MCQ QUESTION BANK ON MATRICES

Type I Rank and Normal Form

Q.1) Which of the following matrix is in normal form?

$$A) \begin{bmatrix} 1 & 2 & 5 \\ 0 & 1 & 9 \\ 0 & 0 & 5 \end{bmatrix} \qquad B) \begin{bmatrix} 1 & 4 & 3 & 1 \\ 0 & 0 & 1 & 4 \\ 0 & 1 & 3 & 8 \\ 0 & 0 & 0 & 1 \end{bmatrix} \qquad C) \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \qquad D) \begin{bmatrix} 1 & 0 & 0 \\ 1 & 0 & 0 \end{bmatrix}$$

Q.2) Echelon form of matrix $\begin{bmatrix} 1 & 1 & 1 & 1 & 1 \\ 5 & 5 & 5 & 5 & 5 \\ 8 & 8 & 8 & 8 & 8 \end{bmatrix}$ i

Q.3) Rank of a matrix is nothing but

- A) number of zero rows in that matrix B) number of zero rows in its echelon form of matrix
- matrix.
- C) number of non-zero rows in that matrix D) number of non-zero rows in its echelon form of

Q.4) The rank of matrix $A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 2 & 2 \\ 3 & 3 & 3 \end{bmatrix}$ is equal to A) 4 B) 3 C) 2

The rank of matrix
$$A = \begin{bmatrix} 2 & 2 & 2 \\ 3 & 3 & 3 \end{bmatrix}$$
 is equal to

Q5) If
$$A = \begin{bmatrix} 1 & 2 & 3 \\ 3 & 4 & 5 \\ 4 & 5 & 6 \end{bmatrix}$$
 and det(A)=0 then rank of a matrix A is

- A) Greater than or equal to 3
- B) Strictly less than 3

C) Less than or equal to 3

- D) Strictly greater than 3.
- Q.6) Which of the following matrix is in normal form?

A)
$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$
 B)
$$\begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$
 C)
$$\begin{bmatrix} 1 & 1 & 1 \\ 0 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix}$$
 D)
$$\begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix}$$

Q.7) Which of the following matrix is in the Normal form?

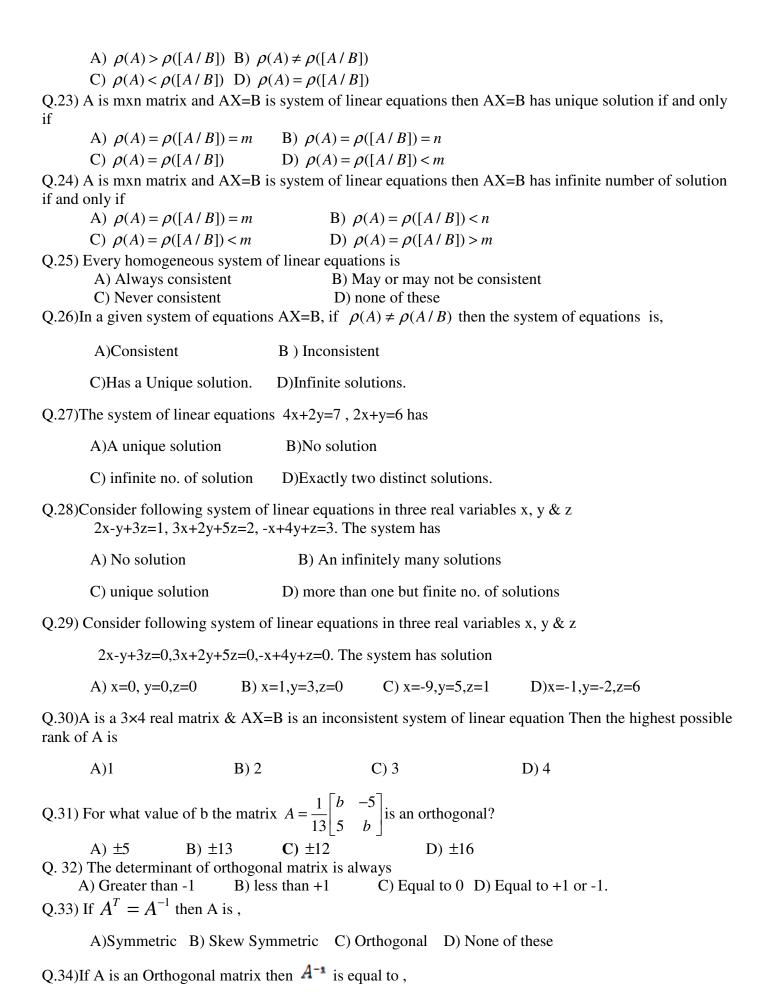
10 10 10 10 10

A) 10 B) 5 C)2 D)1. Q.9)The rank of the matrix
$$\begin{bmatrix} 1 & 1 & 1 \\ 1 & -1 & 0 \end{bmatrix}$$
 is,

Q.9) The rank of the matrix
$$\begin{bmatrix} 1 & 1 & 1 \\ 1 & -1 & 0 \\ 1 & 1 & 1 \end{bmatrix}$$
 is ,

				B) $r \ge \max\{$ D) $r \le \max\{$				
				PAQ is in nor		en A^{-1} is	equal to	
A	A)PQ	B) QP	C) P+Q	D) Q-P				
Q.12) A	5×7 ma	trix has a	all its entrie	es equal to -1,	then rank o	f matrix is		
A	A)7		B) 5	C) 1		D) zero		
				trix by determ	inant metho	$d \begin{bmatrix} 2 & 3 & 4 \\ 4 & 3 & 1 \\ 1 & 2 & 4 \end{bmatrix}$	is	
A	A)2	B) 3	C) 1	D) 0				
Q.14)If	P=3 the	n the ran	k of matrix	$A = \begin{bmatrix} 3 & P & P \\ P & 3 & P \\ P & P & 3 \end{bmatrix}$].			
A	A)1	B) 2	C) 3	D) 0				
Q.15) Gi	iven sys A) uniqu C) infini given s f Rank (tem of line solution tely many ystem of (A) = ran	near equati n y solutions linear equa k (A/B) =N	ons $x-4y+5z=$	-1, 2x-y+3z= o solution ions	=1,3x+2y+ the system	z=3 has n is,	e solutions
C	C) Consi	istent & s	ystem has	unique solutio	on D) None	of the abo	ve	
If	Rank (A) =rank	$(A/B) < N\iota$	ations AX=B, umber of unkr s no solution	nowns then t	the system	is,	solutions
C	C) Consi	istent & s	ystem has	unique solutio	on D) None	of the abo	ve	
Q.18) In		nique sol		ationsAX=B, a	if $det(A) \neq 0$ B)No solutione of the a	ution	m has	C)infinite
c A	ombina A)Linea		e remainin endent	e vector of the g vectors then	these vector	rs are calle linearly d	ed	
Q.21) A	Converts $A) z = B$ $C) z = B$ Linear than Orthor $C) Symn$	s vector x AX $A^{-1}A^{-1}x$ transform onormal r netric Ma	in to a vec nation $y = x$ natrix	are $y = Ax$ are etor z is B) $z = A^{-1}B$ D) $z = ABx$ Ax is said to land B) Orthogon D)Singular Inferior equation	⁻¹ x be orthogona nal matrix Matrix	ıl if A is		
_ /		2	,	1			- 3	

Q.10) For matrix A of order mxn, the rank r of matrix A is



A) A B) A^T C) A^2 D) $-A^T$

Type III] Eigen Values, Eigen Vectors, Cayley Hamilton Theorem.

Q.35) If x is eigen vector of matrix.		eigen value λ then	
A) has same direction as tha	at of x	B) has opposite	
C) x is orthogonal to kx	its characteristic a	D) \mathbf{x} is parallel	to kx
Q.36) If A is any square matrix then A) $det(A - \lambda I) = 0$ B) (A		$\det(A - \lambda A) = 0$	D) $(A - \lambda A) = 0$
Q.37) If eigen values of matrix A ar		, ,	
A) 1 2 2 D)12	2	2.4.0	D) 2,8,18
0.20) (FI)	[1 1 1]	, ,	, , ,
Q.38) The characteristics roots of th	e matrix $\begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$ at	re	
A) (0,0,0)	B)(0,0,3)	C) (0,0,1)	D) (1,1,1)
A) (0,0,0) Q.39)Find sum of the eigenvalues o	f the matrix $\begin{bmatrix} 2 & -3 \\ 4 & -2 \end{bmatrix}$		
A)2 B)4	C)	0	D) 1
Q.40)Find product of eigenvalues of	f matrix $\begin{bmatrix} 2 & -3 \\ 4 & -2 \end{bmatrix}$		
A)4	B)8	C) 6	D) 2
Q.41)The product of two eigen valu	es of the matrix $_{A} =$	$\begin{bmatrix} 6 & -2 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3 \end{bmatrix} $ is 16	. Find the third eigenvalue.
A)1	B)2	C) 4	D) 3
Q.42) For a given matrix A of ord eigenvalues	$der 3\times3, det(A)=32$	& two of its eiger	nvalues are 8 & 2. Find sum of
A)12	B)8	C) 10	D) 2
Q.43) If 2 & 3 are eigenvalues of A	$= \begin{bmatrix} 2 & 0 & 1 \\ 0 & 2 & 0 \\ 1 & 0 & 2 \end{bmatrix} $ find t	he third eigenvalue	
A)2	B)3	C)1	D) 4
Q.44) If 1, 2 & 3 are the eigen value A)1 B)0	es of $A = \begin{bmatrix} 2 & 0 & 1 \\ 0 & 2 & 0 \\ a & 0 & 2 \end{bmatrix}$, C) 2	find the value of a D)	
,	,	ŕ	
Q.45) The characteristic equation of	L -	_	
$A) \lambda^2 + 5\lambda + 21 = 0$			
$C) \lambda^2 + 13\lambda + 36 = 0$	_	_	
Q.46) Find the eigen values of the n			
A) $\lambda_1 = 4, \lambda_2 = 9$ B) λ_1	$=5, \lambda_2=6$		

C) $\lambda_1 = 18, \lambda_2 = 2$ D) $\lambda_1 = 10, \lambda_2 = 3$

Q.47)	Two eigen values of th	the matrix $A = \begin{bmatrix} 2 & 2 & 1 \\ 1 & 3 & 1 \\ 1 & 2 & 2 \end{bmatrix}$ and	re 1 &1, find the 3^{rd} e	igenvalue of A.
	A)1	B)3	C) 5	D)4
Q.48)T	Two eigenvalues of the	matrix $A = \begin{bmatrix} 2 & 2 & 1 \\ 1 & 3 & 1 \\ 1 & 2 & 2 \end{bmatrix}$ are	1 & 1 find the eigenv	values of A^{-1}
	A)1/1 , 1/1 , 1/5	$B)^{1/2}$, 1, 5	$C)^{1/2}$, $^{1/2}$, 5	D)1,1,5
Q.49)	the eigenvalues of are	e eigenvalues are $\alpha - 5$, $A = \begin{bmatrix} -1 & -2 & -3 \\ 4 & 5 & -6 \\ 7 & -8 & 9 \end{bmatrix}$ B) $\begin{bmatrix} -6 & -2 & -3 \\ 4 & 0 & -6 \\ 7 & -8 & 4 \end{bmatrix}$ C)		
			, , ,] [· • • • • • • • • • • • • • • • • • • •
Q.50) matrix			$\lambda^3 - 4\lambda^2 - \lambda + 4 = 0$ the (1) -1, 1, 4	n find the Eigen values of that D) 1, 1, 5
	A)1 B) 0	of order $3X3$, 2 and 3 are C) 2	D) 3	d its 3 rd eigenvalue.
Q.52)		tic equation of the matrix B) $\lambda^3 = 4\lambda^2 + 3\lambda + 1 = 0$		D) $\lambda^3 - 4\lambda^2 - 3\lambda = 0$
Q.53) I	Determinant of square		C) 7(1 47(1 37(- 0	D) 71 471 371-0
·	A) Sum of all elemen C) Product of its eige	ts B) Product of diagonal) Sum of its eigen values of matrix A ³ a	lues.
	A)1,8,27 B)	1,4,9, C) 2,3,4,	D) 4,5,6	5
Q.55)	If λ is eigen value of n	natrix A then eigen value	s of matrix A ⁻¹ is	
	Α) λ	B) $-\lambda$ C) $\frac{1}{\lambda}$	D)1.	
Q.56)	If λ is eigen value of n	natrix A then eigen value	s of matrix kA is	
	A) k λ	B) $-\lambda$ C) $\frac{1}{k\lambda}$	D) λ.	
O 57)	If lis eigen value of r	natriy A than aigan yalı	oc of matrix A±kLic	

D) $\lambda - k$.

Q.58) If λ is eigen value of matrix A then eigen values of matrix A^n is

B) $\lambda + k$

A) $k\lambda$

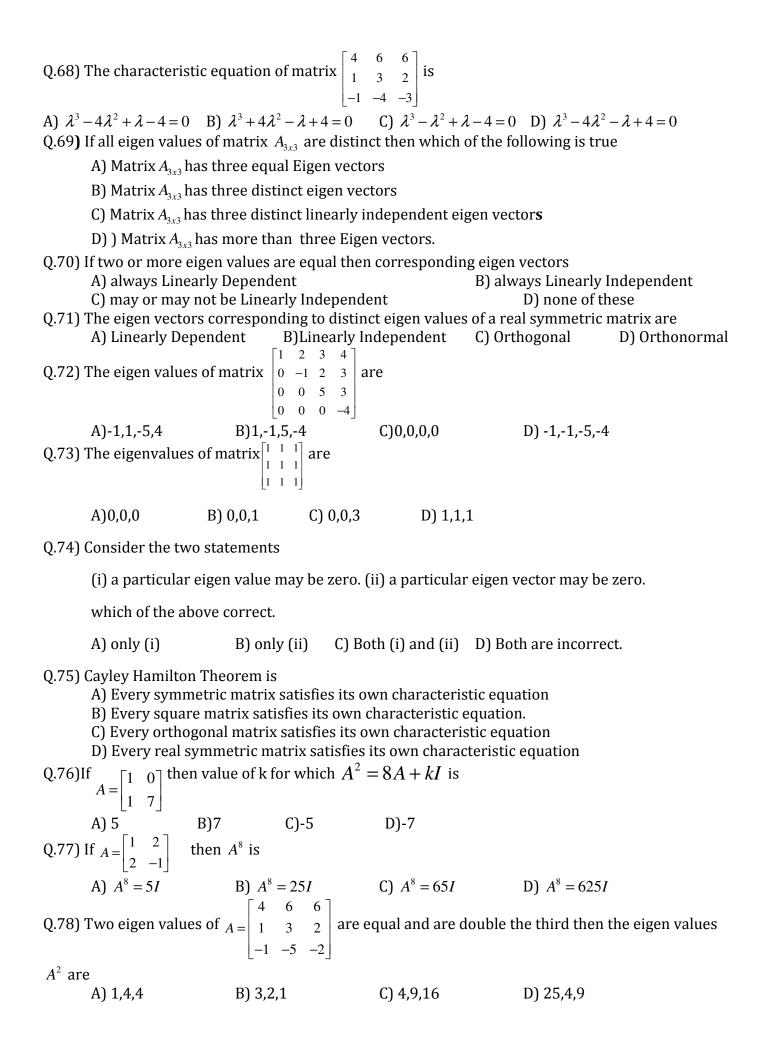
A) n λ	B) λ^n	C) $\frac{n}{\lambda}$		D) λ.	
Q.59) If $\lambda_1, \lambda_2, \lambda_3$ A) $\frac{1}{\lambda_1}, \frac{1}{\lambda_2}$	are eigen values of matrix $-\frac{1}{\lambda_3}$ B) λ_1, λ_2			re D) −λ₁,−	$-\lambda_2,-\lambda_3$
Q.60) The sum 8	& product of the eigen valu	es of matrix	$\begin{bmatrix} 2 & -3 \\ 4 & 2 \end{bmatrix}$ are		
A)0,0		C)0,8	_		
Q.61) For the ma	atrix $\begin{bmatrix} 1 & -2 & 3 \\ 0 & -2 & 5 \\ 0 & 0 & 4 \end{bmatrix}$ product of t	he eigen value	es is		
A)-8	B) 4 C)1	D) -2			
Q. 62) The eigen	values of the matrix $\begin{bmatrix} 1 & 4 \\ 2 & 3 \end{bmatrix}$	are			
A) 2,3	B)4,5 C) 0	,2 D)	5,-1		
Q.63) The Chara	B)4,5 C) 0	$ \begin{array}{c cccc} atrix & 3 & 1 \\ -1 & 5 & \\ 1 & -1 & \end{array} $	$\begin{bmatrix} 1 \\ -1 \\ 3 \end{bmatrix}$ is		
A) $\lambda^3 - 1$	$1\lambda^2 + 38\lambda - 40 = 0$	B) $\lambda^3 - 11\lambda^2 +$	$38\lambda + 40 = 0$		
	$1\lambda^2 + 38\lambda + 40 = 0$				
	racteristic equation of the	matrix A of or	der 3x3 is λ^3 –	$-3\lambda^2 + 3\lambda - 1 = 0$	then by Cayley
Hamilton Theorem	A^{-1} is equal to				
		B) $A^2 - 3A - 3$	I		
C) $3A^2 -$					
Q.65) If $\lambda^2 - S_1 \lambda$	$x + S_2 = 0$ is a characteristic	equation of 2	x2 matrix A the	en	
A) $S_1 = Sum$	n of principle diagonal elen	nents, $S_2 = Sur$	n of all elemen	ıts	
B) $S_1 = Sum$	n of principle diagonal elen	nents, $S_2 = Property$	oduct of princi	ple diagonal ele	ments
C) $S_1 = \text{Trac}$	e of matrix A, $S_2 = \text{Produc}$	t of principle o	diagonal eleme	ents	
D) $S_1 = \text{Trace}$	e of matrix A, $S_2 = Product$	of Eigen valu	es of matrix A.		
Q.66) If $\lambda^3 - S_1 \lambda$	$\lambda^2 + S_2 \lambda - S_3 = 0$ is a charact	eristic equation	on of 3x3 matr	ix A then	
A) S_1	= Sum of principle diagor	nal elements, S	$S_2 = Sum of all \epsilon$	elements, $S_3 = A $	I
	= Sum of principle diagor			•	•
$S_3 = A $				_	

C) S_1 = Trace of matrix A, S_2 = sum of minors of Principle diagonal elements, $S_3 = |A|$

D) S_1 = Trace of matrix A, S_2 = Product of Eigen values of matrix A, S_3 = $\left|A\right|$

Q.67) The characteristic equation of matrix $\begin{bmatrix} 14 & -10 \\ 5 & -1 \end{bmatrix}$ is

A) $\lambda^2 - 13\lambda + 36 = 0$ B) $\lambda^2 - 13\lambda - 36 = 0$ C) $\lambda^2 - 4\lambda - 64 = 0$ D) $\lambda^2 - \lambda + 36 = 0$



Q.79) If
$$_{A=}\begin{bmatrix} 1 & 2 & -3 \\ 0 & 3 & 2 \\ 0 & 0 & -2 \end{bmatrix}$$
 then the eigen values of $3A^3 + 5A^2 - 6A + 2I$ are

- A)5,-6,2
- B)1,3,-2

Q.80) Sum and product of the eigen values of matrix $A = \begin{bmatrix} -1 & 1 & 1 \\ 1 & -1 & 1 \\ 1 & 1 & -1 \end{bmatrix}$ is

- A) -3,-1
- C) 4,3

Q.81) If $A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$ then

- A) $A^{-1} = \begin{bmatrix} 1 & 3 \\ 2 & 4 \end{bmatrix}$ B) $A^{-1} = \begin{bmatrix} 1 & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{4} \end{bmatrix}$ C) $A^{-1} = \begin{bmatrix} -2 & 1 \\ \frac{3}{2} & -\frac{1}{2} \end{bmatrix}$ D) A^{-1} does not exist.
- Q.82) If 2,3,6 are the eigen values of matrix $A = \begin{bmatrix} 3 & -1 & 1 \\ -1 & 5 & -1 \\ 1 & -1 & 3 \end{bmatrix}$ then the eigen values of matrix $A^3 + 2I$

are

- A) 20,39,228
- B)10,29,218
- C) 0,19,208

Q.83) Eigenvalues of matrix $A = \begin{bmatrix} 3 & 2 \\ 2 & 3 \end{bmatrix}$ are 5 & 1 what are the eigen values of matrix A^2

- A) 1 & 25
- B) 2 & 10
- C) 6& 4 D) 5 & 1

GENERAL:

Q84)If $D = diag(d_1, d_2, d_3,d_n)$ where $d_i \neq 0$ for all i=1,2,3,....n ,then D^{-1} is equal to ,

B)
$$diag(d_1^{-1}, d_2^{-1}, d_3^{-1}, \dots d_n^{-1})$$

- C) I_n D) None of these

Q85)If $A = diag(d_1, d_2, d_3, \dots d_n)$ then A^n is equal to,

A)
$$diag(d_1^{n-1}, d_2^{n-1}, d_3^{n-1}, d_n^{n-1})$$
 B) $diag(d_1^n, d_2^n, d_3^n, d_n^n)$

B)
$$diag(d_1^n, d_2^n, d_3^n,d_n^n)$$

C) A

D)None of these.

Q86)If
$$_{A} = \begin{bmatrix} 1 & -5 & 7 \\ 0 & 7 & 9 \\ 1 & 8 & 9 \end{bmatrix}$$
, then Trace of the matrix A is,

- A)17
- B) 25
- C) 10
- D) 63

ANSWERS

Que	Ans								
1	С	21	В	41	В	61	A	81	С
2	С	22	D	42	Α	62	D	82	В
3	D	23	В	43	С	63	A	83	A

4	С	24	В	44	A	64	D	84	В
5	В	25	A	45	В	65	D	85	В
6	A	26	В	46	A	66	C	86	A
7	С	27	В	47	С	67	A		
8	D	28	C	48	A	68	D		
9	C	29	A	49	В	69	C		
10	С	30	В	50	С	70	В		
11	В	31	С	51	В	71	C		
12	С	32	D	52	D	72	В		
13	В	33	C	53	С	73	C		
14	Α	34	В	54	A	74	A		
15	C	35	В	55	C	75	В		
16	C	36	A	56	Α	76	D		
17	В	37	D	57	В	77	D		
18	A	38	В	58	В	78	A		
19	В	39	C	59	A	79	D		
20	A	40	В	60	C	80	В		