

# Schrödinger's Wave Function

Himalaya Satyal<sup>1</sup>

April 26, 2025

<sup>1</sup>Rato Bangala School

$$\int_a^b f(x)dx = \int_0^b f(x)dx - \int_0^a f(x)dx$$

Hello I am Himalaya Satyal and this is a research on Shrödinger's wave equations.The Shrödinger Equation is  $i\hbar\frac{\partial}{\partial t}|\Psi\rangle = \hat{H}|\Psi\rangle$  By definition,  $\int_a^b f(x)dx = \int_0^b f(x)dx - \int_0^a f(x)dx$ .

$$E_k + E_P = E_T$$

$$\implies \frac{-\hbar^2}{2m}\nabla^2\Psi(r) + V(r)\Psi(r) = E\Psi(r)$$

$$x\equiv -1\pmod{5}$$

$$i\hbar\frac{\partial}{\partial t}|\Psi\rangle = \hat{H}|\Psi\rangle$$

$$\implies x+1\equiv 0\pmod{5}$$

Therefore,  $5|x+1$  Let  $m$  be a fixed integer greater than 1. The sequence  $x_0,x_1,x_2,\dots$  is defined as follows:

$$x_i = \begin{cases} 2^i & \text{if } 0 \leq i \leq m-1; \\ \sum_{j=1}^m x_{i-j} & \text{if } i \geq m \end{cases}$$

Find the greatest  $k$  for which the sequence contains  $k$  consecutive terms

divisible by  $m$ .

If  $p$  is a prime and  $p \nmid a$ , then  $a^p \equiv a \pmod{p}$  This is known as Fermat's Last Theorem.

A modified version of the Fermat's Last Theorem  
which gives:

$a^{\phi(n)} \equiv 1 \pmod{n}$  where  $\phi(n)$  is the Euler's Totient  
Function.

Find the greatest  $k$  for which the sequence contains  $k$  consecutive terms divisible by  $m$ .

$$\oint_{e^{-i\pi}}^{\infty} \sin x \, dx = ?$$

$$\begin{aligned} x &= x_0 \cos(\omega t) \\ \implies \frac{dx}{dt} &= -\omega x_0 \sin(\omega t) \end{aligned} \tag{1}$$

$$\begin{aligned} v &= v_0 \sin(\omega t) \\ \implies \frac{dv}{dt} &= \omega v_0 \cos(\omega t) \end{aligned} \tag{2}$$

$$a = a_0 \cos(\omega t)$$

$$a_0 = -\omega^2 x_0$$

$$x = x_0 e^{-\lambda t}$$

$$\implies \frac{dx}{dt} = -\lambda x_0 e^{-\lambda t}$$

$$\frac{\partial x}{\partial t} = \partial \vec{A}$$

$$pV = \frac{1}{3}Nm\langle c^2 \rangle \quad (3)$$

$$\implies c_{r.m.s} = \sqrt{\langle c^2 \rangle}$$

Now we will look at the workfunction relation between the energy of photon and maximum kinetic energy of a photoelectron emitted.

$$E_{\text{photon}} = hf = \Phi + E_{k-\text{max}}$$

$$\therefore E_k = hf - \Phi \quad (4)$$

Also  $E_k = \frac{1}{2}mv^2$ , so:

$$\frac{1}{2}mv_{\text{max}}^2 = hf - \Phi$$

$$hf = \Phi + \cancel{E_k}^0$$

From eq<sup>n</sup>(4) :  $hf_0 = \Phi$

## 0.1 Maxwell's Equations

Differential Form

$$\nabla \cdot \mathbf{E} = \frac{\rho}{\varepsilon_0}$$

$$\nabla \cdot \mathbf{B} = 0$$

$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$$

$$\nabla \times \mathbf{B} = \mu_0 \left( \mathbf{J} + \varepsilon_0 \frac{\partial \mathbf{E}}{\partial t} \right)$$

Integral Form

$$\oint_S \vec{E} \cdot d\vec{a} = \frac{Q_{enc}}{\varepsilon_0}$$

$$\oint_S \vec{B} \cdot d\vec{a} = 0$$

$$\oint_C \vec{E} \cdot d\vec{l} = \int_S \frac{\partial \vec{B}}{\partial t} \cdot d\vec{a}$$

$$\oint_C \vec{B} \cdot d\vec{l} = \mu_0 I + \mu_0 \varepsilon_0 \int_S \frac{\partial \vec{E}}{\partial t} \cdot d\vec{a}$$

Now, let's take a look at the activity and half-life of a radioactive substance.

$$-\frac{dN}{dt} \propto N$$

$$\implies \frac{dN}{dt} = -\lambda N$$

$$\implies \frac{1}{N} dN = -\lambda dt$$

Integrate both sides:

$$\int_{N_0}^N \frac{1}{N} dN = -\lambda \int_0^t 1 dt \quad [ \because N = N_0 \text{ at } t = 0 ]$$

$$\implies \left[ \ln N \right]_{N_0}^N = -\lambda \left[ t \right]_0^t$$

$$\implies \ln N - \ln N_0 = -\lambda t$$

$$\implies \ln \left( \frac{N}{N_0} \right) = -\lambda t$$

$$\implies \frac{N}{N_0} = e^{-\lambda t}$$

$$\therefore N = N_0 e^{-\lambda t}$$

$$\implies \lambda = \frac{\ln 2}{t_{\frac{1}{2}}}$$

$$\therefore t_{\frac{1}{2}} = \frac{\ln 2}{\lambda}$$

$$\therefore A = A_0 e^{-\lambda t} \quad [ \because A = N\lambda ]$$

$$L = 4\pi\sigma r^2 T^4$$

$$F = \frac{L}{4\pi d^2}$$

$$\lambda_{\max} \propto \frac{1}{T}$$

$$f = f_0 \frac{v}{v \pm v_s}$$



## 0.2 Taylor Series

$$x \equiv -1 \pmod{5}$$

$$\frac{-\hbar^2}{2m}\nabla^2\Psi(r)+V(r)\Psi(r)=E\Psi(r)$$

$$i\hbar\frac{\partial}{\partial t}|\Psi\rangle=\hat{H}|\Psi\rangle$$

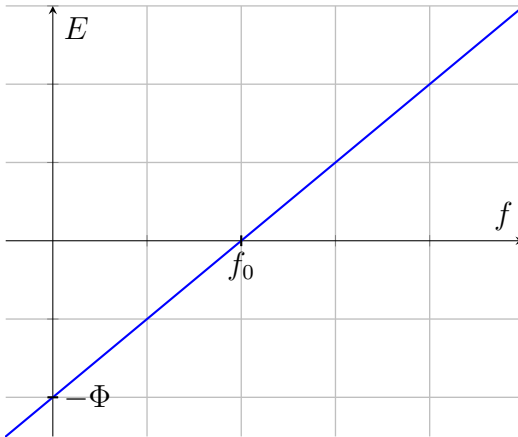
$$y=\begin{cases}2^i&0\leqslant j\leqslant m-1;\\ \sum_{j=1}^mx_{i-j}&i\geqslant m\end{cases}$$

$$\begin{bmatrix}1&2\\3&4\end{bmatrix}\begin{bmatrix}2&7\\3&4\end{bmatrix}=\begin{bmatrix}8&15\\18&37\end{bmatrix}$$

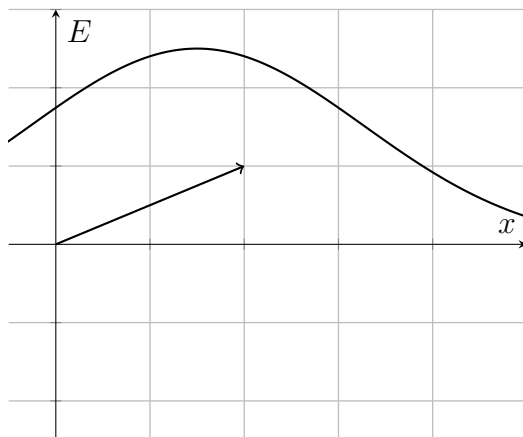
### 0.3 The photoelectric effect

$$\Phi = K.E_{max} + hf$$

$$\therefore E_{k(max)} = \Phi - hf$$



$$E = \begin{cases} 0 & \text{at } 0 \leq f \leq f_0 \\ hf - \Phi & \text{at } f > f_0 \end{cases}$$

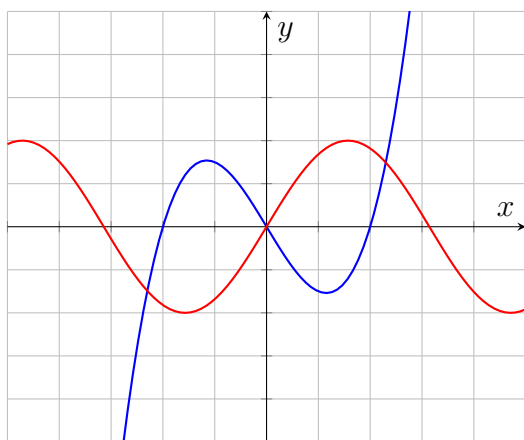
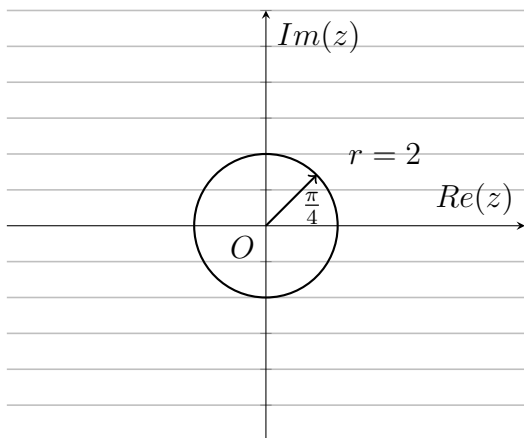


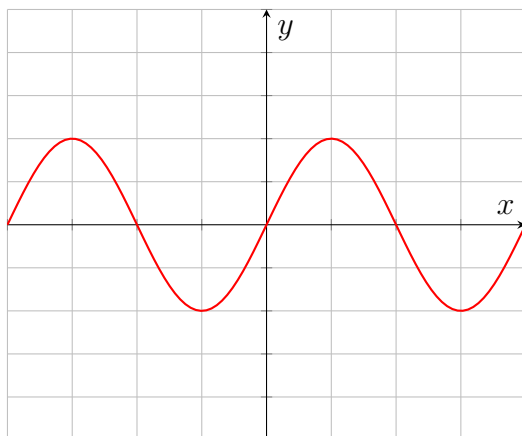
$$E_p = m\Delta\Phi$$

$$E_p = -m\left(\frac{GM}{R_2} - \frac{GM}{R_1}\right)$$

$$\therefore E_p = GMm\left(\frac{1}{R_1} - \frac{1}{R_2}\right)$$

$$x - y = 0$$





$$\frac{2}{4} \oint_{\pi}^7 2x^2 \, dx$$

