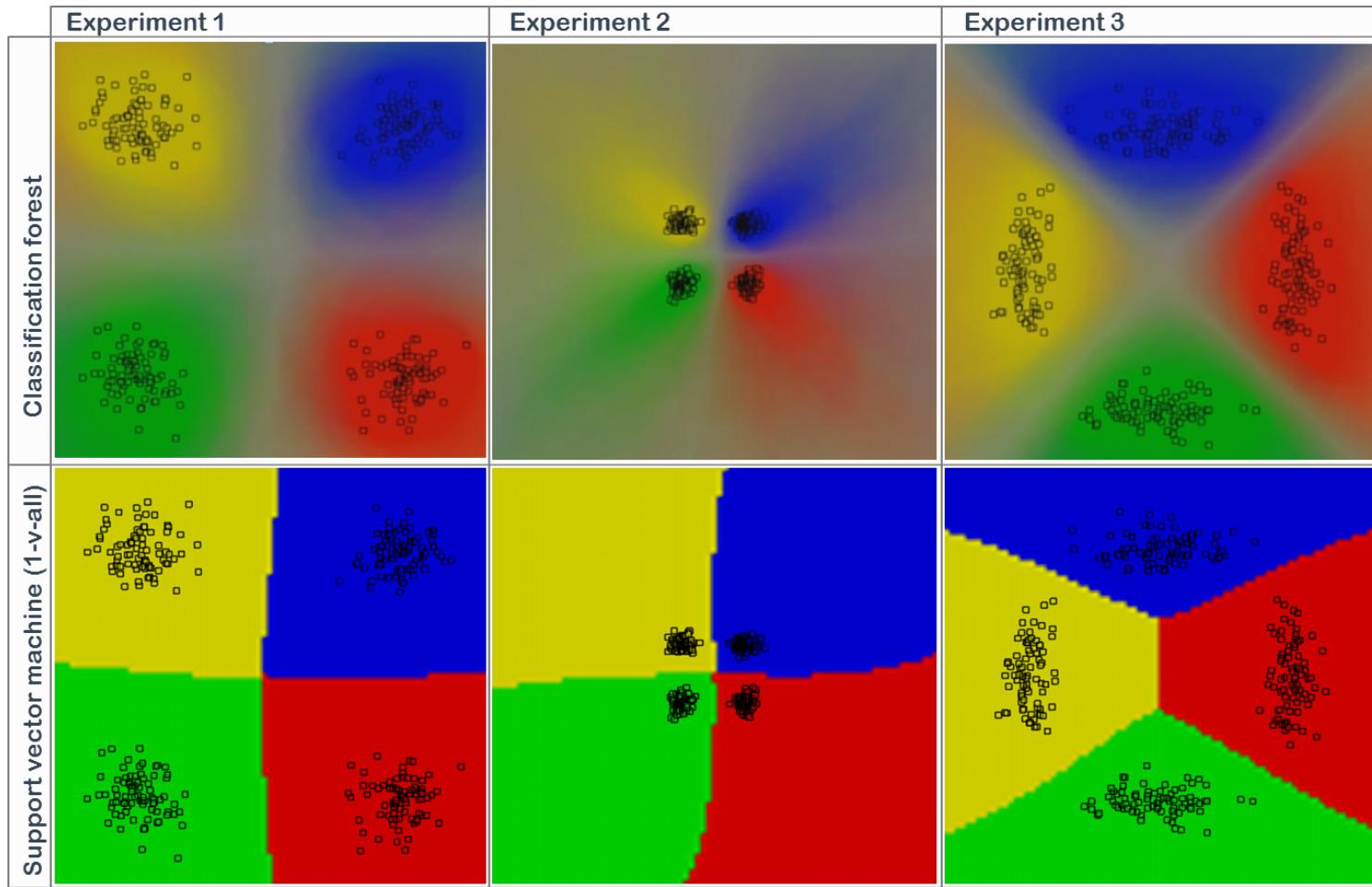


# Random Forest vs. AdaBoost



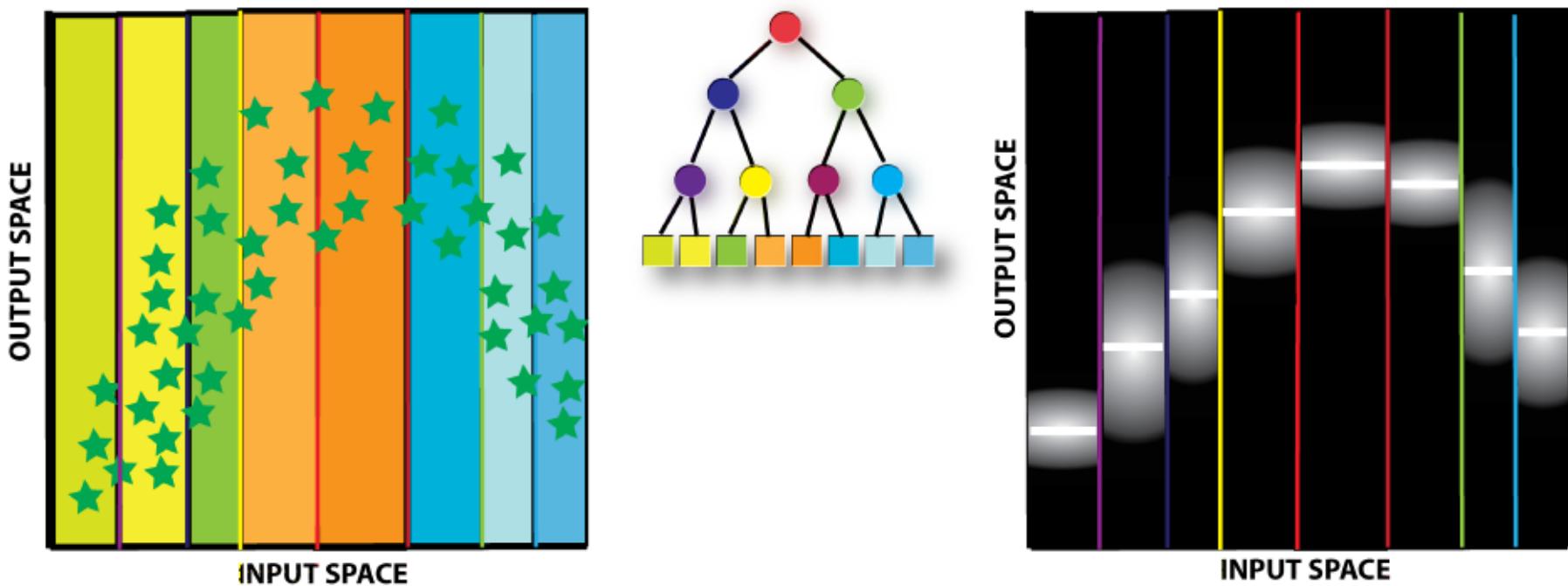


# Random Forest vs. SVM

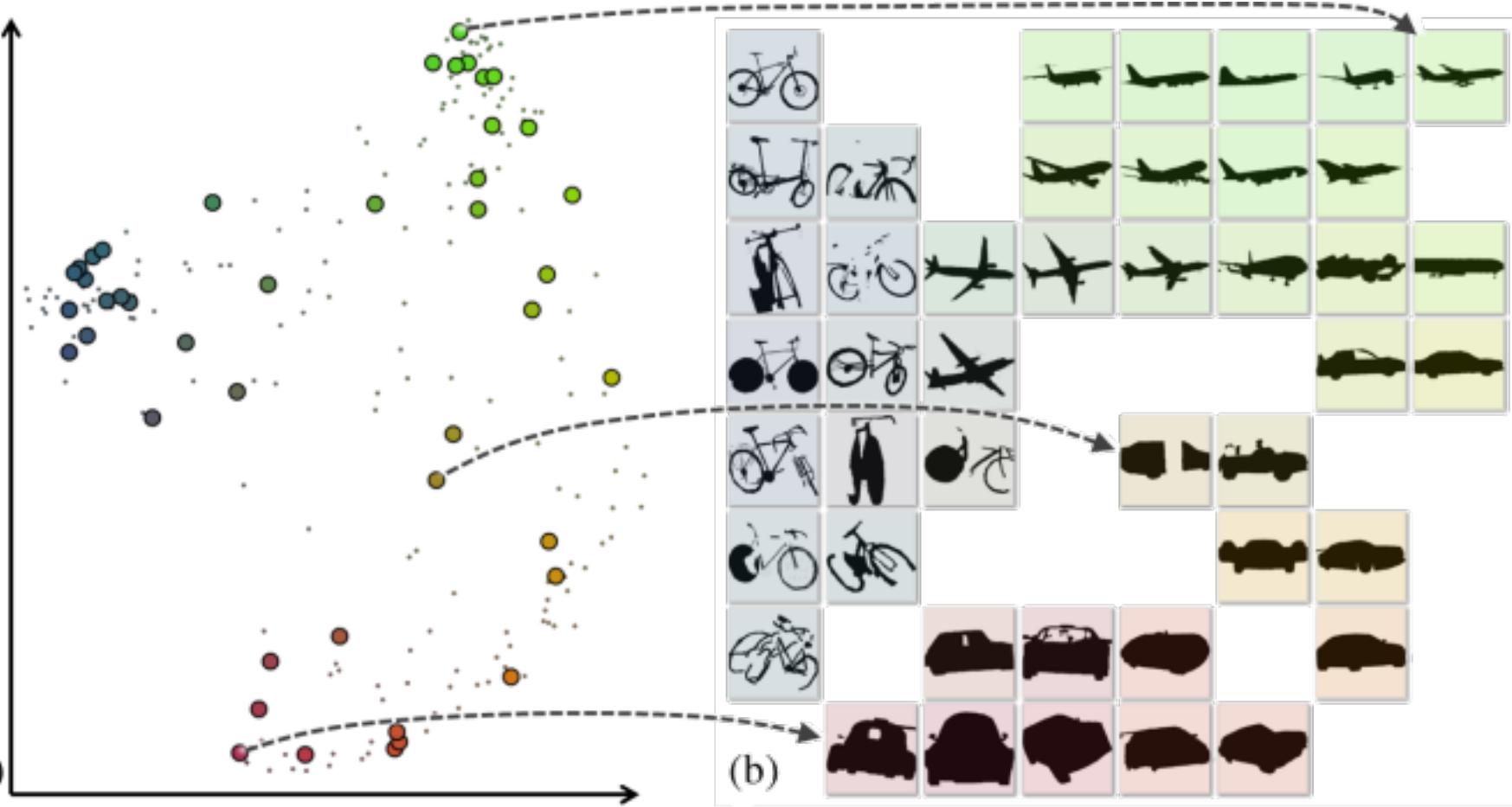




# Regression Forest

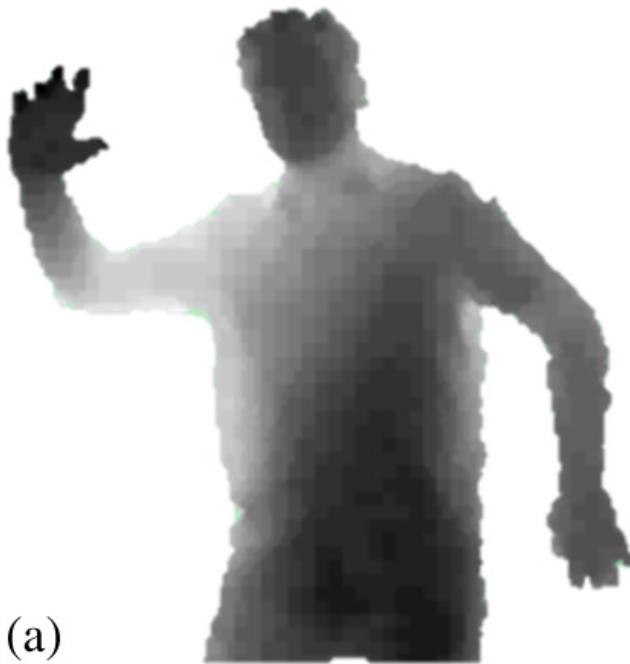


# Manifold Forest



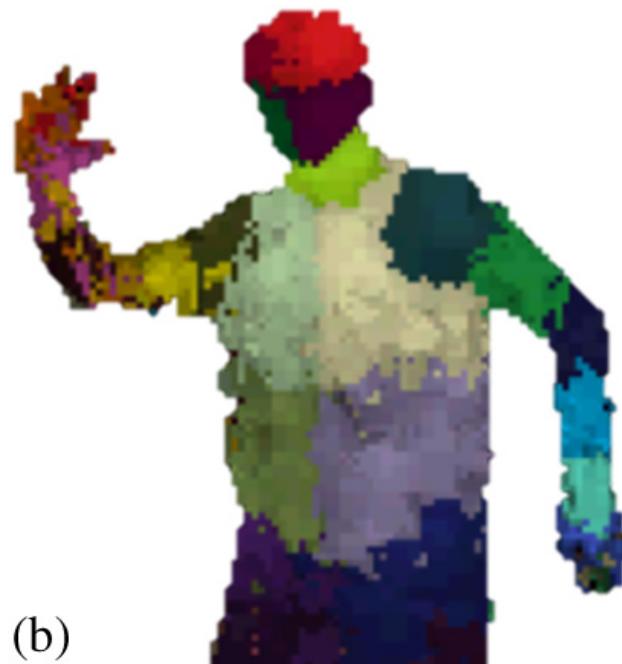


# Gaming – Kinect for Xbox 360



(a)

Depth map



(b)

Body part classification

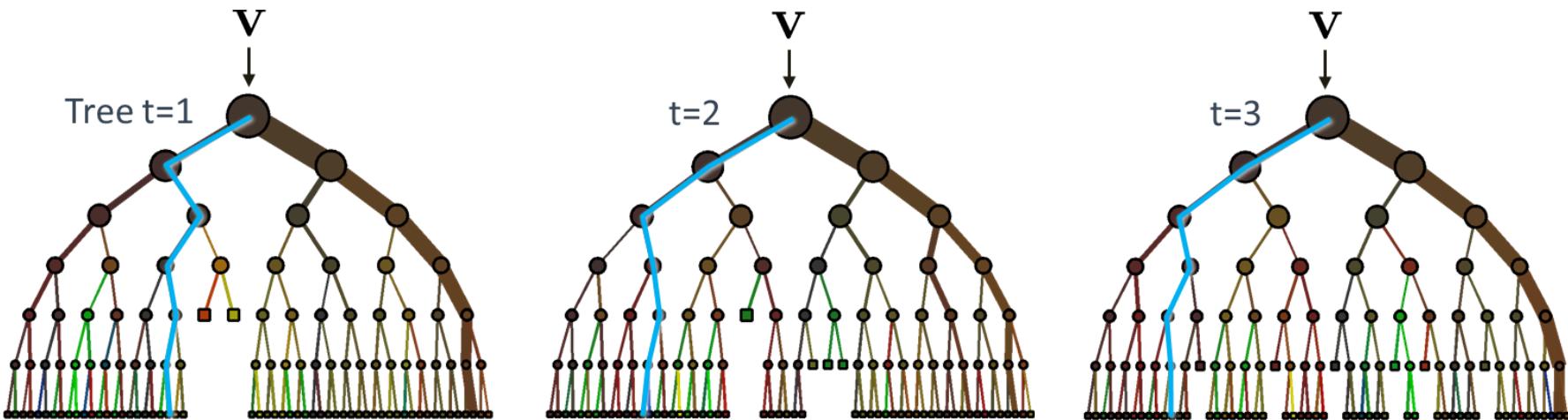
J. Shotton, A. Fitzgibbon, M. Cook, T. Sharp, M. Finocchio, R. Moore, A. Kipman, and A. Blake,  
“Real-time human pose recognition in parts from a single depth image,” in *Proc. CVPR*, 2011.



# **ENGINEERING DESIGN PERSPECTIVE**



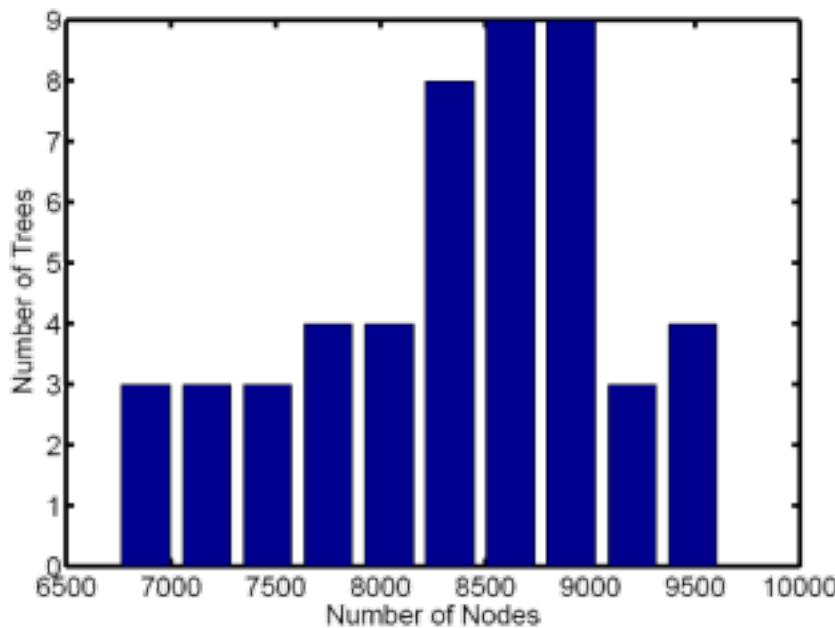
# Understanding Computations



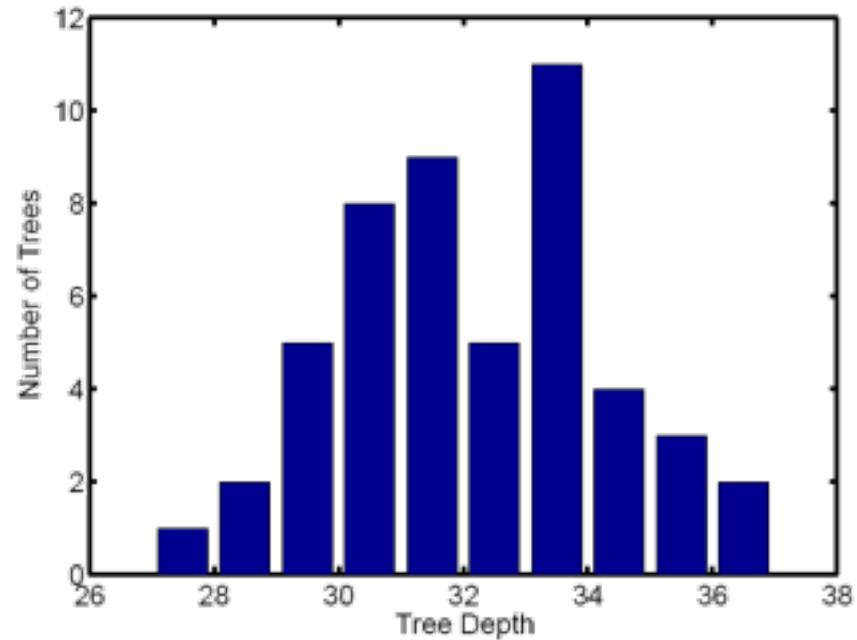


# Computational Complexity

**Training Complexity**

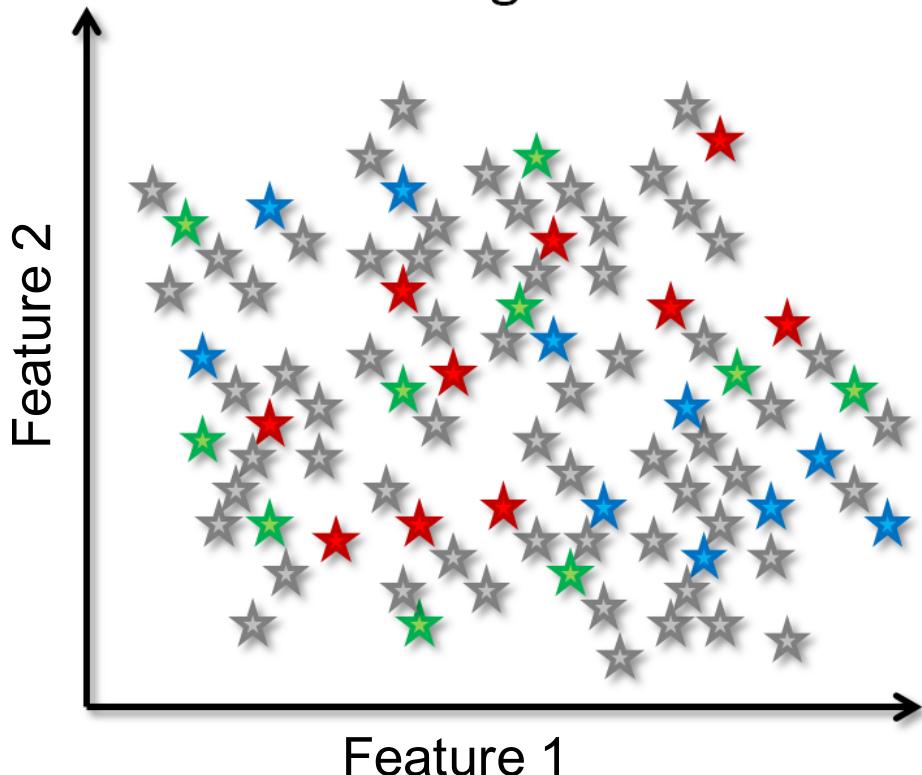


**Testing Complexity**

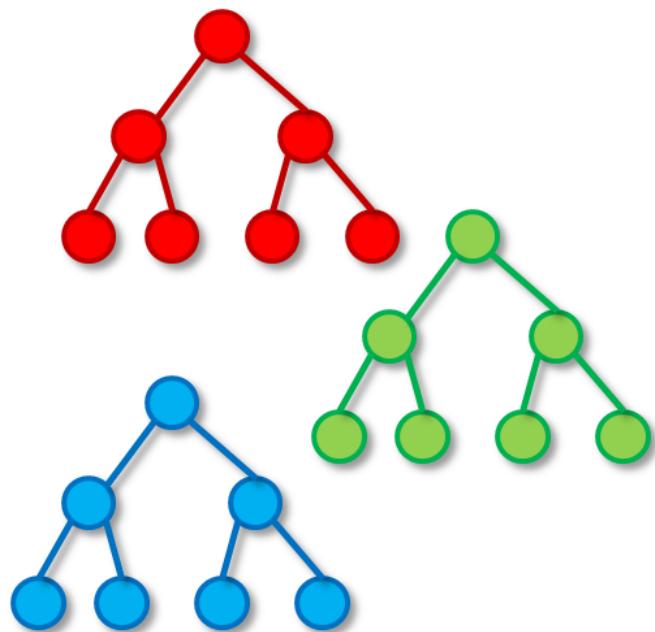


# Features and their Role

Training set

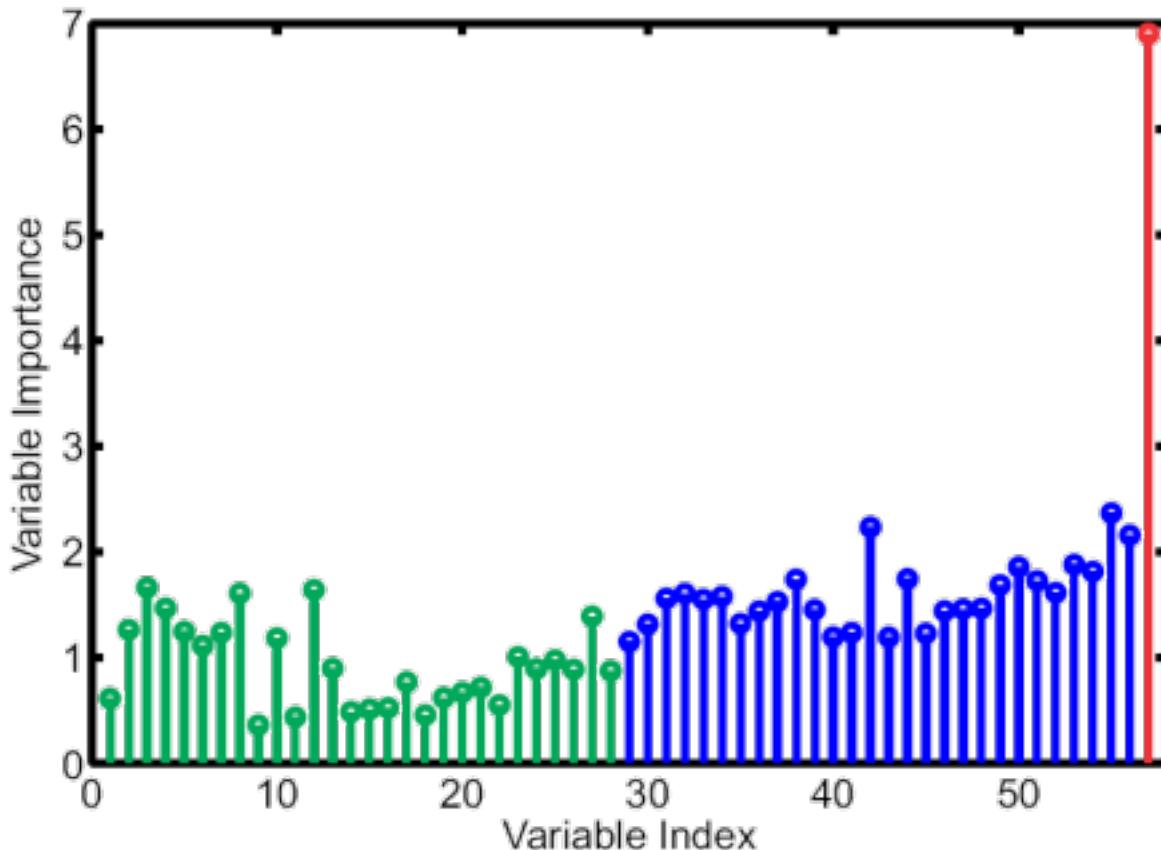


Decorrelated trees





# Variable Importance



Genuer, R., Poggi, J.-M.,  
Tuleau-Malot, C., (2010).  
Variable selection using  
random forests. *Pat. Recog.  
Letters.* **31**(14):2225-2236



# Take Home Message

- Reading
  - L. Breiman, J. Friedman, C. J. Stone, and R. A. Olshen, *Classification and Regression Trees*. Chapman and Hall/CRC, 1984.
  - L. Breiman, "Random forests," *Machine Learning*, vol. 45, no. 1, pp. 5–32, 2001.
  - A. Criminisi and J. Shotton, *Decision Forests for Computer Vision and Medical Image Analysis*, Springer, 2013.
- Toolboxes and Packages
  - randomForest in **R**
  - TreeBagger in **Matlab**
  - sklearn.ensemble.RandomForestClassifier in **Python-Scikit-learn**
- Conferences
  - Int. Conf. Comp. Vis. (ICCV)
  - Eur. Conf. Comp. Vis. (ECCV)
  - Asian Conf. Comp. Vis. (ACCV)
  - Comp. Vis. Patt. Recog. (CVPR)
  - Med. Image Comp., Comp. Assist. Interv. (MICCAI)