

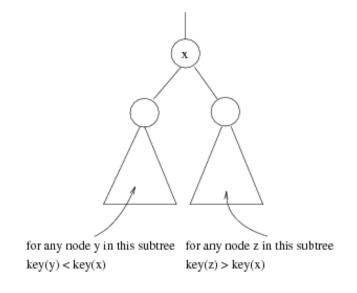
Binary Search Tree

- >introduction,
- >searching,
- >insertion and
- **≻**deletion



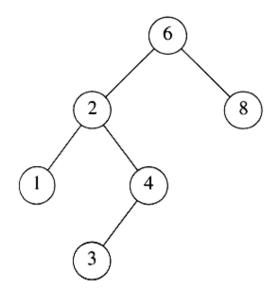
Binary Search Trees (BST)

- A data structure for efficient searching, insertion and deletion
- Binary search tree property
 - For every node X
 - All the keys in its left subtree are smaller than the key value in X
 - All the keys in its right subtree are larger than the key value in X

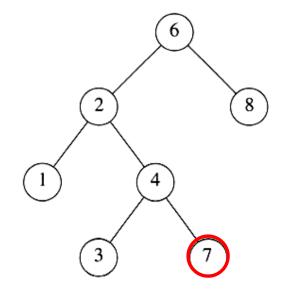




Binary Search Trees



A binary search tree

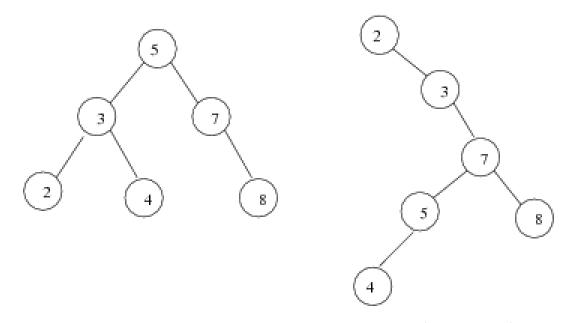


Not a binary search tree



Binary Search Trees

The same set of keys may have different BSTs

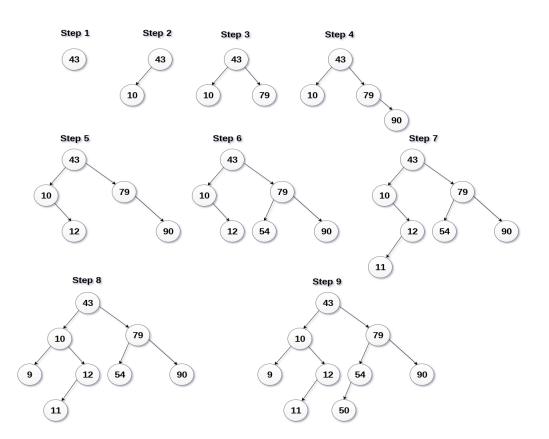


- Average depth of a node is O(log N)
- Maximum depth of a node is O(N)



- Create BST for following:
- 43, 10, 79, 90, 12, 10,54, 11, 9, 50



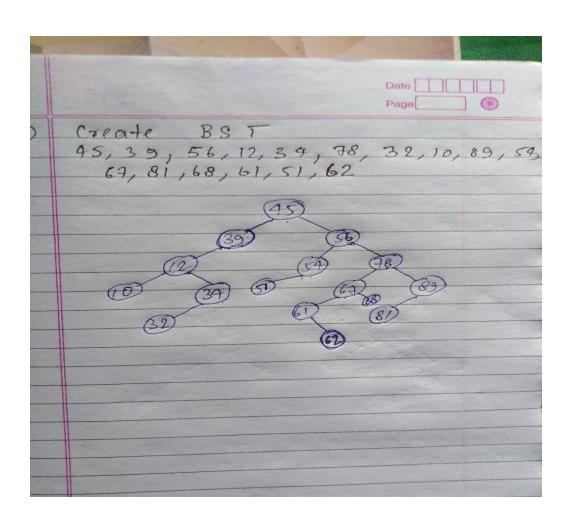


Binary search Tree Creation



- CREATE BST:
- 45, 39, 56, 12, 34, 78, 32, 10, 89, 54, 67, 81, 68, 61,51,62

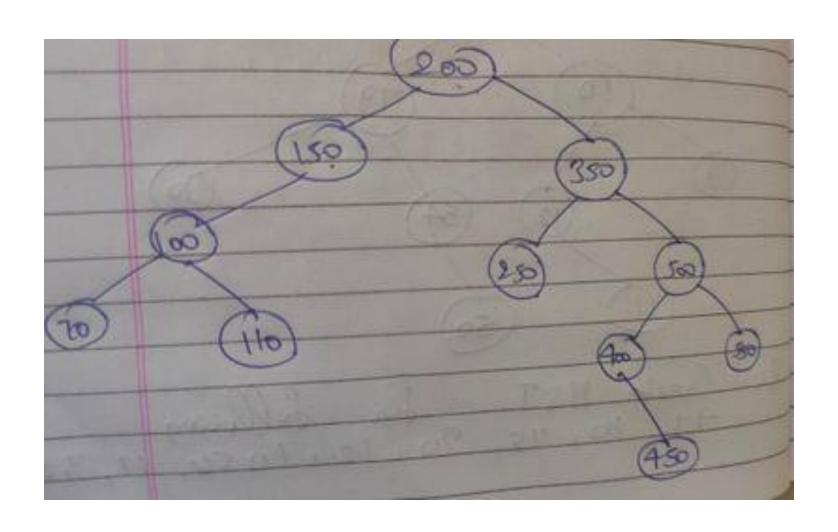






- 1. Create a BST tree with following data by inserting the following elements in order of their occurrence.
 - 200,150,350,100,70,110,250,500,400,550,450



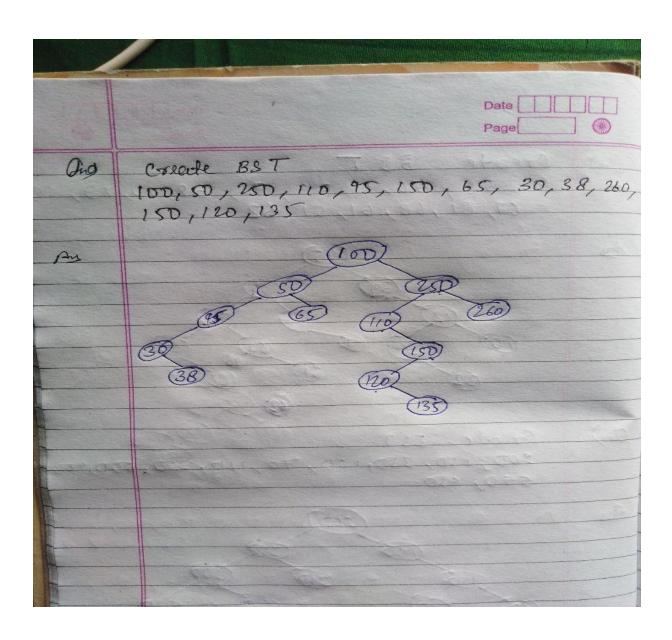




1. Create a BST tree with following data by inserting the following elements in order of their occurrence. [5 marks]

• 100,50,250,110,45,150,65,30,38,260,150,120,135

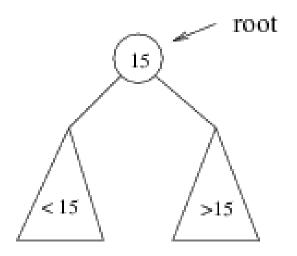






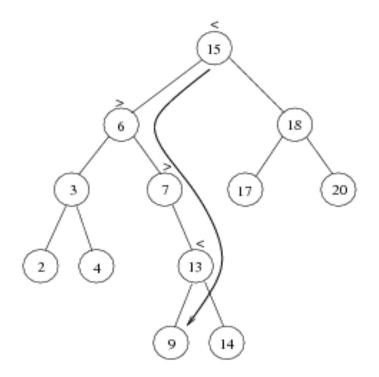
Searching BST

- If we are searching for root (15), then we are done.
- If we are searching for a key < root, then we should search in the left subtree.
- If we are searching for a key > root, then we should search in the right subtree.





Example: Search for 9 ...



Search for 9:

- compare 9:15(the root), go to left subtree;
- 2. compare 9:6, go to right subtree;
- 3. compare 9:7, go to right subtree;
- compare 9:13, go to left subtree;
- compare 9:9, found it!

Searching (Find)

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FIND(info, left, right, root, item, loc, par)- finds the item in tree T with root is root and info, left and right is three array represented in memory. This algorithm returns *loc* i.e. location of item and *par* i.e. parent.

- 1. [Tree Empty??]
 if root==NULL, then set LOC=NULL &
 PAR=NULL and return.
- 2. [Item root ??]

 If item==INFO[ROOT], then LOC=ROOT & PAR=NULL and return.
- [Initialize pointer ptr and save]

 If item<INFO[ROOT]

 then set PTR = LEFT[ROOT] and SAVE=ROOT

 Else

 set PTR = RIGHT[ROOT] and SAVE=ROOT</pre>



- 4. Repeat 5 and 6 while ptr!=NULL
- 5. [item found??]

If ITEM=INFO[PTR], then set LOC=PTR and PAR=SAVE, and return.

6. If ITEM<INFO[PTR], then SAVE=PTR and PTR=LEFT[PTR]

Else

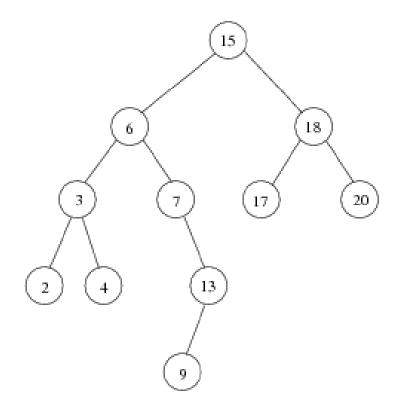
Set SAVE=PTR and PTR=RIGHT[PTR]

- 7. [Search unsuccessful] Set, LOC=NULL and PAR = SAVE
- 8. Exit
- Time complexity: O(height of the tree)



Sorting: Inorder Traversal of BST

• *Inorder Traversal* of BST prints out all the keys in sorted order

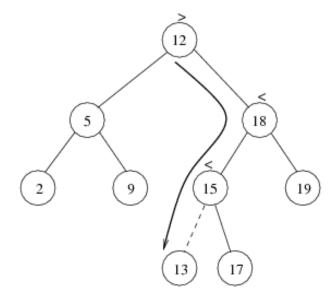


Inorder: 2, 3, 4, 6, 7, 9, 13, 15, 17, 18, 20



Insertion

- Proceed down the tree as you would with a find
- If X is found, do nothing (or update something)
- Otherwise, insert X at the last spot on the path traversed



• Time complexity = O(height of the tree)

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Inserting (ADD node)

INSBST(info, left, right, root, item, loc, avail)- insert the item in tree T with root is root and info, left and right is three array represented in memory. This algorithm returns *loc* i.e. location of item or *ADD* item as new node in tree.

- 1. Call FIND(INFO, LEFT, RIGHT, ROOT, ITEM, LOC, PAR)
- 2. If *LOC!=NULL*, then Exit.
- 3. [Copy ITEM into new node in AVAIL list]
 - a) If AVAIL==NULL, Print "OVER FLOW";
 - b) Set NEW=AVAIL, AVAIL=LEFT[AVAIL] and INFO[NEW]=ITEM.
 - Set LOC=NEW,LEFT[NEW]=RIGHT[NEW]=NULL
- 4. [ADD ITEM to TREE]

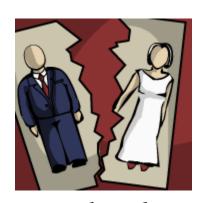
If PAR=NULL then, Set ROOT=NEW.
Else IF ITEM<INFO[PAR], Set LEFT[PAR]=NEW
Else Set RIGHT[PAR]=NEW

- 5. Exit
- Time complexity: O(height of the tree)



Deletion

 When we delete a node, we need to consider how we take care of the children of the deleted node.





• This has to be done such that the property of the search tree is maintained.



Deletion under Different Cases

- Case 1: the node is a leaf
 - Delete it immediately
- Case 2: the node has one child
 - Adjust a pointer from the parent to bypass that node

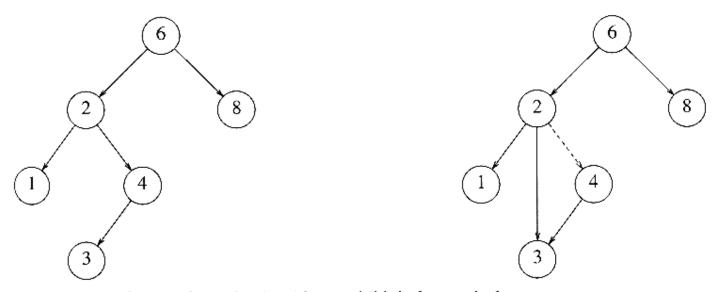


Figure 4.24 Deletion of a node (4) with one child, before and after



Deletion Case 3

- Case 3: the node has 2 children
 - Replace the key of that node with the minimum element at the right subtree
 - Delete that minimum element
 - Has either no child or only right child because if it has a left child, that left child would be smaller and would have been chosen. So invoke case 1 or 2.

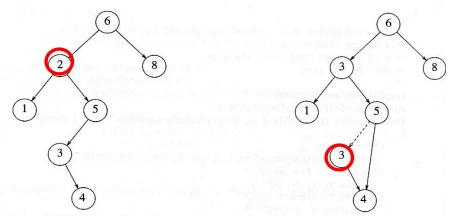


Figure 4.25 Deletion of a node (2) with two children, before and after

• Time complexity = O(height of the tree)



Deletion Algorithm

- DEL(INFO, LEFT, RIGHT, ROOT, AVAIL, ITEM)
- A binary search tree T is in memory, and an ITEM of information is given. This algorithm delete ITEM from the tree.
- 1. Call FIND(INFO, LEFT, RIGHT, ROOT, ITEM, LOC, PAR)
- 2. If LOC=NULL, then write ITEM not in tree and Exit
- If RIGHT[LOC]!=NULL and LEFT[LOC]!=NULL, then: Call CASEB(INFO, LEFT, RIGHT, ROOT, LOC, PAR) Else:
 - Call CASEA(INFO, LEFT, RIGHT, ROOT, LOC, PAR)
- 4. Set LEFT[LOC]:=AVAIL and AVAIL :=LOC.
- 5. Exit



CASEA: only one or, no child

- CASEA(INFO, LEFT, RIGHT, ROOT, LOC, PAR)-delete the Node N at location LOC, where N doesn't have two Children. PAR is location of parent node or, PAR=NULL i.e. ROOT node.
- Initialize CHILD]

 If LEFT[LOC]=NULL and RIGHT[LOC]=NULL, then

 CHILD=NULL

 Else if LEFT[LOC]!=NULL, then CHILD=LEFT[LOC]

 Else CHILD=RIGHT[LOC]
- If PAR != NULL then: (i.e. NOT A ROOT NODE)

 If LOC=LEFT[PAR], then set LEFT[PAR]=CHILD

 Else RIGHT[PAR]=CHILD

 [End of IF]

 Else set ROOT=CHILD.

 [End of IF]
- 3. Exit



CASEB: has 2 children

- CASEB(INFO, LEFT, RIGHT, ROOT, LOC, PAR)-delete the Node N at location LOC, where N has two Children. PAR is location of parent node or, PAR=NULL i.e. ROOT node. SUC gives location of inorder successor and PARSUC gives location of parent of inorder successor.
- 1. [Find SUC and PARSUC]
 - a) Set PTR=RIGHT[LOC] and SAVE=LOC
 - b) Repeat while LEFT[PTR]!=NULL
 Set, SAVE=PTR and PTR=LEFT[PTR]
 [END OF LOOP]
 - c) Set SUC=PTR and PARSUC=SAVE.
- 2. [Delete SUC] Call CASEA(INFO, LEFT, RIGHT, ROOT, SUC, PARSUC)
- 3. [replace node N by SUC]
 - a) If PAR != NULL then: (i.e. NOT A ROOT NODE)

If LOC=LEFT[PAR], then set LEFT[PAR]=SUC

Else RIGHT[PAR]=SUC

[End of IF]

Else set ROOT=SUC.

[End of IF]

b) Set, LEFT[SUC]=LEFT[LOC] and RIGHT[SUC]=RIGHT[LOC]



Thank you !!!