F-Test bur Equality of two population variances' Suppose are want to fest O whether two independent Samples 20, (1=1,2,-n,) and y; (j=1,2,have been drawn from the normal populations certh the same variance o2 (say), or 1 whether the two independent estimates at the population variances gre homogeneous or not. Oncles the null hypothesis (Ho) that

O  $G_{R}^{2} = G_{g}^{2} = \delta^{2}$  i.e. the population variances are equal or, (1) Two independent estimates at the population variance are homogeneous, the statistic F is given by  $= \int_{\eta_{i}-1}^{\eta_{i}} \sum_{\rho=1}^{\chi_{i}-\overline{\chi}} (\chi_{i}-\overline{\chi})^{2}$ and  $S_y^2 = \frac{n_2}{n_2 - 1} \frac{n_2}{\sum_{j=1}^{n_2} (y_j - \overline{y})^2}$ are unhiased estimates at the common population variance or obtained brom two independent samples and et bollows F- destribution conthe (2, 12) degree ab breedom where 2, = n,-1 and 2 = n2-1 Example 1 Remark In 10, greater at the two variances si and sy is to be taken in the numerator and n, corresponds to the greater rarcance.



Example O In one sample cet 8 observations, the our of equares ob deviations ab the sample values brown the sample mean was 84.4 and in the 1 Other cample ob 10 observations et was 102.6. Test achether this deliberence is signebicant at 5% level, given shat the 5 percent point cel F bor n=7 and n=9 degrees ob breedom is 3.29 Solution Here  $n_1 = 8$ ,  $n_2 = 10$ ,  $\sum (x - \overline{x})^2 = 84-4$ 

 $\sum (y-\bar{y})^2 = 102.6$ 

 $S_{x}^{2} = \frac{1}{h_{1}-1} \ge (x-\overline{x})^{2} = \frac{1}{7} \times 84.4 = 12.057$ 

 $S_{y}^{2} = \frac{1}{h_{2}-1} \sum (g-\overline{g})^{2} = \frac{1}{g} \times 102.6 = 11.4$ 

Under Ho;  $G_1^2 = G_2^2 = \sigma^2$  i.e., the estimates ob 62 given by the samples are homogeneous, the

 $f = \frac{S_{x}^{2}}{S_{y}^{2}} = \frac{12.057}{11.4} = 1.057$ 

Tabulated F. bur (7,9) d.f is 3.29

Since calculated F < Foos; Ho may be accepted at 5% level ob significance.

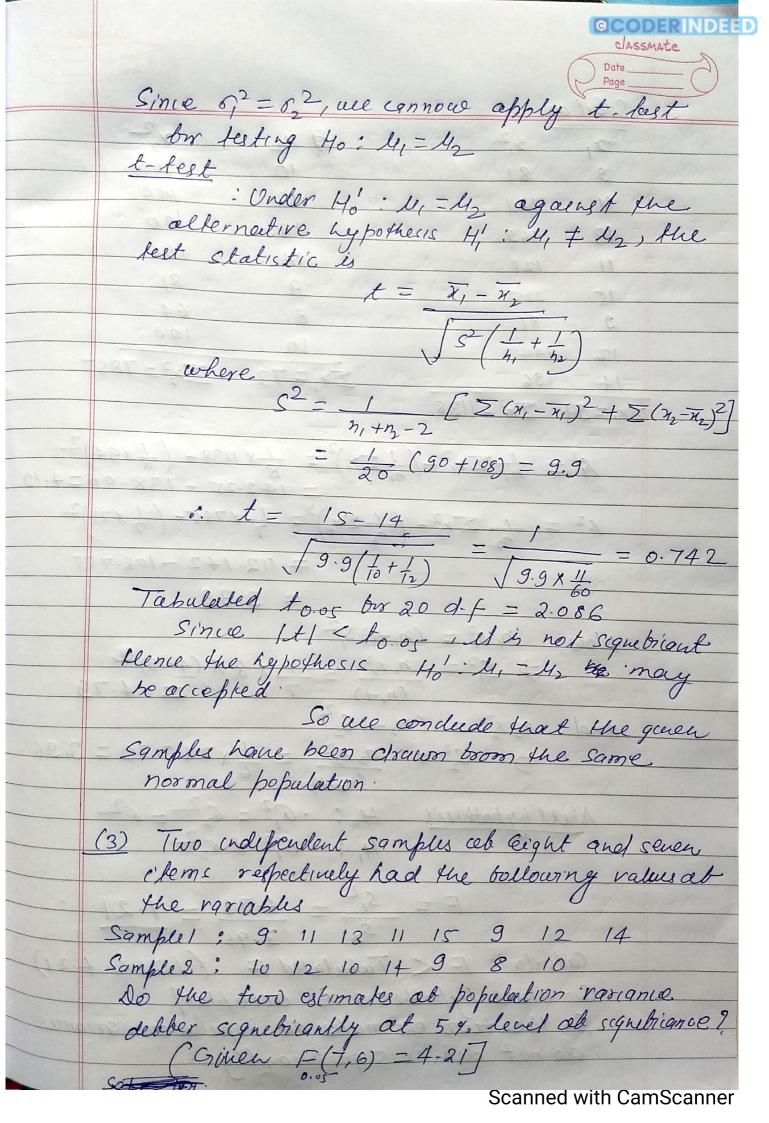
Example (2) Two random samples gave the bollowing results
Sample Size Samplemean Samob squares. Sam ob squares ab

devations brom the mean

Test cockether the samples come brom the same normal population at 5% level ab signebicance.
Foros (9,11) = 2-90; Foros (11,9) = 3.10, to 05(20)=1.086, to 05=2.07 Solution

A normal population has teer parameters namely mean u and variance of To test el tero independent samples have been drawn brown the same normal population, cere have to best O the equality at population means, and 10 the equality cel population variances. Mull hypothers: The two sample have been drawn brom the same normal population, re. Ho: 11=42 and 5,2=5,2 Equality of means certle be tested by applying t-test and equalety ab variance certe be tested by applying F-test. Since t-test assumes 6,2 = 6,2 ; wee shall trost apply F-kest and Griver,  $n_1 = 10$ ,  $n_2 = 12$ ,  $\overline{\chi}_1 = 15$   $\overline{\chi}_2 = 14$ ,  $\Sigma (\chi_1 - \overline{\chi}_1)^2 = 90$ ,  $\Sigma (\chi_2 - \overline{\chi}_2)^2 = 10$  $\frac{F - \text{les} f}{\int_{1}^{2} = \frac{1}{\eta_{1} - 1}} \sum_{i} (x_{i} - \overline{x}_{i})^{2} = \frac{1}{9} \times 90 = 10$  $S_2^2 = \frac{1}{h_2 - 1} \sum (x_2 - \overline{x}_2)^2 = \frac{108}{11} = 9.82$ Since  $S_1^2 7 S_2^2$  under  $H_0$ ;  $G_1^2 = G_2^2$ . The fest statistics is  $F = G_1^2 - 10 = 1.018$   $S_2^2 = 9.82$ Tabulaked Fo.05(9,11) = 2.90 (Criven) Since tabulated F is less P Since calculated F is less than tabulated F F is not significant. Hence null hypothesis of equality ab population variances muy be accepted.

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	Classmate	ADEE
	Date	1
	The state of the s	
73	Solution 8 x2 x2	
	1	-
	9 81 10 100	-
	11 121 12 144	_
Rice	13 169	
	11 121 14 196	
	15 225 9 81	
	9 81 8 64	_
	12, 144	
	14   196	
18 25 M	$\sum x_1 = 94  \sum x_1^2 = 1/38$	
	$g_{i}^{2} = \frac{1}{h_{i}} \sum_{x_{i}}^{2} - \left(\frac{1}{h_{i}} \sum_{x_{i}}^{2}\right)^{2} = \frac{1}{8} \times 1138 - \left(\frac{1}{8} \times 94\right)^{2}$	
	$\frac{p_1-p_1}{p_1}=\frac{p_1}{p_1}=$	19
	$\beta^{2} = \frac{1}{2} \sum_{1}^{2} \left( \frac{1}{2} \sum_{2}^{2} \right)^{2} = \frac{1}{2} \times 785 - \left( \frac{1}{2} \times 73 \right)^{2}$	
745.	n2 (n2 (7/13)	
	= 112.142-108.755	
	2x08 = 2 b 08 mg = 3.39 md of	
4.01	$Nlow, n_1 s_1^2 = (n_1 - 1) s_1^2$	
1200	$\Rightarrow S_{1}^{2} = \frac{\eta_{1} g_{1}^{2}}{1 \times g_{1}^{2}} = \frac{1}{1 \times g_{1}^{2}} \times \frac{g_{2}^{2}}{1 \times g_{2}^{2}}$	
	(n,+) 7 = 4.79	
33333	and not 1/2 = (0/2-1) Sz	
-	$\Rightarrow S_2^2 = \frac{n_2 s_2^2}{6} = \frac{1}{6} \times 7 \times 3.39 = 3.96$	
	$\frac{(\gamma_2-1)}{(\gamma_2-1)}$	_
	Nell hypothesis Ho: . 6,2 = 6,2 - 2	
1 4	$H_1: G_1^2 \neq G_2^2$	_
	$F = \frac{s_1^2}{s_2^2} = \frac{4.79}{2} = 1.21$	
	S <sub>2</sub> = 1.21	
	Calculate F < Tabalated F (1.2/< 4.21)	
	So Null hypothesis is accepted	
inde ?	So the two estimates ab population variances	_
	do not debber signebicantly.	_
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