

Shrödinger's Wave Function

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$$\int_a^b f(x)dx = \int_0^b f(x)dx - \int_0^a f(x)dx$$

Hello I am Himalaya Satyal and this is a research on Shrödinger's wave equations. The Shrödinger Equation is $i\hbar \frac{\partial}{\partial t} |\Psi\rangle = \hat{H}|\Psi\rangle$. By definition, $\int_a^b f(x)dx = \int_0^b f(x)dx - \int_0^a f(x)dx$.

$$E_k + E_P = E_T$$

$$\implies \frac{-\hbar^2}{2m} \nabla^2 \Psi(r) + V(r)\Psi(r) = E\Psi(r)$$

$$x \equiv -1 \pmod{5}$$

$$i\hbar \frac{\partial}{\partial t} |\Psi\rangle = \hat{H}|\Psi\rangle$$

$$\implies x + 1 \equiv 0 \pmod{5}$$

Therefore, $5|x+1$. Let m be a fixed integer greater than 1. The sequence x_0, x_1, x_2, \dots is defined as follows:

$$x_i = \begin{cases} 2^i & \text{if } 0 \leq j \leq m-1; \\ \sum_{j=1}^m x_{i-j} & \text{if } i \geq m \end{cases}$$

Find the greatest k for which the sequence contains k consecutive terms divisible by m .

If p is a prime and $p \nmid a$, then $a^p \equiv a \pmod{p}$. This is known as Fermat's Last Theorem.

A modified version of the Fermat's Last Theorem
which gives:

$a^{\phi(n)} \equiv 1 \pmod{n}$ where $\phi(n)$ is the Euler's Totient Function.

Find the greatest k for which the sequence contains k consecutive terms divisible by m .

$$\oint_{e^{-i\pi}}^{\infty} \sin x \, dx = ?$$

$$\begin{aligned} x &= x_0 \cos(\omega t) \\ \implies \frac{dx}{dt} &= -\omega x_0 \sin(\omega t) \end{aligned} \tag{1}$$

$$\begin{aligned} v &= v_0 \sin(\omega t) \\ \implies \frac{dv}{dt} &= -\omega^2 x_0 \cos(\omega t) \end{aligned} \tag{2}$$

$$a = a_0 \cos(\omega t)$$

$$a_0 = -\omega^2 x_0$$

$$x = x_0 e^{-\lambda t}$$

$$\implies \frac{dx}{dt} = -\lambda x_0 e^{-\lambda t}$$

$$\frac{\partial x}{\partial t} = \partial \vec{A}$$

$$pV = \frac{1}{3}Nm\langle c^2 \rangle \quad (3)$$

$$\implies c_{r.m.s} = \sqrt{\langle c^2 \rangle}$$

Now we will look at the workfunction relation between the energy of photon and maximum kinetic energy of a photoelectron emitted.

$$E_{photon} = hf = \Phi + E_{k-max}$$

$$\therefore E_k = hf - \Phi \quad (4)$$

Also $E_k = \frac{1}{2}mv^2$, so:

$$\frac{1}{2}mv_{max}^2 = hf - \Phi$$

$$hf = \Phi + E_k^0$$

From eqⁿ(4) : $hf_0 = \Phi$

0.1 Maxwell's Equations

Differential Form

$$\nabla \cdot \mathbf{E} = \frac{\rho}{\epsilon_0}$$

$$\nabla \cdot \mathbf{B} = 0$$

$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$$

$$\nabla \times \mathbf{B} = \mu_0 \left(\mathbf{J} + \epsilon_0 \frac{\partial \mathbf{E}}{\partial t} \right)$$

Integral Form

$$\oint_S \vec{E} \cdot d\vec{a} = \frac{Q_{enc}}{\epsilon_0}$$

$$\oint_S \vec{B} \cdot d\vec{a} = 0$$

$$\oint_C \vec{E} \cdot d\vec{l} = \int_S \frac{\partial \vec{B}}{\partial t} \cdot d\vec{a}$$

$$\oint_C \vec{B} \cdot d\vec{l} = \mu_0 I + \mu_0 \epsilon_0 \int_S \frac{\partial \vec{E}}{\partial t} \cdot d\vec{a}$$

Now, let's take a look at the activity and half-life of a radioactive substance.

$$\begin{aligned} -\frac{dN}{dt} &\propto N \\ \implies \frac{dN}{dt} &= -\lambda N \\ \implies \frac{1}{N} dN &= -\lambda dt \end{aligned}$$

Integrate both sides:

$$\begin{aligned} \int_{N_0}^N \frac{1}{N} dN &= -\lambda \int_0^t 1 dt \quad [\because N = N_0 \text{ at } t = 0] \\ \implies \left[\ln N \right]_{N_0}^N &= -\lambda \left[t \right]_0^t \\ \implies \ln N - \ln N_0 &= -\lambda t \\ \implies \ln \left(\frac{N}{N_0} \right) &= -\lambda t \\ \implies \frac{N}{N_0} &= e^{-\lambda t} \\ \therefore N &= N_0 e^{-\lambda t} \\ \implies \lambda &= \frac{\ln 2}{t_{\frac{1}{2}}} \\ \therefore t_{\frac{1}{2}} &= \frac{\ln 2}{\lambda} \\ \therefore A &= A_0 e^{-\lambda t} \quad [\because A = N\lambda] \\ L &= 4\pi\sigma r^2 T^4 \end{aligned}$$

$$8\,$$

$$F=\frac{L}{4\pi d^2}$$

$$\lambda_{\rm max} \propto \frac{1}{T}$$

$$f=f_0\frac{v}{v\pm v_{\mathrm{s}}}$$

0.2 Taylor Series

$$x \equiv -1 \pmod{5}$$

$$\frac{-\hbar^2}{2m} \nabla^2 \Psi(r) + V(r) \Psi(r) = E \Psi(r)$$

$$i\hbar \frac{\partial}{\partial t} |\Psi\rangle = \hat{H} |\Psi\rangle$$

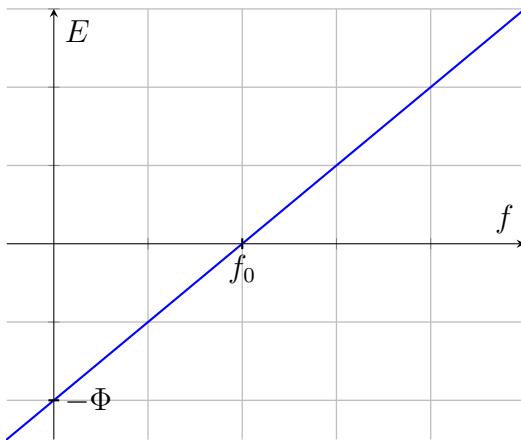
$$y = \begin{cases} 2^i & 0 \leq j \leq m-1; \\ \sum_{j=1}^m x_{i-j} & i \geq m \end{cases}$$

$$\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \begin{bmatrix} 2 & 7 \\ 3 & 4 \end{bmatrix} = \begin{bmatrix} 8 & 15 \\ 18 & 37 \end{bmatrix}$$

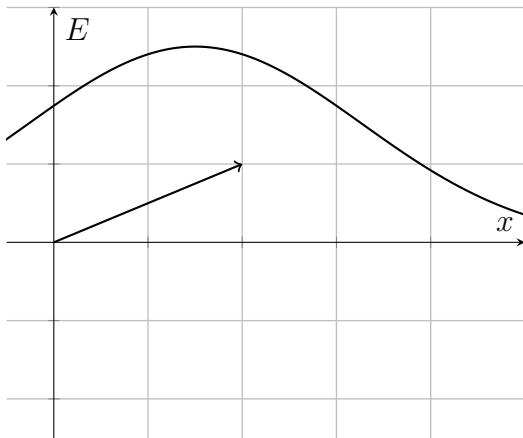
0.3 The photoelectric effect

$$\Phi = \text{K.E.}_{max} + hf$$

$$\therefore E_{k(max)} = \Phi - hf$$



$$E = \begin{cases} 0 & \text{at } 0 \leq f \leq f_0 \\ hf - \Phi & \text{at } f > f_0 \end{cases}$$

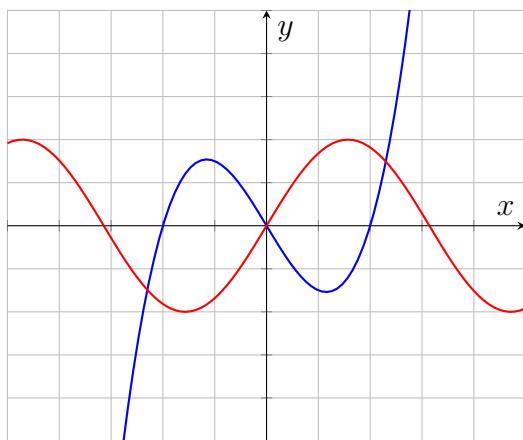
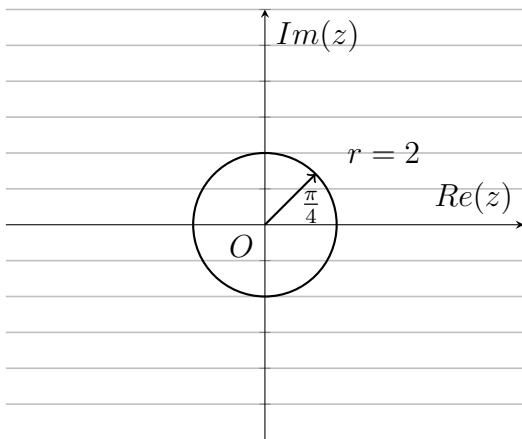


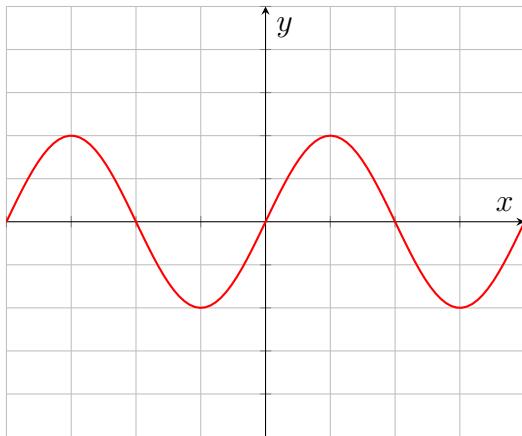
$$E_p = m\Delta\Phi$$

$$E_p = -m\left(\frac{GM}{R_2} - \frac{GM}{R_1}\right)$$

$$\therefore E_p = GMm\left(\frac{1}{R_1} - \frac{1}{R_2}\right)$$

$$x - y = 0$$





$$\frac{2}{4} \oint_{\pi}^7 2x^2 \, dx$$

